

SURVEYING MANUAL

A MANUAL OF FIELD AND OFFICE METHODS FOR THE USE OF STUDENTS IN SURVEYING

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PREFACE TO FIRST EDITION.

In preparing this manual the following points have been kept especially in view: (1) To provide a simple and comprehensive text designed to anticipate and supplement, rather than replace, the usual elaborate treatise. (2) To bring the student into immediate familiarity with approved surveying methods. (3) To cultivate the student's skill in the rare arts of keeping good field notes and making reliable calculations.

It is believed that the discussions of the different instruments, their use and theory, at the beginning of the several chapters is unusually simple, especially in the relations of the elementary lines.

The several series of practice problems at the conclusion of the respective chapters are arranged so as to give the student familiarity with the use of the instrument before taking up its theory and adjustments, this order being more effective than the reverse. The interest of the student may be stimulated and his gain in skill promoted by giving him practice with level and transit very early in the course, after which the scope of the work may be much more flexible both for student and instructor.

Since the list of problems is more extended than can be covered in the time usually available for surveying field practice, some range is permitted in the choice of work from year to year and under varying local conditions. By using some discrimination in selecting the more important problems for actual field work, the others may be covered sufficiently by class room discussions.

The consistent treatment of errors of surveying receives attention throughout the book. The methods of work both in the field and office are designed to reveal and, as far as possible, to eliminate blunders and errors, and the tests of precision are borrowed from the most rational current practice. The distribution of residual errors falling within the permissible limits likewise receives due consideration.

PREFACE.

An important innovation in this manual is the liberal use of field note and other forms executed according to the standard required of the student in like work. The high value of such samples in developing the student's skill in this important detail of field work has been well established. It will be seen that the forms are prescribed in liberal numbers in the earlier stages of the work while the student is engaged in fixing a standard of quality, but that farther on he is required more and more to devise his own forms. A valuable feature of this system is the liberal amount of practice obtained in freehand lettering which has marked effect on the drafting and other work.

It is suggested that the student should be trained to be self-reliant by requiring him to verify his own results before submitting them for criticism. Likewise he should be encouraged to be genuine by placing him on his honor.

This somewhat informal guide to field and office methods is issued primarily for the use of the authors' classes, but it is hoped that others as well may find it of value in presenting principles to the beginner, and in cultivating his spirit and manual skill.

December, 1900.

W. D. P. M. S. K.

PREFACE TO THIRD EDITION.

This third edition is issued to meet the call for the manual at various technical institutions and from practicing engineers. With a view to increase the value of the book both for teaching and reference purposes, various revisions and additions have been made. Among these are the full scale sample of field notes on the inset sheet at the back of the book.

The authors desire to acknowledge the valuable suggestions and criticisms received from various sources.

August, 1902.

W. D. P. M. S. K.

PREFACE TO FOURTH EDITION.

In this enlarged edition the book has been revised, nearly all the cuts have been redrawn, natural, logarithmic and trigonometric tables have been added, and the entire book has been reset and recast. The book has been critically revised and many changes and revisions have been made to increase its usefulness. The extensive use of the book has been due to the following important features, which are retained in the present edition.

1. Clear, definite and concise descriptions of surveying instruments and surveying methods.

2. Clear, definite and concise instructions for surveying field practice.

- 3. Carefully arranged and well executed forms of field notes.
- 4. The field practice unit has been taken as the squad; the idea being to give definite individual training.
- 5. By giving allowable limits of precision the critical instinct of the student is developed and he is taught to use consistent accuracy.
- 6. The main idea has been to train and develop engineering students by a study of surveying, rather than to teach the trade of surveying.

The thanks of the authors are due the McGraw-Hill Book Company for the use of the tables giving squares, cubes, square roots, cube roots and properties of circles, taken from Harger and Bonney's "Highway Engineers' Handbook"; and to the J. B. Lippincott Company for the use of the tables of five-place logarithms of numbers and of logarithmic functions of angles taken from Suplee's "Five Place Logarithms," and the tables of five place natural functions of angles taken from Suplee's "Mechanical Engineers' Reference Book."

The thanks of the authors are also due the Publication Committee of the American Railway Engineering Association for permission to print an abstract of "Conventional Signs and Symbols" adopted by the Association.

The authors desire to express their appreciation for the many suggestions received.

April, 1915.

W. D. P. M. S. K.



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SPECIFICATIONS FOR A GOOD ENGINEER.

"A good engineer must be of inflexible integrity, sober, truthful, accurate, resolute, discreet, of cool and sound judgment, must have command of his temper, must have courage to resist and repel attempts at intimidation, a firmness that is proof against solicitation, flattery or improper bias of any kind, must take an interest in his work, must be energetic, quick to decide, prompt to act, must be fair and impartial as a judge on the bench, must have experience in his work and in dealing with men, which implies some maturity of years, must have business habits and knowledge of accounts. Men who combine these qualities are not to be picked up every day. Still they can be found. But they are greatly in demand, and when found, they are worth their price; rather they are beyond price, and their value can not be estimated by dollars."-Chief Engineer Starling's Report to the Mississippi Levee Commissioners.

[&]quot;Be sure you are right, and then go ahead."—D. Crockett.

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CHAPTER I.

GENERAL INSTRUCTIONS.

FIELD WORK.

Habitual Correctness.—Habitual correctness is a duty. Error should be looked upon as probable, and every precaution taken to verify data and results. Unchecked work may always be regarded as doubtful. A discrepancy which is found by the maker in time to be corrected by him before any damage is done is not necessarily discreditable, provided the error is not repeated. However, habitual error is not only discreditable but dishonorable as well, and nothing except intentional dishonesty injures the reputation of the engineer more quickly or permanently.

Consistent Accuracy.—The degree of precision sought in the field measurements should be governed strictly by the dictates of common sense and experience. Due consideration of the purposes of the survey and of the time available will enable one to avoid extreme precision when ordinary care would suffice, or crudeness when exactness is required, or inconsistency between the degrees of precision observed in the several parts of the survey. It is a very common practice of beginners, and of many experienced engineers as well, to carry calculated results far beyond the consistent exactness.

Speed.—Cultivate the habit of doing the field work quickly as well as accurately. True skill involves both quantity and quality of results. However, while the habit of rapid work can and should be acquired, the speed attempted in any given problem should never be such as to cast doubt upon the results. Slowness due to laziness is intolerable.

Familiarity with Instructions.—The instructions for the day's work should be read over carefully, and preliminary steps, such as the preparation of field note forms, should be taken so as to save time and make the work in the field as effective as possible. The ability and also the desire to understand and obey instructions are as essential as the skill to execute them.

Inferior Instruments.—Should a poor instrument or other equipment be assigned, a special effort should be made to secure excellent results. In actual practice, beginners often have to work with defective instruments, but they should never seek, nor are they permitted, to justify poor results by the character of the field equipment. The student should therefore welcome an occasional opportunity to secure practice with poor instruments.

Alternation of Duties.—The members of each party should alternate in discharging the several kinds of service involved in the field problems, unless otherwise instructed. Training in the subordinate positions is essential whether the beginner is to occupy them in actual practice or not, for intelligent direction of work demands thorough knowledge of all its details.

Field Practice Decorum.—The decorum of surveying field practice should conform reasonably to that observed in other laboratory work.

THE CARE OF FIELD EQUIPMENT.

RESPONSIBILITY.—The student is responsible for the proper use and safe return of all equipment. All cases of breakage, damage, loss or misplacement must be reported promptly. The equipment should be examined when assigned and a report made at once of any injury or deficiency found, so that responsibility may be properly fixed.

PRECAUTIONS.—Careful attention to the following practical suggestions will save needless wear to the equipment and reduce the danger of accidents to a minimum, besides adding to the quality and speed of the work.

Tripod.—Inspect the tripod legs and shoes. The leg is of the proper tightness if, when lifted to an elevated position, it sinks gradually of its own weight. The tripod shoes should be tight and have reasonably sharp points.

Setting Up Indoors.—In setting up the instrument indoors press the tripod shoes firmly into the floor, preferably with each point in a crack. Avoid disturbing other instruments in the room.

Instrument Case.—Handle the instrument gently in removing it from and returning it to the case. It is always

best to place the hands beneath the leveling base in handling the detached instrument. Considerable patience is sometimes required to close the lid after returning the instrument; if properly placed the lid closes freely.

Mounting the Instrument.—See that the instrument is securely attached to the tripod before shouldering it. Undue haste in this particular sometimes results in costly accidents. When screwing the instrument on the tripod head, it should be turned in a reverse direction until a slight jar is felt, indicating that the threads are properly engaged.

Sunshade.—Always attach the sunshade regardless of the kind of weather. The sunshade is a part of the telescope tube and the adjustment of a delicate instrument may sometimes be affected by its absence. In attaching or removing the sunshade or object glass cap, always hold the telescope tube firmly with one hand and with the other twist the shade or cap to the right to avoid unscrewing the object glass cell.

Carrying the Instrument.-Do not carry the instrument on the shoulder in passing through doors or in climbing fences. Before shouldering the instrument, the principal motions should be slightly clamped; with the transit, clamp the telescope on the line of centers; and with the level, when the telescope is hanging down. In passing through timber with low branches, give special attention to the instrument. Before climbing a fence, set the instrument on the opposite side with tripod legs well spread.

Setting Up in the Field.—When setting up in the field, bring the tripod legs to a firm bearing with the plates approximately level. Give the tripod legs additional spread in windy weather or in places where the instrument may be subject to vibration or other disturbance. On side-hill work place one leg up hill. With the level, place two tripod shoes in the general direction of the line of levels.

Exposure of Instrument.—Do not expose the instrument to rain or dampness. In threatening weather the water proof bag should be taken to the field. Should the instrument get wet, wipe it thoroughly dry before returning it to the case. Protect the instrument from dust and dirt, and avoid undue exposure to the burning action of the sun. Avoid subjecting it to sudden changes of temperature. In cold weather when bringing an instrument indoors cover the instrument with the bag or return it to the case immediately to protect the lenses and graduations from condensed moisture.

Guarding the Instrument.—Never leave an instrument unguarded in exposed situations such as in pastures, near driveways, or where blasting is in progress. Never leave an instrument standing on its tripod over night in a room.

Manipulation of Instrument.—Cultivate from the very beginning the habit of delicate manipulation of the instrument. Many parts, when once impaired, can never be restored to their original condition. Rough and careless treatment of field instruments is characteristic of the unskilled observer. Should any screw or other part of the instrument work harshly, call immediate attention to it so that repairs may be made. Delay in such matters is very destructive to the instrument.

Foot Screws.—In leveling the instrument, the foot screws should be brought just to a snug bearing. If the screws are too loose, the instrument rocks, and accurate work can not be done; if too tight, the instrument is damaged, and the delicacy and accuracy of the observations are reduced. Much needless wear of the foot screws may be avoided if the plates are brought about level when the instrument is set up. With the level, a pair of foot screws should be shifted to the general direction of the back or fore sight before leveling up.

Eyepiece.—Before beginning the observations, focus the yepiece perfectly on the cross-hairs. This is best done by holding the note book page, handkerchief, or other white object a foot or so in front of the object glass so as to illuminate the hairs; and then, by means of the eyepiece slide, focus the microscope on a speck of dust on the cross-hairs near the middle of the field. To have the focusing true for natural vision, the eye should be momentarily closed several times between observations in order to allow the lenses of the eye to assume their normal condition. The omission of this precaution strains the eye and is quite certain to cause parallax. After the eyepiece is focused on the cross-hairs, test for parallax by sighting at a well defined object and observing whether the cross-hairs seem to move as the eye is shifted slightly.

Clamps.—Do not overstrain the clamps. In a well designed instrument the ears of the clamp screw are purposely made small to prevent such abuse. Find by experiment just how tight to clamp the instrument in order to prevent slipping, and then clamp accordingly.

Tangent Screws.—Use the tangent screws for slight motions only. To secure even wear the screws should

be used equally in all parts of their length. The use of the wrong tangent movement is a fruitful source of error with beginners.

Adjusting Screws.—Unless the instrument is assigned expressly for adjustment, do not disturb the adjusting screws

Magnetic Needle.—Always lift the needle before shouldering the instrument. Do not permit tampering with the needle. If possible, avoid subjecting the needle to magnetic influence, such as may exist on a trolley car. Should the needle become reversed in its polarity or require remagnetization, it may be removed from the instrument and brought into the magnetic field of a dynamo or electric motor for several minutes, the needle being jarred slightly during the exposure; or a good horseshoe magnet may be used for the same purpose. The wire coil counterbalance on the needle will usually require shifting after the foregoing process.

Lenses.—Do not remove or rub the lenses of the telescope. Should it be absolutely necessary to clean a lens, use a very soft rag with caution to avoid scratching or marring the polished surface. Protect the lenses from flying sand and dust, which in time seriously affect the definition of the telescope.

Plumb Bob.—Do not abuse the point of the plumb bob and avoid needless knots in the plumb bob string.

Cleaning Tripod Shoes.—Remove the surplus soil from the tripod shoes before bringing the instrument indoors.

Leveling Rods.—Leveling rods and stadia boards should not be leaned against trees or placed where they may fall. Avoid injury to the clamps, target and graduations Do not mark the graduations with pencil or otherwise. Avoid needless exposure of the rod to moisture or to the sun.

Flag Poles.—Flag poles should not be unduly strained and their points should be properly protected.

Chains and Tapes.—Chains should not be jerked. Avoid kinks in steel tapes, especially during cool weather. When near driveways, in crowded streets, etc., use special care to protect the tape. Band tapes will be done up in 5-foot loops, figure 8 form, unless reels are provided. Etched tapes should be wiped clean and dry at the end of the day's work.

Axes and Hatchets.—Axes and hatchets will be employed for their legitimate purposes only. Their wanton use in clearing survey lines is forbidden, and their use at all,

for such purpose, on private premises must be governed strictly by the rights of the owner.

Stakes.—The consumption of stakes should be controlled by reasonable economy, and surplus stakes returned to the general store. For the protection of mowing machines in meadows, etc., hub stakes should be driven flush with the surface of the ground, and other stakes should be left high enough to be visible. Whenever practicable, stakes which may endanger machines should be removed after serving the purpose for which they were set.

FIELD NOTES.

Scope of Field Notes.—The notes should be a complete record of each day's work in the field. In addition to the title of the problem and the record of the data observed, the field notes should include the date, weather, organization of party, equipment used, time devoted to the problem, and any other information which is at all likely to be of service in connection with the problem. No item properly belonging to the notes should be trusted to memory. Should the question arise as to the desirability of any item, it is always safe to include it. The habit of rigid self criticism of the field notes should be cultivated.

Character of Notes.—The field notes should have character and force. As a rule, the general character of the student's work can be judged with considerable certainty by the appearance of his field notes. A first-class page of field notes always commands respect, and tends to establish and stimulate confidence in the recorder. The notes should be arranged systematically.

Interpretation of Notes.—The field notes should have one and only one reasonable interpretation, and that the correct one. They should be perfectly legible and easily understood by anyone at all familiar with such matters.

Original Notes.—Each student must keep complete notes of each problem. Field notes must not be taken on loose slips or sheets of paper or in other note books, but the original record must be put in the prescribed field note book during the progress of the field work.

Field Note Book.—The field record must be kept in the prescribed field note book. For ease of identification the name of the owner will be printed in bold letters at the top of the front cover of the field note book.

Pencil.—To insure permanency all notes will be kept with a hard pencil, preferably a 4H. The pencil should be kept well sharpened and used with sufficient pressure to indent the surface of the paper somewhat.

Title Page.—An appropriate title page will be printed

on the first page of the field note book.

Indexing and Cross Referencing.—A systematic index of the field notes will be kept on the four pages following the title page. Related notes on different pages will be liberally and plainly cross referenced. The pages of the note book will be numbered to facilitate indexing.

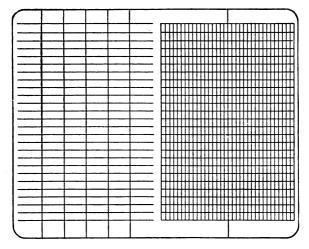
Methods of Recording Field Notes.—There are three general methods of recording field notes, namely: (1) by sketch, (2) by description or narration, and (3) by tabulation. It is not uncommon to combine two or perhaps all three of these methods in the same problem or survey.

Form of Notes.—All field notes must be recorded in a field note book ruled as shown below, except where circumstances require modification. If no form is given, the student will devise one suited to the particular problem.

Lettering.—Field notes will be printed habitually in the "Engineering News" style of freehand lettering, as treated in Reinhardt's "Freehand Lettering." The body of the field notes will be recorded in the slanting letter and the headings will be made in the upright letter. The former slants to the right 1:2.5 and the so-called upright letter is made to slant to the left slightly, say 1:25. Lower case letters will be used in general, capitals being employed for initials and important words, as required. In the standard field note alphabet the height of lower case letters a, c, e, i, m, n. etc., is 3/10 inch, and the height of lower case b, d, f, g, h, etc., and of all capital letters and all numerals is 540 (1/2) inch; lower case t is made four units (4/40) inch high. This standard accords with best current practice and is based upon correct economic principles. Sample pages of field notes with letters and figures drawn full size are given on page 9. The student is expected to make the most of this opportunity to secure a liberal amount of practice in freehand lettering.

Field Note Sketches.—Sketches will be used liberally in the notes and will be made in the field. If desired, a ruler may be used in drawing straight lines, but the student is urged to acquire skill at once in making good plain free-hand sketches. The field sketches should be bold and clear, in fair proportion, and of liberal size so as to avoid con-

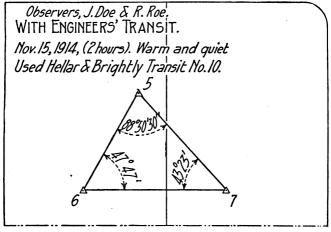
fusion of detail. The exaggeration of certain details in a separate sketch sometimes adds greatly to the clearness of the notes. The sketches should be supplemented by descriptive statements when helpful, and important points of the sketch should be lettered for reference. The precise scaling of sketches in the field note book, while sometimes necessary is usually undesirable owing to the time consumed. It is also found that undue attention to the drafting of the sketch is very apt to occupy the mind and cause



omissions of important numerical data. Since recorded figures and not the size of the field sketch itself must usually be employed in the subsequent use of the notes, it is important to review the record before leaving the field to detect Making sketches on loose omissions or inconsistencies. sheets or in other books and subsequently copying them into the regular field book is very objectionable practice and will not be permitted in the class work. Copies of field notes or sketches are never as trustworthy as the original record made during the progress of the field work. In very rapid surveys where legibility of the original record must perhaps suffer somewhat, it is excellent practice to transcribe the notes at once to a neighboring page, thus preserving the original rough notes for future reference. The original has more weight as evidence, but the neat copy

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Right Hand Page.

made before the notes are "cold" is of great help in interpreting them.

Numerical Data.—The record of numerical data should be consistent with the precision of the survey. In observations of the same class a uniform number of decimal places should be recorded. When the fraction in a result is exactly one-half the smallest unit or decimal place to be observed, record the even unit. Careful attention should be given to the legibility of numerals. This is a matter in which the beginner is often very weak. This defect can be corrected best by giving studious attention and practice to both the form and vertical alinement of tabulated numerals.

Erasures.—Erasures in the field notes should be avoided. In case a figure is incorrectly recorded, it should be crossed out and the correct entry made near by. The neat cancellation of an item in the notes inspires confidence, but evidence of an erasure or alteration casts doubt upon their genuineness. When a set of notes becomes so confused that erasure seems desirable, it should be transcribed, usually on another page. Rejection of a page of notes should be indicated by a neat cross mark, and cross reference should be made between the two places.

Office Copies.—Office copies of field notes will be submitted promptly, as required. These copies must be actual transcripts from the original record contained in the field note book of the individual submitting the copy. When office copies are made, a memorandum of the fact should be entered on the page of the field note book. When so specified, the office copies will be executed in india ink.

Criticism of Field Notes.—The field notes must be kept in shape for inspection at any time, and be submitted on call. All calculations and reductions must be kept up to date. The points to which chief attention should be directed in the criticism of the field notes are indicated in the following schedule. The student is expected to criticise his own notes and submit them in as perfect condition as possible. For simplicity the criticisms will be indicated by stamping on the note book page the reference letters and numbers shown in the schedule.

SCHEDULE OF POINTS FOR THE CRITICISM OF FIELD NOTE BOOKS.

A. SUBJECT MATTER.

(1) General:

- (a) Descriptive title of problem.
- (b) Date.
- (c) Weather.
- (d) Organization of party.
- (e) Equipment used.
- (f) Time devoted to the problem.
- (g) Indexing and cross referencing.
- (h) Page numbering.
- (i) Title page.
- (j) Identification of field note book.

(2) Record of Data:

- (a) Accuracy.
- (b) Completeness.
- (c) Consistency.
- (d) Arrangement.
- (e) Originality.

B. EXECUTION.

(1) Lettering:

- (a) Style. ("Engineering News")
- (b) Size. (a, c, e, i, etc., $\frac{3}{40}$ inch high; b, d, f, g, etc., A, B, C, etc., and 1, 2, 3, etc., $\frac{5}{40}$ ($\frac{1}{8}$) inch high; t, $\frac{4}{40}$ inch.)
- (c) Slant. (In body of notes, "slanting," 1:2.5 right; in headings, "upright," about 1:25 to left.)
 - (d) Form. (See Reinhardt's "Freehand Lettering.")
- (e) Spacing. (Of letters in words; of numerals; of words; balancing in column or across page.)
 - (f) Alinement. (Horizontal; vertical.)
- (g) Permanency. (Use sharp hard pencil with pressure.)(2) Sketches.
 - (a) To be bold, clear and neat.
 - (b) To be ample in amount.
 - (c) To be of liberal size.
 - (d) To be in fair proportion.
 - (e) To be made freehand.
 - (f) To be made in the field.

OFFICE WORK.

Importance of Office Work.—Capable office men are comparatively rare. Skill in drafting and computing is within the reach of most men who will devote proper time and effort to the work. Men who are skillful in both field and office work have the largest opportunity for advancement.

Calculations.—All calculations and reductions of a permanent character must be shown in the field note book in the specified form. Cross references between field data and calculations should be shown. Consistency between the precision of computed results and that of the observed data should be maintained. Computed results should be verified habitually, and the verified results indicated by a check mark. Since most computers are prone to repeat the same error, it is desirable in checking calculations to employ independent methods and to follow a different order. A fruitful source of trouble is in the transcript of data, and this should be checked first when reviewing doubtful cal-Skilled computers give much attention to culations. methodical arrangement, and to contracted methods of computing and verifying results. Familiarity with the slide rule and other labor saving devices is important. (See Chapter X, Methods of Computing.)

Drafting Room Equipment.—The student is responsible for the proper use and care of drafting room furniture and equipment provided for his use.

Drafting.—The standard of drafting is that indicated in Reinhardt's "Technic of Mechanical Drafting."

Drafting Room Decorum.—The decorum of the student in the drafting room will conform to that observed in first-class city drafting offices.

CHAPTER II.

THE CHAIN AND TAPE.

METHODS OF FIELD WORK.

Units of Measure.—In the United States the foot is used by civil engineers in field measurements. Fractions of a foot are expressed decimally, the nearest 0.1 being taken in ordinary surveys, and the nearest 0.01 foot (say 1/8 inch) in more refined work.

In railroad and similar "line" surveys by which a station stake is set every 100 feet, the unit of measure is really 100 feet instead of the foot. The term "station" was originally applied only to the actual point indicated by the numbered stake, but it is now universal practice in this country to use the word station in referring to either the point or the 100-foot unit distance. A fractional station is called a "plus" for the reason that a plus sign is used to mark the decimal point for the 100-foot unit, the common decimal point being reserved for fractions of a foot. The initial or starting stake of such a survey is numbered 0.

The 100-foot chain is commonly called the "engineers' chain" to distinguish it from the 66-foot or 100-link chain which is termed the "surveyors' chain" because of its special value in land surveys involving acreage. The latter is also called the Gunter chain after its inventor, and is otherwise known as the four-rod or four-pole chain. British engineers use the Gunter chain for both line and land surveys. The "surveyors'" or Gunter chain, while no longer used in actual surveying, is described in this book for the reason that the United States rectangular surveys were made throughout with the 66-foot chain.

In the Spanish-American countries the vara is generally used in land surveys. The Castilian vara is 32.8748 inches long, but the state of California has adopted 32.372 inches, and Texas 33½ inches, as the legal length of the vara.

While the metric system is used exclusively, or in part, in

each of the several United States government surveys, except those for public lands, little or no progress has been made towards its introduction in other than government surveys.

Linear Measuring Instruments.—Two general types of linear measuring devices are used by surveyors, viz., the common chain and the tape. There are several kinds of each, according to the length, material, and method of graduation.



Fig. 1.

The common chain is made up of a series of links of wire having loops at the ends and connected by rings so as to afford flexibility. The engineers' chain is shown in (a), Fig. 1, the illustration being that of a 50-foot chain, or one-

half the length generally used. The surveyors' or Gunter chain is shown in (b), Fig. 1. In the common chain the end graduation is the center of the cross bar of the handle, and every tenth foot or link is marked by a notched brass tag. In the 100-foot or 100-link chain the number of points on the tag indicates the multiple of ten units from the nearer end, and a circular tag marks the middle of the chain. The chain is done up hour-glass shape, as shown in the cut.

Chaining pins made of steel wire are used in marking the end of the chain or tape in the usual process of linear measurement. A set of pins usually numbers eleven, as indicated at (c), Fig. 1. The pins are carried on a ring made of spring steel wire.

The flat steel band, shown in (d) and (e), Fig. 1, is the best form of measuring device for most kinds of work. The band tape is usually 100 feet long. The end graduations of the band tape are usually indicated by brass shoulders, which should point in the same direction, as shown in (f), Fig. 1. The 100-foot band tape is commonly graduated every foot of its length, and the end foot to every 0.1 foot, every fifth foot being numbered on a brass sleeve. Brass rivets are most commonly used in graduating this tape. The band tape may be rolled up on a special reel, as indicated in (d) and (e), although some engineers dispense with the reel and do up the tape in the form of the figure 8 in loops of five feet or so.

The steel tapes shown in (g) and (h) have etched graduations. This style of tape is commonly graduated to 0.01 foot or ½ inch. It is more fragile than the band tape and is commonly used on more refined work. The form of the case shown in (h) has the advantage of allowing the tape to dry if wound up while damp.

The "metallic" tape (i), Fig. 1, is a woven linen line having fine brass wire in the warp.

The steel tape is superior to the common chain chiefly because of the permanency of its length. The smoothness and lightness of the steel tape are often important advantages, although the latter feature may be a serious drawback at times. The tape is both easier to break and more difficult to mend than the common chain.

Tapes for measuring base lines with great precision have recently been made of Invar steel. Invar steel has a very small coefficient of expansion. Invar steel tapes are very expensive.

Chaining.—In general, the horizontal distance is chained. Two persons, called head and rear chainmen, are required. The usual process is as follows:

The line to be chained is first marked with range poles. The head chainman casts the chain out to the rear, and after setting one marking pin at the starting point and checking up the remaining ten pins on his ring, steps briskly to the front. The rear chainman allows the chain to pass through his hands to detect kinks and bent links. Just before the full length is drawn out, the rear chainman calls "halt," at which the head chainman turns, shakes out the chain and straightens it on the true line under the direction of the rear chainman. In order to allow a clear sight ahead, the front chainman should hold the chain handle with a pin in his right hand well away from his body, supporting the right elbow on the right knee, if desired. The rear chainman holds the handle in his left hand approximately at the starting point and motions with his right to the head chainman, his signals being distinct both as to direction and amount. Finally, when the straight and taut chain has been brought practically into the true line, the rear chainman, slipping the handle behind the pin at the starting point with his left hand, and steadying the top of the pin with his right, calls out "stick." The head chainman at this instant sets his pin in front of the chain handle and responds "stuck," at which signal and not before the rear chainman pulls the pin.

Both now proceed, the rear chainman giving the preliminary "halt" signal as he approaches the pin just set by the head chainman. The chain is lined up, stretched, the front pin set, and the rear pin pulled on signal, as described for the first chain length. This process is repeated until the head chainman has set his tenth pin, when he calls "out" or "tally," at which the rear chainman walks ahead, counting his pins as he goes and, if there are ten, transfers them to the head chainman who also checks them up and replaces them on his ring. A similar check in the pins may be made at any time by remembering that the sum, omitting the one in the ground, should be ten. This safeguard should be taken often to detect loss of pins. The count of tallies should be carefully kept.

When the end of the line is reached, the rear chainman steps ahead, and reads the fraction at the pin, noting the units with respect to the brass tags on the chain. The number of pins in the hand of the rear chainman indicates the number of applications of the chain since the starting or last tally point. A like method is used in case intermediate points are to be noted along the line.

On sloping ground the horizontal distance may be obtained either by leveling the chain and plumbing down from the elevated end, or by measuring on the slope and correcting for the inclination. In ordinary work the former is preferred, owing to its simplicity. In "breaking chain" up or down a steep slope, the head chainman first carries the full chain ahead and places it carefully on the true line. A plumb bob, range pole or loaded chaining pin should be used in plumbing the points up or down. The segments of the chain should be in multiples of ten units, as a rule, and the breaking points should be "thumbed" by both chainmen to avoid blunders. Likewise, special caution is required to avoid confusion in the count of pins during this process.

The general method of measuring with the band tape is much the same as with the common chain. The chief difference is due to the fact that the handle of the tape extends beyond the end graduation, so that it is more convenient for the head chainman to hold the handle in his left hand and rest his left elbow on his left knee, setting the pin with his right hand. Another difference is in the method of reading fractions. It is best to read the fraction first by estimation, as with the chain, making sure of the feet; then shifting the tape along one foot, getting an exact decimal record of the fraction by means of the end foot graduated to tenths; the nearest 0.01 foot is estimated, or in especially refined work, read by scale.

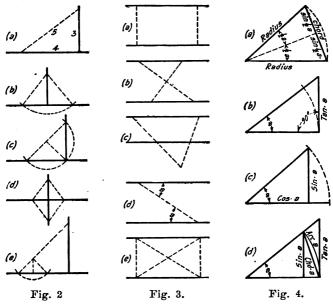
In railroad and similar line surveys, chaining pins are usually dispensed with and the ends of the chain are indicated by numbered stakes. The stake marked 0 corresponds to the pin at the starting point, and the station stakes are marked thence according to the number of 100-foot units laid off.

Perpendiculars.—Perpendiculars may be erected and let fall with the chain or tape by the following methods:

- (a) By the 3:4:5 method, shown in (a), Fig. 2, in which a triangle having sides in the ratio stated, is constructed.
- (b) By the chord bisection method, shown in (b), Fig. 2, in which a line is passed from the bisecting point of the chord to the center of the circle, or vice versa.

(c) By the semicircle method, shown in (c), Fig. 2, in which a semicircle is made to contain the required perpendicular.

The first method corresponds to the use of the triangle in drafting. Good intersections are essential in the second and third methods. Results may be verified either by using another process, or by repeating the same method with the measurements or position reversed, as indicated in (d), Fig. 2.



In locating a perpendicular from a remote point, the ratio method shown in (e), Fig. 2, may be used; or a careful trial perpendicular may be erected at a point estimated by placing the heels squarely on line and swinging the arms to the front, then proving by precise method.

Parallels.—Parallels may be laid off with the chain in various ways, a few of the simpler of which are:

(a) By equal distances, as in (a), Fig. 3, in which two equal distances are laid off, usually at right angles to the given line.

(b) By similar triangles, as in (b) and (c), Fig. 3. The ratio may, of course, have any value.

(c) By alternate angles, as in (d), Fig. 3, in which two

equal angles are laid off in alternation.

The first method is adapted to laying off a rectangle, as in staking out a building, in which case a good check is found in the equality of the diagonals. Precision of alinement is important, especially where a line is prolonged.

Angles.—Angles may be determined by linear measure-

ments in the following ways:

- (a) By the chord method, shown in (a), Fig. 4, in which the radius is laid off on the two lines forming the angle, and the chord measured.
- (b) The tangent method, shown in (b), Fig. 4, in which a perpendicular is erected at one end of the radius, and the length of the perpendicular intercepted by the two lines measured.
- (c) The sine-cosine method, (c), Fig. 4, which is better suited to constructing than to measuring angles.

The chord method is usually the most satisfactory. The tangent method may be applied to the bisected angle when its value approaches a right angle. Measurement of the supplementary angle affords an excellent check. A 100-foot radius is commonly used, although good results may be had with the 50-foot tape. Careful alinement is of the first importance in angular measurements.

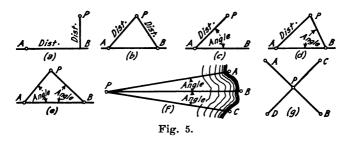
It is sometimes necessary to determine angles, at least approximately, when no tables are at hand. Fair results may be had on smooth ground by measuring the actual arc struck off to a radius of 57.3 feet.

For very small angles, the sine, chord, arc and tangent, (d), Fig. 4, are practically equal. Thus, sin 1° is .017452 and tan 1°, .017455, or either (say) .01745, or 1¾ per cent. Also, arc 1' is .000291, or (say) .0003 (three zeros three); and, arc 1" is .00000485, (say) .000005 (five zeros five).

Location of Points.—Points are located in surveying field practice in the following seven ways.

- (a) By rectangular coordinates, that is, by measuring the perpendicular distance from the required point to a given line, and the distance thence along the line to a given point, as in (a), Fig. 5.
- (b) By focal coordinates or tie lines, that is, by measuring the distances from the required point to two given points, as in (b), Fig. 5.

- (c) By polar coordinates, that is, by measuring the angle between a given line and a line drawn from any given point of it to the required point; and also the length of this latter line, as in (c), Fig. 5.
- (d) By modified polar coordinates, that is, by a distance from one known point and a direction from another, as in (d), Fig. 5.
- (e) By angular intersection, that is, by measuring the angles made with a given line by two other lines starting from given points upon it, and passing through the required point, as in (e), Fig. 5.
- (f) By resection, that is, by measuring the angles made with each other by three lines of sight passing from the required point to three points, whose positions are known, as in (f), Fig. 5.
- (g) By diagonal intersection, that is, by two lines joining two pairs of points so as to intersect in the required point, as in (g), Fig. 5.



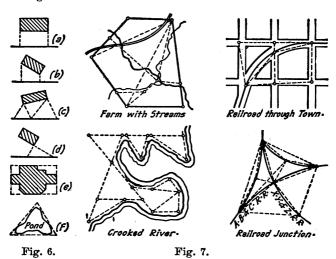
In each of these methods, except (f), the point is determined by the intersection of either two right lines, or two circles, or a right line and a circle.

Methods (a) and (b) are best suited to chain surveys; (c) and (d) are used most in the location of railroad curves; (e) and (f) are employed chiefly in river and marine surveys for the location of soundings, the latter being commonly known as the "three-point problem"; the last method, (g), is much used for "referencing out" transit points in railroad and similar construction surveys.

Location of Objects.—The location of buildings and topographic objects usually involves one or more of the foregoing methods of locating a point.

In Fig. 6, (a), (b), (c), and (d) suggest methods of locating a simple form, and (e) and (f) illustrate more complex cases.

Tie Line Surveys.—For many purposes tie line surveys, made with the chain or tape alone, are very satisfactory. The skeleton of such surveys is usually the triangle, the detail being filled in by the methods just outlined. Much time may be saved by carefully planning the survey. A few typical applications of the tie line method are shown in Fig. 7.



Ranging in Lines.—The range or flag pole is usually painted with alternate feet red and white, and the lower end is shod or spiked. A temporary form of range pole, called a picket, is sometimes cut from a straight sapling.

In flagging a point, the spike of the pole is placed on the tack and the pole plumbed by holding it symmetrically between the tips of the fingers of the two hands, the flagman being squarely behind the pole.

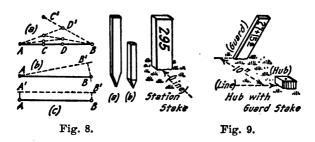
In hilly or timbered country the two land corners or other points between which it is desired to range in a line, are often invisible one from the other. In many cases two intermediate points C' and D', (a), Fig. 8, may be found, from

which the end points B and A, respectively, are visible; so that after a few successive linings in, each by the other, the true points, C and D, are found.

Otherwise, as shown at (b), Fig. 8, a random line may be run from A towards B. The trial line is chained and marked, the perpendicular from B located, and points interpolated on the true line.

If the desired line is occupied by a hedge or other obstruction, an auxiliary parallel line may be established in the adjacent road or field, after one or two trials, as in (c), Fig. 8.

A line may be prolonged past an obstacle by rectangular offsets or by equilateral triangles.



Signals.—There is little occasion for shouting in surveying field work if a proper system of sight signals is used. Each signal should have but one meaning and that a perfectly distinct one. Signals indicating motion should at once show clearly both the direction and amount of motion desired. Some of the signals in common use are as follows:

- (a) "Right" or "left,"—the arm is extended distinctly in the desired direction and the motion of the forearm and hand is graduated to suit the lateral motion required.
- (b) "Up" or "down,"—the arm is extended laterally and raised or lowered distinctly with motions to suit the magnitude of the movement desired. Some levelers use the left arm for the "up" signal and the right for "down."
- (c) "Plumb the pole (or rod),"—If to the right, that arm is held vertically with hand extended and the entire body, arm included, is swung distinctly to the right, or vice versa.
- (d) "All right,"—both arms are extended full length horizontally and waved vertically.

- (e) "Turning point" or "transit point,"—the arm is swung slowly about the head.
- (f) "Give line,"—the flagman extends both arms upward, holding the flag pole horizontally, ending with the pole in its vertical position. If a precise or tack point is meant, the signal is made quicker and sharper.
- (g) Numerals are usually made by counted vertical swings with the arm extended laterally. A station number is given with the right hand and the plus, if any, with the left; or a rod reading in like manner. The successive counts are separated by a momentary pause, emphasized, if desired, by a slight swing with both hands.

Stakes and Stake Driving.—A flat stake is used to mark the stations in a line survey, and a square stake or hub to mark transit stations, (a) and (b), Fig. 9. The station stake is numbered on the rear face, and the hub is witnessed by a flat guard stake driven slanting 10 inches or so to the left, Fig. 9. The numerals should be bold and distinct, and made with keel or waterproof crayon, pressed into the surface of the wood.

Having located a point approximately with the flag pole, the stake should be driven truly plumb in order that the final point may fall near the center of its top. In driving a stake, the axeman should watch for signals. It is better to draw the stake by a slanting blow than to hammer the stake over after it is driven. Good stake drivers are scarce.

PROBLEMS WITH THE CHAIN AND TAPE.

General Statement.—Each problem is stated under the following heads:

- (a) Equipment.—In which are specified the articles and instruments assigned or required for the proper performance of the problem. A copy of this manual and of the regulation field note book, with a hard pencil to keep the record, form part of the equipment for every problem assigned.
- (b) Problem.—In which the problem is stated in general terms. The special assignments will be made by program.
- (c) Methods.—In which the methods to be used in the assigned work are described more or less in detail. In some problems alternative methods are suggested, and in others the student is left to devise his own.

PROBLEM A1. LENGTH OF PACE.

- (a) Equipment.—(No instrumental equipment required.)
- (b) Problem.—Investigate the length of pace as follows:
- (1) the natural pace; (2) an assumed pace of 3 feet; and
- (3) the effect of speed on the length of the pace.
- (c) Methods.—(1) On an assigned course of known length count the paces while walking at the natural rate. Observe the nearest 0.1 pace in the fraction at the end of the course. Secure ten consecutive results, with no rejections, varying not more than 2 per cent. (2) Repeat (1) for an assumed 3-foot pace. (3) Observe (in duplicate) time and paces for four or five rates from very slow to very fast, with paces to nearest 0.1 and time to nearest second. Record data and make reductions as in the form.

PROBLEM A2. DISTANCES BY PACING.

- (a) Equipment.—(No instrumental equipment required.)
- (b) Problem.—Pace the assigned distances.
- (c) Methods.—(1) Standardize the pace in duplicate on measured base. (2) Pace each line in duplicate, results differing not more than 2 per cent. Record and reduce as in form.

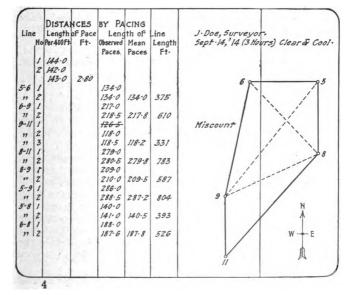
PROBLEM A3. AXEMAN AND FLAGMAN PRACTICE.

- (a) Equipment.—Flag pole, axe, 4 flat stakes, 1 hub, tacks.
- (b) Problem.—Practice the correct routine duties of axeman and flagman.
- (c) Methods.—(1) Number three station stakes to indicate representative cases and drive them properly. (2) Drive a hub flush with ground and tack it; number a witness stake and drive it properly. (3) Arrange program of signals with partner, separate 1,000 feet or so and practice same. (4) Signal say five station numbers to each other and afterwards compare notes. Make concise record of the foregoing steps.

PROBLEM A4. RANGE POLE PRACTICE.

- (a) Equipment.—4 flag poles.
- (b) Problem.—Given two hubs approximately 1,000 feet apart, interpolate a flag pole say 100 feet from one hub,

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Section		INI	ESTIG.	HOITA	OF		LENGTH					veyor.
Kind	Paces per	- 400 Ft-	Length	Rem	erke	5	EFFECT	OF SP	EED ON	LEN	TH OF	PACE .
of Pace		Mean	of Pace	Sept-13,		lear	Kind	Paces i	n 400 Ft.	Mean	Time	Speed of
No	Paces	Paces	Ft.	Smooth	grou	ind.	of Pace	Observd	Mean	Pace, P.	400 Ft	Pacing, 5
Natural-1	138.0		100	With th	e W	ind.		Paces	Paces	Ft.	Sec.	Ft. per Sec
2	137-4			Aga	insf	"	Very slow	214.6		(a)		(a)
3	139.0			"	1	"	" "	217.8	216.20	1.85	182	2.20
4	137-6				19	99	Slow	168.0		(6)		(6)
5	138.0			"		,,	"	167.5	167-75	2.38	111	3.60
6	139.0				77	,,	Natural	139.4		(0)		(c)
7	137-3		1	79		"	"	137.5	138-45	2.89	71	5.63
8	139.0				77	"	3-Foot	133.3		(0)	1	(0)
9	138-0			"		22	"	133.6	133.45	3.00	77	5.20
10	139-3	138-26	2.89		"	79	Fast	124.7		(0)		(e)
	(12.6)						"	125.3	125.00	3.20	58	6-90
3-Foot /	-131-0			With th	e W	ind	. 4-					
2	132.6			Aga	inst	17	a. 4					
3	133.0			"		"	£3-				d	0
4	133.4				"	19	6			6	1	c
5	134.0			"		"	Pace,					
6	133.3				99	"		135	8			
7	132.0			"		"		11.5				
8	133.0				79	"	# L					-
9	133-3			77		"	Length					
10	13206				22	"	70	1	2 3	4	5	6 7
11	133.0	133-02	3-01	,,	1	"	9	peed o	f Wall	ing, I	t. per	Sec ., 5 .
1	(10-2)									1		



remove the distant pole, prolong the line by successive 100foot sights and note the error at distant hub. Repeat

process for 200-foot and 300-foot sights.

(c) Methods.—(1) Set distant flag pole precisely behind hub and hold spike of pole on tack of near hub; lying on ground back of near hub, line in pole 100 feet (paced) distant; remove pole from distant hub, and prolong by 100foot sights up to distant hub, noting error to nearest 0.01 foot. (2) Repeat in reverse direction, using 200-foot sights. (3) Repeat with 300-foot sights. Avoid all bias. Record data in suitable form, describing steps concisely.

PROBLEM A5. STANDARDIZING CHAIN OR TAPE.

- (a) Equipment.—Chain or tape assigned in any problem where standard length of chain may be of value.
- (b) Problem.—Determine the length of the assigned chain or tape by comparison with the official standard under the conditions of actual use.
- (c) Methods.—In standardizing tape, reproduce the conditions of actual use as regards tension, support, etc., bring one end graduation of chain or tape to coincide with one standard mark, and observe fraction at the other end with a scale. As a general rule, observe one more decimal place than is taken in the actual chaining.

PROBLEM A6. DISTANCES WITH SURVEYORS' CHAIN.

- (a) Equipment.—Surveyors' chain, set of chaining pins, 2 plumb bobs, 2 flag poles (unless instructed otherwise).
- (b) Problem.—On an assigned chaining course about one mile long measure distances with the surveyors' chain to the nearest 0.1 link, and repeat the measurements in the opposite direction.
- (c) Methods.—(1) Standardize the chain before and after, as prescribed in A5. (2) Chain along the assigned course, noting the distances from the starting point to the several intermediate points and to the end station. Observe fractions to the nearest 0.1 link by estimation. (3) Repeat the chaining in the opposite direction, noting the distances from the end point, as before. The difference between the totals in the two directions should not exceed 1: 3,000. Retain the same party organization throughout the problem. Record the data as in the prescribed form.

	No.	DIST	NCES	WIT	H	SURY	/EYO	R'S C	HAIN .	
Line	Direction Chained			Ratio 1: d	Coef. C Lk.	Sept-1	8, 14	(2 Hour	Doe; Rear Ch s) Clear and Mº 210, Loc	d Cool-
Chain	Before	1-0020	Cit		LK.				th official	
"	After	1.0022							after day's	
A-B	E.	7.327							ning Course	
A-C	17	30-306			1 1	beg	innin	ng at hu	b with tack	k, marked
A-D	29	60-357							ke, located	
A-E	"	79-838	1			OF	W. bi	rick wa	k on Green	St; at E.
E-D	W.	19-479	1		1				hews Ave-,	
E-C	"	49.531	1						along said .	
E-B	"	72.506	1						Ik. to tack	
E-A	77		0.005	1:15970	0.06				nd E, the to	
346		*L		CYL or					aint A being	
			1000	G	1 12				rse in the	
				See D.	iagram)				total dist	
					1	From	Hub	E.		
Note:	- The a						ions d	Falink	were estin	ated - Pocker
					scussing	[U]	e was	s used in	standardiz	ing chain.
	the p	recisi	n of c	hainin	9.			W.	→E.	
						A	B	C	D	E
						0	<u> </u>	_	0	
	1					100	Hub	Hub	90	Hub
					1		4	1	4	*

PROBLEM A7. DISTANCES WITH THE ENGINEERS' CHAIN.

- (a) Equipment.—Engineers' chain, set of chaining pins, 2 plumb bobs, 2 flag poles (unless instructed otherwise).
- (b) Problem.—On an assigned chaining course about one mile long measure distances with the engineers' chain to the nearest 0.1 foot, and repeat the measurements in the opposite direction.
- (c) Methods.—(1) Standardize the chain before and after, as prescribed in A5. (2) Chain along the assigned course, noting the distances from the starting point to the several intermediate points and to the end station. Observe fractions to the nearest 0.1 foot by estimation. (3) Repeat the chaining in the opposite direction, noting the distances from the end point, as before. The difference between the totals in the two directions should not exceed 1:3,000. Retain the same party organization throughout the problem. Record the data as in the form.

PROBLEM A8. DISTANCE WITH 100-FOOT STEEL TAPE.

(a) Equipment.—100-foot steel band tape with end foot graduated to tenths, set of chaining pins, 2 plumb bobs, 2 flag poles (unless instructed otherwise).

(b) Problem.—On an assigned chaining course about one mile long measure distances with the 100-foot steel band tape to the nearest 0.01 foot, and repeat the measurements

in the opposite direction.

(c) Methods.—(1) Standardize before and after, as prescribed in A5. (2) Chain along the assigned course, noting the distances from the starting point to the several intermediate points and to the end station. In observing the fractions, first determine the foot units, then estimate the nearest 0.1 foot, then shift the tape along one foot and read the exact fraction on the end of the tape, estimating the nearest 0.01 foot. (3) Repeat the measurement in the opposite direction, noting the distances from the end point, as before. The difference between the totals in the two directions should not exceed 1:5,000. Retain the same party organization. Record data as in the form.

PROBLEM A9. HORIZONTAL DISTANCE ON SLOPE WITH STEEL TAPE.

- (a) Equipment.—100-foot steel tape with etched graduations to 0.01 foot, set of chaining pins, 2 plumb bobs, 3 flag poles, axe, supply of pegs, engineers' level and rod (unless otherwise instructed).
- (b) Problem.—Determine the horizontal distance between two assigned points on a steep slope, (1) by direct horizontal measurement, and (2) by measurement on the slope and reduction to the horizontal.
 - (c) Methods.—(1) Standardize the tape for each method, as prescribed in A5, both before and after the day's chaining. (2) In chaining down hill, rear chainman lines in flag pole in hand of head chainman, then holds tape end to tack on hub; flagman stands 50 feet or more from line opposite middle of tape and directs head chainman in leveling front end, then supports middle point of tape under direction of head chainman; head chainman, with spring balance attached to tape and using pole as help to steady pull, brings tension to 12 pounds; recorder plumbs down front end, and sets pin slanting sidewise. After checking the pin, proceed

Line	Direction Chained	Observed		Ratio 1:d	CoeF	ENGINEER'S CHAIN - Head Chainman, R-Roe-Rear Chainman, J-Doe Sept-19, '14 (2 Hours) Cloudy & Cool - Used 100 Ft- Chain Nº 63, Locker Nº 35 -
Chain	Before	100:10				Compared chain with official standard
"	AFter	100-12				both before and after day's chaining
A-B	E.	484.0				Chained along chaining course "A",
A-C	"	2002-2				beginning at hub with tack, marked
A-0	27	3987-5				A on guard stake, located at 5.
A-E	•"	5274.6	1			edge of N. brick walk on Green St. at E. curb line of Mathews Ave.,
E-D	W.	1286.9	11			Urbana, Ille; thence E'ly along said
E-C	11	3272.4	!			5-line of M. brick walk, observing
E-B	22	4790-2	1			distances to nearest 0.1 Ft. to
E-A	"	5274:3 L=1 52:74:3		1:17580 CYI or	11 C= E	tacked hubs B, C, D and E, the total distances From starting point A being noted. Chained same course in the reverse
Note:			ata wi	Il be us	ed in	direction, carrying total distances
	2 500	sequer	at proc	lem in	discuss-	Fractions of a Foot were estimated.
	ing th	e prec.	ision o.	chail	ing.	A pocket rule was used to compare
						chain with standard.
			1 -			W <> E
						AB C D E
						0-0-0-0
						Hub Hub Hub
	-			1		F F F F

Line	Direction Chained	Length	Diff. of Total	WITI! Ratio 1:d	CoeF C.	Sept-2	0,14 · Roe 5	(2 hours	PE Rear Ci Clear, m. e Nº312, Lo	oderate. cker 35
Tape	Before		Ft.		Ft.	60	th befo	ore and	h official: after day:	s chaining-
"		100-008							ion with eng	
A-B	E.	484:58				Chaine	ed aloi	ng Chair	ing Course	A, previ-
A-C	"	2003.79							ith Gunter	
A-D A-E	"	3991-69 5279:48							observing	
E-D E-C E-B E-A	W.	1287-83 3275-72 4794-96 5279-57 L= 52-7957	F =	1:58660 CVL or	CE E	ou E Chain Frac to	to near	ences to est of a forest of a	hubs B, C	direction- timated end Foot
	197		10000	agram			V	V	-E	
Note.	- The					A	В	C	0	E
	disc	subseq ussing ining				Hub S	Hub	Hub	Hub	Hub o

with the next 100 feet. In chaining up hill, follow same general method, using plumb bob at rear end. In leveling the tape the tendency will be to get the down hill end too low. Chain the line in duplicate, retaining the same organization. (3) Chain the line again in duplicate, tape lying on the ground, pull 12 pounds, pins set plumb, fraction direct to nearest 0.01 foot. Set temporary pegs flush with ground every 100 feet and also at intermediate sudden changes of slope, for levels. Determine differences of elevation between successive pegs, unless the leveling data are supplied to the party. Record data and make reductions and comparisons as in the form.

PROBLEM A10. ANGLES OF A TRIANGLE WITH TAPE.

- (a) Equipment.—100-foot steel tape, 50-foot metallic tape, set of chaining pins, 2 plumb bobs, 2 flag poles, five-place tables of trigonometric functions (each member of party to have tables).
- (b) Problem.—Measure the angles of an assigned triangle with the steel tape and also with the metallic tape, the error of closure not to exceed 3 minutes.
- (c) Methods.—(1) Measure each angle with the steel tape by both the chord and tangent methods, 100-foot radius, the difference in the two results not to exceed 2 minutes. If the angle is near 90°, the tangent method may be applied to the bisected angle. (2) After securing satisfactory check on an angle with the steel tape, make a rapid but careful measurement with the metallic tape, radius 50 feet. The results may be taken to the nearest half minute. (3) Measure at least one angle, preferably on smooth ground, by laying out an arc with radius of 57.3 feet, setting pins every few feet, and measuring the actual arc. Give close attention to alinement throughout. Record data and make reductions as in the form.

PROBLEM A11. SURVEY OF FIELD WITH STEEL TAPE.

- (a) Equipment.—100-foot steel tape, set of chaining pins, 2 plumb bobs, 4 flag poles, five-place table of functions.
- (b) Problem.—Make survey of an assigned field with tape, collecting all data required for plotting the field and calculating its area by the "perpendicular," "three-side," and "angle" methods.

_						
Hor	ZONTA	L DIST	ANCE	Δ14-	A17	Hd Chain, J. Doe RA Chain, R. Roe-
			tal Mea			Recorder, B.F. Keen. Flagman, G.W. Sure.
No.	Ohserved	Mean	Cor. for	Reduced	DIFF.(F)	Sept-21, 14. (3 Hours) Cloudy; moderate.
110.					Coef. (C)	
	Ft.	Ft.	Ft.		Ratio (1:d)	
T 1	99.995		11.		Katio(1.0)	1st. Method: Standardized tape (before and
Tape 1		99.996			F=0-04	
" "		33.330			c= 0.015	
1	761-45	201 12	1 12	701.44	1:25380	
2	761-49		-0.03	101.44		
6000		40000-0			(See. *	
100		030			Diagram	
						leaning sidewise.
					pe and	Reduction to the Horizontal
No-					Diff. (E)	
PITT					Coef (C)	
	Ft.	Ft.	Ft.	Ft.	Ratio(1:d)	
	100-007		1			Chained line in duplicate, tape supported on
2	100-008	100-008			E=0.02	
1	761-81				c=0.007	
2	761-79	761-80	+0.06	761-86	1:38590	
Correct	ion For	Inclinati	on	-0.47	(500 K	Ran levels over line with following results:
Reduced	Horizon	al Meas	urement	761-39	Diagram)	C 3 32 d
Result	by First	Metho	d	761-44	Viegrain	100 +3.5 12.25 0.06 6
Differe	nce bet	veen Re	sults	0.05	= E	100 +3.7° 13.69 0.07 100 +4.1 16.81 0.08 b
	of Two			761.42	c=0-018'	100 +2.8 7.84 0.04 With a small
			1		1:15230	100 +4.5 20.25 0.10 1 8 (4 -1)
			1			100 +3-1 9-61 0-05 0=2c (nearly)
-			1	1	1	762 -0.47 = Zd

6	ANGLE S OF TRIANGLE Trigo- Functions Name Value Sin-460 0-4050 25 33-5 47 47 47 47 47 47 47 47 47 47 47 47 47	5-6-8 WITH TAPE. Surveyors, J. Doe and R. Roe. Sept. 22, "14. (2 Hours) Used Roe 100-FF. Steel Tape, 16-362, and Lufkin 50-FF. Metallic Tape, 16-411, Lkr. 35. Though not needed in problem, noted the
8	JIN-2(8) 0.3696 21 41.3 43 23	
"	Tan-(8) 0.9450 43°23' 43°23'	lengths of tapes by standard, 100-01
5	Sin-1(5) 0.6995 4423 8846	and 50.01 ft., respectively.
"	Tan-15) 0.9796 44245 88°491	Measured each angle by chord method and
"	5in- ± (5) 0-6997 44°24' 88°48'	checked by tangent method, using radius
Che	Tam-\frac{1}{2}(5) 0.9799	of 100 ft with steel tape In measuring 15, (nearly 90°) the tangent method was applied to the bisected angle · Each angle was verified before proceeding to next, a difference of 2' being allow- ed in each.
	Sin-tA- tA. A.	After an angle was thus verified, a rapid
	0-4051 23°54' 47°48'	but careful measurement was made
	0-3696 21°41.5 43°23'	with metallic tape, by chord method
5	0.6999 44°25' 88°50'	only, using 50-ft. radius.
9	180°01'	Used Flagpoles for distant and pins for
Angle 6	ing equal weight to the three results by tape, the most probable values are: 47475 45233 88494 180°00'	

(c) Methods.—(1) Standardize the tape once. (2) Examine the field carefully and plan the survey. (3) Measure the required angles with tape. (4) Locate the perpendiculars. (5) Chain all necessary lines, and also take distances to feet of perpendiculars. Follow the form.

PROBLEM A12. AREA OF FIELD BY PERPENDICULAR METHOD.

- (a) Equipment.—Five-place logarithms.
- (b) Problem.—Calculate the area of the assigned field by the perpendicular method, using the data collected in Problem A11.
- (c) Methods.—(1) Prepare form for calculations; transcribe data, and carefully verify transcript. (2) Calculate double areas of the several triangles by contracted multiplication, perpendicular method, preserving a consistent degree of precision. (3) Make the same calculations with logarithms, as a check. (4) Combine the verified results, as shown in the form.

PROBLEM A13. AREA OF FIELD BY THREE-SIDE METHOD.

- (a) Equipment.—Five-place logarithms.
- (b) Problem.—Calculate the area of the assigned field by the three-side method, using data collected in A11.
- (c) Methods.—(1) Prepare form for calculation; transcribe data, and carefully verify transcript. (2) Calculate the areas of the several triangles by logarithms, three-side method, preserving proper units in the results. (3) Carefully review the calculations, and combine the verified results, as in the form.

PROBLEM A14. AREA OF FIELD BY ANGLE METHOD.

- (a) Equipment.—Five-place logarithms.
- (b) Problem.—Calculate the area of the assigned field by the "two sides and included angle" method, using the data collected in A11.
- (c) Methods.—(1) Prepare form, transcribe data, and verify copy. (2) Calculate the double areas of the several triangles by contracted multiplication, angle method, preserving consistent accuracy in results. (3) Make same cal-

SUR	VEY OF	FIELD	A-B-	C-D-E	WITH	TAPE . (DATA FOR AREA AND PLAT.)
Angle	Sin & A		A	Proof		Head Chainman, R. Roe.
ABE	-2968	17961	34321	1.		Rear Chainman, J. Doe.
EBD	-7131	45 29.5	90°591	190 101		Sept-25, 14 . (3 Hours) Cloudy & Cool-
DBC	-5347	32995	64°391	180°00'		Used Roe 100 Ft. Steel Tape Nº 361, Locker #35
ABd	-0888	5061	100121	10°10	1	Standardized tape before only-
	1				1	Let fall perpendiculars Aa, Bb and Bc by
						First estimating positions of a, b and
Line	Observ'd	Cor. for	Reduced			c, then erecting precise perpendiculars
	Length	Standard	Length		1	and shifting as required . Set pegs
	Ft.	Ft-	Ft.			at points a, b and c.
Sept-25						Measured angles ABE, EBD and DBC with
Tape	99.992					tape by chord method, 100 ft. radius,
Sept-26						and checked by measuring angle be-
Tape	99.980	100				tween AB and Bd (line CB prolonged)
AB	336.83	-0.07	336.76			Sept-26, (2 Hours) Drizzling & Cold.
BC	465.07	-0.09	464.98			Chained each line carefully once.
CD	483.82	-0.10	483.72			Sketch shows reduced values.
DE	616.65	-0.12	616.53		1	464.98
EA	241.89	-0.05	241.84			
BE	425.93		425.84			A 336.76
BD	438-70	-0.09	438-61			8 60-1
Aa	190.69	-0.04	190-65			3 190 39 7 5 618
Ea	147.90	-0.03	147.87			1 8 3 8 DI 18 8 W
Bb	302-16	- 0.06	302-10			8 1 10 8
Db	318-05	-0.06	317-99	- 3	1	b 5 4-317.99
BC	381-49	-0.08	381-41		1	E 616'53
DC	265-90	-0.05	265.85			

						Sept-27,14.	Compute	r, J.Doe.	
COM	UTATI	N OF	AREA	of Fi		A-B-C-D-E, PE	RPENDI	CULAR	METHOD.
Triangle		Base, b	Altitude, a	Multipli-	Logar-			$Area = \frac{1}{2}$	ab.
ABE	BE Aa	F†- 425-84	Ft. 190-65	cation 425.84 56.091 42584 38326 256 21 8/187	ithms 2-62925 2-28024 4-90949 (81190)	5q. Ft. Data From ; Transcript 81 190	hecked.	nearest	b 10 5q. Ft.)
BDE	De Bb	616-53	302-10	616.53 01.203 184959 1233 62 186254	2-78995 2-48015 5-27010 (186 250)	186 250		. "	" " "
BĊD	CD Bc	483.72	381-41	483.72 14.183 14.5116 38698 484 193 5 184.496	5.26598 (184500)	18.7 500			" " " " st 0.001Ac-)
43,56 Acre 15q-F:	0. $5pec$ = 43.56 = 6×6 = 0.006	luce square squa	Feet = 1 Ac. = 996 Ac.	given 0 square 1 43560 of the	chains. Ac.	5hort Division 6/225970 6/37661-667 11/6276-944 11/570-631 10/51-876 5-1876	Contract 225970] 217800 8170 4356 3814 3485 329 305 24	ed Div'n (225970 075922000000 45194 4519 2034 113 16 5-1876
sho	wn in	the app	Vication	oppos	vre.		26		

culations by logarithms, as a check. (4) Combine the checked results. Follow the form.

PROBLEM A15. AREA OF FIELD FROM PLAT.

- (a) Equipment.—Drafting instruments, paper, etc., planimeter (as assigned).
- (b) Problem.—Determine the area of the assigned field directly from the plat.
- (c) Methods.—(1) Make an accurate plat of the field from the notes secured in A11, using a prescribed scale. (2) Determine the area of the field by resolving the polygon into an equivalent triangle. (3) Determine the area from the plat by the polar planimeter and by one of the following "home-made" planimeters: "bird shot" planimeter, "jack knife" planimeter, cross-section paper, parallel strip, weighing, etc. (4) Prepare on the plat a tabulated comparison of results secured by the several methods. (5) Finish the plat, as required.

PROBLEM A16. SURVEY OF FIELD WITH CURVED BOUNDARY.

(a) Equipment.—100-foot tape, 50-foot metallic tape, set of chaining pins, 2 plumb bobs, 4 flag poles.

(b) Problem.—Make survey with tape of an assigned tract having a curved boundary, collecting all data required for

plotting the field and calculating its area.

(c) Methods.—(1) Standardize the tape once to nearest 0.01 foot. (2) Examine the tract carefully and plan the survey so as to secure a simple layout of base lines designed to give short offsets to the curved boundaries. (3) Locate the perpendiculars, if any, and chain all lines; on the curved sides, take offsets so as to secure a definite location, and as a rule take equal intervals on the same line. Follow the form.

PROBLEM A17. AREA OF FIELD WITH CURVED BOUNDARY.

- (a) Equipment.—(No instrumental equipment required).
- (b) Problem.—Calculate the area of the assigned field with curved boundary by "Simpson's one-third rule," using the data collected in Problem A16.

Сом	PUTAT	ION O	F ARE	A OF	FIELD		D-E, 3 SIDE		D.
Triangle				(5-a)	(s-b)		Area of Triangle		
	Line		2(a+b+c)				√s(s-a)(s-b)(s-c)		
1	200	Ft.	Ft.	Ft.	Ft.	Ft	Logarithms	5q.Ft.	\wedge
ABE	AB=a		502-22				2.70089		18/ 6
63. 1	BE= b	425.84		165.46	20.70		2.21869		
		241.84			76.38	260.38	1.88298		C
9777	5=	502.22				200.38	2) 9-21817		
ES.P.	5=	302.22					4.60908	40 650	(To near-
76.	2019						4.00300	40 000	est 10 sq.ft.
BDE	BD=a	438.61	740-49				2.86952		EST 10 39.11.
222	DE=b	616.53		301-88			2.47983		
Park !	EB=c	425.84		20,00	123.96		2.09328		
		1480-98			,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	314.65	2.49783		1
875	1	740-49					2) 9.94046		
644							4.97023	93 380	
BCD	BC=a	461.98	693-66				2.84115		
DUD	CD=b	483.72	033 00	228-68			2.35923		
-	Db=c	438-61		22000	209.94		2.32210		
		1387-31			2000	255.05			1
	-2	693-66				200 00	2) 9.92910		
							4.96455	92 160	
			7				5-35447	226 190	5-193 Ac.
Data	From p	10.	Transc	ript ch	ecked.		-4-63909		
							0-71538		

Сом	UTAT	OH OF	AREA	OF I	IELD	5ept-22, 14 A-B-C-D-E	ANGLE	METH	op.
Triangle	Part	Value				Double Areas		Area = 2	ab sin.C.
ABE	AB= 8 BE= b ABE= C	336·76 425·84	202	190-91 48-524 76364 38/8 955 153 8	2.52732 2.62925 9.75350 4.91007	Data from Transcript	checked.	_	6
F10-1			19091	81298	(81300)	81 300	(Result to	nearest	10 5g.Ft.)
BDE	8E=a 8D=b E8D=C	425-84 438-61 90°591	38326 38326 3833 83 34	170312 12773 3406 255	2.62925 2.64208 9.99994 5.27127 (186750)	186 750	,, ,,	"	"""
BCD	BD=8 BC=b DBC=C	438-61 464-98 64°39'	438.61 17309.0 39475 132 31 396.38	396·38 89·464 158552 23783 1586 357	2.64208 2.66743 9.95603 5.26554				
200				184309	(184 310)	184 310	29 19	"	11 11 11
					5-35446	2] 452 360			
Y				_		(÷ 43560)	(Kesuit I	neares	st 0.001 Ac-
-					0-71537	(5-192 Ac-)			
4									

(c) Methods.—(1) Prepare form for calculation; transcribe data in convenient form for calculation, and carefully check copy. (2) Calculate the area of the polygon formed by the base lines, preferably by the perpendicular method. (3) Calculate the areas of the curved figures by "Simpson's one-third rule," which is as follows: "Divide the base line into an even number of equal parts and erect ordinates at the points of division; then add together the first and last ordinates, twice the sum of all the other odd ordinates, and four times the sum of all the even ordinates; multiply the sum by one-third of the common distance between ordinates." (The field notes might have been taken with special reference to the rule, but it is better to take from the notes the largest even number of equal segments, assuming the remaining portion to be trapezoid or triangle.) signs to the several results by reference to the field sketch, and combine them algebraically to get the net area, as shown in the accompanying form.

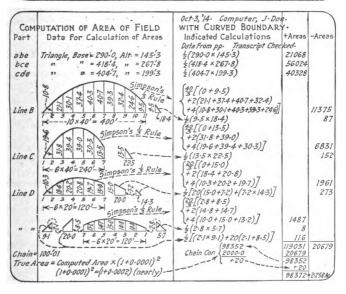
PROBLEM A18. AREA OF FIELD WITH CURVED BOUNDARY FROM PLAT.

- (a) Equipment.—Drafting instruments, paper, etc., planimeter (as assigned).
- (b) Problems.—Determine the area of the field with curved boundary directly from the plat.
- (c) Methods.—(1) Make an accurate plat of the field from the notes obtained in A16, using a prescribed scale. (2) Determine its area directly from plat by two methods mentioned in (3) of A15, other than those used in that problem. (3) Prepare on the plat a tabulated comparison of the results by the several methods. (4) Finish the plat, as required.

PROBLEM A19. PASSING AN OBSTACLE WITH TAPE.

- (a) Equipment.—100-foot steel tape, set of chaining pins, plumb bobs, 4 flag poles.
- (b) Problem.—Prolong an assigned line through an assumed obstacle by one method and prove by another, finally checking on a precise point previously established.
- (c) Methods.—Given two hubs, A and B, 200 feet apart prolong line and establish C 200 feet from B: (1) by constructing a 200-foot square in one direction; and (2) by lay-

	Su	RVEY	OF FI	ELD V	HTIV	CURVED BOUNDARY LINE.
Offset L	Dist-	Offset R	Offset L	Dist.	Offset R	Head Chainman, R. Roe. Rear Chainman, J. Doe.
Ft-	Fho	Ft.	Ft-	Ft.	Ff.	Oct. 2, 14. (3 Hours) Clear and warm.
0	262.5	= d		1111		Tape Nº361, Locker Nº35 = 100:01
13.5	240					Sketch shows observed lengths . Final
30.3	200		e=	309-1	0	area result corrected for standard
39.0	160			300	2.1	
39.4	120			280	8.5	
31.8	80			260	13.2	ď
19.6	40			240	14.7	Line C. Cles's)
.0	0			220	15-0	2 F R62's
	Line C	(c to d	7	200	14.8	23 / 2
		-		180	10.0	is to
0	418.4	= 0		160	2.8	13/10
9.5	400		0	154.3	0	A water M
24.6	360	+	7.2	140		L' (1047) h
32.4	320	1	15.0	120		P 6 14.
39.3	280		19.7	100		Line 6 (4041)
40-7	240		20.8	80	1	e &
40.3	200		20.2	60		6 767.8
37.4	160		18.4	40		6 13
30.1	120		10-3	20		(6:502)
21.2	. 80		0	0	= d	19
10.8	40			Line D	(d toe)	Time F.
0	0	= 6		100:01		Line A (209.3)
	Line B	(b toc)			& warm	a & Line A (209.5) B
(Read Up)	4		Read Up	1	



ing off a 200-foot equilateral triangle on the opposite side using pins to mark points thus established. (3) Prolong the line by each method to the hub D, 200 feet from C, and record discrepancies in line. (4) Interpolate a point at C on true line between B and D, and note errors of prolongation at C. Record as in the form.

PROBLEM A20. OBSTRUCTED DISTANCE WITH TAPE.

- (a) Equipment.—100-foot steel tape, set of chaining pins, 2 plumb bobs, 4 flag poles.
- (b) Problem.—Determine the distance between two assigned points through an assumed obstruction to both vision and measurement, using two independent methods, and finally chain the actual distance.
- (c) Methods.—(1) Standardize the tape. (2) Determine the distance between the assigned points by constructing a line parallel to the given line, and equal or bearing a known relation to it. (3) Secure a second result by running a random line from one hub past the other so that a perpendicular less than 100 feet long may be let fall, measuring the two sides and calculating the hypothenuse. (4) After securing two results differing by not more than 1: 1,000, chain the actual distance. Follow the form.

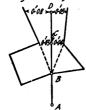
PROBLEM A21. RUNNING IN CURVE WITH TAPE.

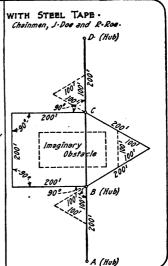
- (a) Equipment.—100-foot steel tape, 50-foot metallic tape, set of chaining pins, 2 plumb bobs, 3 hubs, 6 flat stakes, marking crayon, tacks, five-place table of functions.
- (b) Problem.—Lay out two lines making an assigned angle with each other, and connect them with a prescribed curve by the "chord offset" method.
- (c) Methods.—(1) Calculate the radius, R, for the given degree of curve, D. (2) Calculate the tangent distance, T, for the given radius, R, and angle of intersection, I. (3) Calculate the chord offset, d, and tangent offset, t, for the known radius, R, chord, c and degree, D. (4) At the given point intersection (P. I.), A, lay off the given angle, I, by the chord method. (5) From the P. I. lay off T along the two tangent lines and locate point tangent (P. T.) and point curve (P. C.), setting hubs at P. C. and P. T., with guard stake at each hub. (6) Run in the curve, by chord offsets, beginning at P. C. and checking at P. T. Calling P.

PASSING AN OBSTACLE

Oct 4, 14, (2 Hours) Clear and warmTape 10-361, Locker 10-35, Length = 100-016ivan three hubs, (set on true line by
transit), 8 200 Ft. From A, and D
400 Ft. beyond B, all on smooth groundAssumed obstacle as shown in sketch,
and then (ignoring D) passed obstacle
by 200 Ft. equilateral triangle to right
and by 200 Ft. square to left. Resumed
line by each method and prolonged to
point D. Used pins marked by slips
of paper to indicate points.
Also interpolated C on BD carefully by

eye. Results are given in diagram below.





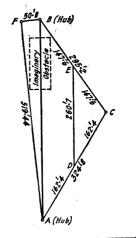
CBSTRUCTED DISTANCE

Oct. 5. 14 (2 Hours) Cloudy and cool-Tape No.361, Locker No.35, Length 99:99 Given two hubs A and B an unknown distance apart, on smooth ground. Assumed an obstruction to vision and measurement, as shown in sketch. Selected point C visible From A and B, chained CA and CB, observing nearest 0-1 ft. and bisected CA at D and CB at E. Chained DE. Then calculated AB by doubling ED. 260-7 x 2 = 521-4 Ran random line From A as close as practicable to obstruction so as to reduce BF to a minimum · Let fall perpendicular BF from B on random line . Measured BF and FA to nearest 0-1 ft - Calculated hypothenuse AB . AB = \$\sqrt{50.82 + 519.42 = 521.0}

Finally, after securing the above results, chained the actual distance AB. The three results are sumarized below-

Method ·	Obs-Dist-	Std-Cor-	Red-Dist-
			521:3
By right triangle	521.0	-0.1	520.9
By actual measurement	521.5	-0.1	521.4
Total range = /			

WITH STEEL TAPE . Chainmen, J. Doe and R. Ros.



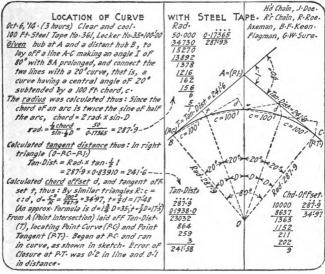
C. Station 0, establish Station 1 by laying off tangent offset, t, and chord, c. Having one station on the curve, the next is located by prolonging the chord and forming an isosceles triangle having the chord offset as a base. Check on the P. T., noting the discrepancy of distance and line. Also establish the tangent again by tangent offset and observe the error of line. Follow the form.

PROBLEM A22. DISCUSSION OF ERRORS OF CHAINING

- (a) Equipment.—(No instrumental equipment, unless further data are desired, in which case Problems A6, A7 and A8 may be assigned again).
- (b) Problem.—Investigate the errors of linear measurement with the several kinds of chains and tape, with the view to determine practical working tests or coefficients of precision for actual use.
- (c) Methods.—Assume that the conditions in Problems A6, A7 and A8 are practically constant in the same problem, and that the actual differences between observed lengths of the several segments when chained in opposite diretions, represent the normal errors with the particular chain and chainmen; then tabulate: (1) the measured lengths of all possible segments of the chaining course, either from direct observation or by subtraction; (2) the actual errors or differences between the two results, giving signs; (3) the chaining ratios, l: d, and the decimal expressions of the same to six places; (4) the "coefficients of precision" for each case, calculated by formula, or more quickly, taken from the diagram in the chapter on errors of surveying; (5) the mean decimal chaining ratio and its equivalent; and (6) the mean coefficient of precision. Follow the form.

PROBLEM A23. TESTING (OR ESTABLISHING) AN OF-FICIAL STANDARD OF LENGTH.

- (a) Equipment.—Standard tape (with certified length given), turnbuckle adjustments with bolts, spring balance, standard steel rule graduated to 0.01 inch, 2 thermometers, 2 microscopes, strips of wood, a watch.
- (b) Problem.—Make a series of ten observations with a standardized steel tape for the purpose of testing (or establishing) an official standard of length, observing the nearest 0.0001 foot. (The Bureau of Standards, Washington, D. C., will standardize a tape for a small fee.)



		Discu	5510N	of Er	RORS		9,14 · CO.		APE .		
Line	Direction	Observed	Differ-	Chaining	Coef of	Data	From pp	. 7	ranscrip	+ O.K	
	Chained	Length Ft.	ence, E Ft.	Ratio 1:d	Precision (C), Ft.			C			E
A-B	E.	484.58	E+ W-	0.000062			Dista	nces	by Subti	ractio	n.
B-A	W-	484.61		1:16150		B-A	5279.57				5279-57
A-C	E.	2003-79	(0-000029		E-B	4794.96	F-C	3275-72	E-D	1287-83
C-A	W.	2003-85	-0.06			B-A	484.61	C-A	2003-85	D-A	3991-74
A-D	E.	3991-69		0-000012				1			
D-A	W.	3991-74		1:79830		A-C	2003-79	E-B	4794.96	A-D	3991-69
A-E	E.	5279.48		0-000017	1	A-B	484.58	E-C	3275-72	A-B	484.58
E-A	W.	5279-57		1:58660	0.012		1519-21		1519-24		
B-C	E.	1519-21		0-000019							
C-B	W-	1519-24	-0.03	1:50640	0.008	E-B	4794.96	A-E	5279.48	A-D	3991-69
B-D	E.	3507-11		0.000006		E-D	1287.83	A-B	484.58	A-C	2003-79
D-B	W-	3507-13		1:175350		D-B	3507-13	B-E	4794.90	C-D	1987.90
B-E	E.	4794.90		0.000012						1	
E-B	W.	4794.96		1:78250		B-C	3275-72	A-E	5278-48	A-E	5279.48
C-D	E.	1987.90		0.000005		E-D	1287-83	A-C	2003-79	A-D	3991-69
D-C	W.	1987-89		1:198790		D-C	1987-89	C-E	3279-69	D-E	1287-75
C-E	E.	3275-69		0.000009							
E-C	W.	3275-72	-0.03	1:109190	0.005	Desi	gnating E	+ and	1 W- (4t)	Colui	nn) it is
D-E	E.	1287-79		0.000030					vrning re		
E-D	W.	1287-73		1:32920					This is		
	77.7	(L. in		0-000202	0.085				ngths, vi		
		100-Ft.	Mean =	1:49500	0-008 E	=100.011, after = 100.008, i.e. the tape gradually decreased in length, causin					tape
		will b)	E=CVE (See Diag	OF (C =	FI				d length		sosing

(c) Methods.—(If a new official standard is being established, one standard mark may be made permanent, and the precise distance taken to an approximate temporary point on the other bolt, the exact correction being applied after a sufficient number of results have been obtained. If the sun is shining, the tape should be protected by a wooden box or other covering throughout its length. Cloudy days or night time give best results. The observations should be made briskly so as to have slight range of temperature.

Oct. IQ '14. Cloudy and Cool.	Party: J.Doe, R.Roe, B.F.Keen, G.W.Sure-							
TEST OF 100-FT STANDARD	UNIVERSITY.							
Selected cloudy day with slight range of	temperature during period of observations.							
Used Standard Tape No. 417, marked "U.S.W								
at 62°F with 12-16 pull, tape supporte	d, coefficient of expansion = 0.0000061							
"Bolt Turnbuckle -Hook West Bolt	100' ATape _East Bolt Turnbuckle.							
	100 Standard - Zero 4"Bolt in Gaspipe							
Spring Balance	Zero & Bott in Gaspipe							
Program. Arranged "bucksaw" adjustments,								
	at east standard mark with reading glass.							
	Served Fraction at west standard mark,							
	Vin., estimating to nearest 0.001 in with							
	and observed time and temperature, two							
The moments praced one each at 35 and	67'- Released pull between observations							
No Time Temperature Temp Cor	Tape West Fraction Standard Prob. Error							
P.M. At 33' At 67' Mean 62º-Mh Ft.	Ft. In Ft. Ff- d(0001) d2							
1 2:23 52:0 53:0 52:5 9:5 0.0058	99-9909 0-116 0-0097 100-0008 1 1							
2 128 52.0 53.0 52.5 9.5 0.0058	99-9909 -118 -0098 100-0007 0 0							
3 :32 52.0 53.0 52.5 9.5 0.0058	99-9909 -116 -0097 100-0006 1 1							
4 35 52-0 53-0 52-5 9-5 0-0058	99-9909 -118 -0098 100-0007 0 0							
5 39 52.0 52.5 52.2 9.8 0.0060	99-9907 -121 -0101 100-0008 1 1							
6 46 52.0 52.5 52.2 9.8 0.0060	99-9907 -120 -0100 100-0007 0 0							
7 53 525 525 525 9.5 0.0058	99.9909 119 0099 100.0008 1							
8 58 52.5 52.0 52.2 9.8 0.00GO	99.9907 122 0102 100.0009 2 4							
9 3:04 52.0 52.0 52.0 10.0 0.0061	99-9906 -121 -0101 100-0007 0 0							
10 :08 52.0 52.0 52.0 10.0 0.0061	99.9906 122 0102 100.0008 1 1							
$\int_{0}^{\infty} E_{r} = 0.67 \sqrt{\frac{\sum_{i} d^{2}}{n-i}} = 0.000067 E_{m} = \frac{E_{r}}{In} = 0.000021$	Mean = 100.0007 \(\Sigma de = 9\) Length of Standard = 100.0007 \(\Delta 0.00002 \) Ft.							

If isolated standard monuments are used, their foundation should go below frost line, and the monuments should be located so as to suffer as little as possible from heaving. If the standard marks are indoors, the conditions are less difficult to control.)

(1) Arrange "bucksaw" or turnbuckle adjustments, each held firmly by a bolt dropped into a piece of gaspipe driven flush with surface of ground, with spring balance and tape lined up, as shown in sketch in accompanying form; place the two thermometers at the one-third points as nearly as possible under the actual conditions of the tape. (2) With

four men in party, No. 1 sets end graduation precisely at one standard mark by means of screw adjustments and microscope; No. 2 sets balance at 12 pounds; No. 3 observes fraction at other standard mark by means of steel scale graduated to 0.01 inch, estimating to nearest 0.001 inch (say 0.0001 foot) by microscope; and No. 4 records all data, observes time to nearest minute, and temperature to nearest 0.1 degree. Nos. 1, 2 and 3 should lie flat. Release the tension between observations. Record and reduce as in the form.

PROBLEM A24. DETERMINATION OF CONSTANTS OF A STEEL TAPE.

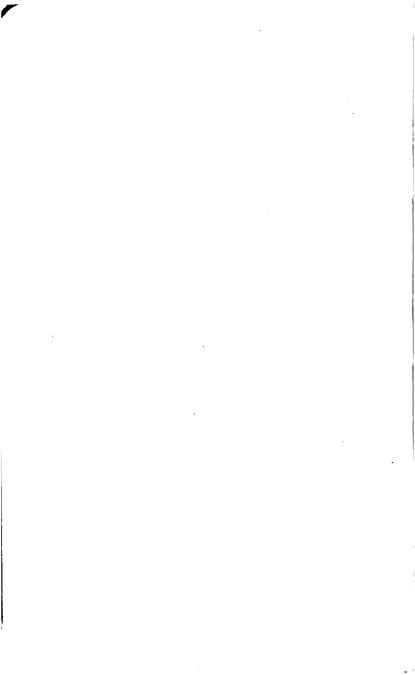
- (a) Equipment.—Steel tape and other articles named in preceding problem.
- (b) Problem.—Determine coefficients of expansion and stretch of the assigned tape.
 - (c) Methods.—(See Problem E9.)

PROBLEM A25. MAKING A STANDARD WIRE TAPE.

- (a) Equipment —Spring balance, thermometer, etc., as in A23, and a piece of piano or other suitable steel wire.
- (b) Problem.—Make a 100-foot or other standard tape by graduating the wire with reference to the official standard.
 - (c) Methods.—(To be devised by the student.)

PROBLEM A26. COMPARISON OF DIFFERENT MAKES AND TYPES OF CHAINS AND TAPES.

- (a) Equipment.—Department equipment and collection of catalogs of representative instrument makers.
- (b) Problem.—Make a critical comparison of the several types of chains and tapes made by different makers.
- (c) Methods.—Study the different catalogs and prepare a systematic and concise report.



CHAPTER III.

THE COMPASS.

Description.—The magnetic compass consists of a line of sight attached to a graduated circular box, at the center of which is a magnetic needle supported on a steel pivot. The compass box is attached to a tripod or jacob staff by a ball and socket joint, and is leveled by means of the plate levels. The needle should be strongly magnetized and have an agate cap to receive the point of the hardened steel pivot. The dip of the needle is counter-balanced by a small coil of wire, which can be shifted as desired. The E and W points are reversed.

In Fig. 10 are shown the usual types of magnetic compasses: (a) the vermer compass; (b) the plain compass;

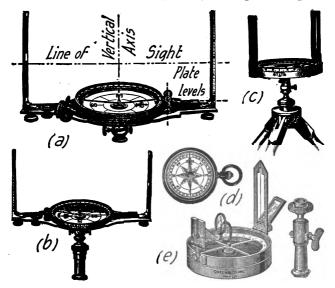
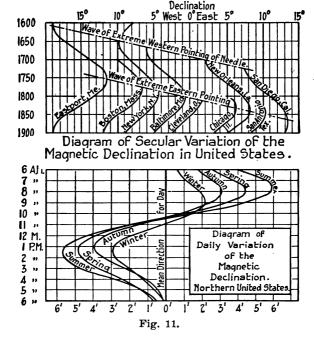


Fig. 10.—Types of Magnetic Compasses.

(c) the vernier pocket compass with folding sights; (d) the ordinary pocket compass; (e) the prismatic compass.

Declination of the Needle.—If the needle is allowed to swing freely, its magnetic axis will come to rest in the magnetic meridian. The horizontal angle between the magnetic meridian and the true meridian at any point is called the magnetic declination for that point. Imaginary lines joining points on the earth's surface having the same declination are called isogonic lines. The isogonic line joining the points of zero declination is called the agonic line. Fig. 12 is an isogonic chart of the United States. Of the three agonic lines on the earth's surface, one passes through Michigan, Ohio, etc.



(For additional data see bulletin of Department of Commerce, U. S. Coast and Geodetic Survey, entitled "Principal Facts of the Earth's Magnetism.")

Variation of the Declination.—The declination of the needle is not a constant at any place. The change or fluctuation is called the variation of the declination. The variations of the magnetic needle are of several kinds:

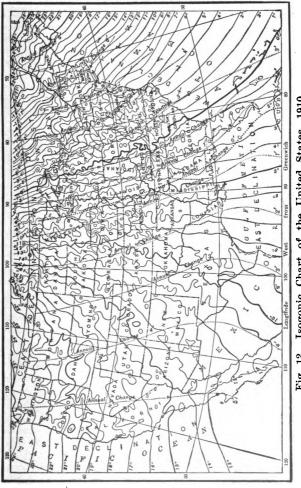
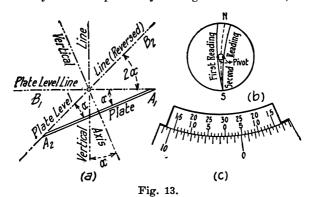


Fig. 12. Isogonic Chart of the United States, 1910.

secular, daily, annual, lunar, and irregular variations due to magnetic storms. The most important of these is the secular variation which is illustrated in the upper diagram of Fig. 11 for a series of representative points in the United States. This diagram shows that the extreme range or swing of the needle is roughly 6° or 7°, and that the period of time between extreme positions is about a century and a half. Also that the wave of magnetic influence progresses across the continent alike in successive cycles. In 1900 the needle was at its extreme western position at Eastport, Me., and at its extreme eastern position at San Diego, Cal. The 3° East isogonic line passed through western Indiana, and was moving westward at the rate of about 4' per year. This rate of change was general throughout the central part of the United States, and is represented by the straight sections of the curve in the upper diagram of Fig. 11.

The daily variation of the magnetic declination is shown graphically in the lower part of Fig. 11, the scale being greatly magnified laterally. It is seen that the needle undergoes each day a vibration similar in a general way to the grand swing of three centuries or so shown in the upper diagram. The magnitude of the daily movement in northern United States ranges from 5' in winter to nearly 12' in summer time. The needle is in its mean daily position between 10 and 11 a. m. for all seasons. The diagram represents the normal magnetic day, of which there are perhaps five or six per month.

Local Attraction.—The pointing of the needle is affected by the close proximity of magnetic substances, such



as iron ore, wire fences, railroad rails, etc. However, local attraction does not prevent correct work, provided back and fore sights are taken without change of magnetic conditions. It is therefore especially important to avoid disturbances of the needle by the chain, axe, passing vehicles, electric wires, etc., or by articles on the person of the observer, such as keys, knife, spectacle frame, wire in the hat rim, reading glass case, etc. Also the glass cover may become electrified by friction and attract the needle, in which case it may be discharged with the moistened finger, or by breathing on it.

The Vernier.—The vernier is an auxiliary scale used to read fractional parts of the divisions of the main scale or limb. Verniers are retrograde or direct, according as the divisions on the vernier are larger or smaller than those on the limb. The vernier used on compasses for the setting off of the declination is direct, and is usually of the type shown in (c) of Fig. 13. In reading a vernier of any kind, blunders may be avoided by first estimating the fraction by eye before noting the matched lines on the two scales.

USE OF THE COMPASS.

Use.—The compass is used: (1) to determine the bearings of lines; (2) to measure the angle formed by two lines; (3) to retrace old lines. The bearing of a line is the horizontal angle between the line and a meridian through one end of it. Bearings are measured from the north or south point 90° each way. The angle between two lines is the difference in their directions as indicated by the bearings. Having the true bearings of one side of a polygon, the true bearings of the others may be obtained by algebraic addition of the angles; or by using the declination vernier so as to read the true bearing direct on the fore sights.

Practical Hints.—Point the north end of the compass box along the line and read the north end of the needle. Protect the pivot from needless wear by turning the needle in about the proper direction before releasing it. Always lift the needle before disturbing the compass. Habitually obtain duplicate needle readings on each sighting. Read the needle by estimation to the nearest five minutes, that is, to the one-sixth part of one-half degree, which is the usual subdivision of the compass box. Care should be taken to avoid parallax in reading the needle.

ADJUSTMENTS AND TESTS.

Elementary Lines.—The elementary lines of the compass, shown in (a) of Fig. 10, are: (1) the line of sight; (2) the vertical axis; (3) the plate level lines.

The maker should see: (1) that the needle is strongly magnetized; (2) that the magnetic axis corresponds with the line joining the two ends; (3) that the metal in the compass box is non-magnetic; (4) that the line of sights passes through the center of graduation; (5) that the plates are perpendicular to the vertical axis; (6) that the zero of the vernier coincides with the line of sights.

The needle may be magnetized with a bar magnet or by putting it into the magnetic field of a dynamo. The metal of the compass box may be tested by reading the needle, then moving the vernier and noting if the needle has moved the same amount, this process being repeated at intervals around the full circle.

The Principle of Reversion.—In adjusting surveying instruments, the presence, direction and amount of the error are made evident by the method of reversions which doubles the apparent error. If there is no difference after reversion, there is no error.

Plate Levels.—To make the plane of the plate level lines perpendicular to the vertical axis.—Level up the instrument by means of the plate levels and reverse the compass box in azimuth, that is, turn it through a horizontal angle of 180°. Correct one-half the error, if any, by means of the adjusting screws at the end of the level tube, and bring the bubble to the center by the ball and socket joint. The reasons for this process are shown in (a) of Fig. 13.

Sights.—To make the plane of sights normal to the plane of the plate level lines.—With one sight removed and the instrument leveled, range in with the remaining sight two points as far apart vertically as possible, say on the side of a building. Reverse in azimuth and bring the bottom of the sight in range with the lower point; if the upper point is then in range, the sight is in adjustment. If not, correct one-half the error by putting paper under one side, or by filing off the other side. Repeat process for the other sight.

The Pivot.—To adjust the pivot to the center of the graduated circle.—Set the south end of the needle to read zero, and read the north end of the needle; reverse the compass box in azimuth, repeat the observations, and correct one-half the difference between the two readings of the north

end of the needle by bending the pivot, using the special wrench for the purpose. Turn the compass box 90° and repeat See (b), Fig. 13.

The Needle.—To straighten the needle.—Having adjusted the pivot, set the north end of the needle to read zero and bend the needle so that the south end reads zero also. Turn the compass box and test for other graduations.

PROBLEMS WITH THE COMPASS.

PROBLEM B1. DECLINATION OF THE MAGNETIC NEEDLE.

- (a) Equipment.—Surveyors' compass, flag pole, reading glass.
- (b) Problem.—At a point on the true meridian determine the mean magnetic declination with the surveyors' compass.
- (c) Methods.—(1) Set the compass over one point and a flag pole at another on the true meridian. (2) Lower the needle and sight at the flag pole carefully with the north end of the compass box to the front. (3) When the vibra-

300	DECLINATION		EDLE	WITH SURVEYOR'S COMPASS.
No	Needle Mean		lean	Oct.12,14. (2 Hours) Clear and Cool.
	Reading N-3*30'E	P·M· 2:05	P-M-	Used Gurley Compass Nº 26 (Needle
	N.3°35'E.	2:11		recently remagnetized), and Watch Set compass on true meridian with dec-
3	N.3.30'E.	2:15		lination vernier set to read zero.
4	N.330'F.	2:22		Sighted at Flag pole set on meridian at
5	N-3'35'E	2:27		a distance of 200 Ft., and read
	N335'E	2:31		needle by estimation to 5 minutes
7	N335'E.	2:35		(one sixth part of one-half degree),
	N-3'30'E-	2:42		carefully avoiding parallax and
	H335'E-	2:48		magnetic disturbances · Observed
10	N335'E. N333'E	2:54 2	2:30	time to nearest minute.
				Disturbed needle by lifting it From
				pivot and verified sighting; then
Hote:	Assuming that			when oscillations had ceased
	ditions are no.			re read the needle.
	the correction			Continued the process until ten consecutive readings, having a maximum
14.7	by Diagram of			range of not more than ten min-
	the mean gives			stes, were obtained.
	most probable			0.00, 1.00 00.01100
	nation for this			
71	ment.			
	100			
10				
				The state of the s

tions of the needle have ceased, move the vernier by means of the tangent screw so that the north end of the needle reads zero, and check the sighting of the compass. (4) Read the declination on the vernier to the nearest minute. (5) Lift the needle, verify the zero needle reading and the sighting, read the vernier and record; repeat the process until ten satisfactory consecutive values of the declination are obtained. Observe the time of each reading to the nearest minute. (6) Correct the mean of the ten values for daily variation by reference to the diagram, Fig. 11, using the mean time. Record and reduce the data as in the form. (Note that the values in the form were obtained by estimating the nearest five minutes. Which is better? Try both if time allows.)

PROBLEM B2. ANGLES OF TRIANGLE WITH COMPASS.

- (a) Equipment.—Surveyors' compass, two flag poles, reading glass.
- (b) Problem.—Measure the angles of a given triangle with the surveyors' compass.
- (c) Methods.—(1) Set the compass over one of the vertices of the triangle and a flag pole behind each of the other two. (2) Lower the needle and sight at one of the flag poles carefully, with the north end of the box to the front. (3) When the vibrations have ceased, read the north end of the needle to the nearest five minutes by estimation. (4) Lift the needle, verify the sighting and also the reading. (5) Turn the compass box to the other point and determine the bearing, as before. The required angle is the difference between the two bearings. (6) Measure the other two angles in like manner. The error of closure must not exceed 5 minutes. Follow the form.

PROBLEM B3. TRAVERSE OF FIELD WITH COMPASS.

- (a) Equipment.—Surveyors' compass, 2 flag poles, engineers' chain, set of chaining pins.
- (b) Problem.—Determine the bearings of the sides of an assigned field with the surveyors' compass and measure the lengths of the sides with an engineers' chain.
- (c) Methods.—(1) Set the compass over one of the corners of the field which is free from local attraction, and set off the declination with the vernier. (2) Take back sight on the last point to the left and fore sight to the next point

	OF TRIANGLE 5-6-	8 WITH SURVEYORS COMPASS.
station Line	Observed Needle	Observers, R. Roe & J. Doe.
	Bearing Angle	Oct-13,14-(2 Hours) Clear, Moderate.
5 5-6	5.83 15W	Used Gurley Compass, Locker Nº 26- Each bearing was observed in
" 5-8	5.540W 77°35'	duplicate, the needle being dis-
	N.540'E H.49'05W 54°45'	turbed and the sighting verified
		between readings.
6 6-8	5.49°00'E	BETWEEN TERBINGE
11 6-5	H8395E 47°451	
	180°05'	(Discrepency not to exceed 5 minutes
		54451

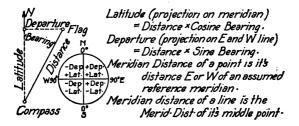
75 M	TRAVE	RSE O	F FIEL	A-B-C	D-E	WITH COMPASS AND CHAIN.
Station	Line	Observed				Observers: J. Doe & R. Roe.
	A-E	5.6030W	Angle	Bearing	rr.	Oct-16,'14 · (3 Hours) Clear & Windy Used Gurley Compass, Locker Nº 24 ·
A	A-B	5:32 45 E			336.5	Made needle read zero when pointing
В	B-A	N33 05 W		1		true north by setting off declination
	R.C	GA3025 F		5.43°05'E	464.6	with vernier on declination are of
0	C-B	N4320 W	5505	1		N.3°36'E.
	6-0	5.81°75'W		15.81 50 W	483.3	Read bearings with N. End of Compa
D	D-C	N.8135'E	103 55			toward the Forward station and
	D-E	H-22 20W		N.22 05 W	616.0	read N. End of Needle.
E	E-D	522°20'E		N-60 25 E	241.6	N A
	E-A	N.6070E	540°05	VI-00 25E	241.0	1
		1	340 03			E W
500 00	Veulatio	of lat	itudes	and dep	ertures	
	pp.	1		,	1000	5 8
		on of a	rea on	pp.		1 3 \
		1		1		
		1	1			1 5 1
	Jot.		1			1 17
			1	1		1
				1		08
		1	1			Allowable error of closure = 0°101.

to the right, following the methods used in Problem B2. (3) Repeat this process for the remaining corners of the polygon taken in succession to the right. (4) Chain the sides of the field to the nearest 0.1 foot by estimation. (5) Compare the chain with standard. (6) From the observed bearings compute the interior angles of the field, and the true bearings of the sides. The angular error of closure must not exceed 10 minutes for a five-sided field. Record and reduce data as in the form.

PROBLEM B4. AREA OF FIELD WITH COMPASS.

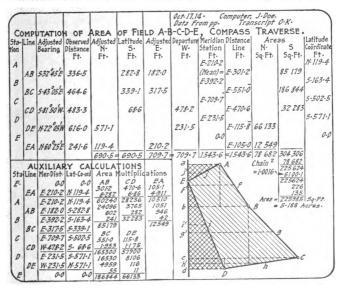
(a) Equipment.—Five-place logarithms.

(b) Problem.—Compute the area of the assigned field by means of latitudes and departures.



(c) Methods.—(1) Prepare forms for calculations; transcribe data, and carefully verify copy. (2) Compute latitudes and departures by contracted multiplication, preserving results to the nearest 0.1 foot. (3) Make the same calculations by logarithms, as a check. (4) Determine the actual linear error of closure. (5) Determine the permissible error of closure (see chapter on errors of surveying). If consistent, distribute the errors in proportion to the several latitudes and departures, respectively, repeating the additions as a check. (7) Transcribe field notes and adjusted latitudes and departures, and verify transcript. (8) Calculate the meridian distances of the several stations and (9) Calculate the latitude coordinates. (10) Calculate the partial trapezoidal areas by multiplying the meridian distances of the lines by the respective latitudes, preserving consistent accuracy, and observing algebraic signs. (11) Determine the area by taking the algebraic sum of the partial areas. Reduce to acres, and correct for standard.

	7 1	172				1	ata Fro	m pp-	Tra	nscript	0-K	
COME	ASS TI	AVERS	E OF	FIELD	A-B-C-D	E	LATIT	UDES A	AND DE	PARTU	RE5	
Line	Adjusted Bearing	Me	Campi	tation	of Lati	lat.	es. Adjusted	Comput Multipli-	Logar-	Depar	Dep-	Adjusted
AB	532°45'E	Ft. 336.5	(Lat=Dist 336.5 40148.0 26920 1346 34	x (os·Bg) 2·52698 9·92481	Ft. 5-283-0	Ft.	Ft.	Dep = Dist	X Sin-Bg-)	Ft. E-182-0	Ft.	Ft. E-182-0
ВС	543°05'E.	464.6	283.01 464.6 63037.0 32522 1394 14	9.86353	5.339.3	-0.2	5.339./	182.03 60386.0 27876 3717 139	(182-04)	E-317-4	+0-1	E-317-5
CD	5-81°50'W	483-3	339.32 483.3 5024j.0 4833 1933	(339·32) 2·68422 9·15245	5.68.6	0-0	5. 68.6	43497 3866 435	(317.35)	W-478-4	-0-2	W-478-2
DE	N-22°05'N	616-0	68.65 68.65 46623.0 55440 1232 370	2-83667 (68-65) 2-78958 9-96697 2-7564	H. 570-8	+0.3	N-571-1	39 378.40 6/6.0 59573.0 18480 4312 308 55	(478·40) 2·78958 9·57514	W-231-6	-0-/	W-23/-3
EA	N-60 25E	241.6	200940	(570-81) 2-38310				19328	2.38310 9.93934	E-709.5	+0.2	E-709-7
Line AB BC CD	ibution of Lat. 3 0.2 3 0.2 1 0.0 6 0.3	Dep. 2 0.0 3 0.1 5 0.2 2 0.1	72 15 27 719.27	2.07655 (119-28	_	105	ore. (5ee Dis	2.32244 (210.11) agram)	rror =	0.5	
DE	6 0.3 1 0.1 14 0.8	2 0.1 2 0.1 14 0.3			82 + 0.52			= 3×5	2142 = 3	3.2 Ft.	000	



Follow the form. (12) Make plat of field, using total rectangular coordinates, and checking by polar planimeter.

PROBLEM B5. ADJUSTMENT OF THE COMPASS.

- (a) Equipment.—Surveyors' compass, adjusting pin, small screw driver.
- (b) Problem.—Make the necessary tests and adjustments of the surveyors' compass.
- (c) Methods.—Observe the following program: (1) test the magnetism of the needle; (2) test the metal of the compass box; (3) test and adjust the plate levels; (4) test the sights; (5) test the pivot; (6) test the needle.

PROBLEM B6. COMPARISON OF DIFFERENT MAKES AND TYPES OF COMPASSES.

- (a) Equipment.—Department equipment, catalogs of representative makers of compasses.
- (b) Problem.—Make a critical comparison of the several types of compasses.
- (c) Methods.—Examine the department equipment and study the several catalogs carefully, noting the characteristic features, prices, etc. The following items, at least, should be included in the tabulated report: name of instrument, length of needle, length of alidade, vernier, tripod, weight, price, etc.

CHAPTER IV.

THE LEVEL.

Description.—The engineers' level consists of a line of sight attached to a bubble vial and a vertical axis. Two types of level, the wye and dumpy, Fig. 14, are used by engineers. In the former the telescope rests in Y-shaped supports, from which it may be removed. In the dumpy level the telescope is fixed. The dumpy is a favorite with British



Engineers' Wye Level.

Fig. 14.

Dumpy Level.

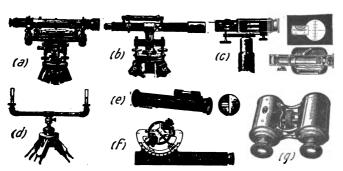


Fig. 15.—Types of Levels. 57

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and the wye level with American engineers. (The dumpy level with erecting eye-piece has been adopted as standard by the Division of Valuation, Interstate Commerce Commission.) The two types differ chiefly in the methods of adjustment. A third type, not shown in the cuts, is called the level of precision because of its use solely for work of extreme refinement.

In Fig. 15 are shown: (a) an architects' or builders' level of the wye type; (b) a road builders' level of the dumpy type; (c) a reconnaissance level with a decimal scale for reading horizontal distances direct; (d) a water level sometimes used in locating contours; (e) a Locke hand level; (f) a clinometer; (g) a binocular hand level.

THE TELESCOPE.

Principles.—The telescope used in the engineers' level and transit, shown in section in Figs. 16 and 22, consists of an objective or object glass which collects the light and forms an image in the plane of the cross-hairs, and an ocular or eyepiece which magnifies the image and cross-hairs. The cross-hairs are thus at the common focus of the objective and eyepiece. The principle of this type of telescope, both optically and mechanically, may be illustrated by the photographic camera if cross lines be ruled on the ground glass focusing plate and a microscope be used in viewing the image formed by the lens. Telescopes of the above class are called measuring telescopes, while those of the opera glass type are termed secing telescopes. The latter have no real image formed between the object glass and eyepiece.

Line of Collimation.—The telescope of the level or transit may be represented by a line, called the line of collimation, which joins the optical center of the objective and the intersection of the cross-hairs. The optical center is a point such that a ray of light passing through it emerges from the lens parallel to its original direction. The line of collimation is independent of the eyepiece.

Objective.—The objective is a double convex or planoconvex lens. In all good telescopes the objective is compound, that is, made up of two lenses, with the view to correct two serious optical defects to which a simple lens is subject. These defects are called *chromatic aberration* and spherical aberration.

Chromatic abcrration is the separation, by the objective, of white light into its component colors. A lens which is

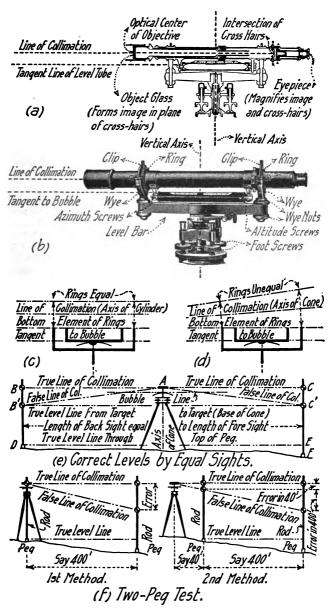


Fig. 16.

free from this defect is called achromatic. A telescope is tested for the chromatic defect by focusing on a bright object, such as a piece of paper with the sun shining on it, and noting the colors on the edge of the object and especially at the edge of the field of view as the focus is slightly deranged. Yellow and purple are the characteristic colors indicating good qualities in the lens.

Spherical aberration is a defect which prevails to a serious extent in a simple lens having spherical surfaces. It is due to a difference in the focal distance for different concentric or annular spaces of the objective, so that the plane of focus for rays passing through the outer edges of the lens is different from that of the middle portion. A telescope is tested for this defect by focusing on a well defined object, such as a printed page, with the rays of light cut off alternately from the middle and the edge of the lens. This is best done by means of a circular piece of paper with a small round hole in it.

As a rule, the object glass in good levels and transits consists of a double convex lens of crown glass fitted to a concavo-convex or a plano-concave lens of flint glass, the former to the front. The defects described above are avoided through the different dispersive and refractive powers of the two kinds of glass, and by grinding the surfaces of the two lenses to the proper curvatures.

Eyepiece.—As in the camera, the image formed by the objective is inverted, so that if a simple microscope be used as an eyepiece, the observer sees objects inverted. Such an eyepiece is commonly used on the dumpy level, as shown in Fig. 14. This form of eyepiece consists of two planoconvex lenses with their convex sides facing each other. The form of eyepiece most used in American instruments is the erecting eyepiece in which two plano-convex lenses replace each of the two in the simpler form. The erecting eyepiece is much longer than the simple one, as may be seen at a glance in Fig. 14. While the simple eyepiece causes a little confusion at first, owing to the inversion of objects, it is much superior to the erecting eyepiece in the matter of clearness and illumination.

The chief inherent defect in the eyepiece is a lack of flatness of the field. A single lens usually causes a distortion or curving of straight lines in the image, especially towards the edge of the field. A telescope is tested for this defect by observing a series of parallel right lines, prefer-

ably a series of concentric squares, which fill the entire field of view.

In the best achromatic eyepieces, one or more of the separate lenses may be compounded, the curvatures being such as to eliminate the color defect and give rectilinear qualities to the lens or combination of lenses.

Definition.—The definition of a telescope depends upon the finish and also the accuracy of the grinding of the curved surfaces of the lenses. It may be tested by reading the time on a watch or a finely printed page at some distance from the instrument.

Illumination.—Illumination and definition are apt to be confused. Poor definition causes indefinite details, while poor illumination causes faintness in the image. The latter may be tested about dusk, or in a room which can be gradually darkened, and can be best appreciated if two telescopes of different illuminating qualities be compared.

Aperture of Objective.—The aperture or effective diameter of the objective is determined by moving the end of a pencil slowly into the field and noting the point where it first appears to the eye when held say 8 or 10 inches back from the eyepiece. The process should be repeated in the reverse order. The annular space is deducted from the actual diameter to obtain the real aperture.

Size of Field.—The field of the telescope is determined by noting the angle between the extreme rays of light which enter the effective aperture of the objective. With the transit telescope, the limiting points may be marked on the side of a building and the angle measured directly with the plates; or with either level or transit the angle may be calculated from the measured spread in a given distance. For simplicity, a distance of 57.3 feet may be taken, and the result reduced to minutes.

Magnifying Power.—The magnifying power of a telescope is expressed in diameters, or as the multiplication of linear dimension. It is determined most readily by making an observation with both eyes open, one looking through the telescope and the other by natural vision. The comparison may be made by means of a leveling rod, or the courses of brick or weather-boarding on the side of a house may be used in like manner.

Parallax.—Parallax is the apparent movement of the cross-hairs on the object with a slight movement of the eye, and is due to imperfect focusing of the eyepiece on the cross-hairs before focusing the objective. The eyepiece

should be focused with the eye normal, the cross-hairs being illuminated by holding the note book page or other white object a few inches in front of the objective.

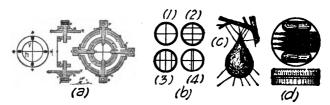


Fig. 17.

Cross-Hairs.—The cross-hairs are attached to a ring or reticule which is held by two pairs of capstan headed screws. The hairs usually consist of spider lines, although some makers use platinum wires for the purpose. To remove the reticule the eyepiece is taken out, one pair of screws is removed and a sharpened stick is inserted in a screw hole. The best spider lines are obtained from the spider's egg nest.

In Fig 17, (a) shows the usual arrangement of the crosshair ring and the method of attaching the hairs; (b) shows the number and positions of hairs used, (1) being the most common, (2) the form for stadia work with the transit and also for estimating the lengths of sights with the level, (3) a form used by some makers with the level, and (4) a style found in English levels; (c) shows the egg pod or case of the large brown spider (about half size) which yields the best lines for engineering instruments; (d) illustrates a convenient vest pocket outfit for replacing cross-hairs in the field, consisting of a supply of spider lines and some adhesive paper (bank note repair paper) each in a capsule or tin tube, and several sharpened sticks for stretching the hairs. Cross-hairs stretched in this manner may last indefinitely, or they may be fastened on permanently with shellac at the first opportunity.

THE BUBBLE VIAL.

Principle.—The spirit level consists of a sealed glass tube nearly filled with ether or other liquid, and bent or ground so that the action of gravity on the liquid may indi-

cate a level line by means of the bubble. The delicacy of the buble depends upon the radius of the curvature in a vertical plane, the greater the radius the more delicate the level. Thus, for example, a perfectly straight tube could not be used as a level.

Curvature of Bubble Vials.—Good bubble vials are now made by grinding or polishing the interior surface of a selected glass tube by revolution, as indicated in exaggerated form at (a) Fig. 18. As a general rule, only one side of the vial is actually used, it being customary to encase it in

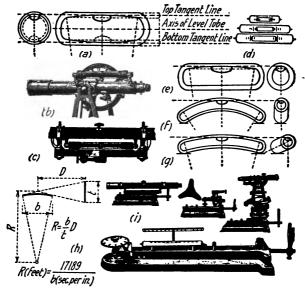


Fig. 18.

a brass tube having a slot or race on one side. However, both sides of the vial may be utilized, as in (b) and (c), Fig. 18, which show the reversion level adapted to the transit and wye level, respectively. Bubble vials of several sizes are shown in (d), Fig. 18. It was formerly customary to grind out only a portion of the upper side of the glass tube, as shown at (e). The cheap vial, consisting merely of a bent tube, used mostly in carpenters' and masons' levels, is

shown at (f); and a method of increasing the precision of the bent tube by tilting it is indicated at (g), Fig. 18.

Delicacy.—The delicacy of the bubble vial is designated either by the radius, usually in feet, or by the central angle in seconds corresponding to one division or one inch of the bubble scale. Two methods are employed to determine the delicacy of level vials, (1) by the optical method, as at (h), Fig. 18, where the radius is calculated from an observed target movement at a given distance for an observed bubble movement, the two triangles being similar; and (2) by the level tester, as at (i), by means of which the angular movement is read from the micrometer head for a given movement of the bubble. The engineer usually employs the radial designation, while the maker expresses the delicacy in angular units. As shown at (h) and (i), Fig. 18, the radius in feet is equal to 17.189 divided by seconds per inch of bubble.

Bubble Line.—The relations of the bubble to the other parts of the instrument are best understood by representing the vial by a line. This line may be either the axis of the surface of revolution in (a), Fig. 18, or to provide for either of the three forms of vial shown, it may be taken as the tangent line at the middle or top point. This tangent line will be meant hereafter in referring to the bubble line.

LEVELING RODS.

Types.—There are two classes or types of leveling rods; (1) target rods, having a sliding target which is brought into the line of sight by signals from the leveler; and (2) self-reading or speaking rods which are read directly by the leveler.

In Fig. 19, (a) is the Philadelphia rod; (b) the New York rod; and (c) the Boston rod. The first is either a target or self-reading rod; the second is a target rod, but may be read from the instrument when the rod is "short"; the Boston rod is strictly a target rod. The Philadelphia rod is perhaps the favorite for most purposes, and the Boston rod is used least. A folding self-reading rod is shown at (d), Fig. 19; (e) is a woven pocket device which may be tacked to a strip of wood and used as a leveling rod; (f) is a rail-road contouring rod with an adjustable base; (g) is a plain rod graduated to feet, for use with the water level.

Targets.—The targets shown on the Philadelphia and New York rods, (a) and (b), Fig. 19, are called quadrant targets. That on the Boston rod, (c), is a modified form of

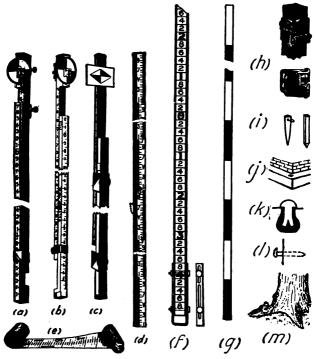


Fig. 19.

the diamond target. A special form, called the corner target, is bent to fit two sides of the rod to assist in plumbing it, and another target has two parallel planes for the same purpose. A detachable rod level is shown at (h). The target on rod (b), with the zero of the vernier 0.09 foot below the center of the target, frequently causes blunders.

USE OF THE LEVEL.

Use.—The engineers' level is used: (1) to determine differences of elevation; (2) to make profile surveys; (3) to locate contours; (4) to establish grade lines; (5) to cross section; (6) to run lines.

Differential Leveling.—Differential leveling consists of finding the difference of elevation between two or more points. In the simplest case the difference of elevation between two points may be found from a single setting of the level, the leveling rod being used to determine the vertical distance from the plane of the instrument to each of the two points, and the difference between the rod readings taken. When the distance between the two points is too great, either vertically or horizontally, or both, to admit of this simple process, two or more settings of the level are taken so as to secure a connected series of rod readings, the algebraic sum of which gives the desired difference of elevation. This difference may be expressed either by the numerical result of the algebraic sum of the rod readings, or by assuming an elevation for the beginning point and calculating the elevation of the closing point by means of the observed rod readings.

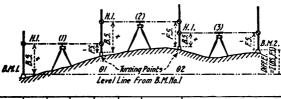
A back sight is a rod reading taken to determine the height of the instrument. A fore sight is a rod reading taken to determine the height of a point. A bench mark is a point selected or established for permanent reference in leveling operations. A turning point is a temporary reference point used in moving the instrument ahead to a new setting. The same point is often both a turning point and bench mark. The datum is the plane or surface of reference from which the elevations are reckoned; it may be sea level, or an arbitrary local datum. A level line is a line parallel to the surface of a smooth body of water. A horizontal line is tangent to a level line at any point. The curvature varies as the square of the distance from the point of tangency, and is 0.001 foot in 204 feet, or 8 inches in one mile.

In Fig. 19, (i) shows a metal and also a wooden peg commonly used for turning points. Several forms of bench marks are shown in Fig. 19; (j) is a mark on the corner of a stone water-table; (k) a rivet leaded into a hole drilled in a stone slab; (l) a railroad spike driven into a wooden post or telegraph pole; (m) a projection cut on the root of a tree, preferably with a spike driven vertically into the top of the bench, and usually with a blaze above marked "B. M. No.—" All bench marks and also turning points should be clearly described in the notes.

Fig. 19a shows the essential details of differential leveling. In practice the calculations are made mentally.

Two chief essentials in correct differential leveling are:
(1) that the bubble be in exactly the same position (usu-

ally the middle) on both back and fore sight; and (2) that the length of back sight and fore sight, horizontally, shall be balanced. It is seen at (e), Fig. 16, that with the bubble always in the middle, the line of collimation generates a horizontal plane when in perfect adjustment, but a cone with axis vertical when out of adjustment; so that in taking equal distances in the opposite directions, the base of the cone is used, this base being parallel to the true colli-



Sta.	B.5.	H.1.	F.5.	Elev.	Dist.	Calculations	Description of B.M.s and O's.
BML				100.00	B.S. F.S.	100.00 BMI +4.42 BS	Gity Datum B.M. Bolt, N.W. cor, water table, Ist Nat. Bank Bida
T(I)	+4.42	IOLAZ			340	104.42 XI -1.16 F.S.	,
01			<i>~1.16</i>	103.26	340	103.26 0 1 +4.37 8.5.	Peq, N.E.cor. J. Green's lot.
X(Z)	+4.37	107:63			270	107.63 T 2 -3.55 F.S.	
82			-3.55	104.08	300	104.08 02 +1.91 8.5.	Sidewalk,E. gatepost, J. Doe.
7(3)	+191	105.99			330 /	105.99 113 -2.40 F.S.	
BMZ	+10.70		<u>-240</u>	103.59 100.00	300	10359 BMZ	N.W. balt, (nicked) water plug S.E. cor. High and East Sts.
1	- 7.11 - 7.11	ا مراجع		+ 3.59	940		(Balanced B.S. and F.S. Dist.
	# 3.37		L		940		Checked Elev. by \(\S(8.5., F.5.) \)

Fig. 19a.—Details of Differential Leveling.

mation plane. In the best leveling practice the instrument is adjusted as perfectly as possible and then used so that the residual errors balance each other.

The three common styles of leveling rods may be read to 0.001 foot by vernier or by estimation on a scale to 0.005 foot. However, for most kinds of leveling, it is an absurd refinement to read the rod closer than 0.01 foot, especially with the usual maximum length of sight of 350 to 400 feet, and with the more or less sluggish bubbles supplied in the general run of leveling instruments. Furthermore, the horizontal hair usually covers 0.01 foot or so of the target at the maximum length of sight, that is, the target can move that amount without being noticed by the observer.

Profile Leveling.—Profile leveling consists of finding the relative elevations of a series of representative points along a surveyed line, for the purpose of constructing a profile or vertical section. The skeleton of profile leveling, that is, the precise bench marks and turning points with the successive heights of instrument, is identical with differential leveling, already described. Having determined the height of instrument by taking a back sight on a bench mark of known or assumed elevation, rod readings are. taken at proper intervals along the measured and staked line. These readings are fore sights, but they are usually termed intermediate sights to distinguish them from the more precise rod readings taken on turning points and bench marks. On railroad surveys intermediate sights are taken usually to the nearest 0.1 foot on the ground; but in other cases, such as tile and sewer surveys, intermediates are often read to the nearest 0.01 foot on small pegs driven beside the station stakes flush with the surface of the ground. In railroad work, the benches, turning points, and intermediates of special importance are commonly read to 0.01 foot, although some engineers persist in the questionable practice of taking the nearest 0.001. In drainage surveys the nearest 0.01 foot is usually taken on bench marks, although more carefully than on the intermediate peg points, and the nearest 0.1 foot is read on ground points.

The errors of profile leveling are balanced on turning points by equal back and fore sights, as in differential leveling. If the instrument is seriously out of adjustment, an error is made in the case of odd bench marks with unbalanced sights, and also on all intermediate sights. However, the error is usually unimportant when ground readings are taken to the nearest 0.1 foot. In important leveling, such as canal and drainage work, it is customary to run a line of check levels to prove benches, before construction begins.

The profile is plotted to an exaggerated scale vertically on a special paper, called profile paper. Three kinds, known as plates A, B and C, are in general use. The most common is plate A, which is ruled in $\frac{1}{4}$ -inch squares with a further subdivision to $\frac{1}{20}$ inch vertically. In railroad profiles the scales most used are 400 feet to the inch horizontally and 20 feet vertically. A still greater exaggeration is generally used in drainage profiles.

Reciprocal Leveling.—The application of differential leveling to the determination of the difference of elevation between two bench marks separated by a wide river or gorge

is termed reciprocal leveling. A setting of the level is taken on each side of the river, and the mean of the two results is taken. The necessary unbalancing of distances in one setting is balanced up in the other. Each back or fore sight should be the mean of a series of careful observations. In best practice, simultaneous readings are taken with two levels.

Contour Leveling.—Contour leveling is an application of the methods of profile leveling to the location of contour lines, that is, lines having the same elevation. Two methods are employed: either (1) actually establishing points on the adopted contour planes on the ground and then locating these points; or (2) taking random elevations at representative points and interpolating the contour lines from the plotted data. The latter is the more common. The chief purpose of contour leveling is to make a contour map, and the process is essentially a part of topographic surveying, where it will be more fully considered.

Grade Lines.—The establishment of grade lines is usually the concluding part of profile leveling. After making the profile, the grade line is established by stretching a fine thread through the ruling points, taking into account the controlling conditions, such as maximum gradient or earthwork quantities on a railroad profile, the carrying capacity or the scour in the case of a ditch, etc. After laying the grade line on the profile, notes are made of the data, and the actual grade line is established. Two methods are used: (1) the height of instrument is determined as usual, and stakes are driven at measured intervals with their tops to match calculated rod readings; and (2) a limited number of ruling points are established by the first method or otherwise, and the remaining stakes are "shot in" by constructing a line parallel to the ruling line used. The latter is more rapid, since a constant rod reading is used; however, the method is unreliable unless the foresight be checked frequently on a fixed target.

Cross-Sectioning.—Cross-sectioning consists of staking out the limits of the transverse section of an excavation or embankment for the purpose of construction, and usually includes the collection of data for the calculation of the quantities. This may be done either with the engineers' level, rod and tape line, or with special rods called cross-section rods. The notes are taken as rectangular coordinates, usually with reference to the center of the finished

roadbed. The slope stakes are set where the side slope lines pierce the surface of the ground.

Running Lines.—Lines are sometimes run with the engineers' level, provision being made in most good levels for the attachment of a plumb bob. A line may be prolonged by sighting in two points ahead. A clamp and tangent movement are necessary. Some builders' levels have a needle and also a roughly divided horizontal circle for use in staking out buildings.

Practical Hints.—The following practical suggestions apply more or less directly to all kinds of leveling, and also in a general sense to transit work.

Speed.—Cultivate the habit of briskness in all the details of the work. While undue haste lowers the standard of the results, an effort should be made to gain speed steadily without sacrificing precision. Gain time for the more important details by moving rapidly from point to point. On rapid surveys both leveler and rodman often move in a trot. Neither rodman nor leveler should delay the other needlessly.

Care of Instruments.—Do not carry the level on the shoulder in climbing fences. Clamp the telescope slightly when hanging down Keep the tripod legs at the proper tightness, and avoid looseness in the tripod shoes. Avoid undue exposure to the elements, and guard the level from injury. Do not leave the instrument standing on the tripod in a room over night.

Setting Up—In choosing a place to set the level up, consider visibility and elevation of back point and probable fore sight. Set up with plates about level. On side-hill ground place one leg up hill. In general, place two tripod shoes parallel to the general line of the levels.

Leveling Up.—A pair of foot screws should be shifted to the general direction of the back or fore sight before leveling up. Set the foot screws up just to a snug bearing and no tighter. If either pair of screws binds, loosen the other pair a little The bubble moves with the left thumb. Level up more precisely in the direction of the sight than transverse to it, but do not neglect the latter. Inspect the bubble squarely to avoid parallax, and also to prevent such blunders as reading the bubble five spaces off center.

Observations.—Adjust the eyepiece for parallax with the eye unstrained. It is much easier on the eye to observe with both eyes open. Read at the intersection of the cross-hairs, since the horizontal hair may be inclined. Set the

target approximately, check the bubble, and repeat the process several times before approving the sight. Be certain that the bubble is exactly in the middle at the instant of approving the target. If the level has horizontal stadia lines, beware of reading the wrong hair (the reticule may be rotated one-quarter so as to have the extra hairs vertical, or a filament may be attached to the middle horizontal hair to assist in identifying it). Avoid disturbance of the tripod by stepping about the instrument. Assist the rodman in plumbing the rod. Let signals be perfectly definite both as to direction and amount, using the left hand for "up" and the right for "down," or vice versa.

The leveler can work much more intelligently if he knows the space covered on the rod by one division of the bubble scale at the maximum length of sight, and also the space on the rod hidden by the cross hair.

Adjustments.—Keep the instrument in good adjustment and then use it as though it were out of adjustment.

Balancing Sights.—Balance the length of back sight and fore sight, and record the approximate distances. The distances in the two directions may be made equal roughly by equality of focus, but it is better on careful work to pace the distances or determine them by means of the stadia lines in the level. If necessary to unbalance the sights, they should be balanced up at the first opportunity, and in general they should be in balance when closing on important benches. When leveling up or down steep slopes, follow a zigzag course to avoid short sights. Take no sights longer than 350 or 400 feet.

Leveling Rod.—The rod should be carefully plumbed, to accomplish which the rodman should stand squarely behind the rod and support it symmetrically between the tips of the extended fingers of the two hands. In precise work wave the rod to and fro towards the observer and take the minimum reading of the target. With "short" rods avoid the somewhat common blunder of 0.09 foot when the vernier slot is below the center of the target. With "long" rods, see that the target has not slipped from its true setting before reading the rod. Read the rod at least twice, and avoid blunders of 1 foot, 0.1 foot, etc. Careless rodmen sometimes invert the rod. Each rod reading on turning points and bench marks should, when practicable, be read independently by both rodman and leveler.

Bench Marks and Turning Points.—Wooden pegs or other substantial points should be used to turn the instrument

on. Select bench marks with reference to ease of identification, the balancing of sights, freedom from disturbance, etc. As a rule, each bench mark should be used as a turning point so that the final closure of the circuit may prove the bench. Mark the benches and turning points and describe them in the notes so plainly that a stranger may readily find them. Green rodmen sometimes hammer at turning point pegs with the rod. When leveling near a still body of water, its surface may be used to save time and check the work.

Record and Calculations.—Describe bench marks and turning points clearly. It is good practice to apply algebraic signs to the back and fore sight rod readings. The elevations should be calculated as fast as the rod readings are taken, and calculations on turning points should be made independently by leveler and rodman, and results compared at each point. The rodman may keep turning point notes in the form of a single column. The calculations should be further verified by adding up the columns of back sights and fore sights for each circuit, or page, or day's work, and the algebraic sum of the two compared with the difference between the initial and last calculated elevation.

Error of Closure.—A circuit of levels run with a good level by careful men, observing all the foregoing precautions, should check within 0.05 foot into the square root of the length of the circuit in miles (equivalent to 0.007 foot into the square root of the length of the circuit in 100-foot stations). In closing a circuit, the error should be carefully determined, as above indicated, and the value of the coefficient of precision found. (See discussion of errors of leveling and precision diagrams in Chapter IX, Errors of Surveying.)

ADJUSTMENT OF THE WYE LEVEL.

Elementary Lines.—The principal elementary lines of the wye level, as shown in Fig. 16, are: (1) the line of collimation; (2) the bubble line; (3) the vertical axis. For the purpose of adjustment there should be added to these: (4) the axis of the rings; (5) the bottom element of the rings. The following relations should exist between these lines; (a) the line of collimation and bubble line should be parallel; (b) the bubble line should be perpendicular to the vertical axis. The first of these relations involves two steps, viz., (1) to make the bubble line parallel to the bot-

tom element of the rings, and (2) to make the line of collimation coincide with the axis of the rings. The other relation involves the wye adjustment, and is similar to the plate level adjustment described in the chapter on the compass.

Bubble.—To make the bubble line parallel to the bottom element of the rings.—Two steps are involved, (a) to place the bubble line in the same plane with the bottom element, and (b) to make the two lines parallel.

Azimuth Screws.—To make the bubble line in the same plane with the bottom element of the rings.—Clamp the level over a pair of foot screws, loosen the wye clips, and level up; rotate the telescope through a small angle, and if the bubble moves away from the middle, bring it back by means of the azimuth adjusting screws. Test by rotating in the opposite direction. Leave the screws snug.

Altitude Screws.—To make the bubble line and the bottom element of the rings parallel.—Make the element level with the foot screws and bring the bubble to the middle by means of the altitude adjusting screws. The element is made level by the method of reversions as follows: With the level clamped over a pair of foot screws, as above, lift the clips and level up precisely; cautiously lift the telescope out of the wyes, turn it end for end, and very gently replace it in the wyes; if the bubble moves, bring it half way back by means of the foot screws. Before disturbing adjusting screws make several reversals, and conclude the adjustment with screws snug. This end for end reversal is similar to that made with the carpenter's level, the straight edge of the level corresponding to the element of the rings. The lines involved are shown in Fig. 16.

Line of Collimation.—To make the line of collimation coincide with the axis of the rings.—Loosen clips, sight on a point, say a nail head or the level target, more distant than the longest sight used in leveling; rotate the telescope half way and note the movement of the hair, if any. The line of collimation generates a cone, the axis of which is that of the rings, and the apex of which is at the optical center of the objective. Correct one-half the observed error by means of the capstan headed screws which hold the crosshair ring. Gradually perfect the adjustment until the intersection of the cross-hairs remains fixed on the same point when reversed by rotation with reference to either hair. The adjustment should be concluded with the screws at a snug bearing.

After collimating the instrument for a long distance, the adjustment should be checked for a short distance, say 50 or 100 feet, so as to test the motion of the optical center of the objective.

Rings.—The theory of the wye level demands perfect equality of the rings, that is, the parallelism of the axis and element, as in (c), Fig 16. Should the rings be unequal, either from poor workmanship or uneven wear in service, they form a cone instead of a cylinder, and the axis is not parallel to the element, as in (d), Fig. 16. Under the latter conditions, the principle of the wye level fails, and an independent test is demanded. This is known as the two-peg test, the details of which are shown in (e) and (f), Fig. 16, and described in the adjustments of the dumpy level. If, after making the wye level adjustments above described. the two-peg test shows that the line of collimation and bubble line are not parallel, the rings are probably unequal and the instrument should thereafter be adjusted as a dumpy level. However, hasty conclusions should be guarded against.

In case the instrument has a reversion level, shown at (c), Fig. 18, the equality of the rings may be tested by first adjusting the top tangent line of the bubble vial parallel to the bottom element of the rings, and then after rotating the telescope half way round in the wyes, compare the bottom (now above) tangent line of the vial with the top (now below) element of the rings, all by the end for end reversion. However, the exact parallelism of the top and bottom tangent lines of the reversion level should first be proven by the two-peg method.

Wyes.—To make bubble line perpendicular to the vertical axis.—Make the vertical axis vertical and bring the bubble to the middle by means of the wye nuts. The vertical axis is made vertical by reversion thus: With clips pinned, level up, reverse over the same pair of screws, and bring the bubble half way back with the foot screws. When adjusted, the bubble will remain in the middle during a complete revolution. This adjustment is identical in principle with the plate level adjustment of the compass and transit, illustrated in (a), Fig. 13. The wye adjustment should follow the adjustment of the bubble line parallel to the element of the rings. The wye adjustment is a convenience, not a necessity.

Centering the Eyepiece.—After collimating the level, the cross-hairs should appear in the center of the field.

The eyepiece is centered by moving its ring held by four screws. This adjustment is desirable, but not essential.

ADJUSTMENT OF THE DUMPY LEVEL.

Elementary Lines.—The principal elementary lines of the dumpy level are identical with those of the wye level (1) the line of collimation; (2) the bubble line; (3) the vertical axis. As in the wye level, the bubble line should be (1) perpendicular to the vertical axis, and (2) parallel to the line of collimation. However, owing to the difference in the construction of the two types of instrument, the auxiliary elementary lines are not recognized in the dumpy level. The transit with its attached level is identical in principle with the dumpy level.

Bubble.—To make the bubble line perpendicular to the vertical axis.—Make the vertical axis vertical by the method of reversions, and adjust the bubble to the middle. This adjustment is identical in principle with the plate level adjustment, shown in (a), Fig. 13. The bubble should remain in the middle through a complete revolution.

Line of Collimation.—To make the line of collimation parallel to the bubble line.—Construct a level line, and adjust the cross-hairs to agree with it. The level line is determined either by using the surface of a pond of water, or by driving two pegs at equal distances in opposite directions from the instrument, and taking careful rod readings on them with the bubble precisely in the middle, as shown at (e), Fig. 16. For simplicity, the two pegs may be driven to the same level, or two spikes may be driven at the same level in the sides of two fence posts, say 400 feet apart. Otherwise, determine the precise difference of elevation, as indicated in (e), Fig. 16. Then set the level almost over one of the pegs, level up, and as in the first method of (f). Fig. 16, set the target of the leveling rod at the line of collimation, as indicated by the center of the object glass or eyepiece (this can be done more precisely than most levels will set the target at 400 feet distance); now with the rod on the other peg, sight at the target (shifted to allow for the difference if the two pegs are not on the same level); adjust the cross-hair to the level line so constructed. If preferred, the second method shown in (f), Fig. 16, may be used: the level is set back of one peg, rod readings are taken on both pegs, allowance made for the difference in level of the two pegs, if any, the inclination of the line of

collimation determined, correction made for the small triangle from the level to the first peg, and finally the level line constructed by means of the calculated rod readings. The second method is simplified and made practically equivalent to the first by setting the level at minimum focusing distance from the first peg. The small corrective triangle is thus practically eliminated. Strictly speaking the rod readings should be corrected for the earth's curvature (0.001 foot in about 200 feet, or say 0.004 foot in 400 feet distance). However, the effect of curvature is reduced by atmospheric refraction; and with errors of observation, sluggishness of bubble, etc., to contend with, the curvature correction should be ignored, especially when the rod is read to the nearest 0.01 foot.

(The foregoing process is known as the "two-peg adjustment." Although exceedingly simple, this adjustment is commonly regarded as a "bug-bear" by many American engineers. But for it, the dumpy level would have the extended use in this country which it merits. It is said that "the wye level is easy to adjust and usually needs adjustment." Many good levelers employ the "two-peg test" to prove the wye level adjustments. Time may be saved by establishing an adjusting base. The adjustments of a good dumpy level are very stable.)

Uprights.—In some dumpy levels the uprights which connect the telescope with the level bar are adjustable, similar to the wyes of the wye level. This adjustment is designed to bring the bubble line perpendicular to the vertical axis in case the bubble is first adjusted parallel to the line of collimation. However, the best order is that already described, viz., first adjust the bubble line perpendicular to the vertical axis, and then the line of collimation parallel to the bubble line, in which case the adjustable uprights are unnecessary.

PROBLEMS WITH THE LEVEL.

PROBLEM C1. DIFFERENTIAL LEVELING WITH THE HAND LEVEL (OR WATER LEVEL).

- (a) Equipment.—Hand level (or water level), rod graduated to feet.
- (b) Problem.—Run an assigned level circuit with the hand level (or water level), observing the nearest 0.1 foot by estimation, and closing back on the starting point.

(c) Methods.—(1) Determine the correct position of the bubble of the hand level by sighting along a water table, or sill course of a building, or by the principles of the two-peg test. (If the water level is used, fill the tube so as to have a good exposure of the colored water in the glass uprights.) (2) Take sights of 100 feet or so (paced), estimating the rod reading to the nearest 0.1 foot; balance back and fore sights; assume the elevation of the starting point, and keep the notes in a single column by addition and subtraction, as in the 7th column, Fig. 19a. (3) Check back on the first point. Determine coefficient of precision. (The error of closure in feet should not exceed 0.5 $\sqrt{\text{distance in miles.}}$)

PROBLEM C2. DIFFERENTIAL LEVELING WITH ENGINEERS' LEVEL (OR TRANSIT WITH ATTACHED LEVEL).

(a) Equipment.—Engineers' level (or transit with attached level), leveling rod, hatchet, pegs, spikes.

(b) Problem.—Run the assigned level circuit, observing the nearest 0.01 foot, and closing back on the initial point.

(c) Methods.—Follow the practical suggestions given at the conclusion of the "Use of the Level," giving special attention to the following points: (1) eliminate parallax of the eyepiece; (2) balance back and fore sight distances; (3) have the bubble precisely in the middle at the instant of sighting; (4) both rodman and leveler read each rod and also make the calculations independently; (5) calculate elevations as rapidly as rod readings are obtained; (6) plumb the rod; (7) avoid blunders; (8) determine coefficient of precision; (9) no sights longer than 350 or 400 feet. Follow the first form shown to begin with,—the other after several circuits have been run.

PROBLEM C3. PROFILE LEVELING FOR A DRAIN.

- (a) Equipment.—Engineers' leveling instrument, leveling rod, 100-foot steel tape, stakes, pegs, axe.
- (b) Problem.—Make a survey, plat and profile, with estimate of cuts and quantities for a drain under assigned conditions.

(c) Methods.—(1) Examine the ground, determine the head and outlet of the drain, and select the general route.
(2) Stake out the line, set stakes every 50 feet, or oftener if required to get a good profile, and drive a ground peg flush, say 2 feet to the right (or left) of each stake; record data for mapping the line. (3) Starting with the assigned datum or bench mark, run levels over the line of the proposed drain, observing the nearest 0.01 foot both on turning points and ground pegs, the former somewhat more carefully; take rough ground levels, as required, to the nearest 0.1 foot; locate and determine the depth of intersecting drains or pipe lines, or other objects which may influence the grade line of the drain, and secure full data for placing the same on the profile; observe due care with the back and

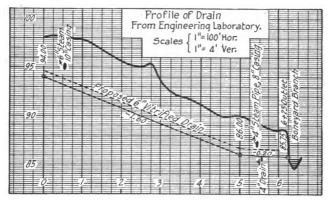


Fig. 19b.

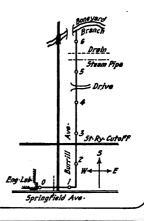
fore sights, as in differential leveling, and conclude the leveling work with a line of check levels back to the initial bench mark; a permanent bench mark should be established at each end of the drain, and if the length is considerable, at one or more intermediate points as well. (4) Make plat and profile of the drain line; lay the grade line, taking into account all ruling points; calculate the cuts, both to the nearest 0.01 foot, and also to the nearest ½-inch; mark the latter on the stakes for the information of the ditcher, using waterproof keel and plain numerals; make estimate of the quantity of drain pipe, and of the cost of the job. Follow the form and the profile in Fig. 19b.

					∙М∙ то	Leveler, J. Doe; Rodman, R. Roe. ENGG HALL B.M. I AND RETURN
Sta-	B-5-	H-1-	F-5-	Elev.	Sights	
	ME I	100			B-5 F-5	7,7
5-L-B-M-			W	720-00		Bolt, E.End, S. Coping, E.Entrance,
X (1)	+ 2.60	722-60			180	University Hall-
01		100	-7.56	715.04		W. End, N. Coping, W. Entrance,
$\pi(2)$	+2.00	717-04			210	Natural History Hall.
H.B.M.I		1500	-3.42	713-62		Bolt, W. End, 1st Step, S. Entrance,
$\pi(3)$	+5.94	719.56	8.20		270	Engineering Hall.
02	-		-0.30	719-26	80	Cement walk, 20 N.E. N. Entrance,
X(4)	+3.87	723-13	-		80	University Hall
	_		-3.14	219.99	-	Bolt, starting point above described.
1.8.M.	+14.41				740 740	
100.00			-14.42		1=14.8	Permissable error = 0.007 VL = 0.027 F
100			+14.41	720-00		Actual error of Closure = 0.01 ft.
			- 0.01	-0.01		Univ- Hall
2			(Ch	eck)		5-1-B-M-N-N
						Chem-Lab.
					9	
						₩ X 0 + >
						V FILL PRINCE
						Net- Hist Hell
						\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \
380						
300						Green 5t.
						E-H-B-M-
	100		-			Eng. Hell

		.s FR	OM R	EYHOL		H.H. Sherwin, Leveler. C.F. Boyer, Rodman. LAFAYETTE, IND.
Sta-	B:5.	H-1-	F-5-	Elev.	Sights BS, F.S.	Nov-29, 14. Cloudy, Cool - B. & B. Dumpy Level -
B-M-I	4.20	694.02	-	689-82	240	Panna-R.B.B.M., M.P. 27, driven rail (Levels
01	5.95	696.30	3.67	690.35	165 240	Peg. direct from tide gage at
02	5.70	698-18	3.82	692.48	240 240	" Sandy Hook, M.Y.)
03	4.93	698.74	4.37	693-81	240,165	" (South along Monon R.R.)
04	4.23	699-75	3.22	695.52	240 240	"
05	4.24	699-04	4.95	694.80	240 240	11
06	4-73	699-33	4.44	694.60	240 240	"
07	4.44	699-61	4.16	695.17	300 240	" opposite Catholic Church, Reynolds.
08	5.18	699.39	5.40	694.21	300 300	"
09	4.54	697-86	6.07	693.32	300 300	" E. side tr'k, between tel. poles 2289-90
010	4.81	698-12	4.55	693.31	300 300	"
011	4.82	698.86	4.08	694.04	300 300	" E. side tr'k, between tel poles 2296-97
B.M.2.	1000		(3.76)	695.10	(200)	B.M. on oak, tel pole 2299, 50' E. track
012	4.10	698-00	4.96	693.90	300 300	Peg at tel. pole 2300.
013	3.65	698-13	5.52	692.48	360,300	11 11 11 11 2305.
014	2.71	692.92	5.92	690-21	360 360	"
015	3.21	690-03	6.10	686-82	360 360	" " " 23/3, E-side frack.
8.M.3		-	(3.15)	(686.88)		N.E.cor. parapet wall, Bridge Nº 97.4
016	4.65	690.83	3.85	686-18	360 360	
8.M.4.	E.A.		(5.29)	(685.54)	(000)	Monon R.R.B.M. Cook, 20'5- tel'pole 2320
017	4.51	691.21	4.13	686.70	360 360	Peg 80' E. trk., El - 688.12
018	5.16	691-37	5.00	686-21	300,360	,,
019			5-13	686.24	300	n at tel' pole 2330.
00.2	85.76	14	89.34	689-82	= B.M.1	
6.31			85.76	-3.58		
			-3.58	Check		

SURVEY FOR A DRAIN FROM Sta-Description +36 Bed of Btream +32 Suitable outlet for drain, Il'W. of W. face of stone arch bridge. +23 Break of N. bank, Boneyard Branch-5-edge of 7' drive. 1665 Crosses drain From Conservatory-5+423 Steam pipe line to Conservatory. 4+52 Center 7'drive to Conservatory. +69-6 | Rails of main track, U-&C-St-Ry-+648 (Gutoff through University Grounds) +58-6 Rails of side track, Urbana and 153-8 Champaign Electric Ry-Drain is 2'L.(E) of stake. 1+21-5 Turns 5- in W. parking, Burrill Ave-+73 12" Ash tree 6' to R. t70 164 | Coment walk E-side Burrill Ave-+54-6 Grosses Military Hall Steam Pipe Line A point 3'W. & 2'5- of N.W. Cor. of Eng-Lab Line runs thence Wparallel to & 9'5. of 5. line of Springfield Ave- Stakes are set 2' to right of proposed trench for drain, with leveling pegs flush with ground beside stakes-

ENGINEERING LABORATORY Head Chainman, J. Doo; Rear Chainman, R. Roe. Apr. 76, 1944. (2 Nours) Cloudy & CoolNO Ft. Steel Tape, Nº 2715, Locker Nº 35.



LE	VEL	Notes	FOR	A D	RAIN		M ENGINEERING LABORATORY.
Sta.	B-5-	H-I-	F. 5-	Elev.	Grade		Oct. 23, 14. (2 hrs) Clear and Cool.
	-			100.00		Y Line	5. End stone sill, W. door, Eng. Lab.
T	+1.23	101-23					Station stakes are 2'R. proposed trench
0			3.05	98.18	94.00	4.18	Peg driven Flush with ground beside stake
+50		-	3.22	98.01	93.20	4.81	
+54.6			3.2	98.0	93-13	4.9	Ground, 6"Steam Pipe, 10" casing, top 2.6 deep.
+66			3.23	98.00	92.94	5.06	
1			3.38	97.85	92:40	5.45	
+21.5		1	3.72	97.51	92.06	545	Drain turns 5-in W. parking Burrill Ave-
+50		1	4.65	96.58	91.60	4.98	Pea
2			5.71	95.52	90.80	4.72	n
+50		1	6.31	94.92	90.00	4.92	1)
0 +59		1	-5.85	95.38	89.86	5.52	(Turning Point) N. Rail, Main Track, U.&C. Ry-
π	+0.13	95.51	-	1		1110	
3			2.08	93.43	89.20	4.23	Peq
+50			3.45	92.06	88.40	3.66	17 Fauth Wye Level.
4			4.34	91-17	87.60	3.57	?? Phila. Rod, Lkr. 20.
+50		1	5.50	90.01	86.80	3.21	77
5			5.52	89.99	€ 86-00	3.99	"
+423			6.1	89-4	85.91	3.5	Ground, 4"Steam Pipe, 8"Casing, top 2:0 deep.
+50			6.26	89.25	85.90	3-35	
+60.5			6.4	89.1	85.88	3.2	Ground, 4"vitrified drain, top 3.4 deep.
6			7.11	88:40	85.80	2.60	Peg.
+23		1	.7.0	88.5	85.75	2.7	Break of N. bank , Boneyard Branch.
+36		1	10.9	84.6			Bed of Stream, water 10" deep.

PROBLEM C4. RAILROAD PROFILE LEVELING.

- (a) Equipment.—Engineers' leveling instrument, leveling rod, 100-foot steel tape, stakes, axe.
- (b) Problem.—Run levels over a short section of line staked out after the manner of railroad surveys, for the purpose of constructing a profile.
- (c) Methods.—Follow the general process outlined in the preceding problem, taking rod readings to the nearest 0.01 foot on turning points and bench marks, and also on important profiling points, when consistent; but take ground rod readings only to the nearest 0.1 foot. In calculating elevations, preserve the same degree of exactness in the result as observed in the rod reading, that is, when the rod readings are taken to the nearest 0.1 foot, use only the nearest 0.1 foot in the height of instrument to determine the elevations. When a hub or station stake is to be used as a turning point, the notes should show the ground rod and elevation to the nearest 0.1 foot on the line preceding the precise turning point record. Bench marks should be selected with reference to their freedom from disturbance during construction, and they should be located not more than 1500 or 2000 feet apart along the line. Check levels by the same parties should not differ more than 0.05 foot into the square root of the length of circuit in miles. Back and fore sights should be balanced, and no sight longer than 350 or 400 feet should be taken. In order to secure a representative profile, ground rods should be taken not only at every station stake, but also at every important change of slope between station points. Pluses may be determined either by pacing, or when short, by means of the leveling rod. The rodman should keep a record of the turning points. The notes should be checked and the other safeguards taken, as outlined in the practical hints under the "Use of the Level." Bottoms of deep gullies may be taken by means of the hand level, or with the engineers' level used like the hand level; or a "long" rod of 17 feet or more may be obtained by holding the 12-foot rod 5 feet or more from the ground.

The profile is best plotted by having another person read off the data. The horizontal scale on railroad profiles is usually 400 feet to the inch and the vertical scale 20 feet to the inch. Gradients are expressed to the nearest 0.01 per

	(PROFI		VEL N	OTES,	GROUND	ELEVATIONS TO 0.1 FOOT.)
5.	+	π_3	-	R.	E.	
209		718.33		5.0	7/3.3	In Brown 5t. (Unimproved)
210		-		4.7	713-6	n n
211 0		9		3.9	714.4	" "
B-M-26	6.79	723-87	1.25		(717-08)	Water Plug, N. bolt, N.W. Cor., Brown-Curtis.
2/2		1		7-6	716.3	Ground, Brown St.
213				6.4	717-5	" "
214				5.9	718-0	" "
+50			1	4.0	719-0	n "
215	1			6-1	717-8	" "
216		0.00		8.0	715-9	" "
2/7				8.5	715.4	17 49
218			1	10.3	7/3-6	" "
219,		6		12.2	711-7	In Corn Field
0 Stake	9.22	721.64	11.45	1	(7/2.42)	0 Stake, Sta-219.
220				8.6	713.0	Corn Field-
221		-		4.4	717-2	**
222				2.7	718.9	,,
223				2.9	718-7	**
224				2.3	7/9-3	"
225				3.4	718-2	Timber Pasture-
+90			4	12.4	709-2	Gully-
226				11.2	710-4	
+35		-		6.0	715-6	Break of bank, Plum River.
B-M-27	2.04	713.52	10-16		(711-48)	B.M., root, 24"elm, 72'R., 5ta. 226+65.
+80	+18.05	718.33	-22.86 +18.05	6.0	707-5	Column S= Station -= Fore Sight.
	110.05	7.0/3	- 4.81	Check	1	Headings X = Height Inst. E = Elevation.

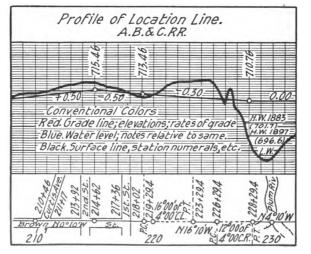


Fig. 19c.

cent. It is usual to give the alinement notes and prominent topography, as shown in Fig. 19c.

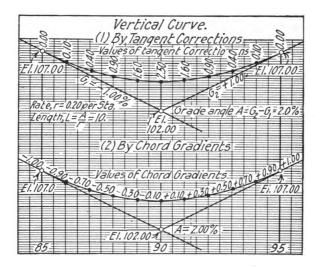
(The complete series of steps involved in railroad and similar leveling for location and construction purposes is: (1) setting the station stakes; (2) running the levels; (3) making the profile; (4) laying the grade line on profile; (5) calculating vertical curves; (6) cross-sectioning for earthwork; (7) calculating earthwork quantities; (8) setting grade stakes.)

PROBLEM C5. VERTICAL CURVE.

- (a) Equipment.—Drafting instruments, profile paper.
- (b) Problem.—Connect two grade lines by a parabolic curve, as assigned.
- (c) Methods.—(1) Plot the given grade lines, station numbers, etc., on a sheet of profile paper. (2) Find the grade angle, i. e. the algebraic difference of the two rates of grade. (3) Determine the length of the vertical curve by dividing the grade angle by the assigned or adopted change of grade per station (notice the analogy to simple circular curves). (4) Calculate the apex correction. (5) Determine the corrections at the several stations or fractional stations (as assigned), and tabulate the stations and elevations. (6) Plot the vertical curve from the data so determined, as in Fig. 19d. (7) Also compute and plot the same curve by the method of chord gradients.

PROBLEM C6. ESTABLISHING A GRADE LINE.

- (a) Equipment.—Leveling instrument, leveling rod, flag pole, 100-foot steel tape, stakes, axe.
- (b) Problem.—Establish an assigned grade line, (1) by measured distances and calculate rod readings, and (2) by "shooting in" the same line, for comparison.
- (c) Methods.—(1) Stake off the distance between ruling points, and drive stakes to the required grade, or if desirable, parallel to it, by dividing up the fall in proportion to the distance. (2) Set the level over one ruling point and determine the height from the point to the line of collimation by means of the leveling rod; set the flag pole behind the other ruling point and establish a target, consisting of a rubber band holding a strip of paper wrapped about the



	COMPARISON OF RESULTS												
Station.	Elevation of Grade Tangent.	By Tangen Tangent Correction.		Chord 6ra	ients. Curv e Elevation								
	Ft	Ft.	Ft.	Per Cent.	Per Cent.	Ft.							
84 85(P.C.) 86 87 88 90(Apex) 91 92 93 94 95(P.T.)	108.00 107.00 106.00 105.00 103.00 103.00 103.00 104.00 106.00 106.00	+0.00 +0.10 +0.40 +0.90 +1.60 +1.60 +0.90 +0.40 +0.10 +0.00	107.00 106.10 105.40 104.60 104.50 104.60 104.90 105.40 106.10 107.00	+0.10 +0.20 +0.20 +0.20 +0.20 +0.20 +0.20 +0.20 +0.20 +0.20 +0.10	61.00) -0.90 -0.70 -0.50 -0.30 -0.10 +0.10 +0.50 +0.70 +0.90 (+1.00)	107.00 106.10 105.40 104.50 104.50 104.50 105.40 105.40 106.10							

Fig. 19d.

pole at a height equal to the rod reading; having thus constructed a line parallel to the desired grade line, direct the telescope on the fore sight target, and with the same rod reading, "shoot in" the same stakes. Make careful record of data and comparative results.

PROBLEM C7. SETTING SLOPE STAKES.

- (a) Equipment.—Leveling instrument, self-reading leveling rod, 50-foot metallic tape, stakes, axe, marking crayon. (Or, instead of levelling instrument and rod, use special cross-sectioning rods, if assigned.)
- (b) Problem.—Set slope stakes for the construction of a railroad, canal, etc., as assigned.
- (c) Methods.—(Follow the methods described in Chapter VIII, "Railroad Surverying," under the head of "Cross-Sectioning.")

PROBLEM C8. CALCULATION OF QUANTITIES.

- (a) Equipment.—(No instrumental equipment unless planimeter is assigned.)
- (b) Problem.—Compute the quantity of earthwork for an assigned set of cross-section notes.
- (c) Methods.—(1) Transcribe the notes and carefully verify the copy. (2) Calculate the sectional area for each station and intermediate in the notes, and prove the results. (3) Calculate the volume by the "average end area" method, results to nearest 0.1 cubic yard, and check the same. (4) If so instructed, plot the notes on cross-section paper and determine the areas by means of the planimeter as a check. Record the results.

PROBLEM C9. STAKING OUT A BORROW PIT.

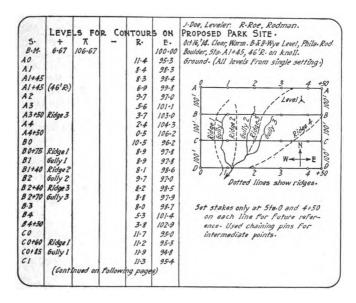
- (a) Equipment.—Engineers' level or transit with attached bubble, leveling rod tape, stakes, axe.
- (b) Problem.—Stake out a borrow pit and take notes required for calculation of earthwork quantities.
- (c) Methods.—(1) Select a base line, preferably outside the limits of the proposed borrow pit, set substantial station stakes say 50 or 100 feet apart along this base; designate these stakes A, B, C, etc. (2) Establish auxiliary reference lines by erecting perpendiculars to the base line at the several stakes, driving temporary stakes for pegs at suitable distances on these lines. (3) Establish a permanent bench mark and run levels, as in profile leveling, along lines starting at A, B, C, etc., noting elevations both at pegs and at marked intermediate changes of slope. (4) In

case actual construction is undertaken, repeat the levels along the same auxiliary lines from time to time and calculate the quantities. (5) Record complete data.

LEVE	B-S-	H-I-	F.S.	T.P.	NTITIES			EMEN				
norran	B. 3.	H-1-	1.2	1.1.	B·M·	Levele		. Rodma VELS				Keeri F.W.Swil
						L-Prop		L-Gutter				
								L:20 Ft.			R-37Ft-	
+43	North F	roperty	Line, h	ealy St		707-4	707-9	707-3	707-4 4-7	707-4	707-2	707-9
4+06	Center	Line, h	ealy 5			708.0 4.1	708.0	707-8	708.2	707-2	707.2 51	706:
+76	South A	ropert	y Line,	Healy S	*	707·5 4·6	707.5	707.6	708.6	707·1 5·0	706·7 5·4	706-6 3-5
3	North E	nd of B.	ridge ov	er Boneya	ard Creek	705·8 6·3	707-2 4-9	708-6 3-5	708·8 3·3	707.5 4.6	705.1	706·2 5·9
0	South En		7.89	708-95 Boneya	d Creek	705·4 11·4	707-0	707-3 9-5	709.0	706·3 10·5	706-1	706-3
2						707-8	708-4	708-2	709.5	708-6	708·2 8·6	708-2
i						711-1 5-7	711-0	710-8	711-3	711-1	711.9	711.9
0 X	North Pr	operty.	Line, Gr	een 5t.		713.9	7/4-0	713·6 3·2	714-0	713.9	7/4.9	714.2
			4.20	715.96								
π	1-07	720-16						3 hours				
0			3.94	719.09				Berger				
T. S.L.B.M.	3.03	723-03			720-00			n. cent				

PROBLEM C10. LEVELS FOR PROFILE AND QUANTI-TIES FOR PAVING A STREET.

- (a) Equipment.—Level, level rod, 3 flag poles, 100-foot steel tape, chaining pins, 50-foot metallic tape, hubs, axe.
- (b) Problem.—Take level rod readings on the center line, right and left curb lines, right and left sidewalk lines, and right and left property lines to determine profiles and quantities for paving street. Plot profiles on Plate A profile paper to a scale of 100 feet to 1 inch horizontal and 10 feet to 1 inch vertical. Estimate the quantities of cut and fill, and paving materials.
- (c) Methods.—(1) Locate the center line of the street and set flag poles on line about 400 feet apart by ranging in with the eye. (2) Drive a hub at one end of the street and call this point station zero. (3) Run a line of differential levels from the Standard B. M. to the zero end of the line.



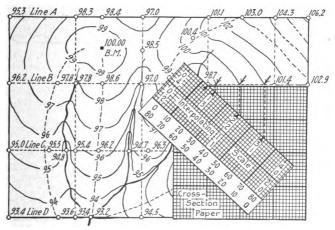
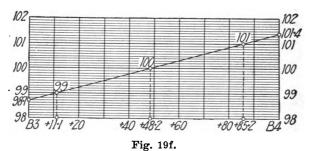


Fig. 19e.—Contour Plat and Device for the Rapid Interpolation of Contours.

Read the rod to 0.01 foot. (4) Read the level rod to 0.1 foot on the ground at center hub. (5) Measure the distance out to the right curb line, right sidewalk and right property lines with the metallic tape and read the rod to 0.1 foot on the ground at station zero. (5) Measure the distance out to the center line to station 1. (8) Measure to the right and left from the chaining pin the required distances with the metallic tape and take rod readings as at station zero. (9) Repeat the process at each station and at abrupt changes intermediate. (10) Check the level circuit. (11) Make profile on Plate A paper, scales 100 feet to the inch horizontal and 10 feet vertical, indicating the several lines by conventional lines or colors. (12) Lay grade line as directed. (13) Show plat at bottom of profile. Plot sections to a scale of 20 feet to the inch and determine areas. (15) Compute quantities of earthwork, paving, etc. Follow the form.



PROBLEM C11. CONTOUR LEVELING.

(a) Equipment.—Engineers' leveling instrument, leveling rod, 100-foot steel tape, stakes, axe.

(b) Problem.—Make a rapid contour survey of an assigned tract of ground with the level and chain.

(c) Methods.—(1) Examine the tract and plan the system of reference lines for locating the points at which levels are to be taken; if the ground is comparatively regular, a simple subdivision into squares of 100 feet may suffice; but if much broken, special lines along gullies and ridges should be included in the survey plan. (2) Stake off the tract according to the plan, and make a record of the same. (3) Starting from an assigned bench, determine the elevations of the ground at the various stakes and at such other

points as may be required to give a correct basis for accurate contouring. (4) Plot the data, and interpolate contours at a specified interval, employing both numerical calculations and geometrical methods, Fig. 19e. (5) Finish the plat, as required.

PROBLEM C12. USE OF CONTOUR MAP.

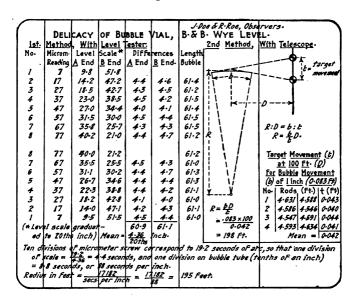
- (a) Equipment.—Contour map, drafting instruments, etc.
- (b) Problem.—From the given contour map: (1) construct profiles on the assigned lines; (2) project a line of specified grade through assigned points on the contour map; make profile, lay grade line and estimate earthwork quantities approximately; (3) calculate the earthwork quantities from the map for given grade planes and limitations of area. (The third step may, perhaps, best be taken with a different map from the first two.)
- (c) Methods.—(1) Use profile paper for the profiles. (2) To project the line on the map, set the dividers at the horizontal distance in which the specified gradient will surmount the vertical interval between successive contour planes, Fig. 19f; then beginning at a specified point, locate points on the successive contour lines up or down on the given gradient, as required; sketch in the route roughly, and project a series of connected curved and tangent lines approximating to it; construct a profile along the new line; lay the required grade line on the profile, and estimate approximate earthwork quantities for specified dimensions and slopes of roadbed. (3) By means of end area method calculate the earthwork quantities required to establish the specified grade planes on the designated contoured area.

PROBLEM C13. RECIPROCAL LEVELING.

- (a) Equipment.—Engineers' level, 2 leveling rods.
- (b) Problem.—Determine the difference of elevation between two bench marks on opposite sides of a river (or wide ravine) by reciprocal leveling.
- (c) Methods.—(1) Set the level up so that a rod reading may be taken on both benches at one setting. Station a rodman at each bench. (2) Take a back sight consisting of a series of say 5 or 10 careful consecutive rod readings.

 (3) Without delay take a like series of readings for a fore-
- (3) Without delay take a like series of readings for a foresight. (4) Set the instrument on the opposite side of the

river or ravine and repeat the above process. (5) Determine a difference of elevation by taking the difference between the mean back sight and fore sight for each setting, and finally take the mean of the two results. Observe rigid care in all details of the problem.



PROBLEM C14. TEST OF DELICACY OF BUBBLE VIAL.

- (a) Equipment.—Engineers' leveling instrument, leveling rod, tape, level tester.
- (b) Problem.—Determine the radius of curvature of the assigned bubble vial. (1) by means of the optical test, and (2) by the level tester.
- (c) Methods.—(1) Measure off a base line say 100 feet long, set level at one end and hold rod on a peg driven at the other end; note the target movement corresponding to a given bubble movement, both in the same linear unit; calculate the radius by the method shown at (h), Fig. 18. (2) Set the level tester on a solid base and place the instrument on it, as indicated at (i), Fig. 18; by means of the

micrometer head and known relations of the level tester, determine the angular equivalent in seconds for one division and also one inch movement of the bubble, from which calculate the radius of curvature of the vial in feet. Follow the form.

PROBLEM C15. COMPARISON OF LEVEL TELESCOPES.

- (a) Equipment.—Five (or other specified number) engineers' levels (both wye and dumpy), leveling rod, metallic tape.
- (b) Problem.—Make a critical examination and comparison of the telescopes of the assigned instruments.
- (c) Methods.—Carefully read the discussion of the telescope in the text. Then compare the telescopes with reference to: (1) magnifying power; (2) chromatic aberration; (3) spherical aberration; (4) definition; (5) illumination; (6) flatness of fields; (7) angular width of field; (8) effective aperture of objective. Make tabulated record of comparisons, giving in separate columns; (a) locker number; (b) kind of level; (c) name of maker; (d) magnifying power, and so on for the other points examined.

PROBLEM C16. TESTS OF THE WYE LEVEL.

- (a) Equipment.—Wye level, Teveling rod, tape.
- (b) Problem.—Test the essential relations and adjustments of the wye level.
- (c) Methods.—Carefully note the construction of the assigned level and the positions of the elementary lines. Then following the methods outlined in the text, test the following adjustments (but do not disturb the adjusting screws): (1) The bubble, both as to the azimuth and altitude movements; find the position of the bubble when parallel to the element of the rings. (2) The line of collimation; its deviation from the axis in 400 feet. (3) The wyes; finding the position of the bubble when the vertical axis is vertical. Keep a neat and systematic tabulated record of observed numerical data, with explanation of the several adjustments.

PROBLEM C17. ADJUSTMENT OF THE WYE LEVEL.

- (a) Equipment.—Wye level (reserved expressly for adjustment), leveling rod, tape, adjusting pin.
- (b) Problem.—Make the full series of adjustments of the wye level.
- (c) Methods.—Follow the methods detailed in the text according to the following program: (1) Adjust the bubble line (a) into the same plane with the bottom element of the rings, and (b) parallel to that element. (2) Adjust the line of collimation to coincide with the axis of the rings, first on a long distance; and then, to test the object glass slide, try it for a short distance; if necessary, shift the reticule in rotation to make the horizontal hair horizontal. and also center the eyepiece. (3) Adjust the bubble line perpendicular to the vertical axis by means of the wye nuts. (4) Test the rings of the wye level by the two-peg test; if the level has a reversion bubble, first test the parallelism of the top and bottom tangent lines, and then test the rings. Keep a clear and systematic record. In each case, state (a) the desired relation, (b) the test, and (c) the adjustment.

PROBLEM C18. SKETCHING THE WYE LEVEL.

- (a) Equipment.—Wye level.
- (b) Problem.—Make a first-class freehand sketch of the assigned wye level.
- (c) Methods.—The sketch should be correct in proportion and clear in detail. The essential parts should be designated in neat and draftsmanlike form, and the elementary lines clearly indicated.

PROBLEM C19. TESTS OF THE DUMPY LEVEL.

- (a) Equipment.—Dumpy level, leveling rod, tape.
- (b) Problem.—Test the essential relations and adjustments of the dumpy level.
- (c) Methods.—Carefully note the construction of the assigned level and the position of the elementary lines. Then, following the methods outlined in the text, test the following adjustments: (1) the bubble line, whether perpendicular to the vertical axis; and if not, what is the angular inclination of the vertical axis when the bubble is in the

middle? (3) The line of collimation, whether parallel to the bubble line. Record the errors and observations systematically.

PROBLEM C20. ADJUSTMENT OF THE DUMPY LEVEL.

(a) Equipment.—Dumpy level (reserved expressly for adjustment), leveling rod, tape, pegs, axe, adjusting pin.

(b) Problem.—Make the essential adjustments of the as-

signed dumpy level.

(c) Methods.—(1) Adjust the bubble line perpendicular to the vertical axis. (2) Adjust the line of collimation parallel to the bubble line by the two-peg method. In describing the adjustments, the record should state (a) the desired relation, (b) the test, and (c) the adjustment.

PROBLEM C21. SKETCHING THE DUMPY LEVEL.

(See Problem C18.)

PROBLEM C22. STRETCHING CROSS-HAIRS.

(a) Equipment.—Engineers' level or transit (or cross-hair reticule), pocket cross-hair outfit, reading glass.

(b) Problem.—Renew the cross-hairs in a level or transit

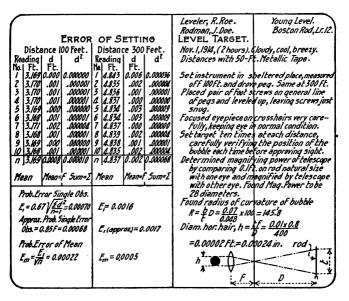
instrument by a method applicable to field use.

(c) Methods.—(If instrument is provided, follow the complete program outlined below; otherwise, merely stretch the lines on the reticule and test same.) (1) Remove the eveniece, carefully preserving the screws from loss. Remove one pair of the capstan headed reticule screws; turn the ring edgewise and insert a sharpened stick in the exposed screw hole, take out the other two screws and remove reticule from telescope tube. (3) Clean the cross-hair graduations, and support the reticule on a sharpened stick, or (if a transit) place it on the object glass with a piece of paper interposed to protect the lens. (4) Select from the capsule (see (d), Fig. 17) two spider lines 2 inches or more long, and fasten a stick to either end of each hair by means of glue from the adhesive paper. (5) Put the hairs in place, '(with the bits of wood hanging loose), shifting them as desired with a pin point or knife blade. (6) Apply a bit of the moistened adhesive paper to the reticule over each hair,

and after a few minutes cut or break the sticks loose. (7) Test the hairs by blowing on them full force. (8) If they stand this test, replace the reticule, and adjust the instrument. Make a record of the process.

PROBLEM C23. ERROR OF SETTING A LEVEL TARGET.

- (a) Equipment.—Engineers' leveling instrument, leveling rod (preferably a New York or Boston rod), tape, pegs.
- (b) Problem.—Determine the probable error of setting the level target at distances of 100 and 300 feet (or such other distances as may be assigned).



(c) Methods.—(1) Determine the magnifying power of the telescope. (2) Determine the radius of curvature of the level vial by the field method. (3) Determine the space on the rod covered by the diameter of the hair. (4) Drive a peg at 100 feet from the level, level up, and secure ten satisfactory consecutive rod readings with rod held truly plumb on the peg; shift the target several inches between read-

ings, and reset without bias; reject no readings; watch the bubble closely, but work briskly. (4) Repeat the series at 300 feet. (5) Determine for each distance the mean rod, the probable error of a single reading, and of the mean, as indicated in the form.

PROBLEM C24. MAKING A LEVELING ROD.

- (a) Equipment.—Piece of straight dressed clear white pine of proper dimensions, steel tape graduated to 0.01 foot, carpenter's tri-square, paint, etc.
 - (b) Problem.—Make a self-reading leveling rod.
- (c) Methods.—(To be devised by the student. See Fig. 27 for suggested graduations.)

PROBLEM C25. COMPARISON OF DIFFERENT MAKES AND TYPES OF ENGINEERS' LEVELS.

- (a) Equipment.—Department equipment, catalogs of representative engineering instrument makers.
- (b) Problem.—Make a critical comparison of the several types and makes of engineers' levels.
- (c) Methods.—Examine the department equipment and study the several catalogs carefully, noting the usual and special features, prices, etc., and prepare a systematic sumurary or digest of the same. Prepare brief specifications for a leveling instrument, and also suggest the preferred make.



CHAPTER V.

THE TRANSIT.

Description.—The engineers' transit consists of an alidade, carrying the line of sight, attached to an inner vertical spindle (or upper motion) which turns in an outer annular spindle (or lower motion). The latter carries the horizontal graduated circle or limb, and is supported by the tripod head. The alidade includes the telescope, magnetic needle with its graduated circle, and the vernier; it may be revolved while the graduated limb remains stationary. The horizontal limb is graduated to degrees and half degrees and sometimes to twenty minutes, and is numbered preferably from zero to 360° in both directions.

The complete transit differs from the plain transit, Fig. 20, in having a vertical arc and level bubble attached to the telescope.



Complete Transit.



Plain Transit.

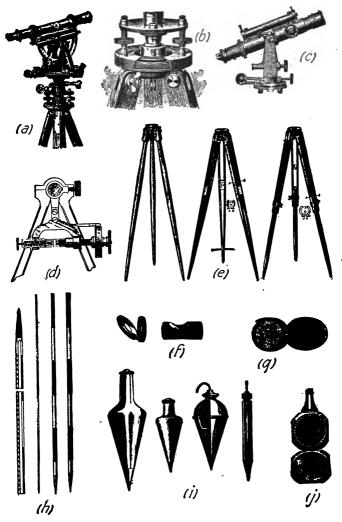


Fig. 21.

In Fig. 21 are shown: (a) the English theodolite; (b) the shifting plates and foot screws of a transit; (c) the Saegmuller solar attachment to the transit; (d) the gradienter; (e) tripods; (f) reflectors; (g) reading glass; (h) flag poles; (i) plumb bobs; (j) the Brunton pocket transit.

The Vernier.—The vernier is an auxiliary scale used to read fractional parts of the main graduated scale or limb. The least count of a direct vernier is found by dividing the value of one division of the limb by the number of divisions on the vernier. With a limb graduated to half degrees and a direct vernier reading to single minutes 30 divisions on the vernier cover 29 divisions on the limb.

In reading a direct vernier observe the following rule: Read from the zero of the limb to the zero of the vernier, then along on the vernier until coincident lines are found. Add the reading of the vernier to the reading of the limb.

In setting the vernier to a given reading, as for example a zero reading for measuring an angle, the tangent movement should be given a quick short motion to secure the last refinement, since a slow movement is not noticed by the eve. Notice adjacent and end graduations.

In Fig. 23, (c) is a vernier reading to single minutes, (d) to half minutes (30"), and (e) to thirds of minutes (20"). The slant in the numerals on the limb corresponds with that on the vernier.

USE OF THE TRANSIT.

Use.—The complete transit is used: (1) to prolong lines; (2) to measure horizontal angles; (3) to measure vertical angles; (4) to run levels; (5) to establish grade lines. The plain transit is confined to the first two uses, unless it has a vertical clamp and tangent movement, when it may be used to "shoot in" grade lines.

Prolongation of Lines.—If the instrument is in adjustment a line can be prolonged by sighting at the rear station and reversing the telescope in altitude. It is, however, not safe to depend on the adjustments of the transit, and important lines should always be prolonged by the method of "double sights," as given in Problem D2. Lines may be prolonged with the plates by sighting at the rear station with the A vernier reading 180°, reversing the alidade in azimuth and locating stations ahead with the A vernier reading zero. A third method employs two points ahead of the instrument.

Measurement of Horizontal Angles.—Horizontal angles are measured as described in Problem D1. If greater accuracy is required, angles may be measured by series or by repetition.

By Series.—In measuring an angle by series all the angles around the point are read to the right, both verniers being read to eliminate eccentricity. The instrument is then reversed in altitude and azimuth and all the angles around the point are read to the left. The readings are checked by sighting back on the first point in each case. These observations constitute one "set." The vernier is shifted between sets 360° divided by the number of sets. The arithmetical mean of the observed values is taken as the true value.

By Repetition.—Angles are measured by repetition as described in Problem D13. This method is especially suited to the accurate measurement of angles with an ordinary transit, and is to be preferred to the series method, which is a favorite where precise instruments are used. In the repetition method all the instrumental errors are eliminated and the error of reading is very much reduced. It is doubtful if it is ever consistent to make more than 5 or 6 repetitions.

Azimuth.—The azimuth of a line is the horizontal angle which it makes with a line of reference through one of its ends, the angles being measured to the right from 0° to 360°, as in (f) Fig. 23. It is usual to assume that the true meridian is the line of reference, the south point being taken as zero in common surveying.

Deflection.—The deflection of a line is the angle that it makes with the preceding line produced, and is called deflection right or left depending upon whether the angle is on the right or left side of the line produced, as in (h), Fig. 23.

Vertical Angles.—Vertical angles are referred to the horizon determined by the plane of the level under the telescope, and are angles of depression or elevation relative to that plane. In measuring vertical angles the instrument should be leveled by means of the level under the telescope and correction should be made for index error of the vernier. With a transit having a complete vertical circle, the true vertical angle may be obtained by measuring the angle with the telescope normal and reversed and taking the mean.

Traversing.—A traverse is a series of lines whose

lengths and relative directions are known. Traverses are used in determining areas, locating highways, railroads, etc.

Azimuth Traverse.—In an azimuth traverse the azimuths of the lines are determined, usually passing around the field to the right. In orienting the transit at any station the A vernier is set to read the azimuth of the preceding course, the telescope is reversed, directed towards the preceding station and the lower motion clamped; the telescope is then reversed in altitude. The reading of the A vernier with telescope normal will then give the azimuth of any line sighted on. If there is any error in collimation the transit may be oriented by sighting back with the A vernier reading the back azimuth of the preceding course. In a closed traverse the last front azimuth should agree with the first back azimuth. The azimuth traverse is especially adapted to stadia and railroad work. Azimuths can be easily changed to bearings, if desired.

Deflection Traverse.—In a deflection traverse the deflection of each line is determined, usually passing around the field to the right. To avoid discrepancies due to error in collimation, the transit may be oriented by sighting at the preceding station with the A vernier set at 180°, the telescope being in its normal position, and the lower motion clamped. The reading of the A vernier will then give the deflection of any line sighted on.

Compass Bearings.—Compass bearings should always be read on an extended traverse as a check against such errors as using the wrong motion or an erroneous reading of the vernier. To guard against errors due to local attraction, back and front bearings should always be read, and the angle thus determined compared with the transit angle.

Leveling with the Transit.—The transit with an attached level is the complete equivalent for the engineers' level. The instrument is leveled up with the plate levels first, after which the position of the attached bubble is controlled by means of the vertical tangent movement.

Grade Lines.—Grade lines may be established with the transit either by means of known distances and calculated rod readings, or by "shooting in" a parallel line by means of the inclined telescope, as described under the use of the engineers' level. For the latter purpose the transit is rather more convenient than the level.

Setting up the Transit.—To set the transit over a point, spread the legs so that they will make an angle of about 30°, place them symmetrically about the point with two legs

down hill. Bring one plate level parallel to two of the legs, force these legs firmly into the ground and bring the plumb bob over the point and the plates approximately level with the third leg, changing the position of the plumb bob with a radial motion and leveling the plates with a circular motion of the leg. Finish the centering with the shifting plates. In leveling up, the bubbles move with the left thumb. Use care to bring the foot screws to a proper bearing.

Parallax.—Before beginning the observations the eyepiece should be carefully focused on the cross-hairs so as to prevent parallax.

Back Sight With Transit.—Always check the back sight before moving the transit to see that the instrument has not been disturbed or that a wrong motion has not been used.

Instrumental Errors.—The transit should be kept in as perfect adjustment as possible, and should be used habitually as though it were out of adjustment, that is, so that the instrumental errors will balance. No opportunity should be lost to test adjustments.

ADJUSTMENTS OF THE TRANSIT.

Elementary Lines.—Fig. 22 shows the elementary lines of the transit, viz., (1) line of collimation; (2) horizontal. axis; (3) vertical axis; (4) plate level lines; (5) attached level lines. These lines should have the following relations: (a) the plate levels should be perpendicular to the vertical axis; (b) the line of collimation should be perpendicular to the horizontal axis; (c) the horizontal axis should be perpendicular to the vertical axis; (d) the attached level line should be parallel to the line of collimation. The following additional relations should exist: (e) the vertical axes of the upper and lower motions should be coincident; (f) the optical center of the objective should be projected in the line of collimation; (g) the center of the graduated circle should be the center of rotation, i. e., there should be no eccentricity.

Plate Levels.—To make the plate levels perpendicular to the vertical axis.—Make the vertical axis vertical and adjust the bubbles to the middle of their race. The vertical axis is made vertical by leveling up, reversing in azimuth, and if the bubbles move, bring them half way back with the foot screws. The adjustment is the same as for the compass, and the reasons are shown in (a), Fig. 13. After adjusting the plate levels with reference to say the upper motion, test them with the lower motion to prove the coincidence of the vertical axes.

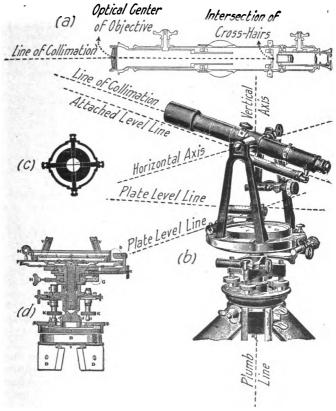


Fig. 22.

Line of Collimation.—To make the line of collimation perpendicular to the horizontal axis.—Construct a straight line and adjust the vertical hair so that the instrument will reverse in altitude on it The straight line may be established either by prolongation beyond a point in front, or

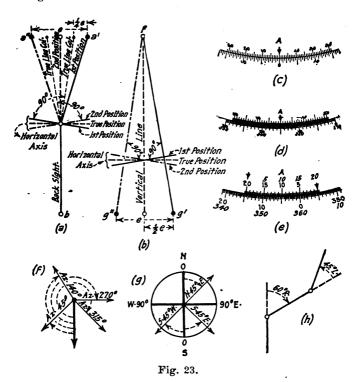
preferably by the methods of double sighting, described in Problem D2. One-fourth the apparent error is corrected in second case as shown in (a), Fig. 23. In deciding which way to move the hair, notice that the optical center is the fulcrum. The transit should be collimated first for equal back and fore sights, say 100 feet or so, and then checked for a distant point in one direction and perhaps 50 feet in the other, so as to test the motion of the optical center of the objective. The points should all be as definite as possible. Chaining pins may be used, or V-marks may be made on the side of a stake driven securely. Each altitude reversal should be checked back and forth to make sure of the prolongations, and the telescope should be handled very carefully. If the cross-hair reticule is removed from the instrument or should be much disturbed, the foregoing adjustment is made approximately and the hair is made vertical by sighting on a plumb line, such as the corner of a building, or by noting whether the hair continuously covers the same point as the telescope is moved in altitude; the collimation adjustment is then made precisely.

Horizontal Axis.—To make the horizontal axis perpendicular to the vertical axis.—Adjust the horiontal axis so that the line of collimation will follow a plumb line. An actual plumb line may be used; or preferably a vertical line may be constructed by first sighting on a high point, then depressing the telescope and marking a low point; then reversing in altitude and azimuth (turning the horizontal axis end for end), sighting at the high point again and marking a second low point beside the first one. The mean of the two low points is vertically beneath the upper one. The transverse plate level is especially important in this process. One end of the horizontal axis is changed, as in (b), Fig. 23.

Attached Level.—To make the attached level and the line of collimation parallel to each other.—Construct a level line and adjust the instrument to agree with it. The level line may be obtained either by using the surface of a still body of water, as of a pond, or it may be constructed by equal back and fore sights, as indicated in (e), Fig. 16. Either the horizontal hair may be changed to bring the line of collimation parallel to the bubble line, or vice versa. The method is the same as used for the dumpy level.

If the bubble vial is a reversion level, as shown at (b), Fig. 18, the adjustment is much simpler. However, the

two-peg test should be applied at least once to the reversion level to prove the parallelism of the top and bottom tangent lines of the bubble vial.



Vertical Arc.—After the last preceding adjustment, the vernier of the vertical circle should be made to read zero when the bubble is at the center of the tube. Bring the bubble to the center and shift the vernier to read zero. If the vernier is fixed, an index correction may be applied to all vertical angles; or the bubble may be made to agree with the vernier and the horizontal hair then adjusted by the two-peg method.

Eccentricity.—Read the two verniers at intervals around the circle; if the verniers have changed the same amount in each case the circle is well centered. If the two verniers have not changed the same amount, the mean of the angles passed over by the verniers is the actual angle through which the instrument has turned. The error cannot be adjusted.

Centering the Eyepiece.—If the intersection of the cross-hairs is not in the center of the field of view, move the inner ring of the eyepiece slide by means of the screws which hold it.

PROBLEMS WITH THE TRANSIT.

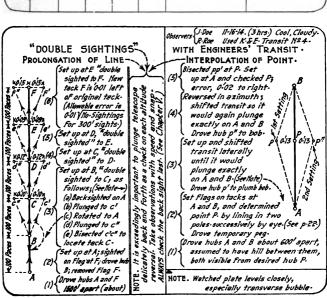
PROBLEM D1. ANGLES OF A TRIANGLE WITH TRANSIT.

- (a) Equipment.—Transit, 2 flag poles, reading-glass.
- (b) Problem.—Measure the angles of a given triangle with the transit.
- (c) Methods.—(1) Set the transit over one of the vertices of the triangle and plumb a transit pole over each of the other two. (2) Set the A vernier to read zero, sight at the left hand point approximately, clamp the lower motion and make an exact bisection with the lower tangent movement. (3) Unclamp the upper motion, sight at the right hand point approximately and make an exact bisection with the upper tangent movement. (4) Read the A vernier to the nearest single minute. This reading is the angle sought. (5) With the A vernier set to read zero repeat the measurement, sighting first at the right hand station and then at the left. The recorded value of the angle is to be the mean of these two determinations which must not differ by more than one minute. (6) Measure the other angles in like manner. The error of closure must not exceed one minute. Follow the prescribed form.

PROBLEM D2. PROLONGATION OF A LINE WITH TRANSIT.

- (a) Equipment.—Transit, 2 flag poles, axe, 6 hubs, 6 flat stakes, tacks.
- (b) Problem.—Prolong a 300-foot base line successively with the transit by the method of "double sights" about 1500 feet, and check on a hub previously established.
- (c) Methods.—(1) Drive two hubs, A and F, about 1500 feet apart. (2) Set the transit over tack in hub A, sight at

Angles of Triangle 5-6-8	Observers, J. Doe & R. Roe. WITH ENGINEERS' TRANSIT.
Station Value of Angle.	Nov-15, 1914 (2 hours). Warm and quiet.
let Meas. 2nd Meas. Mean	Used Hellar & Brightly Transit No-10-
5 88°50' 88°51' 88°50'30"	The lst measurement was made by sighting
6 478471 478501	on Sta-8 with the lower motion, the
" 47°47' 47°47' 47°47'00"	plates clamped at zero; then sighting
8 43°23' 43°23' 43°23'00"	on Sta.6 with the upper motion, and
180°00'30'Y	reading the plates.
100000	The second measurement was made by
(Difference between measurements not	sighting on Sta.6 and then on Sta.8.
to exceed 1')	Used transit poles as targets, plumbing
(Error not to exceed 1')	them very carefully over the monu-
7277 4 70 10 000000 77	ments.
	Sketch shows observed angles.
	Skeren Shows beschieb digital
	1 1
	A 5
	Leaver 2ht
	1.08.30.31
	/- ×
	1 2 10
	7 4
	6 6



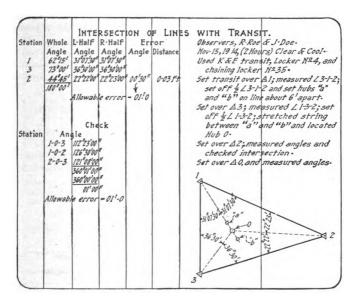
flag pole plumbed over tack in hub F, drive hub B about 300 feet from the transit and locate a tack in line very carefully. Remove the flag pole from hub F. (3) Set the transit over hub B, back sight on hub A and clamp the vertical axis. (4) Reverse the telescope, drive hub C at a distance of about 300 feet and mark line very carefully with a pencil. (5) Reverse the transit in azimuth, sight on hub A; reverse the telescope and locate a second point on hub C. Drive a tack midway between these two points. (6) Set the transit over the mean point on hub C, back sight on hub B, prolong 300 feet and set hub D by double sights. (7) Set over hub D, back sight on hub C, prolong, 300 feet and set hub E, as before. (8) Finally prolong from hub E, with back sight on D, and establish mean tack at terminal hub F. Record the collimation errors at C, D, E, and the final error at F. Follow the form.

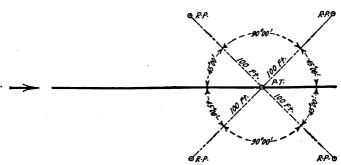
PROBLEM D3. INTERSECTION OF LINES BY TRANSIT.

(a) Equipment.—Transit, 2 flag poles, plumb bob string, axe, 6 hubs, 6 flat stakes, tacks, marking crayon.

(b) Problem.—Determine the intersection of the bisecting lines of two angles of a triangle and check by bisecting the third angle.

(c) Methods.—(1) Drive and tack three hubs so as to form a triangle approximately equilateral and having sides about 400 feet long; properly witness the hubs with guard stakes. (2) Set the transit over one of the vertices of the triangle, and measure the angle as in Problem D1. (3) Set two hubs on the bisecting line, about 6 feet apart, so that the point of intersection of the bisecting lines will come between them, and mark the line by stretching a string between the hubs. Check by measuring each half angle independently. (4) Set the transit over one of the other vertices of the triangle, measure the angle and determine the bisecting line as at the first point. (5) Drive a hub at the intersection of the two bisecting lines and mark the exact point with a tack; check by measuring each half angle independently. (6) Set the transit over the third vertex and determine the angular and linear error of intersection. (7) As a final check measure the angles around the point of intersection of the bisectors. The angular error of closure of any triangle should not exceed one minute. Follow the form.





PROBLEM D4. REFERENCING OUT A POINT.

- (a) Equipment.—Transit, 2 flag poles, 100-foot steel tape, axe, 6 hubs, 6 flat stakes, marking crayon, tacks.
- (b) Problem.—Reference out a point with a transit and tape.

(c) Methods.—(1) Drive two hubs about 500 feet apart and mark them with guard stakes. (2) Set the transit over one of the hubs and reference it out as shown in the diagram. All hubs should be driven flush with the ground, and the exact points should be marked by means of tacks driven into the tops of the hubs. Record in proper form.

PROBLEM D5. TRIANGULATION ACROSS RIVER.

- (a) Equipment.—Transit, 2 flag poles, 100-foot steel tape, axe, 4 hubs, 4 flat stakes, tacks.
- (b) Problem.—Determine the distance across an imaginary river by triangulating with the transit and check by direct measurement.

Simple and Rapid Methods of Triangulation.



Rule of Ten." (I) With transit at A, line in hub at B on opposite side of river.
(2) Turn off angle 5°44' and with one end of tape held at B locate C by swinging on arc under direction of transitman; if the front flagman be provided with a metallic tape, he may locate C alone by hooking the ring of the tape on a projecting tack in hub B.

The desired distance AB may be taken roughly as ten times the measured distance BG. For greater exactness, and 0.1 foot for each 100 foot whit in the distance AB as found by the simple "rule of ten" just stated.

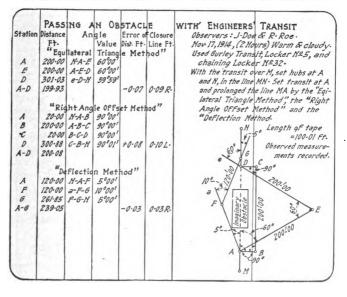
Rod Leveling AB:AD::BC:DE AD=BC

(c) Methods.—(To be devised by the student. Use this and the next problem to learn the relative merits of several good methods. The "rule of ten" method in the sketch below is very rapid and also quite accurate.)

PROBLEM D6. PASSING OBSTACLE WITH TRANSIT.

(a) Equipment.—Transit, 100-feet steel tape, 2 flag poles, axe, hubs, flat stakes, tacks.

	ANGULATION An			ENGINEERS'	
1011011	Ft.	Value			urs) Cold & Clear
0	150-00 D-8-C	9000			
B	150-00 D-5-C	50301			sit, Locker Nº8;
8-0	181.85	3030		nd Chaining L	
0-0	101.00				B, set hub at D
		000			ouble Sights,"
		n of B-D.		ith A as a ba	
	B-D = B-Cx tar				suring B-C with
	Log. B-D = Log.	150-00 + Log- ta	15030		ured L B-C-D.
		609+10-08390			d distance by
	= 2.2			haining B-D.	
	B-D = 181.	96 Ft.			99-98 Ft. Observed
			0	istances rec	arded.
	B-D= B-C x ta				E
2	= 150.00 X				9 39 30' (Complement
	= 181.96 1	7.			TY M
					80
SUN	MARY				N-
Com	puted result	181.96 Ft		7	-
Cha	ned distance	181.85 Ft.		Imaginary /	River
	Difference	0.11 Ft.		To 1	90°00'
	1:0	= 1:1650			
Per	missible 1:d=	1:1000		C & 150 001	$\rightarrow B$
	6			150.00	
				(Base)	
	1				l d A
					1



- (b) Problem.—Prolong a line beyond an imaginary obstacle by three methods and check by direct measurement.
 - (c) Methods.—(To be devised by the student.)

PROBLEM D7. TRAVERSE OF FIELD WITH TRANSIT.

- (a) Equipment.—Transit, 2 flag poles, 100-foot steel tape.
- (b) Problem.—Determine the deflections of the sides of an assigned field with the transit, check angles by observing the magnetic bearings, and measure the lengths of the sides with a steel tape.
- (c) Methods.—(1) Set the transit over one corner of the field, set the A vernier to read 180°, and sight at a flag pole plumbed over the point to the left with the telescope normal. Read and record the magnetic bearing. (2) Keep the telescope normal and sight at the next point to the right. The reading of the A vernier will be the deflection of the second line. (3) Read and record the magnetic bearing and compare the transit and magnetic deflections. (4) Repeat this process for the remaining corners of the polygon taken in succession to the right. Deflections will be based on duplicate readings agreeing within one minute. (5) Measure the sides to the nearest 0.01 foot with the tape. Compare the tape with the standard at the beginning and conclusion of the chaining. (6) From the observed deflections determine the bearings of the field assuming one side as a true meridian. The angular error of closure must not exceed one minuté. Record and reduce data as in the prescribed form. Should a side of the field be obstructed, use one or more auxiliary points (see (c) of D8).

(Most engineers prefer "plunge reversals" to the above method of "plate reversals." To avoid the collimation error involved in a single plunge reversal, the principles of "double sights" must be used and the mean angle taken. To save time, some engineers try to keep the transit always in first-class adjustment, so as to omit one altitude reversal in the "plunge" method, and some turn the transit "end for end" (reverse in azimuth) every setting or so.)

PROBLEM D8. AREA OF FIELD WITH TRANSIT.

- (a) Equipment.—Five-place table of logarithms.
- (b) Problem.—Compute the area of the assigned field by means of latitudes and departures.

7	RAY	ERSE C	F FIELD	A-B-	C-D-E	WITH	ENGINEER'S TRANSIT, DEFLECTION METHOD
Stat	ion	Distance	Deflection	Magnetic	Check	Calculated	Observers: J. Doe & R. Roe.
nst.	Obj.	Ft-	Angle	Bearing	Anale	Bearing	
A		100		N 60°35'E	ringie	Deer my	Used Keuffel & Esser Transit, Locker #
	EB	335-00				5.00°00'E	Assumed that A-B was a true meridia
B	A	0.1		5:33°05'E			Carefully checked each angle.
	C	464.98		54395'F	100704	5.10°13'E	Bubble down on all sights-
0	B		12453'R	543°20'E	10 20 2	DIVISE	Length of Tape = 100.01 Ft.
194		483-72				N.65°20'A	Reduced measurements recorded.
0	0		76°03'P	58135W	DET JON	1100 201	
	E	616-53				N1043'E	Allowable error of closure = 11.
E	0		879468	N.22°25W	, was	1110432	
-	A	242-84	02 70%			586°31'E	E
	-	2.2.44	3700131	100302	370°151	100011	
			100131		100201	7	
	1			(Check)	ZEQUEE!	1	
	- 1		200 00	(CHECK)	239 22	1	
		Calcula	:C	R		/	. /
A-	8	5.00°00'E		N.1043'E	gs		1 98
	8	10°13'L	E	82°46'R			/ 1 1
B-	-	5.10°13'E		5.8631'E			
-		124°53'R	A		(Check	,	A .
C-		N 65 20'N		00 JI.K	CHECK		7
	D	76°03'R					
0-		4.10°43'E					
	1					-	1,40
	1						1
-	_						

		_		1			1				_	_
	1	1					v·21,1914		Trans	J. Doe.	K.	
TRAN	SIT T	RAVER	SE, FI	ELD A	B-C-D-E	-	LATIT	JDES /	AND D			5.
Line	Adjusted	Reduced Distance	COMPL	TATION Logar-	OF LA Computed Latitude	TIT Lat- Cor.	UDES Adjusted Latitude	COMP!	Logar-	OF DE	PAR Dep.	TURES
AB	5.00000	Ft. 335-05			Ff.	Ft.	Ft.			Ft.	Ft.	Ft.
BC	5-10°13'E			200711	5.335-05	1.5	5-334-95	222		00-00		00-00
DC	3-10 13 E	404.38	464.98 4/4.89. 4/8482 37/98 /860	2.66/44 9.99306 2.66050		-10	5-457-51	#64.98 73771- 46498 32549 3255 139	2.66744 9.24888 1.91632	E- 8247	-03	E. 82.50
			457.606	(457-61)				33 82.474	(82.47)			1
CD	N-65 25W	483.72	483.72 206/4.		N-201-24	.05	N-201-29	483.72 63909. 435348 4353		W-439.87	-18	W.439.6
			4837 2902 10 201-237	2.30370 (201.24)		4		145 29 439-875	2.64330 (439.87)			
DE	N-1043E.	616.53	616.53 65289. 354877 49322 1233 308	2.78995 9.99236 2.78231	N-60578	•15	N-605-93	6/6·53 5958/ 6/633 43322 3023 555	2.78995 9.26940 2.05935	E-114:64	.05	E-114-65
EA	5.863/E.	242.84	37 605·777 242·84 67060	(605.78)	5- 14-76	+	5. 14.76	714.644	(114-64)	E24240	. to	E-242-50
LA	5 80 512.	27207	87080- 14570 170 15 14-755	8.78361 1.16893 (14.76)	J- 14-10	-00	3. 14.10	02899. 2/8556 2/8556 1943 49 242-404	2.38452 (242.40)		-10	E-24C30
	Pa	2143-12			N-807-02		N-807-22		1-1019	F43951		E-439.69
2000	of Clos			Ratio Cor.	5-807-42		5-807-22		Ratio Cor.	W-439-87		W-439-69
Actu		55 Ft.	AB BC	2 .10	5- 0-40	-40	0.00	AB BC	2 .03	W- 0.36	.36	0-00
	Diagra		CD DE EA	1 ·05 3 ·15 0 ·00 8 ·40	·40 = ·6	25		CD DE EA	10 ·18 3 ·05 6 ·10 21 ·36	·36 a · l	217	

(c) Methods.—(Follow the instructions in the corresponding problem with the compass, Problem B4, preserving the same degree of precision in the computed latitudes and departures as in the field measurements. In case auxiliary stations are used on an obstructed side of the field, calculate the latitudes and departures of the polygon actually traversed in the field, and then to find the area drop the false corners in calculating the meridian distance and the latitude of the real side of the field.)

PROBLEM D9. STAKING OUT A BUILDING.

- (a) Equipment.—Transit, 100-foot steel tape, 2 flag poles, axe, hubs, tacks, plan of building
- (b) Problem.—On an assigned plot of ground stake out the assigned building.
- (c) Methods.—(1) Orient one side of the enclosing rectangle with reference to a true meridian or a street line. (2) Locate and check up the corners of the rectangle by setting over each corner in turn, passing around to the right, back-sighting on the corner to the left, turning off 90° and locating the corner to the right. (3) Locate the corners of the building by setting stakes on the side lines of the building produced, using the rectangle as a base line. (4) Check all stakes by additional measurements. The rectangle should close to the nearest minute, the linear error should not exceed 1:50,000. Follow the form.

PROBLEM D10. HEIGHT OF TOWER WITH TRANSIT.

- (a) Equipment.—Complete transit, 2 flag poles, leveling rod, 100-foot steel tape, axe, hubs, tacks.
- (b) Problem.—Determine the height of an assigned tower with the transit and steel tape.
- (c) Methods.—(1) Set the transit over a hub located a little further from the base than the height of the tower.
 (2) Level the instrument very carefully with the attached level and determine the index error of the vertical circle.
 (3) Bring the bubble of the attached level to the center and read a level rod held on the base of the tower (4)
- (3) Bring the bubble of the attached level to the center and read a level rod held on the base of the tower (4) Sight at the top of the tower, read the vertical angle, correct for index error and record. (5) Reverse the telescope and locate a second point at least as far from the first as the height of the tower, check by "double sights." (6) Set

STAKING OUT BUILDING
Length of tape = 100 00," this tape being assumed as standard for the constuction of this building.

Located hub A to Fit the site, and then established a true meridian through A by observation on Polaris.

Then constructed a checked rectangle ABGD as Follows:

Set Avansit over hub A and set hub B and temporary hub D; set hub on line Measured all distances twice. Set transit over hub B, sighted at A

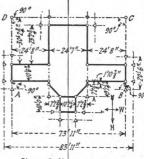
and set temporary hub C; set hub

Set transit over C, sighted on B and checked temporary hub D for angle and distance error &" For line, 32" For distance.

The remainder of the hubs were located with reference to the checked rectangle ABCD.

Surveyors, John Doe & Richard Roe. WITH ENGINEERS' TRANSIT.
Nov. 28,1914. (3 hours). Cool and clear. Used Gurley Transit, Locker No. 6 and Locker No.30.

Hubs are set on line 5' from corners.



Plan of Observatory.

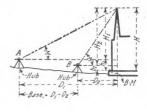
	11000		-			P
Station	Vertical	TOF		ER.	100	
	Angle	Ft.	(Levels)			
A	20°16' 46°24'	150.00				
8	9		3.82=	nz		
	Calc	ulation	of H	eight.		
(1)		Cot. M				
(3)		+h, =h				
(4)		- (h,-				
(5)	D,-D=	= Ha (Co	t. M-Co	.N)-(h.	om (1) , -hz) Cot. M	
(6)	Hz = - :	0,-02+	(h,-h2)	Cot. M		
101	cres 7	60	17-14-66	77-14.		
Subs	ituting		4 50 2	82) Con	and cot	
	H2 =			1-Cot.41		
	=	86.47	Ft.			
403 175	H =	Hzth	= 86.	42 + 3	82	

90.29 Ft.

Observers, J. Doe & R. Roe. WITH ENGINEERS' TRANSIT. Nov. 28, 1914 , (2 hours). Warm & Cloudy. Used Gurley Transit, Locker No.5, and Chaining Locker No. 35.

Set transit over A and measured the vertical angle M, having First determined the index error of vertical circle. Read level rod on base of tower. (h,) Set B in line with A and top of tower and measured D1-D2 as base line. Set transit over B and Found Nand ha. Length of tape = 99.92 ft.

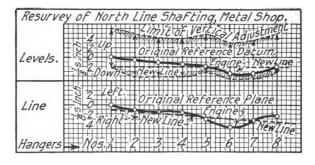
Reduced measurements recorded.



the transit over the second hub, sight at the top of the tower and read the vertical angle, as before. (7) Read the level rod on the base of the tower as before. Each angle and rod reading is to be based on duplicate readings. Follow the form.

PROBLEM D11. SURVEY OF LINE SHAFTING.

- (a) Equipment.—Engineers' transit with attached bubble, leveling rod (or instead of these engineers' instruments, a 16-foot metal-bound straight-edge with an adjustable bubble of say 20-foot radius, a long braided fishing line, and 3 long metal suspenders made exactly alike, from which to suspend straight-edge from line of shafting), 2 good plumb bobs, 50-foot etched steel tape, copper tacks, hatchet.
- (b) Problem.—Make a survey of a line of shafting in a machine shop, and establish a true alinement for it, both vertically and transversely.



(c) Methods.—(1) Establish a reference line for lateral deviations and carefully mark the same. (2) Select a suitable permanent bench mark to which the levels may be referred. (3) Determine the horizontal distance from the vertical reference plane to the line shafting at selected points, say at each hanger. (4) Determine the elevations of the same points by the methods of profile leveling. (5) Plot the data as suggested in the diagram. (6) Note the ruling points and permissible change both laterally and vertically at each hanger, and record the data. (7) Lay grade lines, and prepare data to shift the line shafting to a true position. (8) Make complete record of results.

PROBLEM D12. SURVEY OF RACE TRACK.

- (a) Equipment.—Outfit for transit party (instrument assigned, a long wire, say No. 20, spring balance, thermometer, etc.).
- (b) Problem.—Make the survey for a race track, as instructed.
- (c) Methods.—(1) Standardize steel tape, noting temperature and pull. (2) Make a careful examination of the tract of land with a view to secure the best location for the race



The standard distance is measured on a line 3 feet from the hub-board. The inner edge of the track is thus 2n·3=18.85 feet shorter than the standard distance. The track is banked on curves from 1:12 to 1:15, and, to provide drainage, should be sloped one foot on the straight stretches. The ends of curves are sometimes flattened.

track as regards visibility, drainage, economy of construction and maintenance, etc. (3) After fixing the ruling points, establish the principal axis of the track by locating the centers of the two semi-circles and the intersections of the axis with the curves; also establish the ends of the curves, preferably on the true measured line (3 feet from the hub plank for a sulky track, and 18 inches from the inner edge for a bicycle track). (4) Run in each quadrant,

either by the deflection angle method, or, if trees or other obstructions do not prevent, by using the wire as a radius with observed pull; set points 16 feet apart unless instructed otherwise. (5) After locating the true line, check up the total distance very carefully. (6) Make plat and complete record of survey.

complete record of survey.

PROBLEM D13. ANGLES OF TRIANGLE BY REPETITION.

- (a) Equipment.—Transit, reading glass, 2 chaining pins, 2 tripods with plumb bobs (if necessary).
- (b) Problem.—Measure the angles of a prescribed triangle with transit by repetition.

4.	IGL	De l	or To	ANGLE	5-6	- 8			Richard R	
	Bub	Direc	Object	Vern-A-			Difference		Mean Angle	
A6		tion Right		180°00'00'	00000	00'00"	Nov. 30 1/2	4 (2 Hours)	Cool & Quie	+.
20		1	18	2274720	474720	47'20"	47047'20"		1	Single
					2385620		238°56'20"	47 47 16"		5 Reps.
	Uρ	Left	A 8 A 5		180°00'00' 22747'00		47°47'00"			
			45		58 36 40			47047'20"	4747 18"	s Reps.
A8	D	R	46	000000	180 0000			(3 Hours)	Warm & Qu	iet.
			A5		2237220		43°22'20"			Single.
	١				363200		216 32 00"	43°22'24"		5 Reps.
	U	L	A5 A6		0 00 00" 43°22'20'	22'20"				Single
			20		2165140			43022'20"	43°22'22"	5 Reps
A5	0	R	. 48	00000	1800000	00'00"				100
			46		268 30 20					Single
	U				264 1240			88°50'32'		5 Reps-
	U	7	A6 A8		8830'20					Single
		1	20		849220		444912'20"		88°50'30"	5 Reps.
				1			Error not	to exceed 15	18000010"	

(c) Methods.—(1) Set the transit over one of the vertices of the triangle and set chaining pins in the tops of the monuments at the other two. (2) Set the A vernier to read zero. (3) Sight at the left hand station with the bubble down, and clamp the lower motion. (4) Unclamp the upper motion, sight at the right hand station, read both verniers and record. (5) Unclamp the lower motion, sight at the

left hand station, and check the verniers to see that they have not moved. (6) Unclamp the upper motion and sight at the right hand station but do not read verniers. Repeat until five repetitions of the angle are secured, and read both verniers to eliminate errors of eccentricity. (7) Divide the arithmetical mean of the two vernier readings by five and compare with the value obtained by single measurement. (8) Reverse the instrument in altitude, and set the A vernier to read zero. (9) Sight at the right hand station with the bubble up, and clamp the lower motion. (10) Unclamp the upper motion, sight at the left hand station, read both verniers and record. (11) Unclamp the lower motion, sight at the right hand station, and check the verniers to see that they have not moved. (12) Unclamp the upper motion and sight at the left hand station, but do not read the verniers. Repeat until five repetitions of the angle are secured, and read both verniers to eliminate errors of eccentricity. (13) Divide the mean of the two vernier readings by five and compare with the value obtained by single measurement. (14) Take the mean of the two sets as the most probable value. (15) Measure the other angles in the same manner. The angular error of closure should not exceed 15". Follow the form.

PROBLEM D14. DETERMINATION OF TRUE MERIDIAN BY OBSERVATION ON POLARIS AT ELONGATION.

- (a) Equipment.—Complete transit, reading glass, hub, 2 flat stakes, board 2"x 4"x 3', 4 8d nails, axe, 2 lanterns, good watch set and regulated to keep railroad time.
- (b) Problem.—Determine a true meridian by an observation on Polaris at elongation.
- (c) Methods.—(1) Calculate the time of elongation of Polaris, and regulate and set a good reliable watch to keep railroad time (mean solar time). Calculate the time of elongation of Polaris from Table II.

Set the transit over a hub about 40 minutes before the time of elongation. Level the instrument very carefully, and set the vernier of the vertical circle to read the latitude of the place. (2) Focus the objective on a bright star; sight at Polaris which will be found by following the pointers of the Great Dipper, at an elevation equal to the latitude of the place. (3) With a reflector or a piece of white paper reflect light into the telescope so that the cross-hairs and the

image of Polaris will be visible at the same time. (4) Depress the telescope and establish a target at a distance of about 500 feet; place the plank on the ground and nail it firmly to flat stakes, driving one at each end. (5) Level up again and follow Polaris with the telescope by means of the tangent movement; at elongation it will appear to traverse the vertical hair for several minutes. (6) Depress the tele-

Observers, J. Doe & R. Roe. DETERMINATION OF TRUE MERIDIAN BY OB'S ON POLARIS AT ELONGATION-No. but-Retime A zimuth of Poleris Error

Obs- ble Obs- Observed Corect'n Elongt'n Azimuth

/ Nowe 2 17 m / 29.4 0 00 1 / 29.4 - 07

2 n 2 30 1 28.9 0 01 1 129.4 - 07

3 Up 2 40 1 29.9 0 05 1 / 30.4 + 1/3

4 n 2 48 1 29.9 0 10 1 / 30.9 + 1/8 Dec. 7, 1915 (2 Hours), Clear and warm Buff & Berger Transit No.9, 2 Lanterns, hubs, 2 flat stakes, plank 18"×4"×2", 4 8 d nails, axe, watch set to keep Railread time. Set transit over hub at 1:40 A.M., sighted 129-8 +07 Mean at Polaris, depressed the telescope and [Allowable error = 1:0) established target about 500 ft. From instrument. The plank was placed at right angles to line and nailed to Calculation of Railroad Time of Elongation-Latitude 40°06', Langitude 88°15' a stake driven at each end. Astron-Time U-C Polaris, Pec. 1,1915 8 50.8 Reduction For 3 days is 3 x 3.94 - 23.6 Nade first observation at western elaquiton Reversed instrument in altitude and Astron. Time U.C. Polaris, Dec 7,1915 8 27-2 azimuth between 2nd and 3rd readings Correction for Railroad Time 7.0 Reduced observations R.R. Time U.C. Polaris, Dec. 7, 1915 8 20-2 2,3&4 by the Reduction for Western Flongation + 5 55.0

Pailroad Time " " 2" 15.0" 5.4. following formule: corr. "= 0-058 +2 Calculation of Azimuth of Polaris at Elong'n where t = time Azimuth Polaris, Elong't'n, Jan-1, 1915 12949 from elongation Garrection for Dec.7, 1915 - 0.1
Azimuth Polaris, Elong't'n, Dec.7, 1915
Time of Elongation of Polaris in minutes: the correction being seconds of arc. For Western Elongation add 5 h55 m. to (For Latitude 40°, time U.C. Polaris - For Eastern Elongation 30 min From Polaris at subtract 5h 55 m. From time U.C. elongation). Upper Culmination

scope, sight at a pencil held on the target and mark the point very carefully. (7) As a check make three observations within half an hour after elongation, noting the time of sighting on the star. Reverse the instrument in altitude and azimuth after the first check observation. (8) Reduce the check observations to observations at elongation by the following rule: Multiply the square of the time since elongation in minutes by 0.058, and the product will be the correction to the azimuth of Polaris in seconds of arc, for latitude 40°. (9) The next morning lay off the azimuth of Polaris for each observation to the east or west, depending upon whether the observation was made at western or east-

ern elongation. (10) Check the observed meridian with the standard meridian. The error of the mean of the four observations should not exceed one minute. Record and reduce the data as in the form.

PROBLEM D15. DETERMINATION OF TRUE MERIDIAN BY OBSERVATION ON POLARIS AT ANY TIME.

- (a) Equipment.—The same as in Problem D14.
- (b) Problem.—Determine a true meridian by observing Polaris at any time.
- (c) Methods.—Make the observations as described in Problem D14, noting the time of observation to the nearest minute, and reversing the instrument in altitude and azimuth between the 3rd and 4th observations. The transit should be leveled up very carefully with the attached bubble, particular attention being given to the horizontal plate level at right angles to the line of sight. (2) Reduce the observations by means of the tables.

A star comes to the meridian 4 minutes (nearly) earlier each day than it did the preceding day. The sideral day is therefore shorter than the solar day, the time from upper culmination to upper culmination being 23 hours 56.1 minutes mean solar time. The time from Upper Culmination to Lower Culmination is 11 hours 58 minutes.

Astronomical time, or Local Mean Solar time, is the time that would be kept by the mean sun and is obtained from Standard, or railroad time, by adding or subtracting 4 minutes for each degree of longitude that the place of observation is east or west of the Standard Meridian. The Astronomical day begins at noon of the civil day of the same date, and is reckoned from zero to 24 hours.

The Hour Angle of Polaris is found by subtracting the correct Local Mean Solar time of Upper Culmination, Table II, from the Local Mean Solar time of observation.

The Time Argument used in entering Table IV is the Hour Angle of Polaris, or 23 hours 56.1 minutes minus the Hour Angle of Polaris. Table IV is used as follows: Find the "hours and minutes" of the time argument in the left hand column of either page of Table IV. On the horizontal line with the "time before or after upper culmination" (time argument), the azimuth of Polaris for a declination of Polaris of 88° 51' will be found in the column under the given latitude. The correction to the azimuth for each

TABLE I.

AZIMUTH OF POLARIS AT ELONGATION FOR ANY YEAR BETWEEN
1915 AND 1924.

Latitude	1915	1916	1917	1918	1919	1920	1921	1922	1923	1924
30°	1°19.6	1°19.2	1°18.8	1°18.5	1°18.1	1°17.8	1°17.4	1°17.0	1°16.7	1°16.4
31	20.4									17.2
32	21.2		20.5		19.8		19.1	18.7	18.3	18.0
33	22.1	21.8								18.8
34	23.1		22.4	22.0	21.6		20.9	20.5		19.8
35		1 23.7	1 23.3	1 23.0	1 22.6	1 22.2	1 21.8	1 21.5	1 21.1	1 20.7
36	25.2	24.8	24.4	24.0	23.6			22.5	22.1	21.7
37	26.3	25.9	25.3	25.1	24.7	24.3	24.0	23.6	23.2	22.8
38	27.4	27.0	26.6	26.2	25.9	25.5	25.1	24.7	24.3	23.9
39	28.6	28.2	27.8	27.5	27.1	26.7	26.3	25.8	25.5	25.1
40	1 29.9	1 29.5	1 29.1	1 28.7	1 28.3	1 27.9	1 27.5	1 27.1	1 26.7	1 26.3
41	31.3		30.4	30.0	29.6	29.1	28.8	28.4	28.0	27.6
42	32.7	32.3	31.9	31.5	31.0	30.6	30.2	29.8	29.4	29.0
43	34.2	33.8	33.4		32.5	32.1	31.8	31.2	30.8	30.4
44	35.8	35.3	34.9	34.5	34.1	33.6	33.2	32.8	32.4	31.9
45	1 37.4	1 37.0	1 36.6	1 36.1	1 35.7	1 35.3	1 34.8	1 34.4	1 34.0	1 33.5
46	39.2	38.7	38.3	37.8	37.4	37.0	36.5	36.1	35.6	35.2
47	41.0			39.7	39.2			37.9		37.0
48	43.0	42.5	42.0	41.6	41.1	40.7	40.2	39.8	39.3	38.8
49	45.0	44.5	44.1	43.6	43.1	42.7	42.2	41.7	41.3	40.8
50	1 47.2	1 46.7	1 46.2	1 45.7	1 45.3	1 44.8	1 44.3	1 43.8	1 43.4	1 42.9

Correction For Above Table

The above table was computed with the mean declination of Polaris for each year. A more accurate result will be had by applying to the tabular values the following corrections, which depend on the difference of the mean and the apparent place of the star. The deduced azimuth will, in general, be correct within 0.3.

For middle of	Correction in minutes	For middle of	Correction in minutes
January	-0.5	July August September October November	+0.2
February	-0.4		+0.1
March	-0.3		-0.1
April	0.0		-0.4
May	+0.1		-0.6
June	+0.2		-0.8

minute of change in Declination of Polaris are given in the last two columns on each page. The changes for latitudes between 30° and 40° and between 40° and 50° may be interpolated. The Declination of Polaris at any date may be

TABLE II.

LOCAL MEAN (ASTRONOMICAL) TIME OF THE CULMINATION AND ELONGATION OF POLARIS IN THE YEAR 1915. (Computed for latitude 40° and longitude 90° or 6^h west of Greenwich.)

Date	East elongation	Upper culmination	West elongation	Lower culmination						
1915 January 1. February 1. 15. March 1. 15. April 1. 15. May 1. 15. June 1. 15. July 1. 15. September 1. 15. October 1. 15. November 1. 15. December 1. 15.	h m 0 51.7 23 52.5 22 45.3 21 50.1 20 54.8 19 59.6 18 52.7 16 54.8 15 59.9 14 53.3 13 58.5 12 01.1 10 54.5 9 59.8 8 53.2 7 58.3 6 55.5 6 00.6 4 53.7 3 58.6 2 55.6 2 00.4	h m 6 46.9 5 51.6 4 44.5 3 49.2 2 54.0 1 58.8 0 67.9 22 50.0 21 55.1 20 48.5 19 53.1 17 56.3 16 49.7 15 55.0 14 48.4 13 53.5 12 50.7 11 55.8 10 48.9 9 53.8 8 50.8 7 55.6	h m 12 42.1 11 46.8 10 39.7 9 44.4 8 49.2 7 54.0 6 47.1 5 52.0 4 49.2 2 47.6 1 52.8 0 50.2 23 51.5 22 44.9 21 50.2 20 43.6 18 45.9 17 51.0 16 44.1 15 49.0 14 46 0 13 50.8	h m 18 44.9 17 49.6 16 42.5 15 47.2 14 52.0 13 56.8 12 49.9 11 54.8 10 52.0 9 57.0 8 50.4 7 55.6 6 53.0 5 58.2 4 51.7 3 56.9 2 50.3 1 55.4 0 62.7 23 53.8 24 69.9 21 53.8 20 48.8 19 53.6						
	Correctio	n For Years	After 1915							
1916 add										

found from Table III. For example the azimuth of Polaris with a time argument of 9 hours and 15 minutes in latitude 40°, on April 21, 1915, was as follows: From Table III the declination of Polaris on April 21 was very closely 88° 51.25′. From Table IV for declination 88° 51′ the azimuth of Polaris was 58.65′; the correction for 0.25′ was 0.83 \times 0.25 =0.21′, and the azimuth was 58.65′ – 0.21 = 58.44′. If the exact time argument is not found in the table, the azimuth may be found with sufficient accuracy by direct inter-

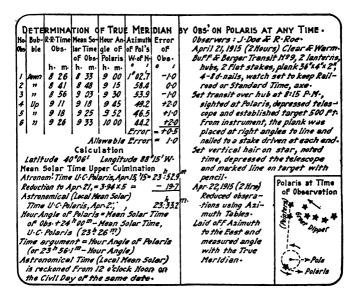
polation. Azimuths for latitudes between values given in Table IV may be found by direct interpolation. The nearest whole degree of latitude is usually sufficiently ac-

TABLE III.

DECLINATION OF POLABIS FOR 1915.

Date	Declination	Date	Declination	
Jan. 1	88° 51′.54	July 1	88° 51′.05	
Feb. 15	51.58 51.57	15 August 1	51 05 51.09	
March 1	51.54 51.49	Sept. 15	51.13 51.21	
15 April 1	51.43 51.35	Oct. 15	51.28 51.38	
15 May 1	51.27 51.20	Nov. 1	51.47 51.58	
June 1	51.14 51.08	Dec. 1	51.67 51.75	
15	51.06	15	51.81	

To obtain the declination for the corresponding time for years after 1915, add $0.31~\rm min.$ for each year to the corresponding declination for 1915.

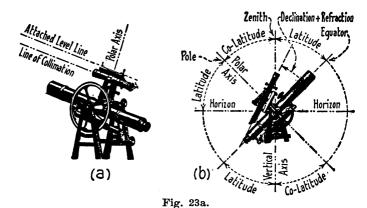


curate. The time used in making observations should be correct to the nearest minute, if accuracy is desired.

Table III was compiled from "Ephemeris for the Sun and Polaris and Tables of Azimuth of Polaris for the year 1915," published by the Department of Interior, General Land Office. Tables I, II and IV were compiled from "Principal Facts of the Earth's Magnetism," published by the U. S. Coast and Geodetic Survey, 1914.

The observations should be made as near elongation as possible, for the reason that Polaris is moving most rapidly in azimuth near culmination and errors in observing the time and using the table are then a maximum.

With careful work the range of 6 reduced observations should in no case exceed 1' of arc. Record the data and make the calculations as in the form.



PROBLEM D16. DETERMINATION OF TRUE MERIDIAN WITH SOLAR TRANSIT.

- (a) Equipment.—Complete transit with solar attachment, reading glass, solar ephemeris, axe, hubs, tacks.
- (b) Problem.—Determine a true meridian with a solar transit.
- (c) Methods.—(There are various forms of solar attachments, to transits, among which are the Saegmuller, (a), and the Buff and Berger, (b), Fig. 23a; the former is the best known. The theory of all solar attachments in general use is the same, and is as follows: In order to bring

TABLE IV. AZIMUTHS OF POLARIS AT ANY HOUR ANGLE.

Hour Angle before or after	Azimu		olaris co 88° uths giv	51'	for Decl	ination	Correct 1' incre declina Pola	tion of
upper cul- mination	Lat. 30°	Lat. 32°	Lat. 34°	Lat. 36°	Lat. 38°	Lat. 40°	Lat. 30°	Lat. 40°
h m 0 15 0 30 0 45	05.28 10.52 15.73	05.38 10.75 16.07	05.52 11.02 16.45	05.67 11.30 16.88	05.82 11.62 17.35	06.00 11.95 17.87	-0'08 -0.15 -0.23	-0.08 -0.17 -0.27
1 00	20.85	21.32	21.83	22.40	23.02	23.70	-0.30	-0.35
1 15	25.90	26.47	27.10	27.80	28.57	29.43	-0.38	-0.43
1 30	30.82	31.50	32.25	33.08	34.00	35.02	-0.45	-0.52
1 45	35.62	36.40	37.27	38.23	39.28	40.45	-0.52	-0.60
2 00	40.25	41.13	42.12	43.20	44.38	45.70	-0.58	-0.67
2 15	44.70	45.68	46.77	47.97	49.30	50.75	-0.65	-0.75
2 30	48.95	50.03	51.22	52.53	53.98	55.58	-0.72	-0.82
2 45	53.00	54.17	55.45	56.87	58.42	60.15	-0.77	-0.88
3 00	56.80	58.05	59.42	60.93	62.62	64.47	-0.83	-0.95
3 15	60.37	61.68	63.13	64.75	66.52	68.48	-0.88	-1.00
3 30	63.67	65.05	66.58	68.27	70.13	72.20	-0.93	-1.05
3 45	66.68	68.13	69.73	71.50	73.45	75.60	-0.97	-1.10
4 00	69.40	70.90	72.57	74.40	76.43	78.67	-1.02	-1.15
4 15	71.82	73.38	75.10	76.98	79.08	81.38	-1.05	-1.20
4 30	73.93	75.53	77.30	79.23	81.38	83.75	-1.07	-1.23
4 45	75.73	77.35	79.15	81.13	83.33	85.75	-1.10	-1.25
5 00	77.18	78.85	80.67	82.68	84.92	87.38	-1.13	~-1.27
5 15	78.32	79.98	81.83	83.88	86.13	88.63	-1.15	-1.28
5 30	79.12	80.80	82.67	84.72	86.98	89.50	-1.15	-1.30
5 45	79.57	81.25	83.12	85.18	87.45	89.97	-1 15	-1.30
6 00	79.68	81.37	83.22	85.28	87 55	90 07	-1.17	-1.30
6 15	79.43	81.12	82.97	85.02	87.28	89.77	-1.15	-1.30
6 30	78.87	80.53	82.37	84.40	86.63	89.10	-1.13	-1.28
6 45	77 97	79.60	81.42	83.40	85.62	88.05	-1.12	-1.27
7 00	76.73	78.33	80.10	82.07	84.23	86.62	-1.10	-1 25
7 15	75.17	76.73	78.47	80.38	82.50	84.83	-1.08	-1.22
7 30	73.28	74.82	76.50	78.35	80.42	82.68	-1.07	-1.20
7 45	71.10	72.57	74.20	76.00	77.98	80.18	-1 03	-1.15
8 00	68.60	70.02	71.60	73.33	75 23	77.35	-1.00	-1.10
8 15	65.82	67.18	68.68	70.35	72.18	74.20	-0.95	-1.07
8 30	62.77	64.07	65.48	67.07	68.82	70.73	-0.90	-1.02
8 45	59.45	60.67	62.02	63.52	65 17	66.98	-0.85	-0.97
9 00	55.88	57.03	58.30	59.72	61.23	62.95	-0.80	-0.90
9 15	52.08	53.15	54.33	55.63	57.07	58.65	-0.75	-0.83
9 30	48.07	49.05	50.13	51.33	52.65	54.12	-0.70	-0.77
9 45	43.85	44.73	45.73	46.82	48 02	49.35	-0.63	-0.70
10 00	39.45	40.25	41.13	42.12	43.20	44.40	-0.57	-0.63
10 15	34.88	35.58	36.37	37.23	38.20	39.25	-0.50	-0.57
10 30	30.17	30.78	31.47	32.20	33.03	33.95	-0.43	-0.48
10 45	25.33	25.85	26.42	27.05	27.73	28.50	-0.37	-0.40
11 00	20.40	20.82	21.27	21.77	22.33	22.95	-0.30	-0.33
11 15	15.37	15.68	16.03	16.40	16.83	17 28	-0.22	-0.25
11 30	10.28	10.48	10.72	10.97	11 25	11.57	-0.15	-0.17
11 45	05.15	05.25	05.37	05.50	05.63	05.78	-0.07	-0.08
Elongation Azimuth Hour Angle	hm s	1°21.37 h m s 5 57 08	hms	hm s	1°27.57 h m s 5 56 24	hms	8	-1.30 +3

TABLE IV. AZIMUTHS OF POLARIS AT ANY HOUR ANGLE.

	1							
Hour Angle before or after	Azimı		88	omputed 51' ven in m	l for decl	ination	Correction for 1' increase in declination of Polaris	
upper cul- mination	Lat. 40°	Lat. 42°	Lat. 44°			Lat. 50°	Lat. 40°	Lat. 50°
h m 0 15 0 30 0 45	06.00 11.95 17.87	06.18 12.35 18.45	06.40 12.77 19.08	06.63 13.23 19.78	06.90 13.77 20.57	07.20 14.35 21.45	-0.08 -0.17 -0.27	-0.10 -0.22 -0 32
1 00	23.70	24.47	25.30	26.23	27.28	28.45	-0.35	-0.42
1 15	29.43	30.37	31.42	32.57	33.87	35.30	-0.43	-0.53
1 30	35.02	36.13	37.38	38.77	40.30	42.02	-0.52	-0.63
1 45	40.45	41.75	43.18	44.77	46.55	48.52	-0.60	-0.72
2 00	45.70	47 17	48.78	50.58	52.58	54.82	-0.67	-0.82
2 15	50.75	52.37	54.17	56.15	58.37	60.85	-0.75	-0.90
2 30	55.58	57.35	59.30	61.48	63.90	66.62	-0.82	-0.98
2 45	60.15	62.07	64.18	66.53	69.15	72.07	-0.88	-1.07
3 00	64.47	66.50	68.77	71.28	74.08	77.20	-0.95	-1.13
3 15	68.48	70.65	73.05	75.72	78.68	82.00	-1.00	-1.20
3 30	72.20	74.48	77.00	79.82	82.93	86.42	-1.05	-1.27
3 45	75.60	77.98	80.62	83.55	86.82	90.45	-1.10	-1.33
4 00	78.67	81.13	83.88	86.90	90.30	94.08	-1.15	-1.38
4 15	81.38	83.93	86.77	89.90	93.40	97.28	-1.20	-1.43
4 30	83.75	86.37	89.27	92.50	96.10	100.07	-1.23	-1.47
4 45	85.75	88.43	91.38	94.68	98.33	102.42	-1.25	-1.50
5 00	87.38	90.10	93.10	96.45	100.17	104.32	-1.27	-1.52
5 15	88.63	91.38	94.42	97.80	101.57	105.75	-1.28	-1.53
5 30	89.50	92.27	95.33	98.73	102.52	106.73	-1.30	-1.55
5 45	89.97	92.75	95.83	99.23	103.03	107.27	-1.30	-1.57
6 00	90.07	92.83	95.92	99.32	103.10	107.32	-1.30	-1.55
6 15	89.77	92.53	95.58	98.97	102.73	106.93	-1.30	-1.55
6 30	89.10	91.83	94.85	98.20	101.93	106.07	-1.28	-1.53
6 45	88.05	90.73	93.72	97.02	100 68	104.77	-1.27	-1.52
7 00	86.62	89.25	92.18	95 42	99.02	103.03	-1 25	-1.48
7 15	84.83	87.40	90.27	93.42	96.93	100.85	-1 22	-1.45
7 30	82.68	85.18	87.97	91.03	94.45	98.27	-1.20	-1.42
7 45	80.18	82.60	85.28	88.27	91.57	95.25	-1.15	-1.37
8 00	77.35	79.68	82.27	85.13	88.32	91.85	-1.10	-1.32
8 15	74.20	76.43	78.90	81.65	84.68	88.08	-1.07	-1.27
8 30	70.73	72.87	75.20	77.82	80.72	83.93	-1.02	-1.20
8 45	66.98	68.98	71.20	73.67	76.40	79.45	-0.97	-1.13
9 00	62.95	64.83	66.92	69.22	71.78	74.63	-0.90	-1.07
9 15	58.65	60.40	62.33	64.48	66.87	69.53	-0.83	-0.98
9 30	54.12	55.73	57.52	59.48	61.68	64.13	-0.77	-0.92
9 45	49.35	50.82	52.45	54.25	56.25	58.48	-0.70	-0.83
10 00	44.40	45.72	47.17	48.78	50.58	52.58	-0.63	-0.75
10 15	39.25	40.42	41.70	43.13	44.72	46.48	-0.57	-0.67
10 30	33.95	34.95	36.07	37.30	38.67	40.20	-0.48	-0.57
10 45	28.50	29.35	30.28	31.32	32.47	33.75	-0.40	-0.48
11 00	22.95	23.62	24.37	25.20	26.13	27.15	-0.33	-0.38
11 15	17.28	17.80	18.37	19.00	19.70	20.47	-0.25	-0.30
11 30	11.57	11.90	12.28	12.70	13.17	13.72	-0.17	-0.20
11 45	05.78	05.97	06.15	06.37	06.60	06.85	-0.08	-0.10
Elongation Azimuth Hour Angle	hm s	hm s	hms	hms	1°43.13 h m s 5 54 53	hms	-1.30 +3	-1 55 +3

the image of the sun into the center of the solar telescope when the line of collimation of the solar telescope makes an angle with the line of collimation of the main telescope equal to the sun's declination corrected for refraction, and the line of collimation of the main telescope is elevated at an angle equal to the co-latitude of the place of observation, it is rigidly necessary that the line of collimation of the main telescope lie in a true meridian as shown in (b), Fig. 23a.

The elementary lines of a solar attachment are: (1) The polar axis; (2) the line of collimation of the solar telescope; (3) the attached level line. These lines should have

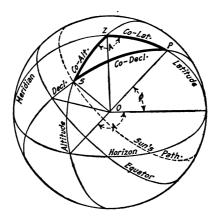


Fig. 23b.

the following relations: (1) The polar axis should be perpendicular to the line of collimation of the solar telescope and the horizontal axis of the main telescope; (2) the line of collimation of the solar telescope and the attached level line should be parallel. The methods of making these adjustments are obvious.

The declination of the sun (see Fig. 23b for explanation of astronomical terms) for the place of observation is found by adding, algebraically, the hourly change multiplied by the number of hours since Greenwich mean noon (6 A. M., 90th Meridian) to the declination of the sun, as given in the solar ephemeris for Greenwich mean noon for the given date. The setting (apparent declination) is found

by taking the algebraic sum of the refraction correction and the declination of the sun obtained as above. The refraction is always plus; the declination is plus when the sun is north and minus when south of the celestial equator; and the hourly change in declination is plus when the sun is moving north and minus when moving south.

The "Pocket Solar Ephemeris and Refraction Tables for Use with Saegmuller's Solar Attachment," is given in "Handbook for Engineers" by George N. Saegmuller, published by Bausch & Lomb Optical Co., Rochester, N. Y. An "Ephemeris of the Sun and Polaris, and Tables of Azimuths of Polaris" is published by the General Land Office for each year. This Ephemeris may be obtained by addressing the Department of Interior, General Land Office, Washington, D. C., or may be purchased at a price of 5 cents per copy from the Government Printing Office, Washington, D. C. The true local mean solar time should always be used, and may be obtained from standard or railroad time by adding or subtracting four minutes for each degree that the place of observation is east or west of the standard meridian. The mean refraction of the sun for different altitudes is given in Table V.)

TABLE V.

MEAN REFEACTION OF THE SUN.

BABOMETER 30 INCHES, TEMPERATURE 50° FAHE.
(Refraction makes observed altitude too large.)

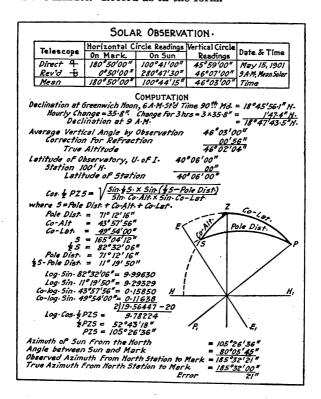
Altitude,	Refraction,	Altitude,	Refraction,	Altitude,	Refraction,
Degrees	Minutes	Degrees	Minutes	Degrees	Minutes
10	5.10	24	2.02	50	0.70
12	4 25	26	1.83	55	0.58
14	3.62	28	1.67	60	0.48
16	3 17	30	1.53	65	0.38
18	2 80	35	1.25	70	0.30
20	2 48	40	1.03	80	0.13
22	2.22	45	0.85	90	0.00

(1) Calculate the apparent declination (setting) of the sun for several different times, varying by 15 minutes, between 8 and 10 o'clock A. M. and 2 and 4 o'clock P. M. (2) Set the transit over the hub, level up very carefully with the attached bubble, and very carefully adjust the main transit and solar attachment. Determine the index error of the vertical circle, and either correct it or apply it to all vertical angles with its proper sign. (3) Level the transit

	ERMIN.					WITH SOLAR TRANSIT.
	Time					Observers, J. Doe & R. Roe.
	of Obs	tion .	Cor.	(App. Dea)	mufh	May 20, 1901. (4 Hrs.) Clear, & warm.
1					Z2"11"	
2	8:45	+19549	+0.6	+/9 35.5	2212'	muller Solar Attachment, hubs, axe,
3	9:00	+1935:1	+06	+1985.7	2290'	
4	9:15	+19 55.2	+0.5	+199557	22013	Ephemeris (Handbook for Engineers,
5	9:30	+19355	+0:5	+19358	22'11'	By Geo.M. Saegmuller, Bausch & Lomb
	P.M.					Optical Co. Rochester, M.Y.)
6	2:30	+19 580	+0.5	18385	22'09'	Tested Transit and Solar Attachment
7		+19'58'1			2290'	and found both in perfect adjustment
8	3:00	+19312			22'09'	Set transit over hub, leveled up very
9	3:15	+19'58'4			22'11'	carefully with long bubble, found
0	3:30	+19385			220091	Index Error of Vert-Circle = Zero.
•	True A	eimuth	af Line	-	22105	circle and leveled solar telescope by
Allowal	ble erro	r 01.		Error =	0003	means of its attached bubble.
					30™A·M·	
	de 40°0					circle-Telescope pointed 5-both times.
	clinatio					Set A vernier at zero and sighted at
	A.M. h					Ste 3 with lower motion-
	tion For					Unclamped upper motion, moved transit
	ntion of					on vertical axis and solar on its
	tion Ga					polar axis, and brought image of sun
	:1· et 8·					into center of solar at 8:30 A·M·
	ent. Dec					Mean Solar Time (M.S.Time = R.R.time + 7.0
TIRIES I	W85 C8	CUIDT	50 IN II	KE MB.	nner.	Read azimuth Repeated until 10 values
<u> </u>						were determined. (5:A.M. & 5 P.M.)

very carefully with the attached bubble. Bring the line of collimation of the main telescope and the line of collimation of the solar telescope parallel by sighting on a distant point, and point the main telescope south. (4) Set off the apparent declination (setting) with opposite sign on the vertical circle, i. e., dip the telescope when the declination is plus (north), and elevate the telescope when the declination is minus (south). (5) Level the solar telescope by means of its attached bubble. (6) Set off a plus vertical angle on the vertical circle equal to the co-latitude of the place. (7) Set the A vernier at zero and sight at a point on the true meridian. (8) Unclamp the upper motion, turn the main telescope about its upper motion and the solar telescope about its polar axis until the image of the sun is brought to the center of the cross lines in the solar telescope at the time for which the declination was computed. and clamp the upper motion. The line of collimation of the main telescope will then be in the meridian. (9) Read the horizontal plates. The reading will be the azimuth of the line first sighted on. (10) Repeat, using the setting corresponding to the time of observation, until ten values are obtained. If possible make five determinations in the A. M.,

and five in the P. M., about the same time from noon. The mean of these observations will eliminate instrumental errors. The most favorable time for making observations with a solar transit is from 8 to 10 A. M. and from 2 to 4 P. M. (11) Determine the true azimuth of the given line. The error of the determination of the meridian should not exceed one minute. Record as in the form.



PROBLEM D17. DETERMINATION OF TRUE MERIDIAN BY DIRECT OBSERVATION ON THE SUN.

(a) Equipment.—Complete transit, reading glass, hub, axe, colored eyepiece or colored shade to fit over objective, good watch set to keep standard time, solar ephemeris.

- (b) Problem.—Determine a true meridian by a direct observation on the sun with a transit.
- (c) Methods.—(1) Set the transit over a hub and level up very carefully with the attached bubble. (2) Test the adjustments of the transit very carefully, and determine the index error of the vertical circle. (3) Sight on a horizontal mark and read the horizontal plates. (4) Sight at the sun directly, by the aid of the colored eyepiece or colored glass shade, and bring his image tangent to the horizontal and vertical wires. (5) Read vertical circle and horizontal plates. (6) Reverse the telescope and make a second observation the same as the first except that the sun should be in the opposite quarter of the field of view. (7) The mean of the vertical and horizontal circle readings will give the apparent altitude and plate reading of the sun's center. (8) Observe the standard time of the observation and reduce to mean solar time by adding or subtracting 4 minutes for each degree that the place of observation is east or west of the standard meridian. (9) Calculate the angle PZS in the P Z S triangle as shown in the accompanying form. Refraction makes the sun appear too high and it should therefore be subtracted. (10) Determine the azimuth of the line from the hub to the mark and check the observed azimuth. (The data for this problem may be obtained from Saegmuller's "Solar Ephemeris and Refraction Tables," or from the "Ephemeris of the Sun and Polaris, and Tables of Azimuths of Polaris," by the General Land Office, mentioned in Problem D16. Mean refraction of the sun for different altitudes is given in Table V.) (11) Where considerable accuracy is desired, make a second observation when the sun is about the same distance on the opposite side of the meridian. The error of the determination should not exceed 1 minute.

PROBLEM D18. COMPARISON OF TRANSIT TELESCOPES.

- (a) Equipment.—Five engineers' transits.
- (b) Problem.—Make a critical comparison of the telescopes of five engineers' transits.
- (c) Methods.—Follow the methods outlined in the comparison of level telescopes.

PROBLEM D19. TEST OF A TRANSIT.

(a) Equipment.—Transit, reading glass, leveling rod, chaining pins, foot rule.

(b) Problem.—Test the following adjustments of an assigned transit: (1) Test the graduation for eccentricity. (2) Test the plate levels to see if they are perpendicular to the vertical axis. (3) Test the line of collimation to see if it is perpendicular to the horizontal axis. (4) Test the horizontal axis to see if it is perpendicular to the vertical axis. (5) Test the level under the telescope to see if the tangent to the tube at the center is parallel to the line of collimation. (6) Test the vertical circle to see if the vernier reads zero when the line of sight is horizontal.

(c) Methods.—Make the tests as described in the first part of this chapter but do not make any of the adjustments or tamper with any of the parts of the instrument. Check each test. Make a careful record of the methods and errors, including a statement of the manner of doing correct work with each adjustment out.

PROBLEM D20. ADJUSTMENT OF A TRANSIT.

(a) Equipment.—Transit, reading glass, leveling rod, chaining pins, adjusting pin, small screw driver.

(c) Methods.—Make the following tests and adjustments of an assigned transit that has been thrown out of adjustment by the instructor: (1) Test the graduation for eccentricity. (2) Adjust the plate levels perpendicular to the vertical axis. (3) Adjust the line of collimation perpendicular to the horizontal axis. (4) Adjust the horizontal axis perpendicular to the vertical axis. (5) Adjust the level under the telescope parallel to the line of collimation. (6) Adjust the zero of the vertical circle to read zero when the line of sight is horizontal. (7) Center the eyepiece.

(c) Methods.—Make the tests and adjustments as described in the first part of this chapter. Use extreme care in manipulating the screws and if any of the parts stick or work harshly, call the instructor's attention before proceeding. Repeat the tests and adjustments. Make a careful record of methods and errors.

PROBLEM D21. SKETCHING A TRANSIT.

- (a) Equipment.—Engineers' transit.
- (b) Problem.—Make a first-class sketch of an engineers' transit.
 - (c) Methods.—(See similar problem with the level.)

PROBLEM D22. ERROR OF SETTING FLAG POLE WITH TRANSIT.

- (a) Equipment.—Transit, iron flag pole, flat stake 1"x 2"x 15", foot rule.
- (b) Problem.—Determine the probable error of setting a flag pole with the transit at a distance of 300 feet. Repeat for 600 feet.

		1		l		Observers , J. Doe & R. Roe.
	OR OF		ING F		POLE	WITH ENGINEERS' TRANSIT.
Distance	No-of	Distance	ď	9z	· '	Dec. 6, 1914. (2 hours) Cool and Quiet.
Ft.	Setting	ln•	ln•			Used Buff & Berger Transit, Locker No.9,
300	1	1.18	0-18	0-0324		flat stake, I"x 2"x 15", and Iron Flag pole.
1	Ż	1.38	-02	-0004		Sighted at iron Flag pole set on stake
1 1	3	1-30	.06	· 0036		which had been placed on ground at
1 1	4	1.53	•/7	.0289		about 300 ft. from the Transit, and
1 1	.5	1.32	-04	• 0016		clamped both plates; then measured
	6	1.38	-02	.0004		the distance in Inches From a line
1	7	1.29	-07	.0049		drawn across the board.
1 1	8	1.46	-10	.0100		With both plates clamped, lined in the
1 1	9	1-46	-10	-0100		rod 10 times in all, the Plagman not-
1 1	10	1.30	-06	·0036		ing the distance From the line.
]	Mean	1.36		0-0958	-Σd²	The pole was shifted each time.
1 1						Repeated test for 600 ft.
600	1	1.14	0.25	0-0625		Probable Error for 300 Ft.
	2	1.56	•17	-0289		$E_1 = 0.6745 \sqrt{\frac{50^2}{9}} = 0.6745 \sqrt{\frac{0958}{9}} = 0.103 \text{ in}$
1 1	3	1-14	•25	-0625		
1 1	4	1.22	•17	·0289		$E_m = \frac{E_r}{\sqrt{n}} = \frac{0.003}{1.00} = 0.032 \text{ in.} = 0.0027 \text{ Ft.}$
1 1	5	1.76	•37	·/369		1/10 1/10 - 1/10
1 1	6	1.55	•16	·0256		Em (Angle) = lan -1 0-0027 = 1.8.
1 1	1	1.23	./6	-0256		Probable Error For 600 Ft.
1 1	8	1.10	•29	-0841		$E_i = 0.6745 \sqrt{\frac{5478}{9}} = 0.247 in.$
i i	9	1.55	·16	0256		2, 13,72 9 - 1,727 ///
	10	1.65	-26	-0676		$E_m = \frac{0.247}{V_{IO}} = 0.078 in = 0.0065 Ft.$
	Mean	1.39		0-5472	=Σd².	110
1	- 1	- 1			1	E_m (Angle) = $tan^{-1} \frac{0.0065}{600} = 2.2$
	. 1	- 1				

(c) Methods.—(1) Set the transit up and sight at the flag pole plumbed near the middle of the stake at a distance of about 300 feet. (2) Measure the distance from the point of the flag pole to a mark on the stake. (3) Keep the vertical axis clamped, and move the pole to one side. (4) Set the pole with the transit, and measure the distance from the first line. (5) Repeat until at least ten consecutive satisfactory results are obtained. (6) Compute the probable error of a single observation and of the mean of all the observations (see chapter on errors of surveying), and reduce the mean error to its angular value. (7) Repeat for 600 feet. Determine distances by pacing. Follow the form.

PROBLEM D23. REPORT ON DIFFERENT MAKES AND TYPES OF TRANSITS.

- (a) Equipment.—Department equipment, catalogs of the principal makers of engineers' transits.
- (b) Problem.—Make a critical comparison of the several types of transits made by the different makers.
 - (c) Methods.—(See similar problem with the level.)



CHAPTER VI.

TOPOGRAPHIC SURVEYING.

Topographic Map.—A topographic map is one which shows with practical accuracy all the drainage, culture, and relief features that the scale of the map will permit. These features may be grouped under three heads as follows: (1) the culture, or features constructed by man, as cities, villages, roads; (2) the hypsography, or relief of surface forms, as hills, valleys, plains; (3) the hydrography, or water features, as ponds, streams, lakes. The culture is usually represented by conventional symbols. The surface forms are shown by contours (lines of equal height), (a), Fig. 24, or hachures, (b), Fig. 24. The water features are shown by soundings, conventional signs for bars, etc.

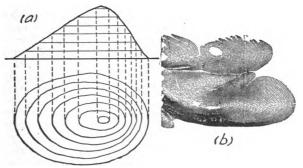


Fig. 24.

Topographic maps may be divided into two classes depending upon the scale of the map. Small scale topographic maps are made by the U. S. Coast and Geodetic Survey and the U. S. Geological Survey, and are drawn to a scale of 1:62,500, 1:125,000 or 1:250,000 with corresponding contour intervals of 5 to 50, 10 to 100, and 200 to 250 feet. These maps show the streams, highways, railroads, canals, etc., in

outline but do not show any features of a temporary character. For topographic symbols, see Chapter XI.

Large scale topographic maps are drawn to a scale of 400 feet to 1 inch (1.4800), or greater, with contour intervals from 1 to 10 feet depending upon whether the ground is flat or hilly Roads, streets, dwellings, streams, etc., are drawn to scale. Features too small to be properly represented when drawn to scale are drawn out of proportion to the scale of the map.

Topographic Survey.—The object of a topographic survey is the production of a topographic map, and hence neither time nor money should be wastefully expended in obtaining field data more refined than the needs of the mapping demand. A topographic survey may be divided into three parts: (1) the reconnaissance; (2) the skeleton of the survey; (3) filling in the details.

Reconnaissance.—The reconnaissance is a rapid preliminary survey to determine the best methods to use in making the survey and the location of the principal points of control. A careful reconnaissance enables the topographer to choose methods that are certain to result in a better map and a distinct saving of time.

Skeleton.—There are three general methods of locating the skeleton of a topographic survey: (1) tie line survey with chain only, (2) fraverse method with transit or compass; (3) triangulation system, (f), Fig. 30. The first method is used for the survey of small tracts. The second method, in which the distances are measured with the chain, tape, or stadia, is used on railroad and similar surveys. The third method, in which triangulation stations are connected with each other and with a carefully measured base line and base of verification, is used on surveys for small scale maps and on detailed or special surveys, such as surveys of cities and reservoir sites.

Filling in Details.—There are three general methods employed for filling in the details: (1) with transit or compass and chain; (2) with transit and stadia; (3) with plane table and stadia. The transit and stadia are used by the Mississippi and Missouri River Commissions. The plane table and stadia are used by the U. S. Coast-and Geodetic and the U. S. Geological Surveys.

Topographic City Survey.—A topographic city survey is one of the best examples of a survey for a large scale map. It is usually based on a system of triangulation executed with precision and connected with carefully measured base

lines. The details of the survey are usually taken up in the following order: (1) reconnaissance and location of triangulation stations; (2) measurement of base line and base of verification; (3) measurement of angles by repetition; (4) establishment of bench marks by running duplicate levels; (5) adjustment of angles of triangulation system; (6) computation of sides, azimuths and coordinates; (7) filling in details, usually with transit and stadia; (8) plotting of triangulation and other important points on the map by rectangular coordinates; (9) plotting the details and completing the map. The instructions given on the succeeding pages are for a survey of this type.

Hydrographic Survey.—Hydrographic surveying is divided into river and marine. The first includes the location of bars and obstructions to navigation, and the determination of the areas of cross-section, the amount of sediment carried, etc. The second includes the making of soundings, location of bars, ledges, buoys, etc. The depth of the water is determined by making soundings with a lead or rod, and the velocity is gaged by means of floats or a current meter, (d), Fig. 31.

Soundings are located: (1) by two angles read simultaneously from both ends of a line on the shore, (f), Fig. 31; (2) by keeping the boat in line with two flags on shore, and determining the position on the line by means of an angle read on the shore, or by a time interval; (3) by intersecting ranges, (g), Fig. 31; (4) by stretching a rope or wire across the stream; (5) by measuring with a sextant in the boat at the instant that the sounding is taken two angles to three known points on the shore, (c), Fig. 31; the point is located by solving the three point problem graphically with the three arm protractor, (e), Fig. 31; (6) by locating the position of the boat at the instant that the soundings are taken with transit and stadia. The first three methods are used on small river or lake surveys. The fourth method is used where soundings are taken at frequent intervals. The fifth method has been used almost exclusively in locating soundings in harbors, lakes, and large rivers. The sixth method is rapidly coming into general use and promises to be the favorite method.

THE STADIA.

Description.—The stadia is a device for measuring distances by reading an intercept on a graduated rod. The stadia-hairs, shown in (g), Fig. 27, are carried on the same

reticule as the cross-hairs and are placed equidistant from the horizontal hair. The stadia-hairs are sometimes placed on a separate reticule and made adjustable. It is, however, considered better practice by most engineers to have the stadia-hairs fixed and use an interval factor, rather than try to space the hairs to suit a rod or to graduate a rod to suit an interval factor.

Stadia Rods.—Stadia rods are always of the self reading type. In Fig. 27, (a) and (b) are the kind used on the U. S. Coast Survey; (c) on the U. S. Lake Survey; (d) and (c) by the U. S. Engineers. A target for marking on the rod the height of the horizontal axis of the transit above the station occupied is shown in (f), Fig. 27.

Theory of the Stadia.—In Fig. 25, by the principles of optics, rays of light passing from points A and B on the rod through the objective so as to emerge parallel and pass through the stadia-hairs a and b, respectively, must inter-

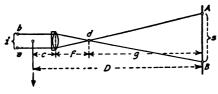


Fig. 25.

sect at the principal focal point d in front of the objective; therefore the rod intercept, s is proportional to the distance, g from the principal focal point in front of the objective.

Stadia Formula For Horizontal Line of Sight and Vertical Rod.—In Fig. 25, from similar triangles we have

$$s:g::i:f$$
 (1)

From which
$$g = \frac{f}{i} s = k. s$$
 (2)

and
$$D = k. s + (c + f)$$
 (3)

Stadia Formula For Inclined Line of Sight and Vertical Rod.—In Fig. 26 we have

141

$$BD = AE. \cos a$$
 (approx.) (4)

and
$$D = k. s. cos a + (c + f)$$
 (5)

but H = D. cos a

$$= k. s. cos^2 a + (c + f) cos a$$
 (7)

$$= k. s - k. s. sin^2 a + (c + f) cos a$$
 (8)

also
$$V = D$$
. sin a (9)

= k. s.
$$\sin a \cdot \cos a + (c + f) \sin a$$
 (10)

$$=\frac{1}{2}$$
 k. s. $\sin 2 a + (c + f) \sin a$ (11)

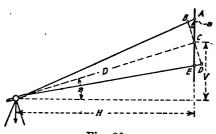


Fig. 26.

Use of the Stadia.—The transit is set up over a station of known elevation and with a given direction or azimuth to another visible station; the height of the line of collimation above the top of the station is determined either by holding the rod beside the instrument and setting the target, or preferably by graduating one leg of the tripod and using the plumb bob; then with the transit oriented on a given line, "shots" are taken to representative points, and record made of the rod intercept, vertical angle and azimuth. In reading the intercept the middle hair is first set roughly on the target, then one stadia-hair is set at the nearest foot-mark on the rod and the intercept read with the other stadia-hair, after which the precise vertical angle is taken, and the azimuth is read.

Reducing the Notes.—The notes may be reduced by means of tables, diagrams, or a special slide rule. The slide rule is the most rapid. There are several forms of stadia slide rule that are very accurate and are convenient for field use.

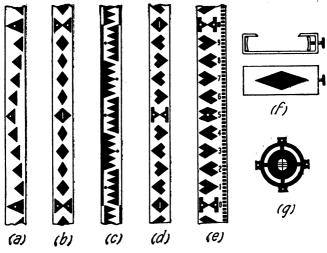


Fig. 27.

THE PLANE TABLE.

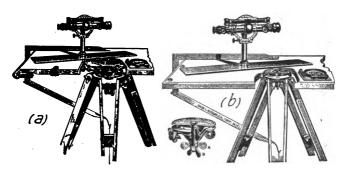
Description.—The plane table consists of an alidade, carrying a line of sight and a ruler with a fiducial edge. The alidade is free to move on a drawing board mounted on a tripod. The drawing board is leveled by means of plate levels. The line of sight should make a fixed horizontal angle with the fiducial edge of the ruler. The complete plane table is a transit in which the horizontal limb has been replaced by a drawing board.

There are three general types of plane tables: (1) the Coast Survey plane table, (a), Fig. 28; (2) the Johnson plane table, (b), Fig. 28; (3) the Gannet plane table, (d), Fig. 29.

Use of the Plane Table.—In making a survey with the plane table the angles are measured graphically and the

lines and points are plotted in the field. The principal methods of making a survey with a plane table are: (1) radiation; (2) traversing; (3) intersection; (4) resection.

Radiation.—In this method a convenient point on the



Complete Plane Tables. Fig. 28.

paper is set over a selected point in the field, and the table clamped. The line of sight is then directed towards each point to be located in turn and a line is drawn along the

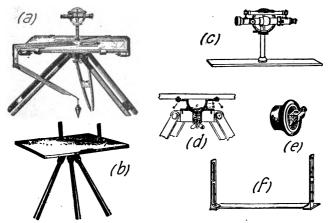
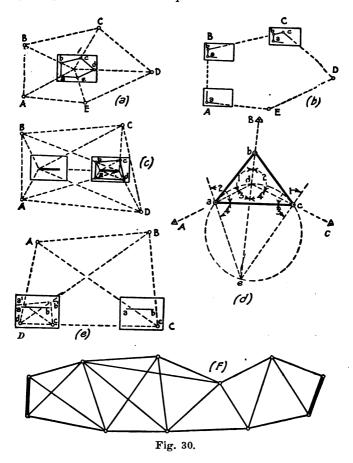


Fig. 29.

fiducial edge of the ruler. The distances, which may be determined by measuring with chain, tape or stadia, are plotted to a convenient scale, (a), Fig. 30.

Traversing.—This method is practically the same as traversing with a transit, (b), Fig. 30. Care should be used in orienting the plane table to get the point on the paper over the corresponding point on the ground as nearly as the character of the work requires.



Intersection.—In this method the points are located by intersecting lines drawn from the ends of a measured base line, (c), Fig. 30.

Resection.—In the resection method the plane table is set up at a random point and oriented with respect to either three or two given points, which gives rise to two methods known respectively as the three-point and two-point problems.

Three Point Problem.—Where three points are located on the map and are visible but inaccessible, the plane table is oriented by solving the "three point problem." There are several solutions, the best known of which are: (1) the mechanical solution; (2) the Coast Survey solution; (3) Bessel's solution; (4) algebraic solution. The problem is indeterminate if a circle can be passed through the four points.

In the mechanical solution the two angles subtended by the three points are plotted graphically on a piece of tracing paper, and the point is located by placing the tracing paper over the plotted points.

In Bessell's solution, (d), Fig. 30, a, b, c are three points on the map corresponding to the three points, A, B, C on the ground, and D is the random point at the instrument whose location, d, it is desired to find on the map. Construct the angle 1 with vertex at point c as follows: Sight along the line ca at the point A, and clamp the vertical axis. Then center the alidade on c and sight at B by moving the alidade, and draw a line along the edge of the ruler. Construct the angle 2 with vertex at a in the same manner. The line joining b and c will pass through the point d required. Orient the board by sighting at d with the line of sight along the line c d, and locate d by resection.

Two Point Problem.—To orient the board when only two points' are plotted, proceed as follows: Select a fourth point, c; that is visible, and with these two points as the ends of a base line, (e), Fig. 30, laid off to a convenient scale, locate two points a' and b' on the map by intersection. The error of orienting the board will be the angle between the lines a-b and a'-b'. The table can now be oriented and the desired point located on the board by resection.

Adjustments.—The adjustments of the plane table are: (1) the plate levels; (2) the line of collimation; (3) the horizontal axis; (4) the attached level. These adjustments are practically the same as those for the transit.

THE SEXTANT.

Description.—The sextant consists of an arc of 60°, with each half degree numbered as a whole degree, (a), Fig. 31, combined with mirrors so arranged that angles can be measured to 120°.

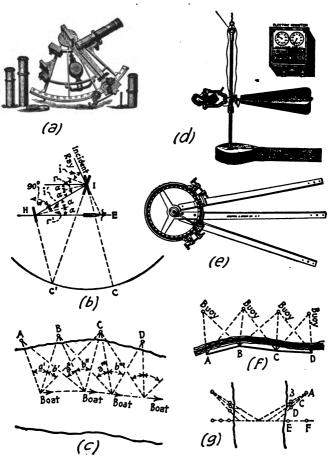


Fig. 31.

Theory.—The principle upon which the sextant is constructed is that if a ray of light is reflected successively between two plane mirrors, the angle between the first and last direction of the ray is twice the angle of the mirrors.

In (b), Fig. 31, the angles of incidence and reflection

are equal,

$$i = r$$
 and $i' = r'$, and $E = (i + r) - (i' + r') = 2(r - r')$ $C' = (90^{\circ} - i') - (90^{\circ} - r) = (r - r')$

and therefore E=2 C'

but C' = angle CIC', by geometry, since the

mirrors are parallel for a zero reading.

Use of the Sextant.—To measure an angle between two objects with a sextant, bring its plane into the plane of the two objects; sight at the fainter object with the telescope and bring the two images into coincidence. The reading is the angle sought. The angle will not be the true horizontal angle between the objects unless the objects are in the same level with the observer. Since the true vertex of the measured angle shifts for different angles, the sextant should not be used for measuring small angles between objects near at hand.

Adjustments, Index Glass.—To make the index glass, I, perpendicular to the plane of the limb, bring the vernier to about the middle of the arc and examine the arc and its image in the index glass. If the glass is perpendicular to the plane of the limb, the image of the reflected and direct portions will form a continuous curve. Adjust the glass by means of the screws at the base.

Horizon Glass.—To make the horizon glass, H, parallel to the index glass, I, for a zero reading. With the vernier set to read zero, sight at a star and note if the two images are in exact coincidence. If not, adjust the horizon glass until they are. If the horizon glass cannot be adjusted, bring the images into coincidence by moving the arm and read the vernier. This reading is the index error which must be applied with its proper sign to all the angles measured.

Line of Collimation.—To make the line of collimation parallel to the limb. Place the sextant on a plane surface

and sight at a point about 20 feet away. Place two objects of equal height on the extreme ends of the limb, and note whether both lines of sight are parallel. If not, adjust the telescope by means of the screws in the ring that carries it.

PROBLEMS IN TOPOGRAPHIC SURVEYING.

PROBLEM E1. DETERMINATION OF STADIA CONSTANTS OF TRANSIT WITH FIXED STADIA-HAIRS.

- (a) Equipment.—Complete transit, stadia rod, steel tape, set chaining pins, foot rule.
- (b) Problem.—Determine the stadia constants c, f and k for an assigned transit.
- (c) Methods.—(1) Set up the transit and set ten chaining pins in line about 100 feet apart on level ground. Plumb the stadia rod by the side of the first pin. (3) Set the lower hair on an even foot or half foot mark keeping the telescope nearly level, and read the upper stadia-hair. (4) Record the intercept. (5) Read the intercept on the rod at the remaining pins. (6) Measure the distance from the center of the transit to each pin with the steel tape. Focus the objective on a distant object, measure f (the distance from the plane of the cross-hairs to the center of the objective), and c (the distance from the center of the objective to the center of the instrument). (8) Calculate the value of the stadia ratio, k, for each distance by substituting in the fundamental stadia formula. (9) Take the arithmetical mean of the ten determinations as the true value. (10) Compute the probable error of a single observation and of the mean of all the observations. The interval factor should be determined by the instrument man under the conditions of actual work. The determination should be checked at frequent intervals during the progress of the field work. Follow the prescribed form.

PROBLEM E2. STADIA REDUCTION TABLE.

(a) Equipment.—(No instrumental equipment required.)

(b) Problem.—Compute a stadia reduction table giving the horizontal distances from a point in front of the objective equal to the principal focal distance for the stadia intervals from 0.01 feet to 10 feet, for the transit used in Problem E1.

10.			MATIO	Y OF			
	S				STADI	A CON	STANTS - FIXED HAIRS.
11			D-(c+F)	K	d	d2	Observers, J. Doe & R. Roe.
	Ft.		(c+f=1-17)		1	- 3.	Dec 14, 14. (2 Hours) Cool & Cloudy.
11	-81	180.41	179.24	99.02	0.02	0.0004	Used Buff & Berger Transit, Locker 12,
2 2	2.70	268.40	267-23	98.96	0.08	0.0064	and Chaining Locker Nº 38.
3 3	.58	355.32	354-15	98.92	0.12	0.0144	Set 10 chaining pins in line about 100 Ff
4 4	.05	400.89	399.72	98.72	0.32	0-1024	apart on level ground.
5 4	1.86	482.80	481.63	99-11	0.07	0.0049	With telescope of transit nearly
6 3	61	556.30	555-13	99.20	0.16	0-0256	level and determined intercept
7 6	5.50	643.58	642-41	98.84	0.20	0-0400	"s" at each pin by setting lower
8 7	.90	786-93	785.76	99.47	0.43	0.1849	hair on a foot or half foot mark
9 9	1.15	914.40	9/3-23	98.91	0.13	0.0169	and reading upper hair.
1010	1.31	1024-71	1023.54	99.26	0-22	0.0484	
	1	a grant	Mean	99.04	2d2=	0.4443	transit to each pin with steel
		-/-		7.11	-		tape to nearest 0.01 Ft.
E	1=	2.67/20	= 0.6	710.44	2 =	0.15 Ff	With object glass focused on a distant
		F.		7-1	1		object, determined c and f by
E	m=	EI	= 0.6	1/20	1, =	0-05 Ft	measuring distance from center
	2	111		1 // //	4		of objective to center of the
	1	c=	0.47 F	f.			horizontal exis and the plane
		F=	0.70 F	f.	1		of the cross-wires respectively.
		C+F=	1-17 F	<i>f</i> .			Determined the different values
		4.5	7			1	of k by substituting in the
		19-4	1	1.5			formula D=K5+c+F.
							Contract and Street Street
		34760				-	
	1						
		*					

		Sec. Co.	6 2 1	1.0			Observers, J. Doe & R. Roe.
		AZIM	TH T	RAVER	SE W	ITH	TRANSIT AND STADIA.
itat	ion	Azimuth	Mag.	Distance	Vertical	Elevation	
	Obj.		Bearing	Ft.	Angle	Ft.	Used Buff & Berger Transit, Locker No-12
A			,			718.00	and Stadia Board No.6.
	F	0000	N.400'W.	432	+00201		Stadia Constants : a+F = 1-17 Ft., k = 100-00
10	8	196931	5-12°10'W.	622	-00401	(-7-2)	Sighted at target set at H.I. For Vert.
B				7		710.8	Angle.
	A	16°13'	N.1200 E.	624	+0°38'		Oriented the transit by Azimuth reversals
	C	2270161	5.43 15W.	499	+0°50'	(+7.3)	k k
C						718-1	
	B	47016'	N-4390'E.	499	-0°50'	3	E F)
	D	0031	N.4°05'W.	758	- 1º10'	(-15.4)	K '-E'
0						702.7	1 8
2	C	180°031	5.490'E.	756	+ 19121		
10	E	6014'	N.2º20 E.	618	+0°56'	(+10-1)	J E-W
E		Marin I				712.8	9- 1 PA;
(7)	0	186°14'	5-2°20'W.	618	-0°56'		11 1/4
44	F	8996'	N-8595'E.	473	+0°54'	(+7.4)	D) , N
F	100	14.00	16			720.2	4 /
-	E	269 461	5-85°15'W.	475	-0°54'		12
	A	180°01'	5.4°05 E.	434	-0°20'	(-2.5)	
A	904	(B. 9)	7			717.7	88
	004	180°00		1		718-0	/ /
E	rol	-= 0°01'	1		Error	= 0.3	1
Al	lowa	ble erro	-2:	Allowa	Ve Erro	-0.5 Ft.	7
	100						CV
	5.1				1		

(c) Methods.—(1) Prepare form for calculation. (2) Compute the horizontal distances by substituting the different values of s in the stadia formula. Compute D' for values of s varying from 0.01 foot to 0.1 foot varying by 0.01 foot; from 0.1 foot to 1 foot varying by 0.1 foot; and from 1 foot to 10 feet varying by 1 foot.

		IA REDUC	TA HOITS		
(c+f)=1.	20 feet.	k=115.75	D=k5+	(c+f) = D	+ (c+F)
Stadia Reading 5	Distance D'=kS	Stadia Reading S	Distance D'= kS	Stadia Reading S	Distance D'= KS
0·01 ·02 ·03 ·04 ·05 ·06 ·07 ·08 ·09 ·10	1·2 2·5 4·6 5·8 6·9 8·1 10·6	0·1 ·2 ·3 ·4 ·5 ·6 ·7 ·8 9 1·0	11.6 23.2 34.7 46.3 57.9 69.4 81.0 92.6 104.2 115.8	1.0 23 4 5 6 7 8 9 10	115.8 231.5 347.2 463.0 578.8 694.5 810.2 926.0 1041.8 1157.5

(To use the table, take the sum of the values of D' corresponding to the units, tenths and hundredths of s as given in the table. To the value of D' thus obtained add c plus f.)

PROBLEM E3. AZIMUTH TRAVERSE WITH TRANSIT AND STADIA.

- (a) Equipment.—Complete transit, stadia rod, steel pocket tape.
- (b) Problem.—Make a traverse of the perimeter of an assigned field with a transit and stadia.
- (c) Methods.—(1) Set the transit over one corner of the field and set the A vernier to read the back azimuth of the preceding course. (2) Sight at a stadia rod held edgewise on the last station to the left with the telescope normal, and clamp the lower motion. (3) Read the intercept on the rod to the nearest 0.01 foot. (4) Sight at the target set at height of first station and read the vertical angle to the nearest minute. (The observer should measure the height of the horizontal axis above the station with the steel pocket tape, or one tripod leg may be graduated and the instrument height determined by swinging the plumb bob out against

the leg.) (5) Unclamp the upper motion, sight at the next station to the right and clamp the upper motion. (6) Read the A vernier, (this will be the azimuth of the course). (7) Read the intercept on the rod. (8) Measure the vertical angle by sighting at the target set at the height of the horizontal axis as before. (9) Set the transit over the next station to the right and determine the intercepts and vertical angles as at the first station. (10) Determine the stadia intercepts and vertical angles at the remaining stations, passing around the field to the right. (11) Reduce the intercepts to horizontal distances before recording. (12) Compute the vertical differences in elevation using mean distances and vertical angles. (13) Compute latitudes and departures to the nearest foot using a traverse diagram or traverse table. Follow form B4. (14) Compute the permissible error of closure of the traverse by means of Baker's formula (see Chapter IX "Errors of Surveying"); using "a" equals one minute times square root of number of sides, and "b" equal 1:500. If consistent, distribute the errors in proportion to the several latitudes and departures, respectively. (15) Compute the area by means of latitudes and departures, and reduce to acres.

PROBLEM E4. SURVEY OF FIELD WITH PLANE TABLE BY RADIATION..

- (a) Equipment.—Plane table, stadia rod, 2 flag poles, engineers' divided scale, drawing paper, 6H pencil.
- (b) Problem.—Make a survey of an assigned field by radiation with the plane table.
- (c) Methods.—(1) Set the plane table up at some convenient point in the field and select a point on the drawing board that will allow the entire field to be plotted on the paper. (2) Sight at one of the stations with the ruler centered on the point on the paper. (3) Draw a line along the fiducial edge of the ruler towards the point. (4) Measure the distance to the point with the stadia. (5) Lay off the distance on the paper to the prescribed scale. (6) Locate the remaining points in the same manner. (7) Complete the map in pencil. The map should have a neat title, scale, meridian, etc. (8) Trace the map on tracing linen. (9) Compute the area by the perpendicular method, scaling the dimensions from the map.

PROBLEM E5. SURVEY OF A FIELD WITH PLANE TABLE BY TRAVERSING.

(a) Equipment.—Plane table, stadia rod, 2 flag poles, engineers' divided scale, drawing paper, 6H pencil.

(b) Problem.—Make a survey of an assigned field by tra-

versing with the plane table.

(c) Methods.—Follow the same general methods as those given for traversing with the transit. Adjust the plane table before beginning the problem. Complete the map and compute the area as in Problem E4.

PROBLEM E6. SURVEY OF FIELD WITH PLANE TABLE BY INTERSECTION.

(a) Equipment.—Plane table, 2 flag poles, engineers' divided scale, drawing paper, 6H pencil.

(b) Problem.—Make a survey of an assigned field with

the plane table by intersection.

(c) Methods.—(1) Select and measure a base line having both ends visible from all the stations in the field. (2) Set the plane table over one end of the base line, sight at the other end of the base line and at each one of the stations of the field. (3) Set the plane table over the other end of the base line, orient the instrument by sighting at the station first occupied and sight at all the stations in the field. (4) Complete map and compute area as in E4.

PROBLEM E7. THREE POINT PROBLEM WITH PLANE TABLE.

(a) Equipment.—Plane table, 2 flag poles, engineers' divided scale, 6H pencil.

(b) Problem.—Having three points plotted on the map, required to locate a fourth point on the map by solving the "three point problem" with the plane table.

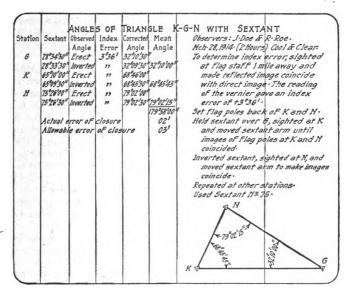
(c) Methods.—(1) Use Bessell's solution. (2) Check by using the mechanical solution.

PROBLEM E8. ANGLES OF TRIANGLES WITH SEXTANT.

(a) Equipment.—Sextant, 2 flag poles.

(b) Problem.—Measure the angles of an assigned triangle with the sextant.

(c) Methods.—(To determine index error, sight at a dis-



tant object and bring the direct and reflected images into coincidence. The reading of the vernier will give the index error, which, with proper sign, must be applied to all angles measured.) (1) Set the flag poles behind the monuments at two of the vertices of the triangle and stand on the monument at the third. (2) Hold the plane of the sextant horizontal, sight at one flag pole directly with the telescope and bring the image of the other flag pole into coincidence by moving the arm. (3) Read the vernier, and correct the angle for index error. (4) Repeat the measurement with the sextant inverted. Take the mean of the two readings, which should not differ more than 2', as the true value of the angle. (5) Measure the other angles in the The error of closure should not exceed 3'. same manner. Record the data in the form.

PROBLEM E9. DETERMINATION OF COEFFICIENTS OF A TAPE.

(a) Equipment.—Steel tape, spring balance, 2 thermometers, steel rule, 2 stout stakes, axe, 2 pieces sheet zinc 2 by 2 inches.

- (b) Problem.—Determine the coefficients of expansion, stretch, and sag of an assigned tape. Make three determinations of each, and take the arithmetical mean as the true value.
- (Standard Tapes.—In laying off a standard or measuring a base line where a high degree of precision is required it is important that all measurements be referred to the same standard. The Bureau of Standards, Washington, D. C., will compare a tape with the government standard for a small fee. The tape tested is certified to be of a given length for a given temperature and pull. For example the standard tape marked "U. S. W. & M. 215" used in laying off the 100-ft. standard in Problem A23, was certified to be 99.9967 feet long at a temperature of 62° F. and a pull of 12 pounds, when tested on a plane surface. The coefficient of expansion of this tape was 0.0000061 per degree F. Tapes for measuring base lines with great precision have recently been made of Invar Steel.)
- (c) Methods.—(1) Correction for Expansion.—Measure the length of the tape on a plane surface at two different temperatures but with a constant pull determined by a spring balance. Then substitute the lengths, l and L, and temperatures, t and T, in the formula

$$l-L = e(t-T)l$$

where e is the coefficient of expansion. Repeat the test and obtain three values of the coefficient e. As large a range of temperatures as possible should be secured. Take the arithmetical mean of the three determinations as the true value.

(2) Correction for Stretch.—Measure the length of the tape on a plane surface with two different pulls but at a constant temperature. Determine the pull with a spring balance. Then substitute the lengths, l and L, and the pulls p and P, in the formula

$$l-L = s(p - P) l$$

where s is the coefficient of stretch. Repeat the test and obtain three values of the coefficient s. The pulls should range from 10 to 40 pounds. Take the arithmetical mean of the three determinations as the true value.

(3) Correction for Sag.—Remove the handles from the tape and determine its weight very carefully. Divide the weight by the length to obtain the weight per foot, w.

Drive two stout hubs a little less than 100 feet apart and fasten a piece of sheet zinc with a line ruled at right angles to the line on the top of each stake. With a pull of 10 pounds, as determined by the spring balance, measure the distance between the stakes. Calculate the correction for sag by substituting the lengths, l and L, pull p, and weight per foot w, in the formula.

$$l-L=\frac{l}{24}\left(\frac{w\cdot l}{p}\right)^2$$

Repeat the measurements using a pull of 20 and 30 pounds, respectively. Add the corrections for sag to each measurement and compare the results. The temperature should remain constant during the tests. To remove the possibility of an error due to temperature, observe the temperature at the time of each observation and correct the observed length for e pansion before substituting in the formula.

Report the methods, data, computations and results on a suitable form.

PROBLEM E10. MEASUREMENT OF BASE LINE.

- (a) Equipment.—Standard tape, transit or level, stakes (number and size to be specified by instructor), axe, spring balance, 2 thermometers, lath stakes, 8-d nails, steel rule, pieces sheet zinc 2 by 2 inches.
- (b) Problem.—Measure an assigned base line with a standard tape.
- (c) Methods.—(1) Set the transit over one end of the base line, sight at the other end and determine the difference in elevation and grade. (2) Drive stout square stakes to grade, by "shooting" them in with the instrument in true line, a little less than a full tape length apart. The top of the lowest stake should not be less than 6 inches above the ground. (3) Fasten a piece of sheet zinc, with a fine line ruled at right angles to the direction of the base line, on the top of each stake. (4) Drive lath stakes in line about 20 feet apart. (5) Drive an 8-d nail through each lath stake at grade to support the tape. (6) Measure from stake to stake, the men working as follows: No. 1 plumbs up from the rear monument or holds the zero on the mark on the rear stake; No. 2 takes the spring balance and puts a pull of 16 pounds on the tape; No. 3 reads the tape and measures the fraction of a tenth with a steel rule to 0.001

feet; No. 4 records the reading of the tape and reads the two thermometers placed at the quarter points of the tape. (7) Obtain at least three determinations of the length of the base line. (8) Correct each measurement of the base for standard, expansion, sag, stretch, and slope (see problem on coefficients of a tape). The three measurements should not differ more than 1:100,000. Report methods, computations and results on a suitable form.

PROBLEM E11. CALCULATION OF TRIANGULATION SYSTEM.

(a) Equipment.—Seven-place table of logarithms.

(b) Problem.—Adjust and calculate an assigned triangu-

lation system and plot the skeleton.

(c) Methods.—Observe the following program: (1) prepare forms for calculations and transcribe data; (2) adjust the angles of the triangulation system (see chapter on errors of surveying); (3) calculate the front and back azimuths of each line; (4) beginning with the base line compute the sides, to the nearest 0.001 foot; (5) calculate the latitudes and departures to the nearest 0.001 foot (6) calculate the coordinates of the triangulation stations to the nearest 0.001 foot. In computing the coordinates of the stations take the mean of the values found by taking the different routes from the base line as the true value. (7) Plot the skeleton of the triangulation system to the prescribed scale by means of the coordinates of the points. Check by lengths of sides. Use a steel straight edge.

PROBLEM E12. SKETCHING TOPOGRAPHY.

(a) Equipment.—Small drawing board or plane table, plat of assigned field, 4H pencil.

(b) Problem.—Sketch in the roads, walks, buildings and five-foot contours on the plat of the assigned field by eye

having given the elevations of the ruling points.

(c) Methods.—(1) Transfer from the level notes to the plat the elevations of the ruling points of the field. (2) Locate the roads, buildings, etc., on the map as nearly as possible in their relative positions (the topographers' estimate of distance should be frequently checked by pacing). (3) Estimate the slopes and locate the contour points by smooth curved lines. (5) Finish the map in pencil, put-

ting on a neat title, the scale of the map and a meridian.

(6) Compare the finished map with a contour map furnished by the instructor.

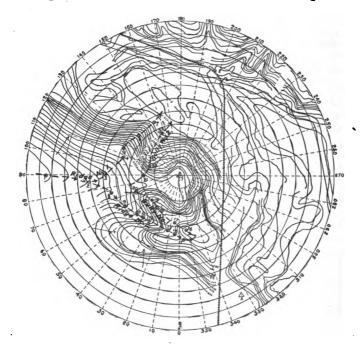
PROBLEM E13. FILLING IN DETAILS WITH TRANSIT AND STADIA.

- (a) Equipment.—Complete transit, 2 stadia rods, pocket tape.
- (b) Problem.—Locate the topographic details of an assigned area with the transit and stadia.

						Recorde	r, 0.8.0 r, A.M. 50	re	Stadiamen J. Doe.
		(TOP	OGRAP	HY BY	TRAN	SIT-5	TADIA	MET	HOD.)
Sta.	Ver. A.	Ver. B.	Obs-Dist-	Cor. Dist	Vert-Ang	DIFF. EI-	Elev.	Des	ription of Point
	AT A7	. Elev	47=63	3.5. H.	-57	(A.58.)	ransit.	k= 100-	00) 11-6-14 clear.
45	152°51	332°51'		523.2		- 1.6	631.9	No. E	1-A5 = 631-8 (Check)
Shat No I	89°25'		524	520	+ 5%3'	+ 47-3	680-8		idge No·I·
2	85°/8"		355	353	+ 548'	+ 35.5	669.0	2	,, ,,
3	90'06'		293	290	+ 527	+ 27.6	661.1	3	" "
4	106°35′		235	235	+ 123'	+ 5.8	639.3	4	n n
5	114050'		245	245	+ 033	+ 2.3	635.8	5	n n
6	/32°33′		223	220	- 7952	- 30.4	603-1	6)" #
1	152°57′		228	202	- 18955'	- 69.2	564.3	7	<i>"</i> "
8	75%4'		277	273	+ 5°20'	+ 25.5	659.0	8 1	idge No-2
9	60°40'		245	245	+ 406'	+ 17.6	651-1	9	ñ n
10	46°55'		226	226	+ 1032	+ 60	639.5	10	n n
11	41°51'		218	2/8	+ 0044'	+ 2.7	636-2	//	n n
12	34'00'		2/4	2/4	- 1'20'	- 5.0	628.5	/2	" "
13	//*58'		2/7	210	- 920'	- 34.4	599-1	/3	""
14	4010'	ì	228	221	- 9'34'	- 37.5	596-0	14	""
15	355°48'		250	238	- 1145'	- 45.9	587.6	15	17 17
16	352°40'		2/2	196	- 15012'	- 53.5	580-0	16 6	VIIV No.1
17	506		185	177	- 1/58	- 37.4	596-1	17	n n
18	33°28'		158	153	- 11°00'	- 29.7	603.8	18	" "
19	47°15′	l	146	142	- 802/	- 21.0	6/2-5	19	""
20	67°58'	l	182	182	+ 100	+ 3.7	637-2	20	11 11
21	88'41'	1	145	145	+ 037	+ 2.4	635-9	21 6	ally No. 2
22	104°55'	l	124	119	- 1202	- 25.1	608.4	22	,, ,,
23	155°52′		180	153	- 22°55	- 69.2	564.3	23	" "

(c) Methods.—(1) Set transit up over assigned triangulation or other point. (2) Orient instrument, i. e., set plates to given azimuth and sight at given back sight. (3) Measure height of axis above station hub with tape or by graduations on tripod leg, and set target to correspond. (4) Take shot on given back sight and reduce results as a check before proceeding. (The program for each shot is: (a) set middle hair roughly on target, then set one stadia

hair on nearest foot-mark and read intercept; (b) set middle hair precisely on target and signal rodman "all right"; (c) read vertical angle; (d) read azimuth.) (5) Take side shots to representative points, keeping in mind the scale of the proposed map. Select points according to a systematic plan, following along ridges, gullies, etc. Contour points should be taken with reference to change of



slope. (6) Reduce and plot the notes, and interpolate the contours, as in the accompanying diagram. (This toporaphy sheet should be carefully preserved for use in Problem E15.) (7) After completing the survey at the assigned station, move the instrument ahead to a new stadia station, taking both fore and back sights. (8) Lose no opportunity to take check sights at other triangulation stations, traverse points, etc.

PROBLEM E14. FILLING IN DETAILS WITH PLANE TABLE AND STADIA,

(a) Equipment.—Complete plane table (preferably with prismatic eyepiece), 2 stadia rods, engineers' divided scale, drawing paper, 6H pencil, pocket tape.

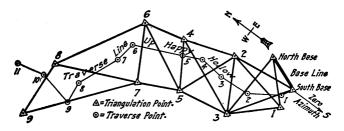
(b) Problem.—Locate the topographic details of an as-

signed area with the plane table and stadia.

(c) Methods.—Follow the same methods as in Problem E13 except that the notes are to be plotted on the drawing paper in place of being recorded in the field book. Mark the points by number and write the elevation of each point under the number in the form of a fraction. Locate the contour points by interpolation on the map and connect the points by smooth curves. Complete the map in pencil and make a tracing if required.

PROBLEM E15. TOPOGRAPHIC SURVEY.

(a) Equipment.—Complete transit, 2 stadia rods, stakes, hubs, spring balance, pocket tape, stadia slide rule, seven-place logarithm table, (extra tripods, stadia reduction table, stadia reduction diagrams, etc., as required).



(b) Problem.—Make a complete topographic survey of an assigned area and make a topographic map.

(c) Methods.—(1) Make a reconnaissance and locate the triangulation stations. Care should be used to select the triangulation stations so that the sights will be clear and the triangles well formed. A system composed of quadrilaterals or more complicated figures will give more conditions and checks than a simple string of triangles. A system composed of simple triangles is sufficient for this survey. (2) Mark the triangulation stations with gas pipe

monuments about 4 feet long, the exact point being marked by a hole drilled in a bolt screwed into a cap on the top of the gas pipe. (3) Measure the base line and base of verification as described in Problem E10. (4) Measure the angles by repetition as described in Problem D13. (5) Calculate the skeleton as described in Problem E11. (6) Establish permanent bench marks and determine their elevations and the elevation of the stations of the triangulation system by running duplicate levels with the engineers' level. reading the rod to 0 001 foot. (7) Fill in the details with either the transit and stadia or the plane table and stadia, or both, as described in Problems E13 and E14. plete the map in pencil on manila paper, and after it has been approved by the instructor trace it on tracing linen. The title, meridian, scale, lettering and border should receive careful attention.

CHAPTER VII.

LAND SURVEYING.

Kinds of Surveys.—Surveys of land are of two kinds:
(a) original surveys; (b) resurveys.

Original Surveys.—An original survey is made for the purpose of establishing monuments, corners, lines, boundaries, dividing land, etc. The survey of a townsite and the government survey of a section are examples of original surveys.

Resurveys.—A resurvey is made for the purpose of identifying and locating corners, monuments, lines and boundaries that have been previously established. The resurvey of a city block, or a survey to relocate a section corner are examples of resurveys.

Functions of a Surveyor.—In an original survey it is the function of the surveyor to make a perfect survey, establish permanent monuments and true markings, and make a correct record of his work in the form of field notes and a plat.

In a resurvey it is the function of the surveyor to find where the monuments, courses, lines and boundaries originally were, and not where they ought to have been. Failing in this it is his business to reestablish them as nearly as possible in the place they were originally placed. No reestablished monument, no matter how carefully relocated, will have the same weight as the original monument if the latter can be found. In making resurveys the surveyor has no official power to decide disputed points. He can act only as an expert witness. If the interested parties do not agree to accept his decision the question must be settled in the courts.

Also see Problem F6, "Resurvey of a City Block."

Responsibility of the Surveyor for the Correctness of His Survey.—An engineer in the discharge of his professional duties requiring an exercise of judgment can be held liable only for failure to exercise reasonable care and skill, or for negligence or fraud. A surveyor is liable not only

for negligence or fraud but for want of skill. A surveyor agrees to not only do his work carefully, honestly, diligently, but skillfully as well. The precision required in making any particular survey in order to satisfy the requirement for skill will depend upon the conditions; greater accuracy being required for making a survey of an expensive city lot than for a survey of a farm. Surveying is a trade and the precision required in any particular case to show proper skill is a matter to be decided by the court after evidence has been submitted.

Ownership of Surveyors' Notes.—Survey notes, data, maps, plats and records obtained by a surveyor while in the employ of a city, state, railroad or other corporation, or of a consulting or independent engineer belong to the employer. A city engineer or a county surveyor has no ownership rights in the notes, data, maps, plats and records which he prepares or obtains, or are prepared or obtained by him or by his assistants, in the exercise of the duties of his office as city engineer or county surveyor. Survey notes, data, maps, plats and records obtained by a consulting or independent engineer in preparing a report or plans for a client, belong to the consulting or independent engineer. The client, whether it be an individual, city, state, or corporation, is entitled only to the finished report or plans, and is not entitled to the notes and data used in the preparation of the report or the plans.

Rules for Resurveys.—The following rules may be safely observed in making resurveys.

- (1) The description of boundaries in a deed are to be taken as most strongly against the grantor.
- (2) A deed is to be construed so as to make it effectual rather than void.
- (3) The certain parts of a description are to prevail over the uncertain.
- (4) A conveyance by metes and bounds will convey all the land included within.
- (5) Monuments determine boundaries and transfer all the land included.
- (6) When a survey and a map disagree the survey prevails.
- (7) Marked lines and courses control courses and distances.
- (8) The usual order of calls in a deed is; natural objects, artificial objects, course, distance, quantity.
 - (9) A long established fence line is better evidence of

actual boundaries than any survey made after the monuments of the original survey have disappeared.

- (10) A resurvey made after the monuments have disappeared is to determine where the monuments were and not where they should have been.
- (11) All distances measured between known monuments are to be pro rata or proportional distances.

If the above rules do not cover the case in question special court decisions on that particular point should be consulted.

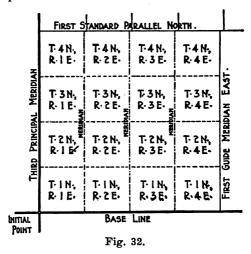
THE UNITED STATES RECTANGULAR SYSTEM OF PUBLIC LAND SURVEYS.

Historical.—The United States rectangular system of subdividing lands was adopted by congress May 20, 1785. The first public land surveys were made in the eastern part of the present state of Ohio under the direction of Capt. Thomas Hutchins,* Geographer of the United States, and were known as the "Seven Ranges." The townships were six miles square, and were laid out in ranges extending northward from the Ohio river; the townships were numbered from south to north, the ranges from east to west. In these initial surveys only the exterior lines of the townships were run, but mile corners were established on the township lines, and sections one mile square were marked on the plat and numbered from 1 to 36, commencing with section 1 in the southeast corner and running from south to north in each tier to 36 in the northwest section.

The act of congress approved May 18, 1796, provided for the appointment of a surveyor general and changed the law relating to the surveys of public lands. Under this law the townships were subdivided into sections by running parallel lines two miles apart each way and setting a corner at the end of each mile. This law also provided that the sections be numbered beginning with section 1 in the northeast corner of the township, thence west and east alternately to 36 in the southeast corner. This is the method of numbering still in use, shown in Figs. 33 and 34.

*The earliest published reference to the rectangular system of land surveys is found in an appendix to "Bouquet's March," published in Philadelphia, 1764. Hutchins was engineer with this expedition to the forks of the Muskingum river, and wrote the appendix. (See reprint by Robt, Clarke, Cincinnati.)

The act of congress approved May 10, 1800, required that townships be subdivided by running parallel lines through the same from east to west and from south to north at a distance of one mile from each other. Section corners and half section corners on the lines running from east to west were required to be set. The excess or deficiency was to be thrown into the north and west tiers of sections in the townships.



The act of congress approved February 11, 1805, required that interior section lines be run every mile; that corners be established every half mile on both township and section lines; that discrepancies be thrown on the north and west sides of the township. This act of congress further provided "that all corners marked in the original surveys shall be established as the proper corners of sections, or subdivisions of sections; and that corners of half and quarter sections not marked shall be placed as nearly as possible 'equidistant' from those two corners which stand on the same line. The boundary lines actually run and marked shall be established as the proper boundary lines of the sections or subdivisions for which they were intended; and the length of such lines as returned by the surveyor shall be held and considered as the true length thereof, and

the boundary lines which shall not have been actually run and marked as aforesaid shall be ascertained by running straight lines from the established corners to the opposite corresponding corners." Under this law, which is still the established rule of procedure, each reported distance between established monuments is an independent unit of measure.

The revised instructions issued in 1855 required that the sections be subdivided as shown in Fig. 33. The full lines representing "true" lines, are parallel to the east exterior line of the township, and the dotted lines, representing "random" lines, close on corners previously established. The order of the survey of the interior section lines is indicated by the small numerals. Double corners on the north and west township lines, which were common in the earlier surveys, were thus avoided in the revised practice.

Laws Inconsistent.—It is obviously impossible to preserve a true rectangular system on a spherical surface, owing to the convergency of meridians.* To harmonize the methods of making surveys, the General Land Office has issued instructions for the survey of public lands from time to time.

DETAILS OF SURVEY.—The details of the survey are taken up in the following order: (1) selection of initial points; (2) establishment of the base line; (3) establishment of the principal meridian; (4) running standard parallels; (5) running the guide meridians; (6) running the township exteriors; (7) subdividing the township; (8) meandering lakes, rivers, streams, etc. See Figs. 32 and 33.

Initial Points.—Initial points from which to start the survey are established whenever necessary under special instructions prescribed by the Commissioner of the General Land Office.

Base Line.—The base line is extended east and west from the initial point on a parallel of latitude. The proper township, section and quarter corners are established and meander corners at the intersection of the line with all meanderable streams, lakes, or bayous. Two sets of chain-

^{*}The angular convergency, a, of two meridians is m. sin L, where m is the angular difference of longitude of meridians and L is the mean latitude of the two positions. The linear convergency, c, for a length, t, is t. sin a. Latitude 40°, the difference between the north and south sides of a township is 0.60 chains.

men are employed and the mean of the two measurements is taken as the true value. When the transit is used, the base line—which is a small circle parallel to the equator—is run by making offsets from a tangent or secant line, the direction of the line being frequently checked by an observation of Polaris.

6 6		#-££ \ 4 - ££ \ 13 - ★	Random	Random	Rendom ▼
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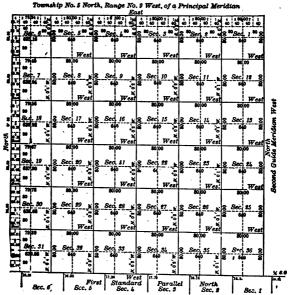
Fig. 33.

Principal Meridian.—The principal meridian is extended either north or south, or in both directions from the initial point on a true meridian. The same precautions are observed as in the measurement of the base line.

Standard Parallels.—Standard parallels, which are also called correction lines, are extended east and west from the principal meridian, at intervals of 24 miles north and south of the base line. They are surveyed like the base line.

Guide Meridians.—Guide meridians are extended north from the base line, and standard parallels, at intervals of 24 miles east and west from the principal meridian, in the manner prescribed for running the principal meridian. When existing conditions require that guide meridians shall be run south from the base or correction lines, they are initiated at properly established closing corners on such lines.

Township Exteriors.—The township exteriors in a tract 24 miles square, bounded by standard lines, are surveyed successively through the block, beginning with the south-

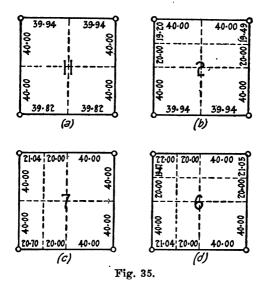


The above plot represents a theoretical town-hip with perfect subdivisions, consignous to the north side of a Standard Parallel. In comme Latitude 15 N. and Longitude 100000 W. of Gr. Arcs 5008.18

Fig. 34.

western township. The meridional boundaries are run first from south to north on true meridians with permanent corners at lawful distances; the latitudinal boundaries are run from east to west on random or trial lines and corrected back on true lines. Allowance for the convergency of meridians is made whenever necessary.

Township Subdivisions.—A true meridian is established at the southeast corner of the township and the east and south boundaries of section 36 are retraced. Then beginning at the corner to sections 35 and 36 on the southern boundary, a line is run north parallel to the township line, corners are established at a distance of 40 and 80 chains; from the last named corner a random line is run eastward, parallel to the south boundary line of section 36, to its intersection with the east boundary of the township. A temporary corner is set at a distance of 40 chains, and a permanent corner is afterwards established midway be-



tween the two permanent corners. The other corners are located in a similar manner, as shown in Fig. 33. The lines closing on the north and west boundary lines of the township are made to close on the section corners already established. A theoretical township with perfect subdivisions is shown in Fig. 34.

Meandering.—Navigable rivers and other streams having a width of three chains and upwards are meandered on both banks, at the ordinary high water line by taking the general course and distances of their sinuosities. The

meanders of all lakes, navigable bayous, and deep ponds of the area of twenty-five acres and upwards are surveyed as directed for navigable streams. Meander corners are established where meander lines cross base lines, township lines, or section lines.

Subdivision of Sections.—In Fig. 35, (a) gives the subdivision of an interior section, (b) of section 2 on the north side, (c) of section 7 in the west tier, and (d) of section 6 in the northwest corner.

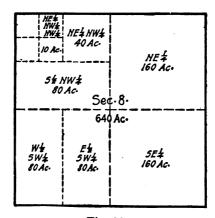


Fig. 36.

Description of Land.—Land is described in the rectangular system by giving its location in a civil township; for example, in Fig. 36, the northeast quarter, containing 160 acres, would be described as: N E ¼, Sec. 8, T 19 N, R 9 E, 3 P. M. The ten acre lot indicated in the northwest quarter would be described as: S E ¼, N W ¼, N W ¼, Sec 8, T 19 N, R 9 E, 3 P. M.

Corners.—The corner monuments may be as follows:
(a) stone with pits and earthen mound; (b) stone with mound of stone; (c) stone with bearing trees; (e) post in mound of earth; (f) post in mound of stone; (g) post with bearing trees; (h) simple mount of earth or stone; (i) tree without bearing trees; (j) tree with bearing trees; (k) rock in place, etc. The trees on line are required to be blazed. The size, markings and proper corners to be used in any particular case and all other details are given in the

"Manual of Surveying Instructions for the Survey of Public Lands of the United States," issued by the General Land Office, Washington, D. C.

The last edition of the "Manual of Surveying Instructions for the Survey of Public Lands" was issued in 1902 and may be obtained from the Superintendent of Documents, Government Printing Office, Washington, D. C., price 75 cents per copy. A new edition of the Manual is promised for 1915. The circular on the "Restoration of Lost and Obliterated Corners" mentioned in the next paragraph gives instructions for making resurveys, and may be obtained free by addressing the Department of Interior, General Land Office, Washington, D. C.

Restoration of Lost or Obliterated Corners. *- "An obliterated corner is one where no visible evidence remains of the work of the original surveyor in establishing it. Its location may, however, have been preserved beyond all question by acts of landowners, and by the memory of those who knew and recollect the true position of the original monument. In such cases it is not a lost corner.

"A lost corner is one whose position can not be determined beyond reasonable doubt, either from original marks

or reliable external evidence."

General Bules.—The following rules are derived from a brief synopsis of congressional legislation relating to sur-

"(1) The boundaries of the public lands established and returned by the duly appointed government surveyors, when approved by the surveyor general and accepted by the government, are unchangeable.

"(2) The original township, section, and quarter-section corners established by the government surveyors must stand as the true corners which they were intended to represent, whether the corners be in place or not.

- "(3) Quarter-quarter corners not established by the government surveyors shall be placed on the straight line joining the section and quarter-section corners and midway between them, except on the last half mile of section lines closing on the north and west boundaries of the townships, or on other lines between fractional sections.
- "(4) All subdivisional lines of a section running between corners established in the original survey of a township
- *Circular on the "Restoration of Lost and Obliterated Corners and Subdivision of sections," Department of Interior, General Land Office, Washington, D. C.

must be straight lines, running from the proper corner in one section line to its corresponding corner in the opposite section line.

"(5) That in a fractional section where no opposite corresponding corner has been or can be established, any required subdivision line of such section must be run from the proper original corner in the boundary line due east and west, or north and south, as the case may be, to the water course, Indian reservation, or other boundary of such section, with due parallelism to section lines."

"From the foregoing it will be plain that extinct corners of the government surveys must be restored to their original locations, whenever it is possible to do so; and hence resort should always be first had to the marks of the survey in the field. The locus of the missing corner should be first identified on the ground by the aid of the mound, pits, line trees, bearing trees, etc., described in the field notes of the original survey.

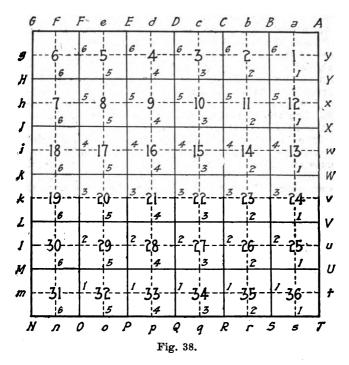
"The identification of mounds, pits, buried memorials, witness trees, or other permanent objects noted in the field notes of survey, affords the best means of relocating the missing corner in its original position. If this can not be done, clear and convincing testimony of citizens as to the place it originally occupied should be taken, if such can be obtained. In any event, whether the locus of the corner be fixed by the one means or the other, such locus should always be tested and confirmed by measurements to known corners. No definite rule can be laid down as to what shall be sufficient evidence in such cases, and much must be left to the skill, fidelity, and good judgment of the surveyor in the performance of his work.

"Actions or decisions by county surveyors which may result in changes of boundaries of tracts of land and involve questions of ownership in connection therewith, are subject to review by the local courts in proceedings instituted in accordance with the local statutes governing such matters."

The pamphlet also contains much additional information of value.

Locations of Principal Meridians.—Principal meridians have been established as the needs of the surveys warranted. There are twenty-four principal meridians in all, the locations of which are given in the "Manual of Instructions," mentioned above.

Abridging Field Notes.—The government surveyors use the method of abridging field notes shown in Fig. 38. Corners in the township boundary are referred to by letter; interior section corners are referred to by giving the numbers of the sections meeting at the corner; interior quarter section corners are referred to by giving the number on the section lines produced.



SURVEYS BY METES AND BOUNDS.

That portion of the United States settled before the adoption of the rectangular system was surveyed by the method of metes and bounds. For the most part these surveys were very irregular and often involved complex and conflicting conditions. The entire eastern portion of the United States, and the state of Kentucky, were surveyed in this manner,

and further examples are found in the French surveys in the states of Michigan, Indiana, Illinois, Missouri, Louisiana, etc., and the Spanish surveys of Texas, California, etc. The general principles underlying the questions of ownership, priority of survey, the restoration of lost corners, etc., are identical whatever the system of survey used.

PROBLEMS IN LAND SURVEYING.

PROBLEM F1. INVESTIGATION OF A LAND CORNER.

- (a) Equipment.—Digging outfit, tape, etc., as required.
- (b) Problem.—Collect complete evidence relative to an assigned land corner, and after giving due weight to the same, make a decision as to the true corner.
- (c) Methods.—(1) Make careful examination of the official field notes and records pertaining to the land corner in question and make extracts from the same for further reference. (2) Seek oral evidence from those acquainted with the history of the corner. (3) Make a survey of fence lines and other physical evidence, such as witness trees or their stumps, etc., near the corner under investigation. (4) Make

INVESTIGATION OF S-W. CORNER,
Original United States Field Notes, on File at Court House at Urbane, III., describe
the SW. Cor., Sec. 8, T.19 N., R.9E., 3 P.M., as "Post in Mound," the corner being
located on the Prairie remote From
the heavy timber which surround. State
of the three corners of the state.

- the SW Car., Sac. 8, 7.1911, R.9.5., 3. PM, as "bat in Mound," the corner being located on the Prairie remote from the heavy timber which surrounds the other three corners of the section. Original survey was made about 1822. On Oct. 25,1896, Col. 5.7. Busey, when asked for information about the corner under investigation, stated that about 1850, when he was a boy, Mr. Campbell, who was then County Surveyor, was called on to re-establish the SW Cor, Sec. 8. At the time mentioned the section lines near the corner were occupied by rail fance. Col. Busey says that his Father (a planeer settler) pointed out to the surveyor near the fence corner evidences of a mound which he believed marked the ariginal U.5. Survey carner. Mr. Campbell, the surveyor dug carefully at the spot and found the decayed point of a sassafras stake which unquestionably marked the true position of the "Pat in Mound" established some ES years or more previous to Campbell's resurvey. Col. Busey states that he himself carried the boulder which was set in place by the County Surveyor to pepetuate the section corner, and that this monoment was not disturbed until it was replaced by a much larger stone when the roads were opened upon the section the
- This stone stood is or so above the level of the road for many years. About 1894 it was carefully lowered by the Street Commissioner under the direction of the City Engineer of Urbana-Resurveys made since the stone was lowered, indicate that its present position is identical with that previous to the change.

 Conclusion. In view of Col-Busey's valuable statement with the corroboration from
- Conclusion. In view of Cot Buseys valuable statement with the corroboration from
 other credible sources, and the entire absence of conflicting evidence of any
 character, it is concluded that the monument now and for many years so
 recognized is the true SW corner of Section 8, T-19 N, R-9 E, 3D. P.M.

careful examination of the site of the corner with the digging outfit; the digging should be done cautiously so as to avoid disturbance of existing stakes or other monuments. (5) If more than one monument be found, make due record of their character and positions, and make further inquiry respecting them. (6) If no monument of any sort be found at first, continue the search diligently and do not give up finding the true corner as long as there is a remote chance of locating it. In any event, avoid wanton disturbance of any object or evidence that may have a bearing on the same. Keep a clear and concise record.

PROBLEM F2. PERPETUATION OF A LAND CORNER.

- (a) Equipment.—Digging outfit, a large boulder or other permanent monument, cold chisel, hatchet, plumb bob, string, stakes.
- (b) Problem.—Replace a temporary land corner by a permanent monument.
- (c) Methods.—(1) Uncover the identified temporary monument and carefully determine the true point with consist-

5-F-Kingsley, Head Chainman - F-Hodgman, Transitu SURVEY OF SEC-14, T-25, R-10 W. FOR J-R COMINGS AND H-ROWLAND. Commenced at the SE. cor. of Sec. 14. Found a piece of strap railroad fron driven for the cor. which Hugh Shafter says he knows to have been kept in the same place, unquestioned, as the cor. For over 30 years. Marked: maple, 8 ins. diam., 5-45 W., 77 lks. dist. burr oak 12 ins. diam., 1-43 W., 123 lks. dist. CHAINS | set up a tall flag on the cor. and then ran W. on random, var 2°15 Eysetting temporary stakes every 10 chs. in line. 40-00 4 sec cor lost Intersected the W. line of Sec. 14, 42 (ks. 5- of the cor. Found rotten stake et correct point, 1826 E., 104 (ks. From stump of who oak, 24 (ins. diam., bearing tree of U.S. Survey, having surveyor's mark distinct on it. Set . piece of steel T rail 28 ins. long For cor. Marked: locust 16 ins. diam., 5.28°W, 116 lks. disf. " , N.78° E., 152 " " burr oak 18 11 (10:30 A-M) Ran thence E. on corrected line at single sight with transit, from con to con. Ver. 2 33 E. 40-12 Found coder stake 3 ft. below surface of road crossing and 2 ks. 5 of line . No other evidence of cor to be found. Put a piece of T rail 24" long on top of the stake for & sec. cor. 55 lks. Sof 5. rail of M.C.R.R. No tree near. 60-18 Planted granite boulder 20 x 12 x 6 ins., with cross + mark for & quer sec. cor., in true line between qr. post and sec cor. and marked: maple, 12 ins. diam., 5-16 E., 55 lks. dist. burr oak. 16 11 " N-54°E 118 "

ent exactness. (2) Reference out the point by driving two pairs of stakes with strings stretched so as intersect squarely over the corner. (3) After carefully checking the referencing, dig out the old monument to a depth sufficient to receive the boulder and permit its top to set several inches beneath the natural surface if located in a road or where disturbance is probable. (4) Cut a plain cross mark on the top of the stone, and set it in place in the hole, packing the earth about it, testing the position of the mark by means of the reference stakes and strings and plumb bob; finally leave the boulder set firmly in the correct position. (5) Make reference measurements to suitable permanent points such as marks on curbing, gas pipes, witness trees, etc., selected with respect to good intersections, and make reliable record of the witness notes after checking the same. (Other forms of permanent monuments are: gas pipe; fish plate; section of T-rail; farm tile or vitrified pipe filled with cement mortar; post hole filled with mortar; special solid monument burned like farm tile; special casting similar to a gas main valve box, with hole in top to receive flag pole; etc.)

PROBLEM F3. REESTABLISHING A QUARTER-SECTION CORNER.

- (a) Equipment—Transit party outfit, digging tools, etc.
 (b) Problem.—Reestablish a quarter-section corner that has been obliterated or lost.
- (c) Methods.—(1) Collect and record all the available evidence which may assist in the discovery and identification of the corner. Examine the field notes of the original survey, the surveyors' plat book and the county atlas on file at the court house, and make diligent inquiry for credible and competent information, either written or oral as to the location of the corner. (2) Make a careful search for the monument. Trace all the lines of the original survey, paying particular attention to bearing and sight trees. Dig in all the places indicated by the different lines and give up the search only after you have exhausted every possible clue. (3) If the corner cannot be found, reestablish it, giving due weight to all the evidence. The surveyor should remember that the corner should be reestablished where it originally was and not where it ought to be. After having located a stake at the supposed location of the original monument, reference it out and renew the search. (4)

After the monument has been relocated, mark it in a permanent manner as indicated in Problem F2, by a stone with a cross cut in its top or with a gas pipe well driven into the ground. Reference it out to at least two permanent objects selected with a view to securing a first class intersection. Make a careful record and preserve consistent accuracy in the work.

PROBLEM F4. REESTABLISHING A SECTION CORNER.

- (a) Equipment.—Transit party outfit, digging tools, etc.
- (b) Problem.—Reestablish an obliterated or lost section corner.
- (c) Methods.—Follow the various methods described in Problem F3, giving special attention to the search for the original corner; upon failing to find trace of it, run out lines with reference to the section, quarter, and quarter-quarter corners in the four directions, with linear measurements from the same and finally reach the most consistent decision with reference to such survey lines, ownership lines, fences, hedges, road centers, etc. (A fruitful cause of disturbance of section and other corners is careless use of road graders, or the failure to lower the corner sufficiently below the surface of the road.)

PROBLEM F5. RESURVEY OF A SECTION.

- (a) Equipment.—Transit party outfit, digging tools, etc.
- (b) Problem.—Make a resurvey of an assigned section.
- (c) Methods.—(1) Make extracts from the field notes of the original survey and of all resurveys on file at the court house, and other notes that may be of value. Make diligent inquiry among the property owners for evidence as to the location of corners. (2) Retrace the lines, recording the location of old fences, timber markings and other evidences as to prior recognition of lines and corners. Use consistent accuracy. Record the original notes as given in the forms. Record the field notes in narrative style using the designation of corners as given in the resurvey plat in the form. Make a plat of the section in the manner prescribed by state law for a resurvey.

INVESTIGATION OF LAND CORNERS COLLECTION OF EVIDENCE

Extracts from Surveyor's Plat Book Nov-5, 1897, found in the County Recorder's office of Urbana, III., the "Surveyor's Plat Book" containing plats of Pownships showing existing menuments and subdivisions of sections made by the County Surveyor, with certificates of various resurveys. Made the Following extracts relating to Sec. 8, T-1916, R.9.5., 380. P.H.:

(From P.156)

"Dec.3, 1876, Surveyed at the request of FAdams the east line of Sec.6 Beginning at a stone previously planted at NE con of Said section, and renning thence 5-to 5-E Cor. of same, where I found a stone previously set by John Thrasher and Lewis Sommers, divided the distance pro rata and set Cor. at NE Cor of 5-E to 5 same."

(Signed) Thos.B.Kyle Co.Surveyor.

(From p. 157)

"Apr. 11, 1884. Surveyed by request of
5:T:Busey the W. lines of Secs. 8 and 5.
Beginning survey at 5:W. Cor. Sec. 8 where

Surveyor, J.Doe.

OF SEC. 8, T.19 N., R.9 E., 3RD. P.M.

Apr. 25, 1899.

To of Resurveys of Chempaign County.

a stone is planted and running thence N. to N.W. Cor Sec. 5, Found an excess of 40 lks., corrected back, came on to a stone planted

(Portion of Plat on p.155, showing existing monuments:)

Stone

Stone by Lewis Sommers at 1 Sec. Car. on line between Secs-5 and 6. l also planted a stone et Sec. (or. (5-6-7-8) and made the following witnesses to the corner, viz .: A double burr oak, 15 "diam. bearing N. 601°E. 102 \$ 1ks.. also a Wh. Oak, 14" diam , bearing N-35 E. 188 Iks. l also set a stone at the NW: Cor. of the SW4. of the S-W4, of Sec. 5. (Signed) Thos B. Kyle

Co-Surveyor.

Stone

Surveyor, J. Doe. INVESTIGATION OF LAND CORNERS OF SEC. 8, T. 19 N., R. 9 E., 3RD P.M. COLLECTION OF EVIDENCE (Continued) Apr. 25, 1899. Extracts From Field Notes of Original United States Survey. Nov. 4, 1897. Found in the County Treasurer's (5ec. 6) (Sec. 5) (Sec.4) Office at Urbana, Ill., the Plat Book contain-80,00 ing Plats and Abstracts of Field Notes of Original United States Survey of Champaign County, and made the following extracts relating to Sec. 8, T.19 N., R.9 E., 3RD P.M. :-DESCRIPTIONS OF ORIGINAL CORNERS (P.30) (5ec.7) (Sec.9) Corners Witness Trees Inches Courses Links Designation Kind Diameter They Bear Distant Sec-Cors-5.58°F. (Ash 24 35 4,5,8,9 B. Oak 14 N-64°W 26 (5ec-18) 4 (Sec-16) (W.Oak 28 N. 88° E. 230 5,6,7,8 DESCRIPTIONS OF "OBJECTS ON THE LINES" (P.75) W. Oak 20 N.36°E. 272 Post in Mound DESIGNATION DISTANCES 7,8,17,18 DESCRIPTION (B. Walnut 24 N.32°E. 44 Chs. Lks. 8,9,16,17 B. Walnut 24 5.10°W. N- between 8 & 9 25.00 42 Brook leading M. thence & Sec. Cor givna the channel of the (Elm 12 5.67°W. 20 same 13 chs. then leaving H to Yat 5 Elm 8 N-78° E. 30 it running E'ly.
Ash 12" diam. 6 N.58°E. 23 W.Oak 50.19 In X .. 5 W-Oak 6 5.26°F. 8=17 24.50 Brook 51ks. rs. N. E'ly. SASH 22 5. 7° E. 18 39.00 Entered timber bs. N&S. R"C"5 FIM 8 N.30° E. 13 5 . 8 4.00 Entered timber bs. N.&S. 5118115 Post in Mound 16.50 Brook 60 lks. rs. 5'ly

5-H-Smith, HeadChainman. L.B. Brown, Axman. 6.W.Smith, Flagman. J.E. Wilson, Rear " RESURVEY OF SEC. 27, T.12N, R.16W. 3D.P.M. FOR THE ESTATE OF JOHN W. SMITH-July 12, 82. Cloudy with showers. CHAINS Began at J. Found stake in place and both bearing trees standing . Planted stone 25"x8"x6"; marked + for cor-RESURVEY REFERENCE PLAT . Thence N. on random, var. 2 30 E., setting temp. stakes every 10 chs. 80-22 Intersected sec. line 26 lks. W. of 5. At 5 found rotten stake at correct point, 5-28°W., 66 lks. from stump of whooak, 16 bearing tree of U.S. Survey . Drove stake for cor and put broken earthenware and glass around it. 6 8 Mkd. wh. oak, 12" diam, N. 66° E., 42 lks., also wh. oak 18" diam., N.34°W. 63 1ks. From 5 ran E. on random, setting temp. 15 stakes every 10 chs. 39.92 Intersected sec. line 12 lks. N. of 2. At Z found earthen post in correct position and bearing trees of 14 resurvey standing. Thence W. on corrected line. 9.98 Set stake on true line . (Cont'd on next page)

RESURVEY. SEC-27, SMITH ESTATE (CONTINUED) CHAINS 19.96 (Line 5-2 cont'd) At 10 set stake with stones around it and marked: pine, IZ"diam., N-46°W., 79 Iks. red oak, 24" diam., 5-194°W, 72 Iks. 29.94 Set stake on true line. From 10 ran 5. on random, var. 219'E-. and set temp stakes at 20 and 40 chs. Then went to 6. Found post and bearing trees of resurvey standing. Ran thence W.on random, var. 2°20'E. 20-02 Intersected random line From N. 6 Iks. 5. of temp. stake 40-18 Intersected random & line & Iks. IL of temp. stake. 80.04 Intersected sec. line 10 lks. 5. of 8. Cor. post dug out in road. Set iron plan beam for cor., 5.29°W., 76 Iks., From bearing tree of U.S. Survey. Thence E. on corrected line. At intersection of quarter lines set 39.99 post.

PROBLEM F6. RESURVEY OF A CITY BLOCK.

- (a) Equipment.—Transit, 100-foot steel tape, chaining pins, axe, hubs, stakes, 4 pieces one-inch gas pipe 2 feet long, notes of previous surveys, etc.
 - (b) Problem.—Make a resurvey of an assigned city block.
- (c) Methods.—(1) Procure full notes of all the surveys and resurveys of the assigned block from the records at the court house and from any other source available. (2) Make a resurvey of the block, using the notes, and drive hubs for temporary corners. (3) Compute the latitudes and departures of the courses, and if consistent balance the survey. (4) If the corners of the block as located are consistent with the existing property and street lines, drive gas pipes as permanent corners. (5) Subdivide the block into lots as shown in the notes. (6) Make a plat of the block on manila paper to the prescribed scale, showing block and lot lines, distances and angles obtained in making the survey, the names of the owners of the property and the names of the streets. Prepare a surveyors' certificate as provided by law. Trace the map if required. (The accuracy attained should be based on the valuation and other local conditions. Before beginning the survey use every possible care to find the corners with reference to which the original survey was made. When lots are sold by number, the excess or deficiency should be divided pro rata. However, when lot lines have been long acquiesced in, it is doubtful if the courts will uphold the surveyor in interfering with the ancient lines of ownership. It then becomes necessary either to make a compromise survey that will be satisfactory to the owners, or to make a survey that is strictly according to the letter of the law, and submit the map and certificate to the courts for settlement. The surveyor should remember that he is simply an expert witness and that he had no final judicial powers.)

PROBLEM F7. RESURVEY BY METES AND BOUNDS.

- (a) Equipment.—Transit party outfit, digging tools, etc.
 (b) Problem.—Make a resurvey of an assigned tract
- (b) Problem.—Make a resurvey of an assigned tract whose original survey was made by metes and bounds.
- (c) Methods.—(1) Collect full notes and data relating to the monuments, magnetic bearings, magnetic variation, date of survey, lengths of lines, etc. (2) Make a careful investigation of the lines and corners on the ground and

make notes of any evidence there found. (3) Locate and identify with certainty as many as possible of the original monuments; where double or contested corners exist, locate each definitely for further reference; if corners are generally lacking or doubtful, concentrate attention on at least two which give most promise of definite relocation, and reestablish these corners as carefully as possible. (4) Having at least two corners, retrace by random line the perimeter of the tract, according to the original description, beginning at one and closing on the other corner; set temporary corner stakes at the several points; note the linear and angular error of closure of the random traverse on the last monument. (5) Calculate the latitudes and departures of the random survey, and determine the angular and linear relations between the random and the original survey; also fix the position of the several random stakes relative to the supposed true positions of the respective corners. (6) Set stakes in the true positions, as calculated, reference them out, and renew the search for the original monuments. (7) Finally reestablish each corner in the most consistent position, put permanent corners in place, and take witness notes for each, making complete notes of the proceedings. Follow the form.

PROBLEM F8. PARTITION OF LAND.

- (a) Equipment.—Transit party and digging outfits, etc.
- (b) Problem.—Make a partition of an assigned tract of land in accordance with instructions.
- (c) Methods.—(1) Make the necessary resurveys of the assigned tract, identifying original monuments, and reestablishing lost corners as required. (2) Make a plat of the partition. (3) Subdivide the land and set permanent corners; carefully establish witnesses to the corners and secure witness notes. (4) Prepare and file plat and description as required by law.

PROBLEM F9. DESIGN AND SURVEY OF A TOWN SITE (OR ADDITION).

- (a) Equipment.—Equipment for topographic survey for both field and office.
- (b) Problem.—Make a preliminary topographic survey of the proposed town site (or addition), design the plat, and make the surveys for blocks, lots, etc.

RESURVEY OF "MISSION RIDGE"
Consulted County Records and confirmed
Following Meander Notes For center
Line of highway as described in J#Merhits
deed to J.D.Clark.

"M.62"E., 14 ch.; M.43\forall E., 8 ch.; M.5"W., 12 ch.; M.72\forall E., 10.25 ch.; 5.12"W., 6.43 ch." Description referred to stones at begin—

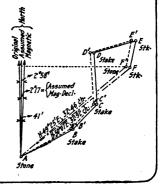
ning and ending points.
Found first stone projecting above road,

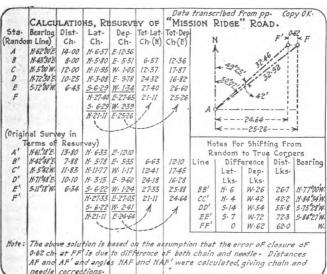
Began at first monument and ran on random according to member notes, with 2117E as magnetic declination. Drove temporary stake at each deflection point and made careful search for monuments. Found no conners at intermediate peints, but identified marked boulder as true corner at closing point 62 links due west of last stake of random. Made careful calculation of notes for shifting over from random to true corners. (See plat opposite and calculations on next pair of pages.)

J. Doe, Surveyor. Mar. 10. 1915.
PUBLIC ROAD FOR J.D. CLARK.

Transferred corners according to calculations and renewed search for original manuments, keeping close watch for decayed stakes, but withour success.

Set stone at each true corners.





(c) Methods.—(1) Make a careful resurvey of the entire tract. Reference the existing monuments and carefully relocate all missing corners. (2) After the monuments have been carefully located, remeasure the distances and angles very carefully. Before beginning the chaining, a standard should be established as described in Problem A23. Fill in the topographic details with the transit and stadia, unless directed otherwise, using consistent accuracy. Make a complete topographic map of the tract. (5) Design the townsite and sketch it in on the map. The questions of surface drainage, sewerage, possible overflow, street gradients, principal thoroughfares, diagonal streets, alleys, etc., should be carefully considered. The streets should be of ample width, and be laid out with reference to ease of grading both the street and adjacent property. Residences should face desirable streets and the cross streets in the residence district should not be too numerous. The principal thoroughfare should pass through the business portion and have minimum gradients. The system of sewerage and drainage should be worked out roughly before the design is completed. Much expensive construction can be avoided by using care in designing the town site. Make preliminary profiles of all the streets on Plate A profile paper to the prescribed scale. (7) Carefully locate the block and other important corners and mark them by permanent monuments of stone, gas pipe, tiling, etc. (8) Subdivide the blocks into lots and mark the lot corners by means of gas pipes or hubs. (9) After the streets have been located carefully, take levels on the same, make profiles. and lay grade lines for all streets, sidewalks, and improvements.

Use accuracy consistent with the value of the property throughout the problem. Make a careful record of the notes. Complete the maps and profiles.

CHAPTER VIII.

RAILROAD SURVEYING.

Classification.—For the purpose of class instruction, railroad surveying will be discussed under the following heads: (1) curve practice, (2) reconnaissance, (3) preliminary survey, (4) location survey, (5) construction, (6) maintenance.

Curve practice is designed to give the student familiarity with the methods of running curves so that the location survey may be made without needless delay. It consists of a series of typical problems covering the usual range of conditions found in such surveys.

The reconnaissance is a rapid preliminary examination of a district or area for the purpose of selecting ruling points to control the general routes of the preliminary survey lines. The distances are paced or scaled from a map; elevations are determined by means of the barometer or hand level.

The preliminary survey is designed to obtain information and to obtain it rapidly, as a guide in making the location survey. A rapid deflection angle traverse is run, following the general route of the proposed line, but keeping in clear ground as far as may be to gain time; levels are run, topography including contours taken, the map made, and one or more location lines projected on the map.

The location survey fixes the exact lines, including the curves, preparatory to building the proposed railroad. Some engineers prefer to run one or more trial location lines, but it is best practice to locate the line as projected on a reliable contour map.

Construction surveys are made for the purpose of fixing the roadbed limits and other constructive details, and estimating earthwork and other quantities.

Maintenance surveys and resurveys are made after the line is built, for ballasting, yard construction or other purpose.

Field Organization of Class.—In order to carry out the foregoing steps, the following field parties are required:
(a) transit party, (b) leveling party, (c) topography party,
(d) land-line party, (e) cross-sectioning party, (f) bridge and masonry party, (g) resurvey party.

General Requirements.—Each party should work with snap and vigor and accomplish the best results practicable, both as to quality and quantity. To this end each member of the party should not only be careful, exact, and rapid in the discharge of his own duties, but avoid interfering with the work of others, such as obstructing the view of the transitman. In order to give each student practice in all the positions, the posts will be shifted daily, progressing to the higher positions in the party. The student should not underrate his practice in the subordinate positions, nor fail to make proper use of his more responsible duties. The usual decorum of field parties will be observed.

TRANSIT PARTY.—It is the duty of the transit party to establish the traverse line upon which to base the levels and topography. The student transit party will consist of the following members: (1) chief of party, (2) transitman, (3) head chainman, (4) rear chainman, (5) stakeman, (6) axeman, (7) front flagman, (8) rear flagman. The duties and equipment of the respective members are stated below.

Chief of Party.—(Party list, map of line, 50-foot metallic tape, railroad curve text book.) The chief of party is responsible for the general progress and quality of the work. It is his duty to direct the survey; see that each man does his work properly and with sufficient accuracy and despatch; check the transitman's work when necessary; keep the transit notes if the transitman is pushed; and make himself generally useful. He should be thoroughly acquainted, before going to the field, with the situation and with the data applicable to the work of the day. In requiring subordinate members of the party to perform their work properly, he should carefully preserve the dignity of his own position. Should there be no chief, these duties will be shared by the transitman and head chainman under the former's directions.

Transitman.—(Transit, reading glass, adjusting pin, transit note book, railroad curve text book, figuring pad.) The transitman runs the transit, keeps the notes, and in the absence of the chief, directs the work of the party. He should do careful and exact as well as rapid work, since the

progress and character of the survey are usually controlled chiefly by the skill of the transitman.

In leveling up, keep the lower parallel plate about level. Avoid undue tightness of foot screws. In setting the vernier to zero, use a quick converging motion with the tangent movement and note the adjacent graduations. If the transit has lost motion, learn which way to get the slack on the tangent screws. As a rule, use the lower motion by preference. Habitually back sight to the rear with telescope reversed, then plunge the telescope on prolongation and read the deflection right or left. If practicable, base the calculated bearings on a true meridian; otherwise, allow for the magnetic declination at a station which seems to be free from local attraction and thus obtain a reference meridian. Check all deflection angles by needle reading, both as to amount and direction. Lack of proper adjustment is no excuse for error. Always prolong a tangent line by double sightings. Also check deflection angles from time to time, by double sightings. Check on back sight before finally approving any precise point; likewise never fail to conclude the observations at each transit station by checking on the back sight. In such check it is usually best to sight back precisely on the point and then note whether the vernier has the proper reading. Assist the flagman in plumbing the pole, and always sight as near the bottom of the pole as possible. The transitman should admonish the chainmen, etc., to keep clear of the line.

On preliminary surveys, usually let the rear chainman line in the head chainman by eye, at least for short stretches. Do not hesitate to offset or zig-zag more or less along open ground to gain time. A rapid method for passing through heavy timber is to zig-zag on slight deflection angles right and left, tabulate the lengths in stations and deflections in minutes, and the products of the two in separate columns on the right hand page. The original line is regained by making the algebraic sum of the products zero, and the original direction is resumed by turning off a deflection which balances the deflection angle columns.

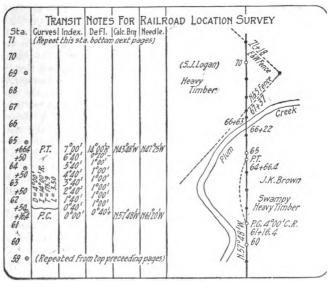
On location, each stake should be lined in carefully by transit. Small obstructions, such as trees, may be passed by parallel lines, using offsets of one foot or so at two hubs a few stations apart; the line is resumed in like manner. Where plate readings are used in rectangular or other offset methods, no sights shorter than 50 feet should be used. The equilateral triangle one station or more on a side is

often used. Obstructions on curves may usually be passed readily with the aid of tables of long chords and mid-ordinates.

Curve index-readings should be calculated as though the entire curve were to be run in from the P. C.; starting with the index-reading of P. C. always equal to zero, check the calculations by noting that the index of M. C. is 1/4 I, and of P. T. is 1/2 I. In using the notes, remember that with the transit at any point whatever on the curve, the following rules apply: (1) When pointing to any station, the vernier must always be set to read the index-reading for that station; and (2) when pointing on tangent at any station, the vernier must be set to read the index-reading for that station. As a rule, the best program in curve location is: Having P. I. located, (1) measure I and assume D; (2) calculate T and E; (3) establish P. T. by chaining off T on front tangent; (4) establish M. C. by laying off E on bisecting line; (5) locate P. C. by interpolating hub at calculated station number on back tangent; (6) move transit to P. C. and foresight on P. I.; (7) calculate curve notes (if not already done); (8) check sight on P. T. and M. C. and if satisfactory; (9) run in curve, checking for distance and angle on M. C. and P. T., moving transit ahead if desirable or necessary; (10) set up at P. T. and resume front tangent. One minute is the limit of allowable error in any curve. Mistakes in calculations or in measurements of angles will be counted serious errors. On final location the curves will be spiraled. After the line is located, reference out P. C., P. T., and other important hub points by two intersecting lines and take careful notes of the same (see method (g), Fig. 5, Chapter II).

The transit notes should be reliable, complete, neat and distinct. Each entry should have but one reasonable meaning and that the correct one. Record station numbers from the bottom upwards, usually with ten stations per page. Repeat the last station at the bottom of the next page. Allow two lines per station so as to provide for sketching at 200 feet to the inch. On the middle line of the right hand page mark each station with a dot and number every fifth station which should also be enclosed in a circle. The transit notes should include sketches of prominent land and street lines, stream crossings and other prominent topographic details, with pluses shown in the sketch. The notes should include date, weather, organization of party, etc. An appropriate title page giving name of survey, date

-	(TRA	NSIT !	NOTES	FOR	RAIL	ROAD PRELIMINA	
66 86	DeFI.	Mag.Ang	Mag.B.S.	Mag.F.S.	Cal.Brg.	(Organization	of Party.)
15 +93 134	25972	25°20′L	N48°30'E	N23°10'E	N2642'E	(Var.=3°32') 84+70	85 84+93 84+36
3						82+31-	82+67 Heavy Timber
3/ 0	8°57′R	9°00'R	N3930'E	N4830'E	N51°39'E	(Var. = 3°29')	81
90 79 o	49°13′R	49°10'R	N9º20W	N39°30'E	N43°02'E	(Var.= 3°12')	80 13 × 3 × 3 × 3 × 3 × 3 × 3 × 3 × 3 × 3
78						Wire Fence	
76 +86.4 75	14°42′1	142401	N4°35'E	N9°45'N		(Var.=3°34')	75+86.4 Timber
74					(N8 3/ E)	deflection point)	
Note.	Magn ing on	etic Bac back to	k Sight angent p	is need	le read- ed.	(Calculated bearing true meridian.)	gs are based on a



of commencement and completion, etc., should be prepared. The notes will be kept in the prescribed form. The field notes are to be returned at the close of the day's work. All estimated data should be noted as such.

Completeness and neatness of notes and records, facility and accuracy in handling the instrument, and promptness in advancing the progress of the survey will count in the estimate of the work of the transitman.

Head Chainman.—(Flag pole.) The progress of the chaining depends chiefly on the activity of the head chainman. After setting a stake he should move off briskly (preferably at a trot) and be prepared for the "halt" signal as he approaches the next station. When the full chain length is pulled out, the head chainman turns, holding the flag pole in one hand and the chain handle in the other, and sets the pole in line by signal from the rear chainman or transitman. Much time can be saved in this process if the head chainman habitually walks about on line and if he sights back over the two stakes last set. If on curve location, he should line himself in on the prolongation of the preceding station chord, and then offset by pacing or with flag pole a distance in feet equal to 134 times the degree of the curve; the calculation is made mentally and the pole can usually be set within a few inches of the correct position by the time a speedy transitman has the deflection angle set off. Having the line established, the pole is shifted to the correct distance, and the stake is driven plumb in the hole made by the flag pole spike. If the survey is a rapid preliminary line, the head chainman hastens ahead the instant the stake is started at the proper point, although in a more careful preliminary the chainmen check the distance to the driven stake. On location surveys it is customary for the chainmen to wait until the stake is driven and mark the exact distance on the top of the stake with the axe blade, and the exact line of signal from the transitman. In this process the head chainman should keep in mind the convenience of the transitman, and in case the line is being run to a front flag, the chainman should be careful to clear the line frequently to allow check sights ahead. In breaking chain on steep slopes the full length of chain should usually be pulled out ahead and the chain thumbed at the breaking points so as to avoid blunders: a plumb bob or flag pole should be used in the process. In passing over fences it often saves time to drive a 10-d nail, with "butterfly" attached, in the top plank to serve as a

check back sight from the next transit point. The chainmen should carefully avoid obstructing the transitman's view, to which end they should walk on the outside when

locating curves.

Rear Chainman.—(100-foot chain or tape, chaining pins (if allowed), figuring pad or note book.) As the rear chainman approaches the stake just set, he calls out "halt" and holds the end of the chain approximately over the stake, quickly lines in the flag pole in the hand of the head chainman (or the pole is lined in by the transitman), the precise distance is given, and the chainmen move on briskly. As a rule, pluses should be read by the rear chainman, the front end being held at the point to be determined. Fractions will usually be taken to the nearest 0.1 foot, although 0.01 foot may at times be properly noted. It is the duty of the rear chainman to keep a record of pluses and topographic details when the transitman is not at hand. This record may be kept on a figuring pad and the memoranda handed at the first opportunity to the transitman, who transfers the data to his book and carefully preserves the slips for future reference. It is usually better, however, to keep the auxiliary notes in a memorandum book instead of on the loose slips. The chainmen should carefully avoid disturbing the transit legs.

The responsibility for correct numbering of the station stakes rests chiefly on the rear chainman. It is his duty to remember the number of the previous station so as to catch blunders on the part of the stakeman. As he reaches the stake just driven, he mentally verifies its number and repeats it distinctly for the guidance of the stakeman in marking the stake to be driven; the stakeman responds by calling the new number, and each repeats his number as a check before final approval. The rear chainman then charges his mind with the numbers and checks the newly set stake on reaching it. In case of doubt he returns to the preceding stake and notes its number.

Stakeman.—(Sack of flat and hub stakes, marking crayon, handaxe.) The stakeman with his supply of flat and hub stakes in a sack, should keep up with the head chainman and be standing, with stake and marking keel in hand, ready to number the new station stake on hearing the rear chainman call out the preceding station number; the numbering is repeated, as already explained, before the stake is driven. Chaining pins are not used, but their equivalent in checking tallies may be had by numbering the

stakes ahead and tieing them up in sets of ten. By numbering stakes at slack moments the stakeman gains time to assist the axeman in clearing the line, etc. However, special care should be taken to avoid omissions and dupli-The stakeman should finish numbering the stake and hand it to the axeman by the time the head chainman has fixed the exact station point. The stakes should be numbered in a bold and legible manner, the keel being pressed into the wood for permanency. The number should read from the top of the stake downward. Stakes on an offsetted line should be so marked as 4'L or 2'R, beneath the station number. When survey lines are lettered, the serial letter should precede the station number. Guard stakes for P. I., P. C., P. T., reference points (R. P.), etc., should be clearly marked. The stakeman should assist the axeman in clearing the line and should drive stakes when the axeman is delayed. He should carefully avoid obstructing the transitman's view. The stakeman is under the direction of the head chainman.

Axeman.—(Axe, tacks, (and if so instructed) an extra sack of stakes with marking keel.) It is the duty of the axeman to drive stakes, remove underbrush from the line, clear an ample space about the transit station, etc. He is expressly warned, however, in student field practice, not to hack or cut trees or damage other property in any way, and in general, not to trespass on the rights of owners of premises entered in the progress of the survey.

The flat station stakes are driven firmly crosswise to the line with the numbered face to the rear. Hubs are driven about flush and usually receive a tack; they are properly witnessed by a flat guard stake driven 10 inches or so to the left, the marked face slanting towards the hub, as shown in Fig. 9, Chapter II. The axeman receives the marked stake from the stakeman and drives it plumb at the point marked by the spike of the flag pole. On location or careful preliminary surveys when the stakes are being lined in by transit, the axeman should stand on one side when driving and keep a lookout for signals from the transitman. In shifting the stake as signaled he should use combined driving and drawing blows with the axe. When the precise point comes much to one side of the top of the hub, another hub should be driven alongside and the first one driven out of sight before the tack is set. The axeman should move ahead briskly and avoid delay to the chaining. The stakeman should, when necessary, drive the stake with the spare handaxe. When the field force is scant, one man may serve in both capacities. The axeman is under the direct charge of the head chainman.

Front Flagman.—(Flag pole, small supply of hubs and guard stakes in stake sack, handaxe, a few 10-d nails.) is the duty of the front flagman to establish hub points ahead of the chaining party under the direction of the chief and transitman. In selecting transit stations he should keep in mind visibility and length of both fore sight and back sight, and to this end, points should be taken on ridge lines and where underbrush, etc., is least in the way. The practice of planting the flag pole behind the hub may be warranted occasionally, as for example, when the field party is shorthanded, but never when the regular flagman is not specially detailed for other duties. The front flagman should keep close watch on the transitman and should habitually stand with the spike of the flag pole on the tack head and plumb the pole by standing squarely behind it and supporting it between the tips of the fingers of the two hands. Should the front flagman be flagging for an interpolated point depending on a foresight which his pole would conceal, he should clear the line for a check sight by leaning the pole to one side. When crossing fences he should. when convenient, establish check sights on the top plank by driving a spike and attaching a "butterfly"

Rear Flagman.—(Flag pole, hatchet, slips of paper.) The rear flagman gives back sight on the preceding transit station. The details of his duties are much the same as those of the front flagman. It is an excellent plan for him to cut a straight sapling or limb and plant it exactly behind the hub when signaled ahead. This picket pole is made more visible by splitting the top and inserting a slip of paper, to make a "butterfly." A series of such pickets on a long tangent line often affords a fine check on the work when an elevated transit point is reached.

LEVEL PARTY.—It is the purpose of the level party to secure data concerning the elevations of the points along the line so that an accurate profile may be made and the grade line established. The leveling party should be on the alert to detect errors in the work of the transit party, such as omitted or duplicated stations, etc. The party consists of two members: (1) leveler, (2) rodman. In very brushy country an axeman may be added, but this is usually unnecessary if the line cleared by the transit party is followed.

			EVEL			
S	+	. 7	-	E	0	Oct. 13, 1893 . Cool . Swift, Rodman.
B-M					712-39	Spike in notch at root of Elm tree, 68'R.
\mathcal{X}	+7.21	719.60				of Sta-15+48, 25. of rail fence.
16	1		8-4	711-2		Ground
17			7-2	712.4	1	17
18			5.4	714.2		41
19			6.4	713.2		11
20			4.5	715-1		11
+50			2.1	717-5		12
21			0.2	719.4		77
0		.3	-0-15		719.45	On hub at Sta. 21-
T	+8.83	728-28				
22			8.4	719.9		Ground
+28			6.6	721.7		77 P.C. 1000'C-R.
23			4.8	723.5		17
24			3.8	724.5		**
25			3.7	724.6		*1
26			1.6	726.7		- 11
B.M.			- 1.57		726-71	Top of granite boulder, 74'R., Sta. 26+17.
T	+8.92	735-63				,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
27			5.6	730.0		Ground
+32			5.7	729.9		11 P.T.
28			3.8	731.8		11
29			3.7	731.9		"
30			4.3	731.3		,1
31			5.2	730.4		11 (Checked O's B.M.'s and H.I's with
	+24.96	735-63	-1.72	Profile		Rodman's Peg. Book.).
	- 1.72	712.39		data		wemans reg. Dook.).
	+23.24	+23.24	Check	above.		

Leveler.—(Level, adjusting pin, level note book.) The leveler should follow the most approved methods described under the head of differential and profile leveling in Chapter IV. The nearest 0.01 foot should be observed on turning points and bench mark rod readings and elevations and on occasional important profile points. The fore sight rod readings on ground profile points are to be taken only to the nearest 0.1 foot and the nearest 0.1 foot in the height of instrument is to be used in calculating the elevation. (Beginners sometimes calculate elevations to 0.01 foot when the rod readings are taken only to the nearest 0.1 foot.) The leveler should be rapid with his level as well as with figures. He should calculate elevations as fast as the rod readings are taken and should systematically check up the turning point and instrument heights as the work proceeds. As results are verified the same should be indicated by check marks. Each page of notes should be checked by summing up turning point back and fore sight rod readings, and comparing their difference with the difference between the first and last elevations or instrument heights, as the case may be, on the page. Follow the prescribed form. As far as

possible, bench marks should be checked by including them in the circuit as turning points. Balance back and fore sight distances on turning points. Permanent bench marks should be established at least every 1500 feet, and located in places at once convenient and free from disturbance during construction. Later levels should check within 0.05 foot into the square root of the length of circuit in miles. When a discrepancy is found, a line of check levels must be run to fix responsibility for the error. In crossing streams, secure high water elevations, with dates, especially of extraordinary floods, also low water level. crossing highways obtain elevations each side for some distance with a view to avoid grade crossings. In going up or down steep slopes, gain all the vertical distance possible each setting, and follow a zig-zag course. The bottom of deep gullies may be determined by hand level. Assist the rodman in plumbing the rod, and on turning points and benches have the rod gently swung in a vertical plane to and from the instrument and take the minimum reading. The self-reading rod is to be preferred. Many levelers use the Philadelphia rod without target. If the target is used on turning points, the leveler should check the rod reading when practicable.

Completeness, correctness and neatness of notes and records, and facility and accuracy in handling the level will be given chief weight in fixing the merit of the leveler's work. The level notes are to be returned at the end of the

day's work.

Rodman.—(Leveling rod, peg book, hatchet, turning point pegs, spikes, keel.) The rodman holds the rod at station stakes and at such plus points as may be required to make a representative profile. It is his duty to identify each station point and be on the lookout for duplicated or omitted stations. To this end he should habitually pace in each station, especially in grass or underbrush, and call out or signal the station number to the leveler. Should a blunder in station numbering appear, he should positively confirm the fact by retracing several stations, and then carry the corrected stationing ahead. The rod should be held truly plumb, which is best done by standing squarely behind the rod and supporting it with the tips of the fingers of both hands. On turning points, the rod should be waved gently in a vertical plane to and from the instrument. The rodman should pay special attention to placing the target right for long rods and examine it to note if it has slipped before reading the rod. Errors of 1 foot, 0.1 foot, etc.. should be carefully guarded against. Turning points should be selected with special reference to their solidity, and care should be taken not to disturb them. Station pegs and hubs are often used for turning points; when so used, the precise fore sight to 0.01 foot should follow the usual ground rod reading to the nearest 0.1 foot. The rodman should use good judgment in selecting bench marks, locating them out of reach of probable disturbance during construction and describing them so as to be easily found. He should be active and do his best to keep close up with the transit party. The rodman should keep a peg book for recording turning points and instrument heights, and check his computations independently and compare results with the leveler.

TOPOGRAPHY PARTY.—It is the purpose of the topography party to secure full data for mapping contours, property lines, buildings, roads, streams, and other important topographic details. The width of territory to be embraced in the survey depends on local conditions; in places it may be as much as one-fourth or one-half mile from the line, although it is usually better to run alternate lines when the distance to be included becomes so great. The topography party often consists of only two men, but a party of four is much more efficient. Sometimes no regular topography party is provided, but after running a few miles of line ahead, the transit and level parties are formed into several parties to bring the topography up to the end of the preliminary line. For student practice the topography party will consist of four members: (1) topographer, (2) assistant topographer, (3) topography rodman, (4) tapeman.

Topographer.—(Topography board, topography sheet (or several sheets), hard pencil, compasses, eraser, etc.) The topography sheet should be prepared before going to the field, showing the alinement and other data needed from the transit notes, and elevations of all stations and pluses from the level notes. Cross-section paper is to be preferred. The center line may be plotted to one side of the center line of the sheet, when the topography is to be taken farther in one direction than the other. In order to secure full details, the scale of the field plat may well be double (or even more) that of the finished map. The topography sheet should show local conditions, such as gravel banks, rock ledges, etc., suitable for ballast or other constructive use; out-croppings of rock or other material which may

affect the classification of the graduation; character of substrata at sites of bridge or other masonry work; springs, wells, streams, etc., suitable for water supply; approximate flood levels and other data relating to waterways or surface drainage: location of streams, especially with reference to desirable crossings, freedom from probable change of channel, etc.; location of highways including elevations some distance either way with special reference to avoiding grade crossings; other railroad lines, with the same point in view; character and condition of crops and other farm improvements, names of owners, etc.,—in short, any and all information that is at all likely to be of service in mapping the route, projecting the location, during construction, etc. In locating a group of buildings some distance from the line, fix the principal one by tie lines, by intersection or polar coordinates, and the others by measurement and sketch from it. Locate buildings near the line by rectangular offsets, or by intersections of the principal outlines with the survey line. Contours are located by means of the hand level used by the assistant topographer. The contour interval should be five feet ordinarily, but may be increased to ten or more feet on very steep slopes. The contour data should be selected with special reference to ridge and gully lines (see problem and plat on contour leveling, Chapter IV). Ordinarily hand level lines may be run out at right angles; angling lines along gulches and ridges may be located by estimation, pocket compass or tie lines. The plat is made by the topographer from data collected by the other members of the party. A common fault with the beginner in such work is the omission from the plat of important numerical data, such as station numbers of landline crossings, etc., owing to an undue attention to the minute details of the drafting work. A good topography record with contour notes on the left hand page and field sketch showing all numerical data on the right, is shown in the accompanying form.

Assistant Topographer.—(Hand level, pocket compass, topography note book.) It is the duty of the assistant topographer to collect data for the use of the topographer in making the plat. He uses the hand level, notes station numbers, distances, bearings, etc., and makes such record of the same as may be required to fit local conditions. In contouring, a special rod with adjustable base (see Fig. 19, Chapter IV.), if available, may be used; otherwise, an ordinary flag pole with alternate feet red and white is em-

	(RAILROAD	TOP	DGRAPHY.)	415 420 415 440 440 440
Sta.	Left Contours	Center Elev.	Right Contours	4 4 4 4 4 4 4
139	415 420 425 430 391 253 124 28	43/·/	435 440 445 107 296 369	Timber 139 Pasture
138	415 420 425 301 178 69	427-2	430 435 440 86 218 367	+040 Pence
137	415 420 202 103	421.9	425 430 435 440 77 97 293 406	1016 +53 Dwelling
136	<u>415</u> 23	418.0	416 420 425 430 435 14 106 212 309	10 1 106 1 20'x 30'
135	<u>415</u> 31	417.6	414 420 425 430 435 28 1/2 2/3 309	Heavy Timber
134	<u>415</u> 33	418.5	440 392 420 425 430 435 26 106 193 296	(Swampy) Pasture
133	415 420 67 5	420.4	(Obstructed)	109 97 Sheep Sheed
/32	415 420 83 51	423.1	413 425 430 435 440 24 103 175 280	Table Fence
131	415 420 425 430 228 139 43 45	430.7	435 440 445 72 195 348	Tan. fo Creek
130	420 425 430 435 333 240 148 64 415 420	437.0	440 445 450 89 223 391 •	E-&W. Fence. Sec. Line 130 3 Wheat,
129	425 430 435 440 308 216 132 31 415 420	440.8	445 450 124 309	1016-3 to Stone, NW. Cor. Sec. 18-
128	425 430 435 440 344 262 173 97 415 420 425	443.4	445 450 455 39 224 389	(Shed) of 0.84 4.55
127 4	431 296 252 430 435 440 445 280 185 121 8	445.2	450 455 182 242	197 197 197 197 197 197 197 197

ployed. Beginning with the known profile elevation, as extracted from the leveler's record, even five-foot contours are located, as a rule, nominally every 200 to 500 feet at right angles to the line, except as ruling ridges or gullies may suggest other directions. His record should be ample and legible, and include data and information which may not properly be placed on the plat. All estimated elevations, distances or dimensions should be noted as such. The assistant topographer works under the direction of the topographer, but is expected to take the initiative in the collection of data so as to permit his superior to devote proper attention to the field plat.

Topography Rodman.—(Topography rod with adjustable base (see (f), Fig. 19, Chapter IV.) or flag pole, hatchet.) It is the duty of the rodman to hold the topography rod as directed by the assistant topographer. He should be active and continually on the alert for information or data which the record book or sheet should contain. The rodman holds the zero end of the tape in measuring the distances. He should acquire skill in pacing on rough as well as smooth ground, and when sufficiently exact es-

pecially on ground remote from the surveyed line, he should gain time by pacing in the distances to contour lines.

Tapeman.—(Metallic (or band) tape, set of chaining pins, flag pole.) It is the duty of the tapeman to determine distances with the help of the rodman. He should be vigilant in checking up tallies, reading fractions, leveling the tape, breaking chain, plumbing down ends, etc., and should never be the cause of needless delay in the work. When required, he should measure angles, take tie lines, etc., with the tape.

OFFICE WORK.—The office work of each student includes: (1) reconnaissance map, profile and report; (2) map showing preliminary lines with topography and projected location lines; (3) preliminary profile with grade lines, approximate estimate of quantities, etc.; (4) final location map (traced from preliminary map); (5) location profile; (6) copies of field notes; (7) cross-section notes and estimate of graduation quantities; (8) estimate of cost of constrution; (9) monthly estimates, progress profile, haul, prismoidal and curvature corrections, vouchers, etc., final estimate.

Reconnaissance Report.—The reconnaissance map showing the area examined will be based upon such maps of the route as may be available. It should show the several ruling points and general routes selected for actual survey. The profile should be based upon barometric or hand level observations and distances scaled from the map or determined roughly by pacing or otherwise on the ground. The report should refer to the map and profile and state the general scheme, the several ruling considerations or conditions, the details of the examination, a rough comparison of the several alternative routes, and a final summary and conclusion with definite recommendations. The report should be made in accordance with best usage as to form, composition, etc.

(Considering the limited point of view of the beginner, the reconnaissance reports may not be required until the actual surveys are well along. In such case, however, the student is not to draw data from sources other than those above outlined.)

Preliminary Map.—The mapping should be the best product of the student's skill as a draftsman, and should conform closely to the department standards, which are based upon best current usage of leading American railroads. Unless otherwise instructed, the preliminary map

N.32°34'W. 2 N.64°41'W. N.36°26'W N.25°48'W. N.23°21'W.	Dist. Ft. 7489-1 2 78-5 464-1 - 725-5	N. 097.7 33.6 373.4	rudes 5.	INARY Depar E	tures W 1339.8	Total Lat · N · 0·0	Total Dep. W. 0-0	
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N-36°26'W N-25°48'W- N-23°21'W-	225.5				71.0	2097-7	1339.8	1
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	1212	203.0			98-1	2504.7	1686.4	1
	436.7	400.9			173-1	2707.7	1784.5	
N.4°41 W.	164.8	164.2			13.5	3108.6	1957-6	١.
	152.9	94.8	1		119.9	3272-8	1971-1	1
N.14°35'W.	176.0	170.3			44.3	3367-6	2091.0	1
	310.1	309.9		8.3	1000	3537-9	2135.3	1
N.1935'W.	105.9	99.6			36-1	3847.8	2127.0	١.
	307-8	276.2			135.9	3947-4	2163.0	1
5.78°42'W.	331.9		65.0		325-5	4223.6	2299.0	1
N-2804'W-	202.7	178.9			95.4	4158.6	2624.5	1
N.49°33'W.	156.4	101.5			119.0	4337.5	2719.9	1
	332.6	48.4	1		329-1	4439.0	2838-9	ı
	308-7	219.2			217-4	4487-4	3168.0	1
N.5640W.	128.1	70.4			107.0	4706-6	3385.4	ľ
- 5.81°00'W.	251.8		39.4		248.7	4777-0	3492.4	1
	334-2	219.5			252.0	4737-6	3741.1	1
N.84°08'W.	266-9	27-3			265.5	4957-1	3993-1	1
N-82°03'W-	317-0	43.8	1		313.8	4984-4		1
. N.89°25'W.	557-8	5.7			557-8	5028-2	4572.4	1
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	181+291		1086.7	2144'R	2001	2865.0	550.0		1 2 2 2 2	P. J. =	
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/	i	l	Check.	54 357	¶ ~ <i>''</i>	Check	256/7-5	/	column)		l /

will be made on eggshell or paragon paper. There are three ways to plot the skeleton of the preliminary survey: (1) by laying off each successive deflection angle and distance from the preceding line; (2) by laying off the successive calculated courses and distances from a precisely drawn meridian or other reference line; and (3) by rectangular coordinates. The first method should not be used, since cumulative errors are probable. The second is rapid and free from serious objection; if preferred, a modified base line may be assumed and the calculated bearings transferred to the same; the angles may be laid off by means of scale and table of natural trigonometric functions from a precisely drawn base line and then transferred, as required, by parallel ruler or triangle; this method is used most in practice. The third method is the most exact, and will be used by the student unless the second is specified. It involves the calculation of a plotting sheet, as shown in the accompanying form. The axis is usually a meridian line, but any line may be taken and the courses changed to suit. In making the plotting table, the data, calculated bearings, distances, etc., should be carefully checked through to the last point in the skeleton before the plotting is begun. Only one axis should be plotted, preferably the one having greater totals, so as to give short perpendiculars. Starting from the origin, 1000-foot points are pricked in along the axis to the specified scale, and marked 0, 10, 20, etc.: the totals are interpolated on the axis and lettered; exact perpendiculars about the right length are erected; the second point is established by scaling the perpendicular and the line is checked back on the preceding point; if correct, the stations are pricked in and every fifth station and deflection points are enclosed in a small circle and neatly numbered; the next course is so located and checked back by length of hypothenuse, the stations fixed and numbered, and so on to the end of the line; the courses should be taken in their order and none passed without checking satisfactorily. After the skeleton is completed, the topographic details are penciled in, and the map finished and inked. The title, border, meridian (both true and magnetic), etc., should be first-class in quality and in keeping with the rest of the map. Crude or careless lettering or other details of the map will cause its rejection. The title of the map, profile, etc., should be given in brief on the outside of the sheet or roll at each end.

Preliminary Profile.—Use Plate A profile paper in making the profiles. The level notes should first be carefully verified and then one person should read off while another plots the data. A hard pencil, 6H or 7H, sharpened to a long needle point should be used. The stations are first numbered along the bottom from left to right (or the reverse, as prescribed); leaving six inches or so at the left for a title, and beginning at a prominent line with station 0, every tenth station is so numbered. The notes are examined for lowest and highest elevation and a prominent line is assumed as an even 50 or 100-foot value relative to the datum. The horizontal scale is 400 feet and the vertical scale 20 feet to the inch. Points should be plotted no heavier than necessary, since the surface of profile paper will not permit much erasing. The surface line should be traced in close up to the plotted points, owing to the danger of overlooking abrupt breaks such as streams, ditches, etc. Pluses should be fixed by estimation. surface line when completed should be inked with a ruling pen used freehand; the weight of the line should be about the average of the ruled lines on the profile paper. special profiling or contouring pen is much used for this purpose.) The profile should show the grade line, grade intersection, elevations and rates of grade in red; water levels, and data relative to same in blue; surface line, station numerals, etc., in black; the alinement, important landlines, streams, etc., should be shown at the bottom of the profile in black. The grade line should be laid nominally with a view to balance the cut and fill quantities, but this should be varied to suit local conditions, such as drainage. the elimination of grade crossings, classification of materials, etc. The maximum gradients, the rate of compensation for curvature, etc., will be made to suit the specified conditions. The compensation for curvature will be allowed for on the preliminary profile by dropping the grade line on maximum gradients at each deflection point. Grade intersection elevations and rates of grade will be given to the nearest 0.01 foot.

Approximate Estimates.—Rapid estimates of earthwork quantities may be made direct from the profile either by reference to a table of level sections, or preferably by means of an earthwork scale. Estimates made in this way from the profile of a careful preliminary survey, often do not vary more than five per cent from the final construction quantities.

Location Map.—The location map may be traced from the preliminary map and should include the topography and such details as usually appear in the final record map of the located line. Contour lines may be traced in cadmium yellow to insure satisfactory blue printing.

Location Profile.—The location profile should be executed according to the standard specimen, and should include estimates of earthwork as determined from the actual cross-section notes, and quantities of other construction materials. Curvature compensation will be shown on the location profile by reduced maximum gradients. Vertical curves will be calculated at a rate of change not to exceed 0.05 foot per station, except at summits where it may be 0.10 foot or more per station. It should be prepared as the final record profile. Approximate profiles of projected lines, determined from the contour map, with rough estimates of quantities will also be prepared, as specified.

Office Copies of Notes.—The complete level and transit notes, and topography notes as assigned, must be copied in the individual books by each student. These copies will be in pencil (or ink if so specified) and will be executed in a faithful and draftsmanlike manner according to the department standards of lettering, etc.

Estimates of Quantities.—The cross-section notes will be copied and the quantities of excavation and embankment calculated, as assigned. The cross-sectional areas will be calculated arithmetically and checked, especially on rough ground, by means of planimeter. The quantities will be calculated by average end areas, by tables, and by diagrams, so as to afford ample practice for the student in all the current methods. The estimate will also include all the other materials of construction.

Estimate of Cost.—Each student will make a detailed summary of the quantities, fix prices, and estimate the probable total cost of the work, or of the assigned section. The prescribed form will be followed. The prices should be based on local conditions as far as possible.

Construction Estimates.—Monthly estimates, estimates of haul, borrow pit estimates, classification, prismoidal and curvature corrections, progress profile, vouchers, force account, etc., and final estimate will be prepared by each student in accordance with prescribed forms and standards.

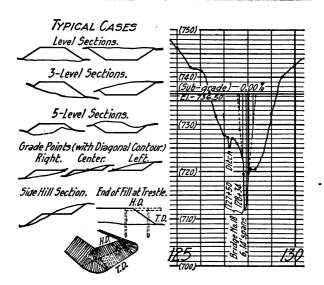
Right of Way Records.—Each student will be assigned a share of work in the preparation of right of way deeds and record maps. The following forms (from the "Engineering Rules and Instructions," Northern Pacific R. R.) will be used as models in preparing right of way descriptions.

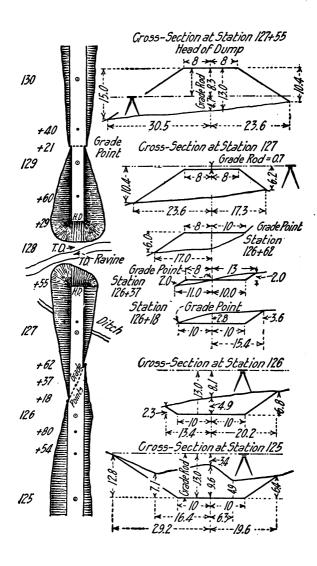
(Lots in platted tracts): "Lot seven (7), block six (6), in Smith's addition to Helena, Lewis and Clark county, Montana, according to the recorded plat thereof."

CROSS-SECTIONING PARTY.—It is the duty of the cross-sectioning party to set slope stakes for the proposed roadbed and to secure data for the calculation of earthwork quantities. The data should first be transcribed from the location level notes and profile into the cross-section book, including station numbers, surface and grade elevations, rates of grade, bench mark record, etc. In order to avoid confusion in relation to directions right and left, the station numbers should run up the page, and plenty of space left for pluses in the notes, especially on rough ground. As shown in the form, the left hand page should be used for data and the other for the cross-section notes.

The organization and equipment of the cross-sectioning party when using the engineers' level is: (1) recorder (note book), (2) leveler (engineer's level), (3) rodman (self-reading leveling rod, 50-foot tape), (4) axemen (axe, sack of flat stakes, marking keel). The usual routine is: (1) Determine height of instrument by back sight on identified bench or turning point. (When a bench mark is remote and an original turning point can not be found, it may suffice in an emergency to check on the ground at several stations to the nearest 0.1 foot and use the mean height of instrument. Such places should be verified later.) Having the height of instrument, check the original elevation of the station about to be cross-sectioned, reading the rod and checking off the elevation if it does not differ more than 0.1 foot or so; in case of a new plus, take a rod reading and record the elevation. (3) Determine the "grade rod" for the station by subtracting the height of instru-

				FORM	FOR	CROS	S-SECT	ION	NOTES)
5ta.	Elev-	Grade	#	Surf-Rod	GradeRod X 747-67	不	L	C	R	Remarks
/30	742.5	736-50	~	5.2	11.2	TT 728-22	***	+60	2000 EOO	(3-level section in cut)
+40	739-8	736-50	Н	7.9	11-2	FS- 057 0 727-65	133	+3-3	//3-8	(Level section in cut)
			П)	T 739.61 (3.D	BS-11-96 7 739-61	0.0		0.0	(c. 1 . 1 . 1 . 1 . 1 . 1 . 1 . 1 . 1 . 1
+2/	736-5		Н	<i>3.1</i>)-	ربي 3٠ <i>١</i>	FS- 2-03	10.0		10.0	(Grade point, L, C and L)
129	732.3		H	4.3	A 728-22	0737-58 BS-10-09	漆	4.2		(3 level section in Fill)
+60	723.9	120-50		4.3		X 747-67	-43-5	7/2-0	-/2:5	(Level section in Fill)
+34	720 5	225 50	8		- 4-	F.S. 548	-16-0		-16.0	Mend stringer, Br. Mº 18-
H.D.+29	720-5	15000	13	7-7	- 8.3	-Check on	350		32.0 -16.0	(Head of Dump)
T.D.+05	720.5		3	7·7 8·1	- 8.3	B-M-No-12 (below)	2:8	(160)	8:0	(Toe of Dump)
128		736-50		8.1		(50.0.1)	1		1 1	Bridge Mº18 (128+34
+90	7/2-2		518		1	T 737-23	0.0		1 1	6,14'spans \127+50
TO (+8).4			5		- 8.3	F-5-10-15	2:0 3:0	-		(Toe of Dump { left.)
(2,20	707.5		8	ا ۔ ۔ ا	- 83	0727-08 B-S-1-14	-/5.0	-	P. 20 8:8	(right)
#0.+55	723.5	736-50	*	4.7	-8.3	T 728-22	- <u>45:0</u>	-13-0	-10:4 #3:8	(Head of Dump)
1+50	- 1		3						1	5 end stringer, Br. Hº 18
+/3			,,		X 73723					Ditch 2.4 × 4.7 × 53.
127	727.8	736:50	1	9.4	0-7	X 749-51	23.8	-8.7	75.8	(3 level section in Fill)
162		736·50	į.	5.3	-0.7	<u>FS-12-58</u> 0736-93	79.8	-4.6	10:0	(Grade point right)
+37		736-50	8	<i>©?</i>	T749-51	B-5-0-30	7.8	0.0	73.8	(Grade point center)
+/8		736-50	-	10.2	13-0	JT 757-23	10:0	+2.8	18 4	(Grade point left)
126	74/-4	736-50		8-1	13.0		海泽	+4.9	20.2	(3 level section in cut)
+80		736-50	80	7.8	13.0		## 3.3	+52	19:3	(Level section in cut)
+54	742.2	736-50	19	7.3	13-0	B·M·№12 742·17	1883 1818 1818	+5-7	72.8	(4 level section in cut)
125	746-1	736-50	ı	3.4	13.0	B.S. 734	#/3:8 +7:/ 20:8 /8:4	+9-6	43 #4	(5 level section in cut)
			t I	- 1		A 14951	ED-2 /6-4		55 19.8	Cuts, 20, 14:1, Fills 16, 14:1.





ment from the grade elevation; then note that cut or fill at any point of the cross-section is equal to surface rod minus grade rod (counting rods as minus when downward from the plane of the level and those upward as plus, this rule gives results always plus for cut and minus for fill, which agrees with the conception that cross-section notes are rectangular coordinates of the sectional area referred to the center of the finished roadbed as an origin). (4) If the ground is level transversely, that is, does not vary more than 0.1 foot or so within the limits of the proposed grading, then the distance from the center out to each side slope stake is half width of roadbed plus center cut or fill times rate of side slope; (thus for 20-foot roadbed, side slopes 1 to 1, and a cut of 18.6 feet, the distance out to slope stake on a level section would be 28.6 feet, or with a slope of 11/2 to 1, the distance out would be 10 plus 11/4 times 18.6, or 37.9 feet. Calculations of this sort should be done mentally in an instant). (5) On three-level ground estimate the rise or fall of the surface from the center to about where the side slope stake should come, and add the same to, or subtract it from the center cut or fill, as the case may be; compute the distance out to the point where the side slope line would pierce the ground surface and test the same with tape, rod and level by the foregoing rule for cut or fill; continue to construct points on the side slope line until the common point is found. (6) The axeman marks "S. S." (slope stake) on one side of the stake with the cut or fill to the nearest 0.1 foot (as C 6.8 or F 10.2) and the station number on the other side; the stake is driven slanting towards or away from the center line according as it is cut or fill. (7) On five-level ground or, in general, on ground involving any number of points or angles in the section, the cut or fill is taken at each break. (8) Should there appear to be danger of land slips, the cross-sectioning should be carried well beyond the limits of the slope stake points. (9) The cross-section notes are recorded as in the accompanying form, expressing the coordinates of each point in the form of a fraction, and distinguishing the slope stake points by enclosure in a circle. (10) Having completed the cross-sectioning at the station. the same program is followed at the next point, first checking the elevation obtained in the original location levels; the grade rod should be determined as before by subtracting the height of instrument from the grade elevation, and then checked by applying to the preceding grade rod the

rise or fall of grade from the preceding point. Cross-sections should be taken as a general rule at every station and at such intermediate points as will insure a reliable measurement of the earthwork quantities. It is not necessarily the lowest and highest points that are required, but those points which, when joined by straight lines, will give the contents as nearly as possible equal to the true volume; if the "average end areas" method is to be used in calculating the quantities, sections should be taken every 50 feet when the difference of center height is as much as 5 feet; as a rule, slope stakes need not be set at cross-sections taken between stations. (12) "Grade point" stakes (marked 0.0), should be set where the center line and each edge of the roadbed pierce the ground; and also in side-hill sections in both cut and fill, where the roadbed plane cuts the ground line; if the width of roadbed is different in cut and fill, the greater half-width is commonly used in locating the side grade point; in the simplest case a contour line is perpendicular to the center line and the three grade points are at the same cross-section, forming two wedges; in the more usual case the contour line is diagonal, and the three grade points are not in the same section, so that two pyramids are formed; if the station numbers of the two side grade points differ by only a few feet, it is usual to simplify the record by taking the notes as for a wedge at the station number of the center grade point, although the side grade point stakes are set in their true positions; as a rule, a complete crosssection is taken at each grade point. (13) In cross-sectioning for the end of an embankment at a wooden trestle the end slope is made the same as the side slope, and the end and side planes are joined by conical quadrants; the distance between "heads of dump" (H. D.) is usually 10 feet (5 feet at each end) less than the total length of stringers; a complete cross-section is taken at the "head of dump," and the "toe of dump" (T. D.) on each edge of the end slope is located and recorded; on level ground the volume of the wedge-like solid so formed is found by dividing it into a triangular prism and two right conical quadrants; on ground sloping transversely the end of dump is made up of a middle prismoid and two conical quadrants, each of the latter being generated by a variable triangle revolved about a vertical axis through a corner of the top roadbed plane at "head of dump."

The calculations in the foregoing method of cross-section-

ing may be simplified by preparing a table of distances out for the standard roadbed widths and slopes, or by using a special tape having the zero graduation at a distance from the end equal to the half-width of roadbed, and the remaining graduations modified to suit the side slope ratio. The calculations may be further simplified by using a special rod having an endless sliding tape graduation. The student will be given practice with these labor saving devices after he has first acquired familiarity with the principles of cross-sectioning without these aids.

Cross-sectioning with rods alone is done in much the same manner as that described above. Two rods are used. The usual length of the rods is ten feet, and each is graduated to tenths and has a bubble vial in one or both ends. The slope stake point is determined by leveling out from the ground at the center stake with reference to the center cut or fill, each rod being held alternately level and plumb. Other points in the cross-section, as well as grade points, etc., are determined in the same manner. The notes are kept as in the other method. On very rough ground, the rod method is usually the more rapid. Some engineers cross-section on rough ground by taking the elevation of each point and plotting the notes on cross-section paper, then using the planimeter to determine the areas. Borrow pits are often cross-sectioned by taking elevations at the intersections of two series of parallel lines forming squares.

Land-Line Party.—It is the duty of the right of way party to secure data for the preparation of right of way deeds. The party should consist of at least four: (1) recorder, (2) transitman, (3) head chainman, (4) rear chainman, (the chainmen also to serve as axemen and flagmen as required). Their equipment is the usual one of a transit party for such work. The party should secure ties with all section and other land lines whenever crossed. notes should show station numbers and angles of intersection and distance along land line to the nearest identified land corner and also to important fences. As a rule, make the intersection by running through from one corner to the other. Where the line passes through a town, tie the center line to the plats, block lines, monuments, etc. Secure anv records and make tracings of any plats, etc., at the recorder's office, that may be of service in preparing deeds.

Bridge and Masonry Party.—The bridge and masonry survey party will determine drainage areas for culverts and other waterways, prospect for foundations, and stake out

trestles, masonry work, etc. The usual organization will be four men: (1) recorder (in charge), (2) transitman or leveler, (3) chainman, rodman, flagman, etc., (4) chainman, axeman, flagman, etc., as the work assigned may demand.

Resurvey Party.—The resurvey party will be assigned to such duties as the resurvey of yards, the collection of data for crossings frogs, running centers on old track, including spiraling, etc. It will usually be a party of four.

PROBLEMS IN RAILROAD SURVEYING.

PROBLEM G1. ADJUSTMENTS OF LEVEL AND TRANSIT.

(a) Equipment.—Engineers' level and transit, adjusting pin.

(b) Problem.—Test the essential adjustments of the assigned instruments and correct any discrepancies found.

(c) Methods.—This problem is designed to freshen the student's knowledge of the adjustments of the instruments, as well as to place the equipment in condition for accurate work. The adjustments will be made under the personal direction of the instructor. The student should attempt to be speedy as well as accurate in testing and making the adjustments.

PROBLEM G2. USE OF FIELD EQUIPMENT.

(a) Equipment.—Complete equipment for railroad transit and level party, as specified in foregoing pages.

(b) Problem.—Practice the detailed duties of each posi-

tion in the transit and level party.

(c) Methods.—This problem is designed as a "breaking in" exercise preparatory to engaging in the regular field work of railroad location. With the manual in hand the duties of each position will be studied and practiced in turn.

For example, each student will go through the following exercise with the transit as briskly as possible: (1) set transit over tack in hub, (2) level up, (3) set plate to zero, (4) reverse telescope and sight on back flag, (5) release needle, (6) plunge telescope, (7) read and record needle on back line prolonged, (8) sight at front flag pole, (9) read and record deflection angle right or left, (10) read and record needle on front line, (11) lift needle, (12) plunge telescope and check on back flag, (13) calculate needle

angle and compare with plate reading, and if checked, shoulder transit; now repeat entire process at the same hub, more briskly than at first, if practicable, avoiding reference to preceding record until the full series of steps is completed.

T Give Giv	ration of Curve Elements. (I = 60°17'R. (P) = 4°17' (R(4°17) = 1337.65' EI = $\frac{60°17'}{2}$ = 30°08'5 (Results to 0.01 ft. (Results to 0.01 ft. (Results to 0.01 ft.) (Results to 0.01 ft.) (Results to 0.01 ft.)
	0°17'= 60°.2833+ 1°17'= 4°2833+ T 776.71 776.77 0.06 E 209.15 209.17 0.02
Indicated Work.	Calculations.
Length of Curve, L. $L = \frac{60^{1/7}}{25^{7/7}}$ (a) = $\frac{3617}{257}$; (4.073) (b) = $\frac{60^{\circ}2833}{4^{\circ}2633}$ = $\frac{4.0739}{4.0739}$	257)36/7)/4.0739 257 a.k. 428333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.28333 /4.283
Tangent Distance, T . (a) $T = R tan \frac{1}{2}I$ = (337.65×0.58066) = (76.7) (b) $T = \frac{T_1 \cdot c_0}{0}$ = $\frac{3327.15}{4.2833}$ = (76.7)	1337.65
External Distance, E. (a) $E = R$ exsec $\frac{1}{2}I$ = 133.65 × 0.15636 = (209.15) (b) $E = \frac{E_1 \cdot c}{5}$ = $\frac{895.95}{42.833}$ = (209.17)	/337.65

Let the student prepare a similar numbered program for each of the other positions and practice the same systematically. This series of exercises may profitably occupy two or more assignments, since the speed and quality of the actual surveys to follow are certain to be much enhanced.

PROBLEM G3. PRELIMINARY FIELD CURVE PRACTICE.

- (a) Equipment.—Transit party equipment, as prescribed in instructions.
- (b) Problem.—Run out the assigned practice curves in the field, with the prescribed organization and conditions.
- (c) Methods.—The preliminary curve practice is designed to give the student a practical knowledge of the principles of railroad curves and the routine methods used in location surveys. The several positions in the field party will be filled in succession, and each student is expected to respond heartly to the spirit of the practice, whatever his assigned duties. Each member of the party should engage in the calculations as far as practicable. The report of the field work should state the precision of linear and angular checks. The field practice will be based in part on the indoor curve problems.

PROBLEM G4. CURVE PROBLEMS.

- (a) Equipment.—Drafting instruments, paper, etc.
- (b) Problem.—Solve the assigned problems in railroad curves and submit results in a neat and draftsmanlike form.
- (c) Methods.—(1) Draw a plain figure to the largest convenient scale. (2) State problem and present data in a concise and systematic manner. (3) Show the separate steps clearly; first state formulas in general terms, then substitute values and give results; as a rule, show actual calculations adjacent to the indicated work; habitually verify results by an independent process; use common sense checks and contracted methods of calculation; in general, make full use of the opportunity to gain skill as a computer. (As a rule, the nearest 0.1 foot only is required in field measurements on curve location, but it is excellent practice, especially for the beginner, to preserve the nearest 0.01 foot in the calculations.)

CHAPTER IX.

ERRORS OF SURVEYING.

Errors.—Errors of observations are of three kinds, viz., (1) mistakes; (2) systematic errors; (3) accidental errors. Systematic errors include all errors for which corrections can be made, as erroneous length of standard, errors of adjustment, refraction, etc. Accidental errors are those which still remain after mistakes and systematic errors have been eliminated from the results.

It has been found from experience that accidental errors are not distributed at random but follow mathematical laws. These laws are fundamental in the Theory of Least Squares and are: (1) small errors are more frequent than large ones; (2) positive and negative errors are equally numerous; (3) very large errors do not occur.

Arithmetical Mean.—The most probable value of a quantity obtained by direct measurements is the arithmetical mean of all the determinations where the observations are of equal weight, or is the weighted mean where the observations are of unequal weight.

Precision of Observations.—In the adjustment of observations it is often necessary to combine results of different degrees of precision or weight. It is also desirable to have some means of comparing observations so that the computer may know what degree of confidence to place in the results. The quantity commonly used for comparing the precision of observations is the probable error.

Probable Error.—The probable error is such a quantity that it is an even wager that the number of errors greater is the same as the number of errors less than the probable error. It is also the limit within which the probability is one-half that the truth will fall. For example, if 4.63±0.12 is the mean of a number of observations, the true value is as likely to be between 4.51 and 4.75 as it is to be some value greater or less.

Probable error is also useful in finding the relative weights that should be given different sets of observations, as it has been found that the weights of observations vary inversely as the squares of their probable errors.

Formulas:

Let $E_1 =$ probable error of a single observation.

 E_{m} = probable error of the mean of all the observations.

n = the number of observations.

d = the difference between any observation and the mean of all the observations.

 $\Sigma =$ symbol signifying sum of.

Then from the Theory of Least Squares

$$E_1 = 0.6745 \sqrt{\frac{\Sigma d^2}{n-1}} \tag{1}$$

$$E_{\rm m} = 0.6745 \sqrt{\frac{\Sigma d^2}{n(n-1)}} \tag{2}$$

$$=\frac{E_1}{\sqrt{n}}\tag{3}$$

The probable error of the weighted or general mean is

$$E_0 = 0.6745 \sqrt{\frac{\Sigma p \cdot d^2}{(n-1)\Sigma p}} \tag{4}$$

where $\Sigma p =$ summation of the weights.

The probable error of a quantity with a weight p is equal to E_0 divided by the square root of p.

The probable error of Z, where $Z = z_1 \pm z_2$, and R_1 , r_1 , and r_2 are the probable errors of Z, z_1 and z_2 , respectively, is

$$R_1^2 = r_1^2 + r_2^2 \tag{5}$$

The probable error of Z, where Z = a. z is

$$R_1^2 = a^2 \cdot r^2 \tag{6}$$

The probable error of Z, where $Z = z_1$. z_2 is

$$R_1^2 = z_1^2 \cdot r_2^2 + z_2^2 \cdot r_1^2 \tag{7}$$

This would be the probable error of the area of a rectangle where r_1 and r_2 are the probable errors of the sides z_1 and z_2 , respectively.

Example.—As an example of the application of these formulas consider the two following series of measurements of an angle given in Table I. The first set was taken with a transit reading to 10 seconds, the second with a transit reading to 30 seconds.

TABLE I

FIRST TRANSIT.					SECOND TRANSIT.						
No.	A	ngle	.	d	d²	No.	Angle.		d	d2	
1 2 3 4 5 6 7 8 9	34	55 56 55	35 35 20 05 15 40 10 30 50 30	2 2 13 28 42 7 23 3 17 3	4 4 169 784 1764 49 529 9 289 9	1 2 3 4 5 6 7 8 9	34	56 55 54 55 56 55 55 55 56 55	15 30 30 15 00 45 30 30 00 45	39 6 66 21 24 9 6 6 24 9	1521 36 4356 441 576 81 36 36 576 81
Mean	n 34°	55′	33"	$\Sigma d^2 =$	= 3610	Mear	34°	55′	36″	$\Sigma d^2 =$	= 774 0
<i>E</i> _m =	$E_{\rm m} = 0.6745 \sqrt{\frac{3610}{9 \times 10}} = \pm 4^{\prime\prime}.3$					$E_m =$	0.674	15 V	7740 9 × 1		± 6″.3

The weights of these mean values vary inversely as the squares of the probable errors, or in this case the weights are as $\frac{1}{4.3^2}$ to $\frac{1}{6.3^2}$ or as 12 to 5. The most probable value of the angle measured with the two transits will be the weighted mean.

$$Z = 34^{\circ} 55' + \frac{33 \times 12'' + 36 \times 5''}{17}$$
= 34° 55′ 33″.9

The probable error of this result from (5) since

$$Z = \frac{1}{4} z_1 + \frac{5}{17} z_2$$
, is $R_1^2 = (\frac{1}{17})^2 r_1^2 + (\frac{5}{17})^2 r_2^2$

Substituting $r_2^2 = \frac{12}{5} r_1^2$ we have

$$R_1^2 = (\frac{12}{17})^2 r_1^2 + (\frac{5}{17})^2 (\frac{12}{5}) r_1^2$$

=\frac{12}{17} r_1^2

$$R_1 = \pm 4.03 \ \sqrt{\frac{13}{13}} = \pm 30.6.$$

For other examples in the use of probable error see probable error of measuring a base line, probable error of setting a level target, probable error of setting a flag pole.

Angle Measurement.—The measurement of an angle requires two pointings and two readings. If r_r and r_s are the probable errors of reading and pointing, respectively; the probable error of the measurement of an angle will from (5) be

$$R_1 = \sqrt{r_r^2 + r_s^2}$$

If r_1 is the probable error of a single reading $r_r = r_1 \sqrt{2}$

If the value of an angle is determined by n separate measurements the probable error due to reading will be

$$r_r = \frac{r_1 \sqrt{2}}{\sqrt{n}}$$

If the value of an angle is determined by measuring the angle n times by repetition the probable error due to reading will be

$$r_r = \frac{r_1 \sqrt{2}}{n}$$

It will thus be seen that the probable error due to reading is very much reduced by measuring an angle by the method of repetition. The errors of pointing, etc., however, make it doubtful whether it is ever advantageous to make n exceed 5 or 6 with an engineers' transit.

Angle Adjustment.—When the three angles of a triangle have been measured with equal care they should be adjusted by applying one-third of the error as a correction to each angle.

When the interior angles of a polygon having n sides have been measured with equal care they should be adjusted by applying *one-nth* of the error as a correction to each angle.

When n-1 angles and their sum angle at a point have been measured with equal care they should be adjusted by applying *one-nth* part of the error as a correction to each angle.

In a quadrilateral the true values of the angles fulfil the following geometrical conditions: (1) the sum of the angles of each triangle is equal to 180° plus the spherical excess

(the spherical excess in seconds of arc is equal approximately to the area in square miles divided by 78); (2) the computed length of any side when obtained from any other side through two independent sets of triangles is the same in both cases.

When the angles of a quadrilateral have been measured, errors are certain to be present and the corrections that satisfy one of these conditions will not satisfy the other. The most probable values of the corrections to the angles are then determined by the Theory of Least Squares.

TESTS OF PRECISION.

Practical Tests.—In careful surveying where blunders are eliminated and the systematic and accidental errors are small and under control, it is found that the magnitude of the errors increases in close accord with the foregoing rational basis, that is, as the square root of the number of observations. The following practical tests of precision are based on this truth.

Linear Errors.—Cumulative or systematic errors usually increase directly as the length of the line chained, while compensating or accidental errors vary about as the square root of the length. While both kinds of errors affect all linear measurements, the former chiefly control the results of crude and the latter of accurate chaining. It is thus fairly consistent to express the precision of chaining in crude work in terms of the simple ratio of the length; but as the chaining becomes more and more exact, the variation of the differences between duplicate measurements approximates more and more closely to the law of square roots.

Coefficients of precision derived from the latter relation may be based on either 100-foot units or foot units in the distance chained, as preferred. The former basis is used in the chaining diagram while the latter is found in the last paragraph of the explanatory matter on the second page referring to the precision of traverse surveys.

The diagram of chaining errors shows chaining ratios by right lines radiating from the origin, and the law of square roots by means of parabolas. The coefficient of precision for a given observed difference between duplicate chainings is determined by inspection from the diagram, interpolating between curves if an additional decimal place is desired in the result. In actual practice a pair of careful chain-

men may determine the coefficient corresponding to a given degree of care, and then use this value either in testing their duplicate results, or in estimating the probable uncertainty of the lengths chained.

For accurate chaining with the steel tape, duplicate measurements reduced for temperature, etc., or made under sensibly identical conditions, should not differ more than 0.05 foot into the square root of the distance in 100-foot units. Careful work with the common chain (estimating fractions to 0.1 foot) should not differ more than 0.1 foot into the square root of the distance in 100-foot units.

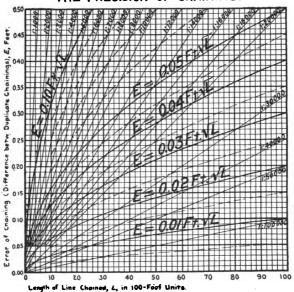
Angular Errors.—In measuring deflection angles by altitude reversals, as in railroad traversing, there is, of course a cumulative discrepancy due to the collimation error, but generally speaking, careful angular measurements with good instruments are subject only to compensating or accidental errors. Under the latter conditions the magnitude of the error of closure in a series of angles, either in a closed polygon or about a point, varies about as the square root of the number of angles. This relation is indicated graphically in the diagram of angular errors.

In measuring angles with a transit reading to the nearest minute, the compensating uncertainty of a single reading is probably somewhat under 0.5 minute per angle, or about one minute for the closure of a triangle. If a reading glass be used and the vernier reads to the nearest half minute, the uncertainty is still further reduced.

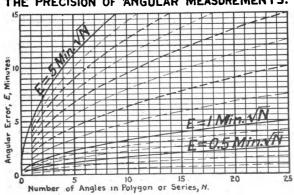
Again, in estimating the needle reading of a compass to the nearest 5 minutes (one-sixth part of a half-degree), the uncertainty of reading alone is perhaps 3 minutes, although this is increased by other conditions such as sluggishness of needle, etc., probably causing an uncertainty of as much as 5 minutes per angle, which later limit would produce an error of closure of a triangle of say 10 minutes, and of a five-sided polygon of perhaps the same amount. (See diagram.)

Traversing Errors.—The errors of traversing are made up of the combined errors of linear and angular measurements. If the error of closure as determined from the latitudes and departures is large, the work should be scanned closely to detect blunders such as the substitution of sine for cosine, errors of 100 feet in chaining, misplacing decimal point, etc. After establishing the consistency of the residual errors, they should be distributed either in proportion to the lengths of the several courses, as in the more

THE PRECISION OF CHAINING.



THE PRECISION OF ANGULAR MEASUREMENTS.



THE PRECISION OF TRAVERSE SURVEYS.

The error of closure of a traverse is usually expressed as the ratio of the celculated linear error to the length of the perimeter of the field or polygon. The following table shows the limits prescribed by various authorities

Prescribed Limits For Closure Of Traverses.

Authority.	Conditions.	Limits.	
Gillespie. (1855). "Surveying," p. 149.	Compass Surveys.	1:300 to 1:1000	
Alsop. (1857). "Surveying," p.199.	Compass Surveys. Transit Surveys.	1:500 1:1000 to 1:1500	
Davies. (1870). "Surveying," p.127.	Farm Surveys.	1:500 to 1:1000	
Jordan. (1877). "Handbuch der Vermessungs- Kunde," Vol.1, p.296.	German Gov't Surveys. Baden Instructions. Prussian Instructions. Swiss Gov'r Surveys. Ordinary Country. Mountainous Country.	1:400 1:333 to 1:1000 1:400 to 1:800 1:267 to 1:533	
Hodgman. (1885). "Surveying," p. 119.	Compass Surveys.	1:300 to 1:1000	
Johnson. (1886). "Surveying," p. 201.	Farm Surveys. City Surveys.	1:300 1:1000 to 1:5000	
Baker. * (1888). "Engineers' Surveying Instruments," p. 53.	(See Footnote).	(See Footnote).	
Carhart. (1888). "Surveying," p. 161.	Ordinary Farm Surveys. Level Ground. Rough Ground. Average Transit Surveys.	1:500 1:1000 1:200 to 1:300 1:1200	
Wood. (Roanoke, Va., 1892). (Baltimore, Md., 1894).	(See Footnote). {Precise Traverses with { Repeated Angles. }	(See Footnote). 1:10 000 1:15 000 + .04 Ft.	
Raymond. (1896). "Surveying," p. 144.	Ordinary Farm Surveys. Good Farm Surveys.	1:500	

^{*}Baker derives the formula $E = P\sqrt{\frac{1}{d^2} + \frac{q^2}{12000000}}$ where

E is the permissible linear error of closure, P the length of the perimeter, I'd the ratio of the chaining error, and a the angular error of closure in minutes. A thorough test of this formula under a wide range of conditions proves it to be trustworthy.

However, the use of a chaining ratio, 1:d, presumably of fixed value for the same chainmen, does not accord with the results of experience in careful work; for it is found that the differences between duplicate chainings vary about as the square root of the

length of line.

On the following page a simplified formula is obtained by assuming the more consistent relation just stated for the chaining errors. The results are about the same as those obtained with Baker's formula, and the form of the expression is identical with that used by Wood in the Baltimore Survey.

THE PRECISION OF TRAVERSE SURVEYS.

The reesonable or permissible error of closure of a traverse survey may be determined by the formula derived below, provided the errors of field work are under control and their magnitude is known, at least experimentary.

Let P knowth of perimeter, belowed.

L= calculated error of latitudes.

L=Calculated error or larruses.
D=cakulated error of departures.
E=actual or Calculated linear error of closure of traverse.
C=coefficient of precision of chaining.
C= linear error of closure due to chaining errors.

a= angular error of closure in minutes.

A = lineer error of closure due to angular errors. E_p= permissible or reasonable linear error of closure due to errors of chaining and angle.

In the triangle of error the hypothenuse is $E_a = \sqrt{L^2 + D^2}$. In Diagram A below values of E_a may be read close enough for most cases. Diagram A may also serve as a crude graphical tremers table, and blunders in the field work may be located by it.

In careful chaining by men of some training, the error varies about as the squere rost of the distance. If a be the compensating error for the unit distance, then Co-CPP.

The angular error of closure in careful surveys probably occurs among the sides in proportion to their lengths. Assuming this to be the case, the resulting linear error is A = a P.arc I'= .0003 aP.

In good work the errors are small in amount and equally liable to be plus and minas. Hence, the probable error of closure due to the two couses, i.e. the reasonable or parmissible linear error of closure is $E_p = \sqrt{\hbar^2 + C^2} = \sqrt{(.0003 aP)^2 + c^2}$

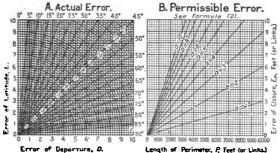
This formula may be much simplified by completing the square and dropping the negative term under the radical, whence with sufficient exactness, there results the general formula

$$E_p = .0003 \, aP + 1700 \, c^2 \cdot \cdot \cdot \cdot \cdot \cdot \cdot (1)$$

The very exact standard, P+15000+04ft, used at Baltimore, The very exact Standary, r+15 000+0+11, used at Battimore, (see table, preceding page), may be obtained from (i) by meking a somewhat less than ; minute, and c=005ft, these values being consistent with the field work of that survey.

The value of c may be determined for the given chainmen, or the chaining term of (!) may be taken as follows:- For best work (<.005 ft.), 05 ft.; for derrage work (<.010 ft.), 25 ft. for fair work (<.015, 4 ft.; and for poor work (<.010, 8 ft. In careful traverse surveys the angle term done affords a rigid test, so the formula (2) may be used except when a=0. Diagram B gives (2) for the general run of traverse problems.

Ep=,0003 aP= 3aP(2)



Error of Departure, D.

Length of Perimeter, P. Feet (or Links.)

THE PRECISION OF LEVEL CIRCUITS. (For Good Average Practice.)

When the length of the level circuit is known in 100-ft. stations, or when merely the number of settings of the instrument and the approximate aeroge distance covered per setting are known, the following modifications of the preceding test are valuable.

L'=approximate average distance covered per setting of the instrument in 100-ft. stations.

5 = number of instrumental settings in the circuit.

For good average work with the engineers' level

E = 0.05 A.VM

from which

E = 0.007 A.VL

and

E = 0.007 A. 125

Substituting for 400-ft. average sights, L'=8, E = 0.0195 ft. V3

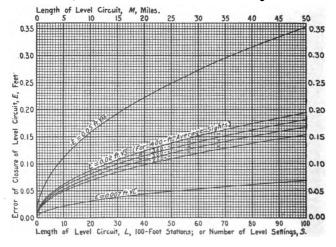
. 350-- " L'=7. E = 0.0102 ft. V3

300-- - L=6, $E=0.0169 + 1\sqrt{5}$ 250-- - L=5, $E=0.0154 + 1\sqrt{5}$

For a very rapid approximate check under ordinary conditions, it may be assumed that E=0.021.75. A graphical representation of these formulas is given below.

Permissible Error of Closure of Level Circuits For Careful Work with a Good Engineers' Level.

Length of Circuit Given in Miles (Upper Gurve); or in the Number of Instrumental Settings (Middle Group of Curves); or in 100-Foot Units (Lower Curve in Diagram).



THE PRECISION OF LEVEL CIRCUITS.

The precision of spirit leveling is expressed by the formula

Error of Closure = Constant V Length of Circuit

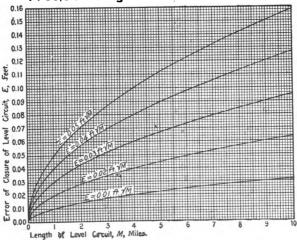
In the following Summery of practice in representative Surveys of the United States, E is the maximum limit of error of closure of a level circuit having a length of K kilometers or M miles.

Precision of Leveling in Representative Surveys.

MAXIMUM PERMISSIBLE ERROR OF CLOSURE. Metric Units. British Units. NAME OF SURVEY. 0.001 7. $E = 3mm\sqrt{K} = 0.012 \text{ ft/M}$ =0.01A.VM Chicago Sanitary District. $E = 3mm\sqrt{2K} = 0.018 \text{ ft.} \sqrt{M}$ Missouri River Commission. Mississippi River Commission. (1891). E= 3mm. VZK = 0.018 ft. VM = 0.02 ft VM Mississippi River Com'n (Before 1891). E= 5mm. VK = 0.021 ft. VM $E = 5mm\sqrt{2K} = 0.029 \text{ ft. } \sqrt{M} = 0.03 \text{ ft.} \sqrt{M}$ United States Coast Survey. E=10mm.VK = 0.042 ft. VM = 0.04 ft. VM United States Lake Survey. $0.050 \text{ ft.} \sqrt{M} = 0.05 \text{ ft.} \sqrt{M}$ United States Geological Survey.

A simple practical test of the degree of pracision attained in spirit fereling is found in the last column of the above rable. This graduated scale of pracision is given below graphically for distances to ten miles.

Precision Diagram for Level Circuits.



common usage, or in the proportion of the respective latitudes and departures, as would seem to be more consistent. If the several courses have not been surveyed with like precision, weights should be assigned in distributing the errors. Absurd refinement should be avoided in making the distribution of errors.

Leveling Errors.—Perhaps in no phase of surveying measurements is it more clearly established that accidental errors follow the law of square roots than in careful leveling. The precision diagrams are based on best current usage.

CHAPTER X.

METHODS OF COMPUTING.

Introduction.—To no one is the ability to make calculations accurately and rapidly of more value than to the engineer. Many fail to appreciate the value of rapid methods of calculation, and have no conception of the amount of time that can be saved by the skillful use of arithmetic, logarithms, reckoning tables and computing machines.

In the field the engineer has to depend upon the ordinary methods of arithmetic, or a table of logarithms for his results. The use of these aids should therefore receive special attention, for the engineer cannot afford to lose the time of his assistants while he makes unnecessary or extended computations.

In the office tables of squares, reckoning tables, slide rules and computing machines can be used in many cases with profit.

Consistent Accuracy.—It is safe to say that at least onethird of the time expended in making computations is wasted in trying to attain a higher degree of precision than the nature of the work requires.

In making arithmetical computations where decimals are involved it is a common practice to carry the result out to its farthest limit and then drop a few figures at random.

In using logarithms time and labor are lost by using tables that are more extensive than the data will warrant. The relative amount of work in using four, five, six and seven-place tables is about as 1, 2, 3 and 4. Besides the extra labor involved, the computer has a result that is liable to give him an erroneous idea of the accuracy of his work.

In making computations, in general, calculate the result to one more place than it is desired to retain.

If several numbers are multiplied or divided, a given percentage of error in any one of them will produce the same percentage of error in the result. In taking the mean of a series of quantities it is consistent to retain one more place than is retained in the quantities themselves.

In direct multiplication or division retain four places of significant figures in every factor for an accuracy of about one per cent; retain five places of significant figures in every factor for an accuracy of about one-tenth of one per cent.

LOGARITHMIC CALCULATIONS.

Logarithm Tables.—Logarithm tables contain the decimal part of the logarithm called the mantissa, the integral part called the characteristic is supplied by the computer.

Four-place tables give the mantissa to four decimal places of numbers from 1 to 999, and by interpolation give the mantissa of numbers from 1 to 9,999. Four-place logarithms should be used where four significant figures are sufficient, and should not be used where an accuracy greater than one-half of one per cent is required.

Five-place tables give the mantissa to five decimal places of numbers from 1 to 9,999, and by interpolation give the mantissa of numbers from 1 to 99,999. Five-place logarithms should be used where five significant figures are sufficient, and should not be used where an accuracy greater than one-twentieth of one per cent is required. Five-place tables are sufficiently accurate for most engineering work.

Six-place tables give the mantissa to six decimal places of numbers from 1 to 9,999, and by interpolation give the mantissa of numbers from 1 to 99,999, the same as the five-place tables. Six-place tables give practically no gain in precision over five-place tables since the same numbers of significant figures are given in both tables, and in addition the labor of using a six- instead of a five-place table is about as 3 to 2, due to interpolation with larger differences. For the above reasons five-place tables have been selected for use in this book as being the most suitable tables for use in surveying.

Seven-place tables give the mantissa to seven decimal places of numbers from 1 to 99,999, and by interpolation of numbers from 1 to 999,999. Seven place tables are rarely needed in engineering work, except in triangulation work where the angles are measured by repetition.

ARITHMETICAL CALCULATIONS.

Requirements.—To become a rapid computer the following requirements are essential:

- (1) A good memory for retaining certain standard numbers for reference.
- (2) The power of performing the ordinary simple arithmetical operations of multiplication, division, etc., on numbers with facility, quickness and accuracy.
- (3) The power of registration, i. e., of keeping a string of numbers in the mind and working accurately upon them.
- (4) The power of devising instantly the best method of performing a complicated problem as regards facility, quickness and certainty.

It is obvious that all do not have the ability to become rapid computers, but even these can become fairly skillful by constant practice and perseverance. The ordinary processes of arithmetic should be performed with numbers in all possible positions. No more figures should be put down than necessary, and all operations should be performed mentally whenever possible. In the mental part the results should alone be stated, much time being lost by repeating each separate figure.

Checks.—In order to check his work the computer should keep the following well known properties of numbers well fixed in his mind:

- (1). The sum or difference of two even or of two odd numbers is even.
- (2) The sum or difference of an even and odd number is odd.
 - (3) The product of two even numbers is even.
 - (4) The product of two odd numbers is odd.
- (5) The product of an even number and an odd number is even.
- (6) Checking results by the familiar operation of casting out the 9's depends upon the following properties of numbers:
- (a) A number divided by 9 leaves the same remainder as the sum of the digits divided by 9. For example:

$$4384 \div 9 = 487 + 1$$

 $(4+3+8+4) \div 9 = 2+1$

(b) The excess of 9's in the product equals the excess of 9's in the product of the excesses of the factors.

(c) The excess of 9's in the dividend equals the excess of 9's in the product of the excesses in the divisor and quotient, plus the excess in the remainder:

(7) Results should be checked by taking aliquot parts wherever possible, and by performing the operations in inverse order or performing inverse operations. Computations performed by means of logarithms should be checked by making the computations roughly by means of arithmetic. The probability of error should be recognized and precaution taken to verify results.

ADDITION.—Since the eye is accustomed to pass from left to right time can be saved, where the columns are not too long, by adding in the same way. The device of increasing or diminishing the numbers to make them multiples of ten and then subtracting or adding to the result is very convenient, especially where several columns are added at one time.

The mental work in detail is as follows: 100 + 47 = 147; 147 - 4 = 143; 143 + 70 = 213; 213 - 1 = 212; 212 + 30 + 90 = 332; 332 - 1 = 331; 331 + 50 = 381;

381 - 1 = 380.

Expert accountants use the method of adding columns in groups of 10, 20, 30, etc., small figures, indicating the number of the group, being placed along the column at intervals depending upon the computer. This method is well

adapted to the addition of long columns where one is liable to be called away from his work. The progress of the work being then shown by the number of the group, plus the excess.

MULTIPLICATION.—In order to make the best use of the methods given, the computer should have perfect command of the multiplication table as far as 20 at least.

(1) When the tens differ by unity and the sum of the units equals 10, numbers may be multiplied by the following rule: From the squares of the tens of the larger number subtract the square of the units of the larger number. For the numbers may be represented by (a + b) and (a-b), and the product will be $(a+b)(a-b)=a^2-b^2$.

Ex. 1.—
$$(93 \times 87) = 90^2 - 3^2 = 8,100 - 9 = 8,091$$
.

(2) The product of composite numbers is best obtained mentally by resolving them into their factors and taking the products of the factors.

Ex. 2.—
$$26 \times 36 = 9 \times 13 \times 8 = 936$$
.

Ex. 3.—
$$48 \times 24 = (24)^2 \times 2 = 1{,}152.$$

Multiples of 10.—To multiply by some number which is a factor of 10 or some multiple of 10, for example: Multi-

A by B, where
$$B = \frac{C10^n}{d}$$

Annex *n* ciphers to *A*, multiply by *C* and divide by *d*.

Ex. 1.-4,324
$$\times$$
 625 = 4,324 $\frac{5 \times 10^3}{8}$ = (4,324,000 \times 5) \div 8 = 2.702.500.

$$Ex. 2.-7,924 \times 25 = 792,400 \div 4 = 198,100.$$

Squaring Small Numbers.—Numbers may be squared mentally by the following rule: Add to or subtract from one factor enough to make its units figure zero. Subtract from or add to the other factor the same amount. Multiply together this sum and difference, and to the product add the square of the amount by which the factors were increased or diminished.

Proof.—
$$a^2 - b^2 = (a+b)(a-b)$$

 $a^2 = (a+b)(a-b) + b^2$.

Ex. 1.—
$$(76)^2 = (72 \times 80) + 4^2 = 5,776$$
.

Ex. 2.—
$$(127)^2 = (124 \times 130) + 3^2 = 16,129$$
.
Ex. 3.— $(6\frac{1}{4})^2 = (6 \times 6\frac{1}{2}) + (\frac{1}{4})^2 = 39\frac{1}{16}$.
Ex. 4.— $(6\frac{1}{2})^2 = (6 \times 7) + (\frac{1}{2})^2 = 42\frac{1}{4}$.

Ex. 5.—
$$(7.5)^2 = (7 \times 8) + (.5)^2 = 56.25$$
.

It will be seen that the process is very simple where the units place is 5.

(2) Having the square of any number the square of the number next higher is obtained by the following rule: To the known square add the number and the next higher and the result will be the square of the next higher number.

Ex. 6.—
$$(25)^2 = 625$$
. $(26)^2 = 625 + 25 + 26 = 676$.

(3) A very close approximation to the square of a quantity which is very near unity is obtained by adding algebraically two times the difference between the quantity and unity to the quantity.

Proof.—
$$(1 \pm b)^2 = 1 \pm 2b + b^2 = 1 \pm 2b$$
, (approximate).

Ex. 7.-
$$(1.05)^2 = 1 + 2(1.05 - 1) = 1 + 10 = 1.10$$
.

Ex. 8.-
$$(.94)^2 = 1 - 2(1 - .94) = 1 - .12 = 88$$
.

Ex.
$$9.-(2.034)^2 = 2^2(1+2\times.017) = 4(1.034) = 4.136$$
.

Cross-Multiplication.—This consists in taking the product of each digit in the multiplicand by each digit in the multiplier and taking the sums, products of the same denomination being determined thus: units \times units gives units; tens \times units and units \times tens gives tens; units \times hundreds, tens \times tens and hundreds \times units give hundreds etc. All products are added mentally, only the final result being put down.

Ex. 1.— $(2,347)^2$ =5,508,409 the final result being all that it is necessary to write down. The mental work is as follows, the figures in heavy type being figures in the product; $7 \times 7 = 49$; $4 + 2(7 \times 4) = 60$; $6 + 2(7 \times 3) + 4^2 = 64$; $6 + 2(2 \times 7) + 2(3 \times 4) = 58$; $5 + 2(2 \times 4) + 3^2 = 30$; $3 + 2(3 \times 2) = 15$; $1 + 2^2 = 5$.

Ex. 2.—The product of any two numbers may be found in the same manner.

The mental work is as follows: $3 \times 2 = 6$; $3 \times 3 + 8 \times 2 = 25$; $2+3\times4+8\times3+5\times2=48$; $4+3\times9+8\times4+5\times3+2\times2=82$; $8+8\times9+5\times4+2\times3=106$; $10+5\times9+2\times4=63$; $6+2\times9=24$.

Ex. 3.—The process of cross-multiplication may be simplified as follows: Required to multiply 4,328 by 736; write the multiplier on a slip of paper in inverse order and place it below the multiplicand with the left hand figure below the units place of the multiplicand thus:

Multiply together the figures in the same vertical column $6 \times 8 = 48$; set down the 8 and carry the 4; then move the slip one space to the left thus:

Multiplying together the figures in the same vertical columns and taking the sum, $4+6\times2+3\times8=40$; set down the 0 and carry the 4; then move the slip one space to the left, multiplying together the figures in the same vertical columns, adding, etc., we will finally have the work standing thus:

Removing the slip we have

The multiplier may be written on the bottom of a sheet in inverse order and placed above the multiplicand instead as above described. The work, however, is very much simplified by simply writing the multiplier in inverse order without using the slip:

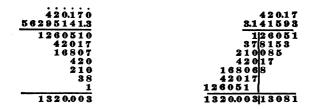
The mental work being as follows: $6 \times 8 = 48$; $4 + 6 \times 2 + 3 \times 8 = 40$; $4 + 6 \times 3 + 2 \times 3 + 7 \times 8 = 84$; $8 + 6 \times 4 + 3 \times 3 + 7 \times 2 = 55$; $5 + 3 \times 4 + 7 \times 3 = 38$; $3 + 7 \times 4 = 31$. It will be seen that this device removes most of the mental strain, there being no cross-products.

CONTRACTED MULTIPLICATION.—In multiplying decimals, when the product is required to a few places of decimals, the work may be shortened as follows: Required a product correct to the nth decimal place. Write the multiplier with its figures in reverse order, its units place under the nth decimal place of the multiplicand. Multiply the multiplicand by the figures in the multiplier, beginning with the right hand figure; rejecting those figures in the multiplicand which are to the right of the figure used as a multiplier, increasing each product by as many units as would have been carried from the rejected part of the multiplicand, taking the nearest unit in each case; place the right hand figure of each partial product in the same column, and add as in common multiplication.

In most cases it is best to compute one more place than required. The following examples illustrate the process:

Ex. 1.—The radius of a circle is 420.17 ft. What is its semicircumference to nearest 0.01 ft.? ($\pi = 3.14159265$.)

In the work below the partial products in the contracted multiplication are seen to correspond to the partials of the common method, taken in reverse order, the part to the right of the vertical line being rejected. The contracted multiplication is carried one more place than required. A dot is placed above each figure when it is rejected from the multiplicand.



Ex. 2.—The observed length of a line is 2231.63 ft. with a tape having a length of 100.018 ft. Required the reduced length of the line to the nearest 0.01 ft.

Noting that each foot of the tape = 1.00018 ft.

2 2 3 1.6 3	• 2 2 3 1.6 3
<u>81000.1</u>	1.00018
223163	1785304
2 2	2 2 3 1 6 3
18	223163000
2 2 3 2.0 3	2 2 3 2.0 3 1 6 9 3 4

Ex. 3.—Same observed length with a tape 99.982 ft. long. Required the reduced length.

Each foot of the tape = 0.99982 = (1 - 0.00018) ft.

Ex. 4.—To compare contracted multiplication with logarithmic work, calculate 861.3 ft. $\times \sin 17^{\circ}$ 19' to the nearest 0.1 ft.

861.3	$\log .861.3 = 2.93515$
56792.0	log. sin 17° 19′ = 9.4 7 3 7 1
1723	$\log. (256.4) = 2.40886$
776	
60	
5	
2 5 6.4	

contracted desired correct to the nth decimal place, the following method may be used: Find one-half of the desired figures in the quotient in the usual way and do not bring down a figure for the last remainder. Drop a figure from the right of the divisor and find another figure in the quotient. Then without bringing down any more figures continue to discard figures from the divisor until the required places are obtained.

Ex 1.—Divide 443.9425 by 24.311 to nearest hundredth. There will be four figures in the quotient, so we will find

the first two in the ordinary way. A dot is placed over each figure in the divisor when it is rejected.

Divisor Near Unity.—When the divisor is near unity a very close approximation is given by the method shown in the following problems:

Ex. 1.
$$-\frac{5}{1.003254}$$
 = 5(1 - .003254) = 5 × .996746 = 4.98373 correct to within one unit in the fifth place.

Ex. 2.
$$\frac{7}{.9982} = 7(1 + (1 - .9982)) = 7 \times 1.0018 = 7.0126$$
 correct to the last place.

CONTRACTED SQUARE ROOT.—A result correct to a required number of decimal places may be found by a process similar to the method employed for contracted division.

Ex. 1.—Required the square root of 12,598.87325 correct to thousandths. We see by inspection that the root will contain six figures. Find in the ordinary way the first three figures. Form a new trial divisor in the usual way,

and bring down only one figure for the dividend in place of two. Find the remaining figures by contracted division.

The last figure brought down is not increased whatever it may be followed by, since the contracted process tends to make the result a little too large. This method may be applied to the extraction of cube roots, where it saves much work in finding long trial divisors.

square Root of Small Numbers.—The approximate square roots of small numbers may be found by means of the following rule: Divide the given number by the number whose square is nearest the given number. The arithmetical mean of the quotient and divisor will be the approximate square root of the number. The nearer the number is to a perfect square the less the error. For example,

Ex.
$$1.-\sqrt{35} = (3\frac{5}{6} + 6) \div 2 = 5.92$$
.

Ex. $2.-\sqrt{8} = (\frac{9}{6} + 3) \div 2 = 2.83$.

Ex. $3.-\sqrt{79} = (\frac{79}{6} + 9) \div 2 = 8.89$.

Ex. $4.-\sqrt{128} = (\frac{129}{11} + 11) \div 2 = 11.31$

Square Root by Subtraction.—While it possesses not points of merit in this connection, it would not be proper to pass the subject of square root without presenting the novel method of extracting square roots used with the Thomas Computing machine. The method depends upon the relation existing between odd numbers and squares in the system of numbers having a radix ten. If we sum up the odd numbers, beginning at 1, we will observe the following relation:

 $1=1^2$; $1+3=4=2^2$; $1+3+5=9=3^2$; $1+3+5+7=16=4^2$, etc. It will be seen that the square root of the sum in each case is the number of the group.

The method of extracting square roots is as follows: Point off in periods of two figures each. Subtract from the left hand period the odd numbers in order, beginning at unity, until a remainder is obtained less than the next odd number. Write for the first figure in the root the number which represents the number of subtractions made. Double the root already found and annex unity. Subtract as before, using for subtrahends the successive odd numbers, the root figure being the number of subtractions made.

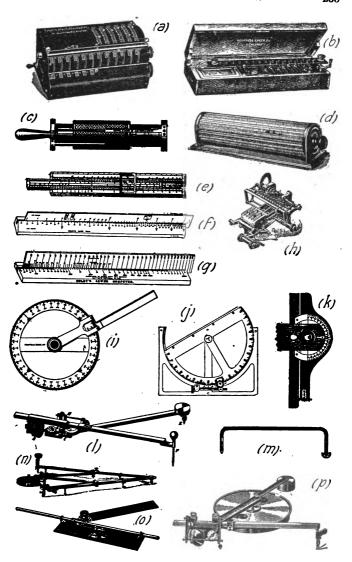
Ex. 1.—Extract the square root of 53,824.

	53824(232 1
_	4 32 subtractions.
41)	138
	97 43 54
4 6	453 subtractions. 1)924 461
	463 4632 subtractions.

RECKONING TABLES.—Tables for use in computing are so numerous and well known that it would be useless to try to refer to them by name. Two valuable tables for obtaining products of numbers—which are well known in Germany, but comparatively unknown in this country—are, "Crelle's Rechentafeln," which gives the products of numbers of three significant figures by three significant figures to 999 by 999; and "Zimmerman's Rechentafeln," which gives the products of numbers of two places of significant figures by numbers of three significant figures to 100 by 999.

computing machine; (b) a Thomas computing machine; (c) a Fuller slide rule; (d) a Thacher slide rule; (e) an ordinary slide rule; (f) a Colby Stadia slide rule; (g) a Colby sewer slide rule; (h) a Grant calculating machine; (i) a full circle protractor; (j) a Crozet protractor; (k) a protractor tee square; (l) a polar planimeter; (m) a "jack knife" planimeter; (n) a pantagraph; (o) a section liner; (p) a spherical planimeter.

In using the "jack knife" planimeter, the point is placed at the center of gravity, and the knife edge is placed on a line passing through the center of gravity of the figure. The point is then made to traverse the perimeter of the figure to be measured; passing out to the perimeter and returning to the center of gravity of the figure on the same line. The distance from the final position of the knife edge to the line through the center of gravity, multiplied by the



length of the arm of the planimeter will give the area of the figure. The arm of the planimeter is usually made ten inches long and the distance measured in inches.

The correct area may be obtained by means of the hatchet planimeter, without using the center of gravity of the figure, as follows: (1) Draw a tangent to the figure. (2) Trace the figure with the point starting with the hatchet on the tangent and the point at the point of tangency. (3) Trace the figure as before except that the point is to move around in the opposite direction. (4) The arithmetical mean of the two areas will be the true area. That this method is correct can be easily proved by the student.

The other machines are described in the instructions ac-

companying them when purchased,

CHAPTER XI.

TOPOGRAPHIC DRAWING AND LETTERING.

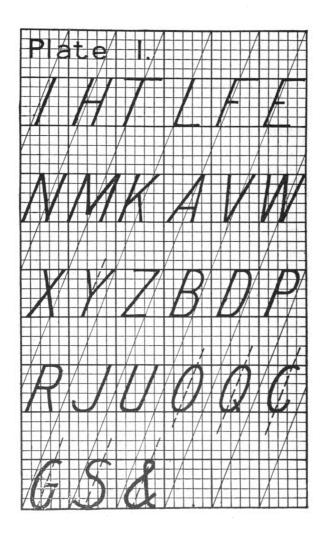
LETTERING.—A magnified scale is used in the first six plates to give familiarity with form of letter and numeral, and also to produce freedom of hand motion. The six plates should first be made with a soft pencil sharpened to a needle point, and afterward with pen and india ink. In Plate 7 the height of letter is that prescribed in Chapter I. This standard size is not only well adapted to field notes and general drafting, but is economical of execution.

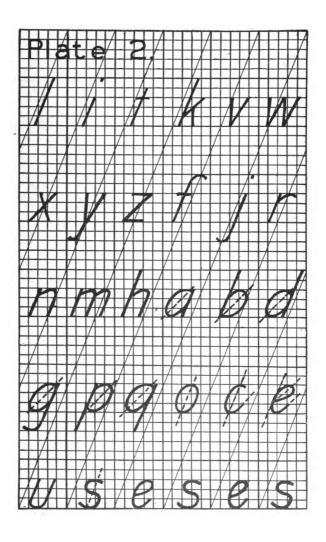
The student should train the eye and acquire a "swing" of the hand by industrious practice in such exercises as the following: (1) Pass a line freehand through two points; first sketch in the line roughly by a free swing of the forearm; then partially erase and retrace; finally test result with ruler. (2) Pass a circular arc through three points freehand; follow sketch method just described and, after perfecting the arc, sketch in the chords and locate the center freehand; test result mechanically. (3) Inscribe a circle in a square. (4) Inscribe an ellipse in a rectangle. (5) Inscribe an ellipse in an oblique parallelogram. (In the last three exercises give particular attention to points and lines of tangency and axes of symmetry.) After making the line or figure satisfactorily with pencil, it should be executed freehand in India ink.

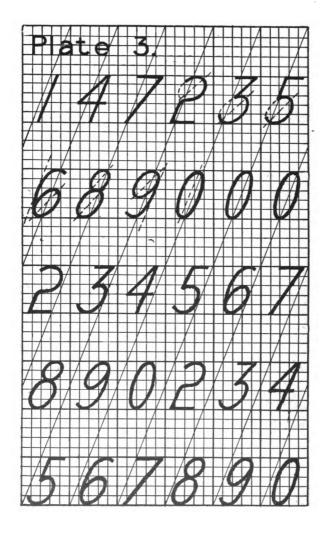
Practice should include spacing of letters and words, and for this purpose it is suggested that the student use the "specifications for a good engineer" following the preface.

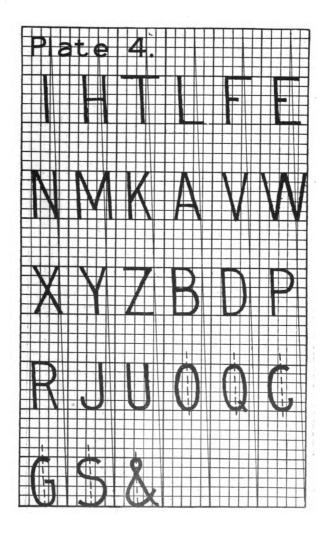
The student should not be content until he can make letters freehand so well that a close inspection is required to determine that they were not made mechanically.

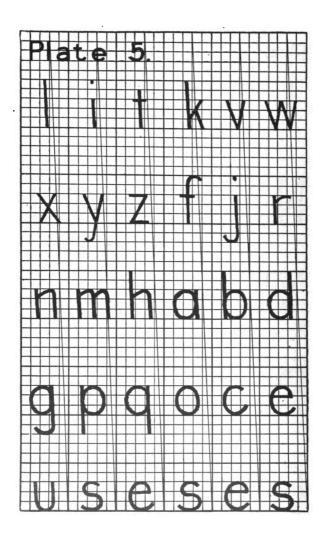
Freehand Titles.—Good freehand titles suffice for most drawings. In a good title consistent emphasis is given to the several parts, and the title as a whole accords with the purpose and character of the drawing. Elaborate and ornamental titles have a limited application, and should not be attempted at all unless the draftsman has special skill

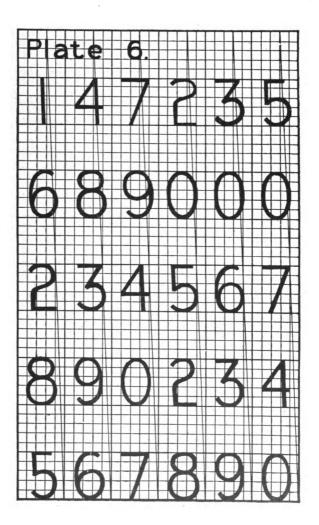








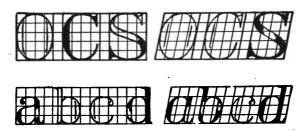




244 TOPOGRAPHIC DRAWING AND LETTERING.

late ABCDEFEGHTUKLMMOPQR57W ABCDEFGH/JKLMWOPQR5TWX ABCDEFGHIJKUMNOPQR5TWY abode f ghijk/mnopgrstuv abcdefghiik/mnopgrstuw abcdefghi/ik/mnoparstuy 1234567890212345678902 234567890&1/234567890& ABCDEFGHIJKLMNOPORSTUV ABCDEFGHIJKLMNOPORSTWX ABCDEFGHIDKLMNOPQRSTYZ abcdefahijklmhoparstuv abcdefiahijklimhoparstuv a b c d e f g h i i k l m n o p a r s t w y 11234567890&11234567890& 1734567890&1734567890& 1234567890&1234567890&

in such work. In designing titles, whether freehand or mechanical, skill in sketching in the outlines, guide lines, axes of symmetry, etc., is of much importance. On the following pages are a few examples of good titles.



DRAWING PENS.—The following pens, arranged in order of fineness, will give sufficient variety for ordinary work.

Gillott's 170, very fine, for very small lettering.

Gillott's 303, extra fine, for small lettering.

Gillott's 404, fine, for small lettering.

Hunt 21, medium, for ordinary lettering.

Hunt 512, Shot Point, for ordinary lettering.

Leonardt 510, E. F. Ball Point, for large lettering and titles.

Hunt 513, Round Point, for large lettering and titles.

Leonardt 516, E. F. Ball Point, for large lettering and titles.

Leonardt 516 F., Ball Point, for very large lettering and titles.

Payzant Pens, K. & E. Co., Nos. 6, 5, 4, 3, 2, 1, for titles. The following rules should be observed in making letters on drawings free hand.

Use the quill in inking the pen.

Never dip the pen in the ink bottle.

Keep the pen clean.

Ink must not be allowed to dry on the pen and spread the points.

Before using a new pen moisten the points and wipe it dry to insure a free flow of ink.

TOPOGRAPHIC SYMBOLS.—The standard symbols for topographic drawings adopted by the American Railway Engineering Association are given on pages 248 to 251.

RIGHT-OF-WAY MAP NEW YORK AND DENVER R.R.

Station 331+55 to Station 542+75 Scale 1 in =400 ft. January 3, 1915 Office of Chief Engineer Denver, Colorado.

RIGHT-OF-WAY MAP NEW YORK AND DENVER R.R.

Station 331+55 to Station 511+10
Scale 1 in =400 ft. January 30, 1915
Office of Chief Engineer
Denver, Colorado.

TOPOGRAPHIC MAP OF THE CITY OF BOULDER, COLORADO

Surveyed by the CLASS IN TOPOGRAPHIC SURVEYING UNIVERSITY OF COLORADO FIRST SEMESTER 1914-15
Scale 1 in = 500 ft.

RIGHT-OF-WAYMAP NEW YORK AND DENVER R.R.

Station 331+55 to Station 542+75 Scale 1 in = 400 ft. January 3,1915 Office of Chief Engineer Denver, Colorado.

Right-of-Way Map New York & Denver R.R.

Station 331+55 to Station 511+10
Scale 1 in = 400ft. January 1,1915
Office of Chief Engineer
Denver, Colorado.

Topographic Map

CITY OF BOULDER, COLORADO

Surveyed by the Class in Topographic Surveying University of Colorado First Semester 1914-15 Scale Lin=508t.

HYDROGRAPHY.

	\
Stream	WEARING TO SE
Springs and Sinks	
Lakes and Ponds	
Falls and Rapids	NAME
Water Line	
Marsh	
Canals	Name Lock
Ditches	Size
RELIEF	.
Contour System	
Sand	all trans
Cliffs	
Cut	
Embankment	

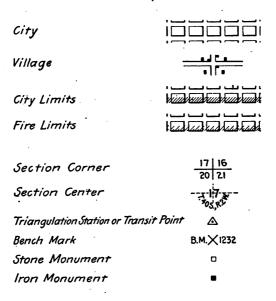
Top of Slope Bottom of Slope

* RAILWAYS (TOPOGRAPHICAL MAPS.)

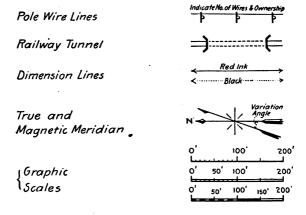
Steam	
Electric	
Street Railways	
* RAILWAY TRACKS (TRA	ACK MAPS.)
Railway Track or Old Track to Remain	
Old Track to be Taken up	
Proposed Tracks	Red
Proposed (Future) Tracks	Red
Foreign Tracks	Color other than Red or Black with Initials of Road
Alinement { 4°Curve to Right } 2° = Left }	4°CR. 2°C.L
Boundary and Surve	Y LINES.
Spolitical Divisions , State, County or Township Lines.	Bethel Twp Wayne Ca, Mich. Posey TwpAdams Ca, Ind.
{ Government Surveys, Base, Meridian, Township, Section or Harbor Line	Sec. 18. T. 12N., R. 1E., 3rd PM. Sec. 13. T. 11N., R. 1E., 3rd PM.
Street, Block or other Property Line	•
Survey Lines	Red Preliminary Location
Center Lines	Original (Tracker)Center Line 19 If Monumented, Show Location and Proper Symbol
Company Property Line	
Fence (on Street Line)	State Kind and Height
Fence (on Company Property Line)	State Kind and Height

₩ For Roilway Track and Yard Studies Use Single or Double Lines.

250 TOPOGRAPHIC DRAWING AND LETTERING.



MISCELLANEOUS.



CULVERTS, SEWERS, ETC.

COLVERTS, SEWE	NS, ETC.
Masonry Arch or Flat Top Culvert	<u>}</u>
Pipe or Wood Box Culvert or Drain	(State Kind and Length and Kind of Walls, if any.)
Catch Basin	
Manhole	О м.н.
Sump	Sump
WATER SUPPLY AND P	PE LINES.
Water Tank	Give Character, Diam & Height
Water Column	Give Size
Track Pan	
Company Water Pipe	Give Size
Other Water Pipe	
Steam or Gas	Give Size
Compressed Air	Give Size
HIGHWAYS AND CROS	5\$1NG5.
Public and Main Roads	
Private and Secondary Roads	========
Trails	
Street and Public Road Crossings	-////-
Private Road Crossing	
BRIDGES.	
Girder	\rightarrow
Truss	
Trestle	

• . •

SURVEYING MANUAL

PART II

FIELD AND OFFICE TABLES FOR USE IN SURVEYING.

BY

WILLIAM D. PENCE

AND

MILO S. KETCHUM

- Table 1. Logarithms of Numbers.
- Table 2. Logarithmic Functions of Angles.
- Table 3. Natural Functions of Angles.
- Table 4. Squares, Cubes, Square Roots, Cube Roots and Circles.
 - Table 5. Trigonometric Functions.

Explanation of Tables.

The authors wish to thank the J. B. Lippincott Company for the use of Tables 1 and 2 taken from Suplee's "Five Place Logarithms," and Table 3 taken from Suplee's "Mechanical Engineers' Reference Book"; and the McGraw-Hill Book Company for the use of Tables 4 and 5, taken from Harger and Bonney's "Highway Engineers' Handbook."

All of the above tables are fully protected by copyright.

Num. 140 to 179. Log. 146 to 255.

N	L	0	1	2	3	4	5	6	7	8	9	P. P.
140	14	613	644	675	706	737	768	799	829	860	891	34 33
141		922	953	983	*014	*045	*076	*106	*137	*168	*198	1 3.4 3.3
142	15	229	259	290	320	351	381	412	442	473	503	2 6.8 6.6
143		534	564	594	625	655	685	715	746	776	806	3 10.2 9.9
144		836	866	897	927	957	987	*017	*047	* 077	*107	4 13.6 13.2 5 17.0 16.5
145	16	137	167	197	227	256	286	316	346	376	406	6 20.4 19.8 7 23.8 23.1
146		435	465	495	524	554	584	613	643	673	702	8 27.2 26.4
147		732	761	791	820	850	879	909	938	967	997	9 30.6 29.7
148	17	026	056	085	114	143	173	202	231	260	289	32 31
149		319	348	377	406	435	464	493	522	551	580	1 3.2 3.1
150		609	638	667	696	725	754	782	811	840	869	2 6.4 6.2
151		898	926	955	984	* 013	*041	*070	*099	*127	*156	3 9.6 9.3
152	18	184	213	241	270	298	327	355	384	412	441	4 12.8 12.4 5 16.0 15.5
153		469	498	526	554	583	611	639	667	696	724	6 19.2 18.6
154		752	780	808	837	865	893	921	949	977	*005	7 22.4 21.7 8 25.6 24.8
155	19	033	061	089	117	145	173	201	229	257	285	9 28.8 27.9
156		312	340	368	396	424	451	479	507	535	562	30 29
157		590	618	645	673	700	728	756	783	811	838	
158		866	893	921	948	976	*003	*030	*058	*085	* 112	1 3.0 2.9
159	20	140	167	194	222	249	276	303	330	358	385	2 6.0 5.8 3 9.0 8.7
160		412	439	466	493	520	548	575	602	629	656	4 12.0 11.6 5 15.0 14.5
161		683	710	737	763	790	817	844	871	898	925	6 18.0 17.4
162		952	978	*005		*059	*085		*139	*165	*192	7 21.0 20.3
163	21	219	245	272	299	325	352	378	405	431	458	8 24.0 23.2 9 27.0 26.1
164		484	511	537	564	590	617	643	669	696	722	28 27
165		748	775	801	827	854	880	906	932	958	985	
166	22	011	037	063	089	115	141	167	194	220	246	1 2.8 2.7
167		272	298	324	350	376	401	427	453	479	505	2 5.6 5.4 3 8.4 8.1
168		531	557	583	608	634	660	686	712	737	76 3	4 11.2 10.8
169		789	814	840	866	891	917	943	968	994	*019	5 14.0 13.5 6 16.8 16.2
170	23	045	070	096	121	147	172	198	223	249	274	7 19.6 18.9
171		300	325	350	376	401	426	452	477	502	528	8 22.4 21.6 9 25.2 24.3
172		553	578	603	629	654	679	704	729	754	779	3 20.2 24.3
173		805	830	855	880	905	930	955	980	*005	*030	26 25
174	.24	055	080	105	130	155	180	204	229	254	279	1 2.6 2.5
175		304	329	353	378	403	428	452	477	502	527	2 5.2 5.0 3 7.8 7.5
176		551	576	601	625	650	674	699	724	748	773	4 10.4 10.0
177		797	822	846	871	895	920	944	969		*018	5 13.0 12.5 6 15.6 15.0
178	25	042	066	091	115	139	164	188	212	237	261	6 15.6 15.0 7 18.2 17.5
179		285	310	334	358	382	406	431	455	479	503	8 20.8 20.0
180		527	551	575	600	624	648	672	696	720	744	9 23.4 22.5
N	L	0	1	2	3	4	5	6	7	8	9	P. P.

Num. 180 to 219. Log. 255 to 342.

N	L	0	1	2	3	4	5	6	.7	8	9	P	. Р	•
180	25	527	551	575	600	624	648	672	696	720	744		2	4
181		768	792	816	840	864	888	912	935	959	983	1	2.	
182	26	007	031	055	079	102	126	150	174	198	221	2		8
183		245	269	293	316	340	364	387	411	435	458	3	7.	.ž
184		482	505	529	553	576	600	623	647	670	694	5	9 12	
185		717	741	764	788	811	834	858	881	905	928	6	14.	.4
186		951	975	988	*021	*045	*068	*091	*114	*138	*161	8	16 19	
187	27	184	207	231	254	277	300	323	346	370	393	ğ	21.	
188		416	439	462	485	508	531	554	577	600	623	ł	•	•
189		646	669	692	715	738	761	784	807	830	852		2	
190		875	898	921	944	967	989	*012	*035	*058	*081	1 2		.3 .6
191	28	103	126	149	171	194	217	240	262	285	307	3	6.	.9
192		330	353	375	398	421	443	466	488	511	533	4	9.	.2
193		556	578	601	623	646	668	691	713	735	758	5	11. 13.	
194		780	803	825	847	870	892	914	937	959	981	7	16.	.1
195	29	003	026	048	070	092	115	137	159	181	203	8	18. 20.	
196		226	248	270	292	314	336	358	380	403	425	1		_
197		447	469	491	513	535	557	579	601	623	645		2	2
198		667	688	710	732	754	776	798	820	842	863	1		.2
199		885	907	929	951	97 3	994	*016	*0 38	*060	*081	3	6.	
200	30	103	125	146	168	190	211	233	255	276	298	5	8. 11.	
201		320	341	363	384	406	428	449	471	492	514	6	13.	.2
202		535	557	578	600	621	' 643	664	685	707	728	7	15	
203		750	771	792	814	835	856	878	899	920	942	8 9	17. 19.	.o .8
204		963	984	*006	*027	*048	*069	*091	*112	*133	*154		2	
205	31	175	197	218	239	260	281	302	323	345	366			
206		387	408	429	450	471	492	513	534	555	576	1	2.	.1
207		597	618	639	660	681	702	723	744	765	785	3	6.	.2
208		806	827	848	869	890	911	931	952	973	994	4	8.	.4
209	32	015	035	056	077	098	118	139	160	181	201	5	10. 12.	
210		222	243	263	284	305	325	346	366	387	408	7	14.	.7
211		428	449	469	490	510	531	552	572	593	613	8	16. 18.	
212		634	654	675	695	715	736	756	777	797	818		10.	. 0
213		838	858	879	899	919	940	960	980	*001	*021	:	20	19
214	33	041	062	082	102	122	143	163	183	203	224	1 :	2.0	1.9
215		244	264	284	304	325	345	365	385	405	425	2 4	1.0 5.0	3.8 5.7
216		445	465	486	506	526	546	566	586	606	626	4	3.0 3.0	7.6
217		646	666	686	706	726	746	766	786	806	826	5 10	0.0	9.5
218		846	866	885	905	925	945	965	985	*005		6 1	2.0 1.0	$11.4 \\ 13.3$
219	34	044	064	084	104	124	143	163	183	203	223	8 1	6.0	15.2
220		242	262	282	301	321	341	361	380	400	420	9 1	5.0	17.1
N	L	0	1	2	3	4	5	6	7	8	9	D	. Р	

Num. 220 to 259. Log. 342 to 414.

220 221 222 223 224 225 226 227 228 229 230	34	242 439	262										
222 223 224 225 226 227 228 229		439		282	301	321	341	361	380	400	420		
223 224 225 226 227 228 229			459	479	498	518	537	557	577	596	616		20
224 225 226 227 228 229		635	655	674	694	713	733	753	772	792	811	1	2.0
225 226 227 228 229		830	850	869	889	908	928	947	967	986	*005	3	4.0
226 227 228 229	35	025	044	064	083	102	122	141	160	180	199	4	6.0 8.0
227 228 229		218	238	257	276	295	315	334	353	372	392	5 6	10.0 12.0
228 229		411	430	449	468	488	507	526	545	564	583	7	14.0
229		603	622	641	660	679	698	717	736	755	774	8	16.0
		793	813	832	851	870	889	908	927	946	965	9	18.0
230		984	*003	*021	*040	*059	*078	*097	*116	*1 35	*154		
	36	173	192	211	229	248	267	286	305	324	342		40
231		361	380	399	418	436	455	474	493	511	530		19
232		549	568	586	605	624	642	661	680	698	717	1	1.9
233		736	754	773	791	810	829	847	866	884	903	2	3.8
234		922	940	959	977	996	*014	*033	*051	* 070	*088	3 4	5.7 7.6
235	37	107	125	144	162	181	199	218	236	254	273	5 6	9.5 11.4
236		291	310	328	346	365	383	401	420	438	457	7	13.3
237		475	493	511	530	548	566	585	603	621	639	8	15.2
238		658	676	694	712	731	749	767	785	803	822	"	17.1
239		840	858	876	894	912	931	949	967	985	*003		
240	38	021	039	057	075	093	112	130	148	166	184		
241		202	220	238	256	274	292	310	328	346	364		18
242		382	399	417	435	453	471	489	507	525	543		
243		561	578	596	614	632	650	668	686	703	721	1	1.8 3.6
244		739	757	775	792	810	828	846	863	881	899	3	5.4
245		917	934	952	970	987	*005	*023	*041	*058	*076	4 5	7.2 9.0
246	39	094	111	129	146	164	182	199	217	235	252	6	10.8
247		270	287	305	322	340	358	375	393	410	428	7	12.6
248		445	463	480	498	515	533	550	568	585	602	8	14.4 16.2
249		620	637	655	672	690	707	724	742	759	777	"	
250		794	811	829	846	863	881	898	915	933	950		
- 251		967	985	*002	*019	*037	*054	*071	*088	*106	*123		
252	40	140	157	175	192	209	226	243	261	278	295		
253		312	329	346	364	381	398	415	432	449	466		17
254		483	500	518	535	552	569	586	603	620	637	1	1.7
255		654	671	688	705	722	739	756	773	790	807	2 3	3.4 5.1
256		824	841	858	875	892	909	926	943	960	976	4	6.8
257		993	*010	*027	*044	*061	*078	*095	*111	*128	*145	5 6	$\begin{array}{c} 8.5 \\ 10.2 \end{array}$
258	41	162	179	196	212	229	246	263	280	296	313	7	11.9
259		330	347	363	380	397	414	430	447	464	481	8	13.6
260		497	514	531	547	564	581	597	614	631	647	9	15.3
N	L	0	1	2	3	4	5	6	7		9	P	. P.

Num. 260 to 299. Log. 414 to 476.

N	L	0	1	2	3	4	5	6	7	8	9	P	. Р.
260	41	497	514	531	547	564	581	597	614	631	647		
261		664	681	697	714	731	747	764	780	797	814		
262		830	847	863	880	896	913	929	946	963	979	1	
263		996	*012	*029	*045	*062	*078	*095	*111	*127	144		
264	42	160	177	193	210	226	243	259	275	292	308	ļ	17
265		325	341	357	374	390	406	423	439	455	472	1	1.7
266		488	504	521	537	553	570	586	602	619	635	2 3	3.4
267		651	667	684	700	716	732	749	765	781	797		5.1
268		813	830	846	862	878	894	911	927	94 3	9 59	5	6.8 8.5
269		975	991	*008	*024	*040	*056	*072	*0 88	*104	*120	6	10.2
270	43	136	152	169	185	201	217	233	249	265	281	6 7 8	11.9 13.6
271		297	313	329	345	361	377	393	409	425	441	9	15.3
272		457	473	489	505	521	537	553	569	584	600	ŀ	
273		616	632	648	664	680	696	712	727	743	759	1	
274		775	791	807	823	838	854	870	886	902	917		
275		933	949	965	981	996	*012	*028	*044	*059	* 075	1	
276	44	091	107	122	138	154	170	185	201	217	232		16
277		248	264	279	295	311	326	342	358	373	389	ł	10
278		404	420	436	451	467	483	498	514	529	545	1	1.6
279		560	576	592	607	623	638	654	669	685	700	3	3.2 4.8
280		716	731	747	762	778	793	809	824	840	855	5	6.4 8.0
281		871	886	902	917	932	948	963	979		*010	6	9.6
282	45	025	040	056	071	086	102	117	133	148	163	7	11.2
283		179	194	209	225	240	255	271	286	301	317	8	12.8 14.4
284		332	347	362	378	393	408	423	439	454	469	-	,
285		484	500	515	530	54 5	561	576	591	606	621	1	
286		637	652	667	682	697	712	728	743	758	773		
287		788	803	818	834	849	864	879	894	909	924		
288		939	954	969	984	*000	*015	*030	*04 5	*060	* 075		
289	46	090	105	120	135	150	165	180	195	210	225		15
290		240	255	270	285	300	315	330	345	359	374	1	1.5
291		389	404	419	434	449	464	479	494	509	523	3	3.0 4.5
292		538	553	568	583	59 8	613	627	642	657	672	4	6.0
293		687	702	716	731	74 6	761	776	790	805	820	5	7.5
294		835	850	864	879	894	909	923	938	953	967	6 7	9.0 10.5
295		982		*012			1	*070				8 9	12.0 13.5
296	47	129	144	159	173	188	202	217	232	246	261	_	,
297		276	290	305	319	334	349	363	378	392	407		
298		422	436	451	465	480	494	509	524	538	553		
299		567	582	596	611	625	640	654	669	683	698		
300		712	727	741	756	770	784	799	813	828	842		
N	L	0	1	2	3	4	5	6	7	8	9	P	. P.

Num. 300 to 339. Log. 477 to 531.

N	L	0	1	2	3.	4	5	6	7	8	9	P	. Р.
300	47	712	727	741	756	770	784	799	813	828	842		
301		857	871	885	900	914	929	943	958	972	986		
302	48	001	015	029	044	058	073	087	101	116	130	İ	
303		144	159	173	187	202	216	230	244	259	273		
304		287	302	316	830	344	359	373	387	401	416		
305		430		458	473							İ	14
306		572	444			487	501	515	530	544	558.	1	1.4
			586	601	615	629	643	657	671	686		2	2.8
307		714	728	742	756	770	785	799	813	827	841	3 4	4.2 5.6
308		855	869	883	897	911	926	940	954	968	982	5	7.0
309		996	*010	*024	*038	*052	*066	* 080	*094	*108	*122	6	8.4
310	49	136	150	164	178	192	206	220	234	248	262	8	9.8 11.2
311		276	290	304	318	332	346	360	374	388	402	9	12.6
312		415	429	443	457	471	485	499	513	527	541		
313		554	568	582	596	610	624	638	651	665	679		
314		693	707	721	734	748	762	776	790	803	817		
315		831	845	85 9	872	886	900	914	927	941	955		
316		969	9 82	996	*010	*024	*037	*051	*065	*079	*092		13
817	50	106	120	133	147	161	174	188	202	215	229		13
318		243	256	270	284	297	311	325	338	352	365	1	1.3
319		379	393	406	420	433	447	461	474	488	501	3	2.6 3.9
320		515	529	542	556	569	583	596	610	623	637	5	5.2 6.5
321		651	664	678	691	705	718	732	745	759	772	6	7.8
322		786	799	813	826	840	853	866	880	8 9 3	907	7	9.1
323		920	934	947	961	974	987	*001	*014	*028	*041	8	10.4 11.7
324	51	055	068	081	095	108	121	135	148	162	175	"	11.0
325		188	202	215	228	242	255	268	282	295	308		
326		322	335	348	362	375	388	402	415	428	441		
327		455	468	481	. 495	508	521	534	548	561	574		
328		587	601	614	627	640	654	667	680	693	706		
329		720	733	746	759	772	786	799	812	825	838	l	12
330		851	865	878	891	904	917	930	943	957	970	1	1.2
331		983	996	*009	*022	*035		*061	*075			2	2.4
332	52	114	127	140	153	166	179	192	205	218	231	3	3.6
333		244	257	270	284	297	310	323	336	349	362	4 5	4.8 6.0
334		375	388	401	414	427	440	453	466	479	492	6	7.2
335		504	517	530	543	556	569	582	595	608	621	8	8.4 9.6
336		634	647	660	673	686	699	711	724	737	750	9	10.8
337		763	776	789	802	815	827	840	853	866	879	l	
338		892	905	917	930	943	956	969	982		*007	l	
339	53	020	033	046	058	071	084	097	110	122	135		
340		148	161	173	186	199	212	224	237	250	263		
												<u> </u>	
N	L	0	1	2	3	4	5	6	7	8	9	P	. P.

Num. 340 to 379. Log. 531 to 579.

N	L	0	1	2	3	4	5	6	7	8	9	P	. Р.
340	53	148	161	173	186	199	212	224	237	250	263		
341		275	288	301	314	326	339	352	364	377	390		
342		403	415	428	441	453	466	479	491	504	517	İ	
343		529	542	555	567	580	593	605	618	631	643		
344		656	668	681	694	706	719	732	744	757	769	1	
845		782	794	807	820	832	845	857	870	882	895		13
346	•	908	920	933	945	958	970	983		*008		1	1.3
347	54	033	045	058	070	083	095	108	120	133	145	3	2.6 3.9
348	0.	158	170	183	195	208	220	233	245	258	270	4	5.2
349		283	295	307	320	332	345	357	370	382	394	5 6	6.5 7.8
350		407	419	432	444	456	469	481	494	506	518	7	9.1
351		531	543	555	568	580	593	605	617	630	642	8	10.4 11.7
352		654	667	679	691	704	716	728	741	753	765	"	
353		777	790	802	814	827	839	851	864	876	888		•
354		900	913	925	937	949	962	974	986		*011		
i							l						
355	Ş 5	023	035	047	060	072	084	096	108	121	133		
356		145	157	169	182	194	206	218	230	242	255	l	12
357		267	279	291	303	315	328	340	352	364	376	ŀ	
358		388	400	413	425	437	449	461	473	485	497	1	1.2
359		509	522	534	546	558	570	582	594	606	618	3	2.4 3.6
360		630	642	654	666	678	691	703	715	727	739	5	4.8 6.0
361		751	763	775	787	799	811	823	835	847	859	6	7.2
362		871	883	895	907	919	931	943	9 55	967	979	7	8.4
363								*062		*086		8	9.6 10.8
364	56	110	122	134	146	158	170	182	194	205	217	ا ا	10.0
365		229	241	253	265	277	289	301	312	324	336		
366		348	360	372	384	396	407	419	431	443	455		
367		467	478	490	502	514	526	538	549	561	573		
368		585	597	608	620	632	644	656	667	679	691		
369		703,	714	726	738	750	761	773	785	797	808		11
370		820	832	844	855	867	879	891	902	914	926	1	1.1
371		937	949	961	972	984	996	*008	*019	*031	*043	2 3	2.2 3.3
372	57	054	066	078	089	101	113	124	136	148	159	4	4.4
373		171	183	194	206	217	229	241	252	264	276	5	5.5
374		287	299	310	322	334	345	357	368	380	392	6	6.6 7.7
375		403	415	426	438	449	461	473	484	496	507	8	8.8
376		519	530	542	553	565	576	588	600	611	623	9	9.9
377		634	646	657	669	680	692	703	715	726	738		
378		749	761	772	784	795	807	818	830	841	852		
379		864	875	887	898	910	921	933	944	955	967	Ì	
380		978	990	*001	*01 3	*024	*035	* 947	*058	*070	*081		
	L	0		2	3	4		6	7		9		. P.

Num. 380 to 419. Log. 579 to 623.

N	L	0	1	2	3	4	5	6	7	8	9	P.	P.
380	57	978	990	*001	*013	*024	*035	*047	*058	*070	*081	,	
381	58	092	104	115	127	138	149	161	172	184	195		
382		206	218	229	240	252	263	274	286	297	309		
883		320	331	343	354	365	377	388	399	410	422		
384		433	444	456	467	478	490	501	512	524	535		11
385		546	557	569	580	591	602	614	625	636	647	١,,	
386		659	670	681	692	704	715	726	737	749	760	1 2	1.1 2.2
387		771	782	794	805	816	827	838	850	861	872	3	3.3
388		883	894	906	917	928	939	950	961	973	984	4	4.4
389		995	*006	*017	*028	*040	*051	*0 62	*073	*0 84	*09 5	5 6	5.5 6.6
390	59	106	118	129	140	151	162	173	184	195	207	7 8	7.7 8.8
391		218	229	240	251	262	273	284	295	806	318	9	9.9
392		329	340	351	362	3 73	384	395	406	417	428	Ì	
393		439	450	461	472	483`	494	506	517	528	539		
394		550	561	572	583	594	605	616	627	638	649		
395		660	671	6 82	693	704	715	726	737	748	759		
396		770	780	791	802	813	824	835	846	857	868		10
897		879	890	901	912	923	934	945	956	966	977		10
398		988	999		*021	*032	*043	*054	*065	*076	*086	1	1.0
399	60	097	108	119	130	141	152	163	173	184	195	3	2.0 3.0
400		206	217	228	239	249	260	271	282	293	304	4 5	4.0 5.0
401		314	325	336	347	358	369	379	390	401	412	6	6.0
402		423	433	444	455	466	477	487	498	509	520	8	7.0 8.0
403		531	541	552	563	574	584	595	606	617	627	9	9.0
404		638	649	660	670	681	692	703	713	724	735		
405		746	756	767	778	788	799	810	821	831	842	ļ.	
406		853	863	874	885	895	906	917	927	938	949		
407		959	970	981	991	*002	*013	*023	*034	*045	*055	l	
408	61	066	077	087	098	109	119	130	140	151	162		
409		172	183	194	204	215	225	236	247	257	268		
410		278	289	300	310	321	331	34 2	352	363	374		
411		384	395	405	416	426	437	448	458	469	479		
412		490	500	511	521	532	542	553	563	574	584	ļ	
413		59 5	606	616	627	637	648	658	669	679	690		
414		700	711	721	731	742	752	763	773	784	794		
415		805	815	826	836	847	857	868	878	888	899	1	
416		909	920	930	941	951	962	972	982		*003		
417	62	014	024	034	045	055	066	076	086	097	107		
418		118	128	138	149	159	170	180	190	201	211		
419		221	232	24 2	252	263	273	284	294	304	315		
420		325	335	346	356	366	377	387	397	408	418		
N	L	0	1	2	3	4	5	6	7	8	9	P	Р.

Num. 420 to 459. Log. 623 to 662.

N	L	0	1	2	3	4	5	6	7	8	9	P.	P.
420	62	325	335	346	356	366	377	387	397	408	418		
421		428	439	449	459	469	480	490	500	511	521		
422		531	542	552	562	572	583	593	603	613	624	l	
423		634	644	655	665	675	685	696	706	716	726	1	
424		737	747	757	767	778	788	798	808	818	829		
425		839	849	859	870	880	890	900	910	921	931		
426		941	951	961	972	982	992	*002	*012	*022	*033	ļ	
427	63	043	053	063	073	083	094	104	114	124	134	İ	
428		144	155	165	175	185	195	205	215	225	236	ł	10
429		246	256	266	276	286	296	306	317	327	3 37		
430		347	357	367	377	387	397	407	417	428	438	1 2	1.0 2.0
431		448	458	468	478	488	498	508	518	528	538	3 4 5	3.0
432		548	558	568	579	589	599	609	619	629	639	5	4.0 5.0
433	•	649	659	669	679	689	699	709	719	729	739	6	6.0
434		749	759	769	779	789	799	809	819	829	839	7 8	7.0 8.0
435		849	859	869	879	889	899	909	919	929	939	ğ	9.0
436		949	959	969	979	988	998	*008	*018	*028	*038	1	
437	64	048	058	068	078	088	098	108	118	128	137		
438		147	157	167	177	187	197	207	217	227	237		
439		246	256	266	276	286	296	306	316	326	335		
440		345	355	365	3 75	385	395	404	414	424	434		
441		444	454	464	473	483	493	503	513	523	532	l	
442		542	552	562	572	582	591	601	611	621	631		
443		640	650	660	670	680	689	699	709	719	729		
444		738	748	758	768	777	787	797	807	816	826		9
445		836	846	856	865	875	885	895	904	914	924	1	y
446		933	943	953	96 3	972	982	992	*002	*011	*021	1	0.9
447	65	031	040	050	060	070	079	089	099	108	118	3	1.8 2.7
448		128	137	147	157	167	176	186	196	205	215	2 3 4 5	3.6
449		225	234	244	254	263	273	283	292	302	312	5 6	4.5 5.4
450		321	331	341	350	360	369	379	389	398	408	7	6.3
451		418	427	437	447	456	466	475	485	495	504	8 9	7.2 8.1
452		514	523	533	543	552	562	571	581	591	600	"	1 0.1
453		610	619	629	639	64 8	658	667	677	686	696	ŀ	
454		706	715	725	734	744	753	763	772	782	792		
455		801	811	820	830	839	849	858	868	877	887		
456		896	906	916	925	935	944	954	963	97 3	.982		
457		992	*001	*011	*020	*030	*039		* 058		*077	1	
458	66	087	096	106	115	124	134	143	153	162	172		
459		181	191	200	210	219	229	238	247	257	266		
460		276	285	295	304	314	323	332	342	351	361		
N	L,	0	1	2	3	4	5	6	7	8	9	P.	P.

Num. 460 to 499. Log. 662 to 698.

N	L	0	1	2	3	4	5	6	7	8	9	P.	P.
460	66	276	285	295	304	314	323	332	342	351	361		
461		370	380	389	398	408	417	427	436	445	455	1	
462		464	474	483	492	502	511	521	530	539	549	i	
463		558	567	577	586	59 6	605	614	624	633	642		
464		652	661	671	680	689	699	708	717	727	736	İ	
465		745	755	764	773	783	792	801	811	820	829		
466		839	848	857	867	876	885	894	904	913	922		
467	l	932	941	950	960	969	978	987	997	*006	*015	ĺ	
468	67	025	034	043	052	062	071	080	089	099	108	1	10
469		117	127	136	145	154	164	173	182	191	201	١	
470		210	219	228	237	247	256	265	274	284	293	1 2	$\frac{1.0}{2.0}$
471		302	311	321	330	339	348	357	367	376	385	3	3.0
472	1	394	403	413	422	431	440	449	459	468	477	4	4.0
473	l	486	495	504	514	523	532	541	550	560	569	5 6	5.0 6.0
474°		578	587	596	605	614	624	633	642	651	660	7 8	7.0 8.0
475		669	679	688	697	706	715	724	733	742	752	9	9.0
476		761	770	779	788	797	806	815	825	834	843		
477		852	861	870	879	888	897	906	916	925	934	1	
478		943	952	961	970	979	988	997	*006	*015	*024	l	
479	68	034	043	052	061	070	079	088	097	106	115		
480		124	133	142	151	160	169	178	187	196	205	^	
481		215	224	233	242	251	260	269	278	287	296		
482		305	314	323	332	341	350	359	368	377	386		
483	i	395	404	413	422	431	440	449	458	467	476		
484		485	494	502	511	520	529	538	547	556	565		_
485		574	583	592	601	610	619	628	637	646	655		9
486	l	664	673	681	690	699	708	717	726	735	744	1	0.9
487		753	762	771	780	789	797	806	815	824	833	2 3	1.8 2.7
488		842	851	860	869	878	886	895	904	913	922	4	3.6
489		931	940	949	958	966	975	984	993	*002	*011	5	4.5 5.4
490	69	020	028	037	046	055	064	073	082	090	099	6 7	6.3
491		108	117	126	135	144	152	162	170	179	188	8	7.2 8.1
492		197	205	214	223	232	241	249	258	267	276	"	0.1
493		285	294	302	311	320	329	338	346	355	364		
494		373	381	390	399	408	417	425	434	443	452		
495		461	469	478	487	496	504	513	522	531	539		
496		548	557	566	574	583	592	601	609	618	627		
497		636	644	653	662	671	679	688	697	705	714	1	
498		723	732	740	749	758	767	775	784	793	801		
499		810	819	827	836	845	854	862	871	880	888		
500		897	906	914	923	932	940	949	958	966	975	ĺ	
N	L	0	1	2	-3	4	5	6	7	8	9	P.	P.
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Num. 500 to 539. Log. 698 to 732.

500 501 502 503 504 506 506 507 508 509 510 511 512 513 514 515 516 517 518 519 520 521 522 523 524	69 70 71	897 984 070 157 243 329 415 501 586 672 757 842 927 012 096 181 265	906 992 079 165 252 338 424 509 595 680 766 851 935 020 105	088 174 260 346 432 518 603 689 774 859 944 029	922 *010 096 183 269 355 441 526 612 697 783 868 952	932 *018 105 191 278 364 449 535 621 706 791 876	940 *027 114 200 286 372 458 544 629 714	949 *036 122 209 295 381 467 552 638 723	958 *044 131 217 303 389 475 561 646 731	966 *053 140 226 312 398 484 569 655 740	975 *062 148 234 321 406 492 578 663		9
502 503 504 506 506 507 508 509 511 512 513 514 515 515 516 517 518 519 522 522 523 524		070 157 243 329 415 501 586 672 757 842 927 012 096 181	079 165 252 338 424 509 595 680 766 851 935 020	088 174 260 346 432 518 603 689 774 859 944 029	096 183 269 355 441 526 612 697 783 868	105 191 278 364 449 535 621 706	114 200 286 372 458 544 629 714	122 209 295 381 467 552 638	131 217 303 389 475 561 646	140 226 312 398 484 569 655	148 234 321 406 492 578 663		9
503 504 505 506 507 508 509 310 511 512 513 514 515 516 517 518 519 320 521 522 523 524		157 243 329 415 501 586 672 757 842 927 012 096 181	165 252 338 424 509 595 680 766 851 935 020	174 260 346 432 518 603 689 774 859 944 029	183 269 355 441 526 612 697 783 868	191 278 364 449 535 621 706	200 286 372 458 544 629 714	209 295 381 467 552 638	217 303 389 475 561 646	226 312 398 484 569 655	234 321 406 492 578 663		9
504 506 506 507 508 509 510 511 512 513 514 515 516 517 518 519 520 521 522 523 524	71	243 329 415 501 586 672 757 842 927 012 096 181	252 338 424 509 595 680 766 851 935 020	260 346 432 518 603 689 774 859 944 029	269 355 441 526 612 697 783 868	278 364 449 535 621 706 791	286 372 458 544 629 714	295 381 467 552 638	303 389 475 561 646	312 398 484 569 655	321 406 492 578 663		9
505 506 507 508 509 310 511 512 513 514 515 516 517 518 519 320 521 522 523 524	71	329 415 501 586 672 757 842 927 012 096	338 424 509 595 680 766 851 935 020	346 432 518 603 689 774 859 944 029	355 441 526 612 697 783 868	364 449 535 621 706 791	372 458 544 629 714	381 467 552 638	389 475 561 646	398 484 569 655	406 492 578 663		9
506 507 508 509 810 511 512 513 514 515 516 517 518 619 820 521 522 523 524	71	415 501 586 672 757 842 927 012 096	424 509 595 680 766 851 935 020	432 518 603 689 774 859 944 029	441 526 612 697 783 868	449 535 621 706 791	458 544 629 714	467 552 638	475 561 646	484 569 655	492 578 663		9
507 508 509 510 511 512 513 514 515 516 517 518 519 820 521 522 523 524	71	501 586 672 757 842 927 012 096	509 595 680 766 851 935 020	518 603 689 774 859 944 029	526 612 697 783 868	535 621 706 791	544 629 714	552 638	561 646	569 655	578 663		9
508 509 510 511 512 513 514 515 516 517 518 519 520 521 522 523 524	71	586 672 757 842 927 012 096 181	595 680 766 851 935 020	603 689 774 859 944 029	612 697 783 868	621 706 791	629 714	638	646	655	663		9
509 810 511 512 513 514 515 516 517 518 519 820 521 522 523 524	71	757 842 927 012 096 181	680 766 851 935 020	689 774 859 944 029	697 783 868	706 791	714						9
510 511 512 513 514 515 516 517 518 519 520 521 522 523 524	71	757 842 927 012 096 181	766 851 935 020	774 859 944 029	783 868	791	}	723	731	740	F40		y
511 512 513 514 515 516 517 518 519 820 521 522 523 524	71	842 927 012 096 181	851 935 020	859 944 029	868		900			120	749		
512 513 514 515 516 517 518 519 820 521 522 523 524	71	927 012 096 181	935 020	944 029		976	000	808	817	825	834	1 2	0.9 1.8
513 514 515 516 517 518 519 820 521 522 523 524	71	012 096 181	020	029	050	010	885	893	902	910	919	3	2.7
514 515 516 517 518 519 820 521 522 523 524	71	096 181			902	961	969	978	986	995	*003	4	3.6
514 515 516 517 518 519 820 521 522 523 524		181	105		037	046	054	063	071	079	088	5 6	4.5 5.4
516 517 518 519 820 521 522 523 524				113	122	130	139	147	155	164	172	7	6.3
517 518 519 820 521 522 523 524		265	189	198	206	214	223	231	240	248	257	8 9	7.2 8.1
518 519 520 521 522 523 524			273	282	290	299	307	315	324	332	341		
518 519 820 521 522 523 524		349	357	366	374	383	391	399	408	416	425		
519 520 521 522 523 524		433	441	450	458	466	475	483	492	500	508		
521 522 523 524		517	525	533	542	550	559	567	575	584	592		
522 523 524	-	600	609	617	625	634	642	650	659	667	675		
522 523 524	-	684	692	700	709	717	725	734	742	750	759		
523 524		767	775	784	792	800	809	817	825	834	842		
524		850	858	867	875	883	892	900	908	917	925		
505		933	941	950	958	966	975	983	991	999	*008		
020	72	016	024	032	041	.049	057	066	074	082	090		8
526		099	107	115	123	132	140	148	156	165	173	1	8.0
527		181	189	198	206	214	222	230	239	247	255	2	1.6
528		263	272	280	288	296	304	313	321	329	337	3	2.4 3.2
529		346	354	362	370	378	387	395	403	411	419	5	4.0
530		428	436	444	452	460	469	477	485	493	501	6 7	4.8 5.6
531		509	518	526	534	542	550	558	567	575	583	8	6.4
532		591	599	607	616	624	632	640	648	656	665	9	7.2
533		673	681	689	697	705	713	722	730	738	746		
534		754	762	770	779	787	795	803	811	819	827		
535		835	843	852	860	868	876	884	892	900	908		
536		916	925	933	941	949	957	965	973	981	989		
537					*022		*038	*046			*070		5
538	73	078	086	094	102	111	119	127	135	143	151		
539	10	159	167	175	183	191	199	207	215	223	231		
540		239	247	255	263	272	280	288	296	304	312		
N		0	1	2	3	4	5	6	7	8	9		P.

Num. 540 to 579. Log. 732 to 763.

N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.
									<u> </u>				
540	73	239	247	255	263	272	280	288	296	304	312		
541		320	328	336	344	352	360	368	376	384	392		
542		400	408	416	424	432	440	448	456	464	472]	
543		480	488	496	504	512	520	528	536	544	552		
544		560	568	576	584	592	600	608	616	624	632		
545		640	648	656	664	672	679	687	695	703	711		
546		719	727	735	743	751	759	767	775	783	791	1	
547		799	807	815	823	830	838	846	854	862	870	ì	
548		878	886	894	902	910	918	926	933	941	949		8
549		957	965	97 3	981	989	997	*005	*013	*020	*028	1 1	0.8
550	74	036	044	052	060	068	076	084	092	099	107	3	1.6
551		115	123	131	139	147	155	162	170	178	186	3 4	2.4 3.2
552		194	202	210	218	225	233	241	249	257	265	5	4.0
553		273	280	288	296	304	312	320	327	335	343	6	4.8
554		351	359	367	374	382	390	398	406	414	421	7 8	5.6 6.4
555		429	437	445	453	461	468	476	484	492	500	9	7.2
556		507	515	523	531	539	547	554	562	570	578		
557		586	593	601	609	617	624	632	640	648	656	1 .	
558		663	671	679	687	695	702	710	718	726	733	}	
559		741	749	757	764	772	780	788	796	803	811		
560		819	827	834	842	850	858	865	873	881	889		
561		896	904	912	920	927	935	943	950	958	966	1	
562		974	981	989	997	*005	*012	*020	*028	*035	*043		
563	75	051	059	066	074	082	089	097	105	113	120		
564		128	136	143	151	159	166	174	182	189	197		_
565		205	213	220	228	236	243	251	259	266	274		7
566		282	289	297	305	312	320	328	335	343	351	1	0.7
567		358	366	374	381	389	397	404	412	420	427	2 3	1.4 2.1
568		435	442	450	458	465	473	481	488	496	504	4	2.8
569		511	519	526	534	542	549	557	565	572	580	5	3.5 4.2
570		587	595	603	610	618	626	633	641	648	656	6 7	4.9
571		664	671	679	686	694	702	709	717	724	732	8 9	5.6 6.3
572		740	747	755	762	770	778	785	793	800	808	•	, 0.0
573		815	823	831	838	846	853	861	868	876	884		
574		891	899	906	914	921	929	937	944	952	959		
575		967	974	982	989	997	*005	*012			*035		
576	76	042	050	057	065	072	080	087	095	103	110		
577		118	125	133	140	148	155	163	170	178	185		
578		193	200	208	215	223	230	238	245	253	260		
579		268	275	283	290	298	305	313	320	328	335		
580		343	350	358	365	373	380	388	395	403	410		
N	L	0	- 1	2	3	4	5	6	7	8	9	P.	P.

Num. 580 to 619. Log. 763 to 792.

N	L	0	1	2	3	4	5	6	7	8	9	P.	P.
580	76	343	350	358	365	373	380	388	395	403	410		- 8
581		418	425	433	440	448	455	462	470	477	485		
582		492	500	507	515	522	530	537	545	552	559	$\frac{1}{2}$	0.8
583		567	574	582	589	597	604	612	619	626	634	3	1.5 2.4
584		641	649	656	664	671	678	686	693	701	708	4 5	3.2 4.0
585		716	723	730	738	745	753	760	768	775	782	6 7	4.8
586		790	797	805	812	819	827	834	842	849	856	8	5.6 6.4
587		864	871	879	886	893	901	908	916	923	930	ğ	7.2
588		938	945	953	960	967	975	982	989	997	*004		-
589	77	012	019	026	034	041	048	056	063	070	078		
590		085	093	100	107	115	122	129	137	144	151		
591		159	166	173	181	.188	195	203	210	217	225		
592		232	240	247	254	262	269	276	283	291	298		
593		305	313	320	327	335	342	349	357	364	371		
594		379	386	39 3	401	408	415	422	· 430	437	444		
595		452	459	466	474	481	488	495	503	510	517		
596		525	532	539	546	554	561	568	576	583	590	1	
597		597	605	612	619	627	634	641	648	656	663		7
598		670	677	685	692	699	706	714	721	728	735		
599		743	750	757	764	772	779	786	793	801	808	1 2	0.7
600		815	822	830	837	844	851	859	866	873	880	3	2.1 2.8
601		887	895	902	909	916	924	931	938	945	952	4 5	3.5
602		960	967	974	981	988	996	*003	*010	*017	* 025	6	4.2
603	78	032	039	046	053	061	068	075	082	089	097	7	4.9 5.6
604		104	111	118	125	132	140	147	154	161	16 8	8 9	6.3
605		176	183	190	197	204	211	219	226	233	240		
606		247	254	262	269	276	283	290	297	305	312	l	
607		319	326	333	340	347	355	362	369	376	383		
608		390	398	405	412	419	426	433	440	447	45 5		
609		462	469	476	483	490	497	504	512	519	526		
610		533	540	547	554	561	569	576	583	590	597		
611		604	611	618	625	633	640	647	654	661	668		
612		675	682	689	696	704	711	718	725	732	739		
613		746	753	760	767	774	781	789	796	802	810		
614		817	824	831	838	845	852	859	866	873	880		
615		888	895	902	909	916	923	930	937	944	951		
616		958	965	972	979	986		*000			*021		
617	79	029	036	043	050	057	064	071	078	085	092		
618		099	106	113	120	127	134	141	148	155	162		
619		169	176	183	190	197	204	211	218	225	232		
620		239	246	253	260	267	274	281	288	2 95	302		
N	L	0	1	2	3	4	5	6	7	8	9	D	P.

Num. 620 to 659. Log. 792 to 819.

N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.
620	79	239	246	253	260	267	274	281	288	295	302		
621		309	316	323	330	337	344	351	358	365	372		
622		379	386	393	400	407	414	421	428	435	442		
623		449	456	463	470	477	484	491	498	505	511		
624		518	525	532	539	546	553	560	567	574	581		
625		588	595	602	609	616	623	630	637	644	650		
626		657	664	671	678	685	692	699	706	713	720	ļ	
627		727	734	741	748	754	761	768	775	782	789		
628		796	803	810	817	824	831	837	844	851	858		
629		865	872	879	886	893	900	906	913	920	927		
630		934	941	948	955	962	969	975	982	989	996		
631	80	003	010	017	024	030	037	044	051	058	065		
632		072	079	085	092	099	106	113	120	127	134		
633		140	147	154	161	168	175	182	188	195	202		
634		209	216	223	229	236	243	250	257	264	271		
635		277	284	291	298	305	312	318	325	332	339		-4
636		346	353	359	366	373	380	387	393	400	407		7
637		414	421	428	434	441	448	455	462	468	475		
638		482	489	496	502	509	516	523	530	536	543	1	0.7
639		550	557	564	570	577	584	591	598	604	611	3	1.4 2.1
640		618	625	632	638	64 5	652	659	6 65	672	679	4 5	2.8 3.5
641		686	693	699	706	713	720	726	733	740	747	5 6	4.2
642	,	754	760	767	774	781	787	794	801	808	814	7	4.9
643	ļ	821	828	835	841	848	855	862	868	875	882	8 9	5.6 6.3
644	*	889	895	902	909	916	922	929	936	943	949	•	, 5.5
645		956	963	969	976	9 83	990	996					-
646	81	023	030	027	043	050	057	064	070	077	084		
647		090	097	104	111	117	124	131	137	144	151		100
648		158	164	171	178	184	191	198	204	211	218		
649		224	231	238	245	251	258	265	271	278	285		100
650		291	298	305	311	318	325	331	338	345	351		
651		358	365	371	378	385	391	398	405	411	418		
652		425	431	438	445	451	458	465	471	478	485	ľ	
653		491	498	505	511	518	525	531	538	544	551		
654		558	564	571	578	584	591	598	604	611	617		
655		624	631	637	644	651	657	664	671	677	684		
656		690	697	704	710	717	723	730	737	743	750		
657		757	763	770	776	783	790	796	803	809	816		
658		823	829	836	842	849	856	862	869	875	882		
659		889	895	902	908	915	921	928	935	941	948		
660		954	961	968	974	981	987	994	*000	*007	*014		
N	L	0	1	2	3	4	5	6	7	. 8	9	P.	Р.

Num. 660 to 699. Log. 819 to 845.

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N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.
660	81	954	961	968	974	981	987	994	*000	*007	*014		7
661	82	020	027	033	040	046	053	060	066	073	079	,	
662		086	092	099	105	112	119	125	132	138	145	1 2	0.7 1.4
663		151	158	164	171	178	184	191	197	204	210	3	2.1
664		217	223	230	236	24 3	249	256	263	269	276	5	2.8 3.5
665		282	289	295	302	308	315	321	328	334	341	6 7	4.2
666		347	354	360	367	373	380	387	393	400	406	8	5.6
667		413	419	426	432	439	445	452	458	465	471	9	6.3
668		478	484	491	497	504	510	517	523	530	536		
669		54 3	549	556	562	569	575	582	588	595	601		
670		607	614	620	627	633	640	646	653	659	666		
671		672	679	685	692	698	705	711	718	724	730		
672		737	743	750	756	763	769	776	782	789	795		
673		802	808	814	821	827	834	840	847	853	860		
674		866	872	879	885	892	898	905	911	918	924		
675		930	937	943	950	956	963	969	975	982	988		
676		995				*020				*046			
677	83	059	065	072	078	085	091	097	104	110	117		6
678		123	129	136	142	149	155	161	168	174	181	١,	
679		187	193	200	206	213	219	225	232	238	245	1 2	0.6 1.2
680		251	257	264	270	276	283	289	296	302	308	3 4	1.8 2.4
681		315	321	327	334	340	. 347	353	359	366	372	5	3.0
682		378	385	391	398	404	410	417	423	429	436	6	3.6
683		442	448	455	461	467	474	480	487	493	499	8	4.2 4.8
684		506	512	518	525	531	537	544	550	556	563	. 9	5.4
685		569	575	582	588	594	601	607	613	620	626		
686		632	639	645	651	658	664	670	677	683	689		
687		696	702	708	715	721	727	734	740	746	753		
688		759	765	771	778	784	790	797	803	809	816		
689		822	828	835	841	847	853	860	866	872	879		
690		885	891	897	904	910	916	923	929	935	942		
691		948	954	960	967	973	979	985	992		*004		
692	84	011	017	023	029	036	042	048	055	061	067		
693		073	080	086	092	098	105	111	117	123	130	1	
694		136	142	148	155	161	167	173	180	186	192		
695		198	205	211	217	223	230	236	242	248	255		
696		261	267	273	280	286	292	298	305	311	317		
697		323	330	336	342	348	354	361	367	373	379		
698		386	392	398	404	410	417	423	429	435	442		
699		448	454	460	466	473	479	485	491	497	504		•
700		510	516	522	528	535	541	547	553	559	566		
N	L	0	1	2	3	4	5	6	7	8	9		Р.

		r	lum.	700) to	739.	Log	. 84	3 to	869	•		
N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.
700	84	510	516	522	528	535	541	547	553	559	566		
701		572	578	584	590	597	603	609	615	621	628	1	
702		634	640	646	652		665	671	677	683	689	-	
703		696	702	708	714		726	733	739	745	751	1	
704		757	763	770	776		788	794	800	807	813		٠.
705		819	825	831	837	844	850	856	862	868	874		
706		880	887	893	899	905	911	917	924	930	936		
707		942	948	954	960	967	973	979	985	991	997	1	
708	85	003	009	016	022	028	034	040	046	052	058		
709		065	071	077	083		095	101	107	114	120		•
710		126	132	138	144	150	156	163	169	175	181		
711		187	193	199	205	211	217	224	230	236	242	1	
712		248	254	260	266	272	278	285	291	297	303		
713		309	315	321	327	333	339	345	352	358	364	1	
714		870	376	382	388		400	406	412	418	425	1	
715		431	437	443	449	455	461	467	473	479	485		
716		491	497	503	509	516	522	528	534	540	546		
717		552	558	564	570	576	582	588	594	600	606		6
718		612	618	625	631	637	643	649	655	661	667	1 _	
719		673	679	685	691	697	703	709	715	721	727	1 2 3	0.6 1.2
720		733	739	745	751	757	763	769	775	781	788	3 4	1.8 2.4
721		794	800	806	812	818	824	830	836	842	848	5	3.0
722		854	860	866	872	878	884	890	896	902	908	6 7	8.6
723		914	920	926	932	938	944	950	956	962	968	8	4.2
724		974	980	986	992	998	*004	* 010	* 016	*022	*028	9	5.4
725	86	034	040	046	052		064	070	076	082	088		
726		094	100	106	112		124	130	136	141	147		
727		153	159	165	171	177	183	189	195	201	207	1	
728		213	219	225	231	237	243	249	255	261	267		
729		273	279	285	291	297	303	308	314	320	326		,
730		332	338	344	350		362	368	374	380	386		
731		392	398	404	410		421	427	433	439	445	1	;
732	:	451	457	463	469		481	487	493	499	504	1	
733	i	510	516	522	528		540	546	552	558	564		
734		570	576	581	587	593	599	605	611	617	623		1
735		629	635	641	646	652	658	664	670	676	682		
736	1	688	694	700	705		717	723	729	735	741		
737		747	753	759	764		776	782	788	794			
738		806	812	817	823		835	841	847	853	859		
739		864	870	876	882	888	894	900	906	911	917		
740		923	929	935	941	947	953	958	964	970	976		
N	L	0	1	2	3	4	5	6	7	8	9	P	Р.

Num. 740 to 779. Log. 869 to 892.

N	L	0	ť	2	3	4	5	6	7	8	9	P.	Р.
740	86	923	929	935	941	947	953	958	964	970	976		
741		982	988	994	999	*005	*011	*017	*023	*029	*035	i	
742	87	040	046	052	058	064	070	075	081	087	093	i	
743		099	105	111	116	122	128	134	140	146	151	l	
744		157	163	169	175	181	186	192	198	204	210		
745		216	221	227	233	239	245	251	256	262	268		
746		274	280	286	291	297	303	309	315	320	326	1	
747		832	338	344	349	355	361	367	873	379	384	l	
748		390	396	402	408	413	419	425	431	437	442	ł	
749		448	454	460	466	471	477	483	489	495	500		
750		506	512	518	523	529	535	541	547	552	558		
751		564	570	576	581	5 87	593	599	604	610	616	1	
752		622	628	633	639	645	651	656	662	668	674		
753		679	685	691	697	703	708	714	720	726	731	1	
754		737	743	749	754	760	766	772	777	783	789		
755		795	800	806	812	818	823	829	835	841	846		
756		852	858	864	869	875	881	887	892	898	904	l	
757		910	915	921	927	933	938	944	950	955	961		6
758		967	973	978	984	990	996	*001	*007	*013	*018		
759	88	024	036	036	041	047	053	058	064	· 07 0	076	1 2 3	0.6 1.2
760		081	087	093	098	104	110	116	121	127	133	3 4	1.8 2.4
761		138	144	150	156	. 161	167	173	178	184	190	5	3.0
762		195	201	207	213	218	224	230	235	241	247	6 7	3.6 4.2
763		2 52	258	264	270	275	281	287	292	298	304	8	4.8
764		309	315	321	326	332	338	343	349	855	360	9	5.4
765		366	372	377	383	389	395	400	406	412	417		
766		423	429	434	440	446	451	457	463	468	474		
767		480	485	491	497	502	508	513	519	525	530	l	
768		536	542	547	553	559	564	570	576	581	587	1	
769		593	598	604	610	615	621	627	632	638	643		
770		649	65 5	660	666	672	677	683	689	694	700		
771		705	711	717	722	728	734	739	745	750	756		
772		762	767	7 73	779	784	790	795	801	807	812		
773		818	824	829	835	840	846	852	857	863	868		
774		874	880	885	891	897	902	908	91 3	919	925		
775		930	936	941	947	953	958	964	969	9 75	981		
776		986	992	997	*003	*009	*014	*020	* 025	*031	*037		
777	89	042	048	053	059	064	070	076	081	087	092	1	
778		098	104	109	115	120	126	131	137	143	148	1	
779		154	159	165	170	176	182	187	193	198	204		
780		209	215	221	226	232	237	243	248	254	260		
N	L	0	1	2	3	4	5	6	7	8	9		P.

Num. 780 to 819. Log. 892 to 913.

N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.
780	89	209	215	221	226	232	237	243	248	254	260		
781		265	271	276	282	287	293	298	304	310	315	ŀ	
782		321	326	332	337	343	348	354	360	365	371	l	
783		376	382	.387	393	398	404	409	415	421	426		
784		432	437	443	448	454	459	465	470	476	481	l	
785		487	492	498	504	509	515	520	526	531	537		
786		542	548	553	559	564	570	575	581	586	592	l	
787		597	603	609	614	620	625	631	636	642	647		
788		653	658	664	669	675	680	686	691	697	702		
789		708	713	719	724	730	735	741	746	752	757	ţ	
790		763	768	774	779	785	790	796	801	807	812		
791		818	823	829	834	840	845	851	856	862	867		
792		873	878	883	889	894	900	905	911	916	922	İ	
793		927	933	938	944	949	955	960	966	971	977	1.	
794		982	988	993		*004		*015				ĺ	
795	90	037	042	048	053	059	064	069	075	080	086	ł	
796		091	097	102	108	113	119	124	129	135	140		
797		146	151	157	162	168	173	179	184	189	195		5
798		200	206	211	217	222	227	233	238	244	249	ĺ	•
799		255	260	266	271	276	282	287	293	298	304	1 2	1.0
800		309	314	320	325	331	336	342	347	352	358	3	1.5
801		363	369	37,4	380	385	390	396	401	407	412	4 5	2.0 2.5
802		417	423	428	434	439	445	450	455	461	466	6	3.0
803		472	477	482	488	493	499	504	509	515	520	7	8.5
804		526	531	536	542	547	553	558	563	569	574	8	4.0
805		580	585	590	596	601	607	612	617	623	628	•	
806		634	639	644	650		l .					ŀ	
						655	660	666	671	677	682	İ	
807		687	693	698	703	709	714	720	725	730	736	İ	
808 809		741 795	747 800	752 806	757 811	763 816	768 822	773 827	779 832	784 838	789 843		
1													
810 811		849 902	854 907	859 913	865 918	870	875	881 934	886	891	897	1	
812		956	961	966	972	924	929		940	945	950	l	
	01					977	982	988	993		*004	ŀ	
813 814	91	009 062	014 068	020 073	025 078	030 084	036 089	041 094	046 100	052 105	057 110		
							ĺ						
815		116	121	126	132	137	142	148	153	158	164	ĺ	
816		169	174	180	185	190	196	201	206	212	217		
817		222	228	233	238	243	249	254	259	265	270		
818		27 5	281	286	291	297	302	307	312	318	323	ļ	
819		328	334	3 39	344	350	355	360	365	371	376		
820		381	387	392	397	403	408	413	418	424	429	1	
N	L	0	1	2	3	4	5	6	7	8	9	D	Р.

Num. 820 to 859. Log. 913 to 934.

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_ <u>N</u> _	L	0	1		3	4	5	6	7	8		Р.	Р.
820	91	381	387	392	397	403	408	413	418	424	429	1	
821		434	440	445	450	455	461	466	471	477	482		
822		487	492	498	503	508	514	519	524	529	535		
823		540	545	551	556	561	566	572	577	582	587		
824		59 3	598	603	609	614	619	624	630	635	640	ł	
825		645	651	656	661	666	672	677	682	687	693	1	
826	ļ	698	703	709	714	719	724	730	735	740	745		
827		751	756	761	766	772	777	782	787	793	79 8		
828		803	808	814	819	824	829	834	840	845	850		
829		855	861	866	871	876	882	887	892	897	903		
830		908	913	918	924	929	934	939	944	950	955	ŀ	
831		960	965	971	976	981	986	991		*002			
832	92	012	018	023	028	033	038	044	049	054	05 9	ļ	
833		065	070	075	080	085	091	096	101	106	111	1	
834		117	122	127	132	137	143	148	153	158	163		
835		169	174	179	184	189	195	200	205	210	215		
836	İ	221	226	231	236	241	247	252	257	262	267		
837		273	278	283	288	293	298	304	309	314	319		5
838		3 24	330	335	340	345	350	355	361	366	371	1	0.5
839		876	381	387	392	397	402	407	412	418	423	2	1.0
840		428	433	438	443	449	454	459	464	469	474	3 4	1.5 2.0
841		480	485	490	495	500	505	511	516	521	526	5	2.5
842		531	536	542	547	552	557	562	567	572	578	6 7	3.0 3.5
843	Ì	583	588	593	598	603	609	614	619	624	629	8	4.0
844		634	639	645	650	6 55	660	665	670	675	681	9	4.5
845	1	686	691	696	701	706	711	716	722	727	732		
846		737	742	747	752	758	763	768	773	778	783		
847		788	793	799	804	809	814	819	824	829	834		
848	l	840	845	850	855	860	865	870	875	881	886		
849		891	896	901	906	911	916	921	927	932	937		
850		942	947	952	957	962	967	973	978	983	988		
851		993	998		*008				*029		*039		
852	93	044	049	054	059	064	069	075	080	085	090		
853		095	100	105	110	115	120	125	131	136	141	İ	
854		146	151	156	161	166	171	176	181	186	192		
855		197	202	207	212	217	222	227	232	237	242		
856		247	252	258	263	268	273	278	283	288	293	1	
857		298	303	308	313	318	323	328	334	339	344		
858		349	354	359	364	869	374	379	384	389	394	1	
859		399	404	409	414	420	425	430	435	440	445		•
860		450	455	460	465	470	475	480	485	490	495	1	
N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.

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	!	Yum	. 860) to	899.	Log	. 934	i to	954.		
L	0	1	2	3	4	5	6	7	8	9	P. P.
93	450	455	460	465	470	475	480	485	490	495	
	500	505	510	515	520	526	531	536	541	546	
	551	556	561	566	571	576	581	586	591	596	
	601	606	611	616	621	626	631	636	641	646	
	651	656	661	666	671	676	682	687	692	697	
	702	707	712	717	722	727	732	737	742	747	
	752	757	762	767	772	777	782	787	792	797	
	802	807	812	817	822	827	832	837	842	847	
	852	857	862	867	872	877	882	887	892	897	
	902	907	912	917	922	927	932	937	942	947	
	952	957	962	967	972	977	982	987	992	997	
94	002	007	012	017	022	027	032	037	042	047	
	052	057	062	067	072	077	082	086	091	096	
	101	106	111	116	121	126	131	136	141	146	
	151	156	161	166	171	176	181	186	191	196	
	201	206	211	216	221	226	231	236	240	245	
	250	255	260	265	270	275	280	285	290	295	
	300	305	310	315	320	325	330	335	340	345	5
	349	354	359	364	369	374	379	384	389	394	1105
	399	404	409	414	419	424	429	433	438	443	1 0.5 2 1.0
	448	453	458	463	468	473	478	483	488	493	3 1.5 4 2.0
	498	503	507	512	517	522	527	532	537	542	5 2.5

Num. 900 to 939. Log. 954 to 973.

N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.
900	95	424	429	434	439	444	448	453	458	463	468		
901		472	477	482	487	492	497	501	506	511	516		
902		521	525	530	535	540	545	550	554	559	564		
903		569	574	578	583	588	593	598	602	607	612		
904		617	622	626	631	636	641	646	650	655	660		
905		665	670	674	679	684	689	694	698	703	708		
906		713	718	722	727	732	737	742	746	751	756		
907		761	766	7 70	775	780	785	789	794	799	804		
908		809	813	818	823	828	832	837	842	847	852		
909		856	861	866	871	875	880	885	890	895	899		
910		904	909	914	918	923	928	933	938	942	947		
911		952	957	961	966	971	976	980	985	990	995		
912		999	*004		*014				*033	*038			
913	96	047	052	057	061	066	071	076	080	085	090		
914		095	099	104	109	114	118	123	128	133	137		
915		142	147	152	156	161	166	171	175	180	185		
916		190	194	199	204	209	213	218	223	227	232		
917		237	242	246	251	256	261	265	270	275	280		5
918		284	289	294	298	303	308	313	317	322	327	1	0.5
919		332	336	341	346	350	355	360	365	369	374	2	1.0
920		379	384	388	393	398	402	407	412	417	421	3 4	1.5 2.0
921		426	431	435	440	445	450	454	459	464	468	5	2.5
922		473	478	483	487	492	497	501	506	511	515	6 7	3.0 3.5
923		520	525	5 30	534	539	544	548	553	558	562	8	4.0
924		567	572	577	581	586	591	595	600	605	609	9	4.5
925		614	619	624	628	633	638	642	647	652	656		
926		661	666	670	675	680	685	689	694	699	703		
927		708	713	717	722	727	731	736	741	745	750		
928		755	759	764	769	774	778	783	788	792	797		
929		802	806	811	816	820	825	830	834	839	844		
930		848	853	858	862	867	872	876	881	886	890		
931		895	900	904	909	914	918	923	928	932	937		
932		942	946	951	956	960	965	970	974	979	984		
933		988	993		*002	*007	*011	*016	*021	*025	* 030		
934	97	035	039	044	049	053	058	063	067	072	077		
935		081	086	090	095	100	104	109	114	118	123		
936		128	132	137	142	146	151	155	160	165	169		
937		174	179	183	188	192	197	202	206	211	216		
938		220	225	230	234	239	243	248	253	257	262		
939		267	271	276	280	285	290	294	299	304	308		
940		313	317	322	327	331	336	340	345	350	354		
N	L	0	1	2	3	4	5	6	7	8	9	D	P.

Num. 940 to 979. Log. 973 to 991.

N	L.	0	1	2	3	4	5	6	7	8	9	P.	Р.
940	97	313	317	322	327	331	336	340	345	350	354		
941		359	364	368	373	377	382	387	391	396	400		
942		405	410	414	419	424	428	433	437	442	447	١.	
943		451	456	460	465	470	474	479	483	488	493	•	
944		497	502	506	511	516	520	525	529	534	539		
945		543	548	552	557	562	566	571	575	580	585		
946		589	594	598	603	607	612	617	621	626	630		
947		635	640	644	649	653	658	663	667	672	676		
948		681	685	690	695	699	704	708	713	,717	722		
949		727	731	736	740	745	749	754	759	763	768		5
950		772	777	782	786	791	795	800	804	809	813	1	0.5
951		818	823	827	832	, 836	841	845	850	855	859	3	1.0 1.5
952		864	868	873	877	882	886	891	896	900	905	4	2.0
953		909	914	918	923	928	932	937	941	946	950	5	2.5
954		955	959	964	968	973	978	982	987	991	996	64	3.0 3.5
955	98	000	005	009	014	019	023	028	032	037	041	8	4.0
956		046	050	055	059	064	068	073	078	082	087		1 2.0
957		091	096	100	105	109	114	118	123	127	132		
958		137	141	146	150	155	159	164	168	173	177		
959		182	186	191	195	200	204	209	214	218	223		
960		227	232	236	· 241	245	250	254	259	263	268		
961		272	277	281	286	290	295	299	304	308	313		
962		318	322	327	331	336	340	345	349	354	358		
963		363	367	372	376	381	385	390	394	399	403		
964		408	412	417	421	426	430	435	439	444	448		
965		453	457	462	466	471	475	480	484	489	493		4
966		498	502	507	511	516	520	525	529	534	538	1	0.4
967		54 3	547	552	556	561	565	570	574	579	583	2	0.8 1.2
968		588	592	597	601	605	610	614	619	623	628	3 4	1.6
969		632	637	641	646	650	655	659	664	668	673	5	2.0
970		677	682	686	691	695	700	704	709	713	717	7	2.4 2.8
971		722	726	731	735	740	744	749	753	758	762	8 9	3.2 3.6
972		767	771	776	780	784	789	793	798	802	807	, ,	0.0
973		811	816	820	825	829	834	838	843	847	851		
974		856	860	865	869	874	878	883	887	892	896		
975		900	905	909	914	918	923	927	932	936	941	1	
976		945	949	954	958	963	967	972	976	981	985	İ	
977		989	994		*003				*021			l	
978	99	034	038	043	047	052	056	061	065	069	074		
979		078	083	087	092	096	100	105	109	114	118		
980		123	127	131	136	140	145	149	154	158	162	_	
N	L	0	1	2	3	4	5	6	7	8	9	D	P.

Num. 980 to 1000. Log. 991 to 999.

N	L	0	1	2	3	4	5	6	7	8	9	P.	P.
980	99	123	127	131	136	140	145	149	154	158	162		
981		167	171	176	180	185	189	193	198	202	207		
982		211	216	220	224	229	233	238	242	247	251		
983		255	260	264	269	273	277	282	286	291	295		
984		300	304	308	313	317	322	326	330	335	339		
985		344	348	352	357	361	366	370	374	379	383		
986		388	392	396	401	405	410	414	419	428	427		
987		432	436	441	445	449	454	458	468	467	471		
988		476	480	484	489	493	498	502	506	511	515		
989		520	524	528	533	537	542	546	550	555	559		4
990		564	568	572	577	581	585	590	594	599	603	1	0.4
991		607	612	616	621	625	629	634	638	642	647	2 3	0.8 1.2
992		651	656	660	664	669	673	677	682	686	691	4	1.6
993		695	699	704	708	712	717	721	726	730	734	5	2.0
994		739	743	747	752	756	760	765	769	774	778	6	2.4 2.8
995		782	787	791	795	800	804	808	813	817	822	8	3.2 3.6
996		826	830	835	839	843	848	852	856	861	865		0.0
997		870	874	878	883	887	891	896	900	904	909		
998		913	917	922	926	930	935	939	944	948	952		
999		957	961	965	970	974	978	983	987	991	996		
1000	000	000	043	087	130	174	217	260	304	347	391		
N	L	0	1	2	3	4	5	6	7	8	9	Р.	P.

Logarithms of Important Numbers.

Number.	Logarithm.
π' = 3.141 593	0.497 150
$\frac{4}{3}\pi = 4.188790$	0.622 089
$\frac{1}{6}\pi = 0.523599$	1.718 999
$\frac{1}{\pi}$ = 0.318 310	1.502 850
$\pi^2 = 9.869 604$	0.994 300
$\frac{1}{\pi^2} = 0.101 \ 321$	1.005 700
$V_{\pi}^{-} = 1.772454$	0.248 575
$\frac{1}{V_{\pi}} = 0.564 \ 190$	T.751 425
$V_{\pi}^{-} = 1.464 592$	0.165 717
$\frac{1}{p'\pi} = 0.682784$	T.834 283
$\sqrt[3]{\frac{6}{\pi}} = 1.240 \ 701$	0.093 667

0 °			Logar	ithms.		1	179
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	Inf. Neg.	Infinite.	Inf. Neg.	Infinite.	10.00000	10.00000	60
1	6.46373	13.53627	6.46373	13.53627 23524	00000	00000	59
3	76476	23524 05915	76476	23524 05915	00000	00000	58
4	94085 7.06579	12,93421	94085 7.06579	12.93421	00000	00000	57 56
5	7.16270	12.83730	7.16270	12.83730	10.00000	10.00000	55
6	24188	75812	24188	75812	00000	00000	54
6 7 8	30882	69118	30882	69118	00000	00000	53
9	36682 41797	63318 58203	36682 41797	63318 58203	00000	-00000 -00000	52 51
10	7.46373	12.53627	7.46373	12.53627	10.00000	10.00000	50
11	50512	49488	50512	49488	00000	00000	49
12	54291	45709	54291	45709	00000	00000	48
13	57767	42233	57767	42233	00000	00000	47
14 15	60985 7.63982	39015 12.36018	60986 7.63982	39014 12,36018	10.00000	00000 10.00000	46 45
16	66784	33216	66785	33215	- 00000	00000	44
17 l	69417	30583	69418	30582	00001	9.99999	43
18	71900	28100	71900	28100	00001	99999	42
19	74248	25752	74248	25752	00001	99999	41
20	7.76475 78594	12,23525 21406	7.76476 78595	12.23524 21405	10.00001 00001	9.99999 99999	40 39
20 21 22 23 24	80615	19385	80615	19385	00001	99999	38
23	82545	17455	82546	17454	00001	99999	37
24	84393	15607	84394	15606	00001	99999	136
25 26 27 28 29	7.86166	12.13834	7.86167	12.13833	10.00001	9.99999	35
26	87870 89509	12130 10491	87871 89510	12129 10490	00001 00001	99999 99999	34
2/	91088	08912	91089	08911	00001	99999	33 32
29	92612	07388	92613	07387	00002	99998	31
30	7.94084	12.05916	7.94086	12.05914	10.00002	9.99998	30
31	95508	04492	95510	04490	00002	99998	29
32 33	96887 98223	03113 01777	96889 98225	03111 01775	00002 00002	99998 99998	28
34	99520	00480	99522	00478	00002	99998	27 26
35	8.00779	11.99221	8.00781	11.99219	10.00002	9.99998	25
36	02002	97998	02004	97996	00002	99998	24
37	03192	96808	03194	96806	00003	99997	23
38 39	04350 05478	95650 94522	04353 05481	95647 94519	00003 00003	99997 99997	22 21
40	8.06578	11.93422	8.06581	11.93419	10.00003	9.99997	20
41	07650	92350	07653	92347	00003	99997	19
42	08696	91304	08700	91300	00003	99997	18
43	09718	90282	09722	90278	00003	99997	17
44 45	10717 8.11693	89283 11.88307	10720 8.11696	89280 11.88304	00004 10.00004	99996 9.99996	16 15
46	12647	87353	12651	87349	00004	99996	14
47	13581	86419	13585	86415	00004	99996	13
48	14495	85505	14500	85500	00004	99996	12
49	15391	84609	15395	84605	00004	99996	11
50 51	8.16268 17128	11.83732 82872	8.16273 17133	11.83727 82867	10.00005 00005	9.99995 99995	10
52	17971	82029	17976	82024	00005	99995	9
53	18798	81202	18804	81196	00005	99995	8 7
54	19610	80390	19616	80384	00005	99995	6
55	8.20407	11.79593	8.20413	11.79587	10.00006	9.99994	5
56 57	21189 21958	78811 78042	21195 21964	78805 78036	00006 00006	99994	4
58	21908 22713	78042	21964 22720	78036 77280	00006	99994 99994	3 2
59	23456	76544	23462	76538	00006	99994	í
60	24186	75814	24192	75808	00007	99993	ō
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

10				178°			
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	8.24186	11.75814	8.24192	11.75808	10.00007	9.99993	60
1	24903	75097	24910	75090	00007	99993 99993	59
2	25609 26304	74391 73696	25616 26312	74384 73688	00007 00007	99993	58 57
4	26988	73012	26996	73004	00008	99992	56
5	8.27661	11.72339	8.27669	11.72331	10.00008	9.99992	55
5 6 7 8 9	28324	71676	28332	71668	00008	99992	54
7	28977	71023	28986	71014	00008	99992	53
8	29621 30255	70379 69745	29629 30263	70371 69737	00008 00009	99992 99991	52 51
10	8.30879	11.69121	8.30888	11.69112	10.00009	9.99991	50
11	31495	68505	31505	68495	00009	99991	49
12	32103	67897	32112	67888	00010	99990	48
13	32702	67298	32711	67289	00010	99990	47
14	33292	66708	33302	66698	00010	99990	46
15 16	8.33875 34450	11.66125 65550	8.33886 34461	11.66114 65539	10.00010 00011	9.99990 99989	45
17	35018	64982	35029	64971	00011	99989	43
18	35578	64422	35590	64410	00011	99989	42
19	36131	63869	36143	63857	00011	99989	41
20 21 22 23	8.36678	11.63322	8.36689	11.63311 62771	10.00012	9.99988	40
21	37217	62783	37229	62771	00012	99988	39
22	37750 38276	62250 61724	37762 38289	62238 61711	00012 00013	99988 99987	38 37
24	38796	61204	38809	61191	00013	99987	36
25	8.39310	11.60690	8.39323	11.60677	10.00013	9.99987	35
25 26	39818	60182	39832	60168	00014	99986	34
27	40320	59680	40334	59666	00014	99986	33
28	40816	59184	40830	59170	00014	99986	32
27 28 29 30 31	41307 8.41792	58693 11.58208	41321 8.41807	58679 11.58193	00015 10.00015	99985 9,99985	31 30
30 81	42272	57728	42287	57713	00015	99985	29
32	42746	57254	42762	57238	00016	99984	28
23	43216	56784	43232	56768	00016	99984	27
84	43680	56320	43696	56304	00016	99984	26
35	8.44139	11.55861	8.44156	11.55844	10.00017	9.99983	25 24
36 37	44594 45044	55406 54956	44611 45061	55389 54939	00017 00017	99983 99983	23
36	45489	54511	45507	54493	00018	99982	22
38 39	45930	54070	45948	54052	00018	99982	21
40	8.46366	11.53634	8.46385	11.53615	10.00018	9.99982	20
41	46799	53201	46817	53183	00019	99981	19
42	47226	52774	47245	52755	00019	99981	18 17
43 44	47650 48069	52350 51931	47669 48089	52331 51911	00019 00020	99981 99980	16
45	8.48485	11.51515	8.48505	11.51495	10.00020	9.99980	15
46	48896	51104	48917	51083	00021	99979	14
47	49304	50696	49325	50675	00021	99979	13
48	49708	50292	49729	50271	-00021	99979	12
49	50108	49892	50130	49870	00022	99978	11
50 51	8.50504 50897	11.49496 49103	8.50527 50920	11.49473 49080	10.00022 00023	9.99978 99977	10
52	51287	48713	51310	48690	00023	99977	8
53	51673	48327	51696	48304	00023	99977	7
54	52055	47945	52079	47921	00024	99976	6
55 56 57	8.52434	11.47566	8.52459	11.47541	10.00024	9.99976	5
56	52810	47190	52835	47165	00025	99975	4
57	53183 53552	46817 46448	53208 53578	46792 46422	00025 00026	99975 99974	3 2
58 59	53919	46081	53945	46055	00026	99974	î
60	54282	45718	54308	45692	00026	99974	ō
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

2 °			Logar	ithms.		:	17 7 °
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	8.54282	11.45718	8.54308	11.45692	10.00026	9.99974	60
1	54642	45358	54669	45331	00027	99973	59
2	54999	45001	55027	44973	00027	99973	58 57
3	55354	44646	55382	44618 44266	00028 00028	99972 99972	56
4	55705 8.56054	44295 11.43946	55734 8,56083	11.43917	10.00029	9.99971	55
5 6,	56400	43600	56429	43571	00029	99971	55 54
7	56743	43257	56773	43227	00030	99970	53
8	57084	42916	57114	42886	00030	99970	52
9	57421	42579	57452	42548	00031	99969	51
10 11	8.57757	11.42243	8.57788	11.42212	10.00031	9.99969 99968	50 49
11	58089	41911	58121	41879 41549	00032 00032	99968	48
12 13	58419 58747	41581 41253	58451 58779	41221	00033	99967	47
14	59072	40928	59105	40895	00033	99967	46
15	8.59395	11.40605	8.59428	11.40572	10.00033	9.99967	45
16	59715	40285	59749	40251	00034	99966	44
17	60033	39967	60068	39932	00034	99966	43
18	60349	39651	60384	39616 39302	00035 00036	99965 99964	42
19	60662 8.60973	39338 11.39027	60698 8.61009	11.38991	10.00036	9.99964	40
20 21 22 23 24	61282	38718	61319	38681	00037	99963	39
22	61589	38411	. 61626	38374	00037	99963	38
23	61894	38106	61931	38069	00038	99962	37
24	62196	37804	62234	37766	00038	99962	36
25 26 27 28 29	8.62497	11.37503	8.62535	11.37465	10.00039	9.99961	35
26	62795	37205	62834	37166	00039 00040	99961 99960	34 33
2/	63091 63385	36909 36615	63131 63426	36869 36574	00040	99960	32
20	63678	36322	63718	36282	00041	99959	31
30	8.63968	11.36032	8.64009	11.35991	10.00041	9.99959	30
31	64256	35744	64298	35702	00042	99958	29
31 32 33 34	64543	35457	64585	35415	00042	99958	28
33	64827	35173	64870	35130	00043	99957 99956	27 26
34 35	65110 8.65391	34890 11.34609	65154 8.65435	34846 11.34565	00044 10.00044	9.99956	25
96	65670	34330	65715	34285	00045	99955	24
36 37 38 39	65947	34053	65993	34007	00045	99955	23
38	66223	33777	66269	33731	00046	99954	22
39	66497	33503	66543	33457	00046	99954	21
40	8.66769	11.33231	8.66816	11.33184	10.00047	9,99953	20 19
41 42	67039 67308	32961 32692	67087 67356	32913 32644	00048 00048	99952 99952	18
43	67575	32425	67624	32376	00049	99951	17
44	67841	32159	67890	32110	00049	99951	16
45	8.68104	11:31896	8.68154	11.31846	10.00050	9.99950	15
46	68367	31633	68417	31583	00051	99949	14
47	68627	31373	68678	31322	00051	99949	13
48	68886	31114	68938	31062	00052	99948	12 11
49 50	69144 8.69400	30856 11.30600	69196 8,69453	30804 11,30547	00052 10.00053	99948 9,99947	10
51	69654	30346	69708	30292	00054	99946	9
52	69907	30093	69962	30038	00054	99946	8 7
52 53	70159	29841	70214	29786	00055	99945	
54	70409	29591	70465	29535	00056	99944	6 5
55	8.70658	11.29342	8.70714	11.29286	10.00056	9.99944	5
56 57	70905 71151	29095 28849	70962 71208	29038 28792	00057 00058	99943 99942	9
57 58	71131	28849	71208	28547	00058	99942	2
59	71638	28362	71697	28303	00059	99941	3 2 1
60	71880	28120	71940	28060	00060	99940	Ō
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

3°			Logar	ithms.			176°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	8.71880	11.28120	8.71940	11.28060	10,00060	9.99940	60
1	72120	27880	72181	27819	00060	99940	59
2 3 4	72359	27641	72420	27580	00061	99939	58
3	72597	27403	72659	27341	00062	99938	57
4	72834	27166	72896	27104	00062	99938	56
5	8.73069	11.26931	8.73132	11.26868	10.00063	9.99937	55
6	73303	26697	73366	26634	00064	99936 99936	54
8	73535 73767	26465 26233	73600 73832	26400 26168	00064 00065	99935	53 52
9	73997	26003	74063	25937	00066	99934	51
10	8.74226	11.25774	8.74292	11.25708	10.00066	9.99934	
ii	74454	25546	74521	25479	00067	99933	50 49
12	74680	25320	74748	25252	00068	99932	48
13	74906	25094	74974	25026	00068	99932	47
14	75430	24870	75199	24801	00069	99931	46
15	8.7 353	11.24647	8.75423	11.24577	10.00070	9.99930	45
16	7 5575	24425	75645	24355	00071	99929	44
17	'/5795	24205	75867	24133	00071	99929	43
18	76015	23985	76087	23913	00072	99928	42
19	76234	23766 11.23549	76306	23694 11.23475	00073 10.00074	99927 9,99926	41
20 21	8 76451 76667	23333	8.76525 76742	23258	00074	999926	39
22	76883	23117	76958	23042	00075	99925	38
23	77097	22903	77173	22827	00076	99924	37
24	77310	22690	77387	22613	00077	99923	36
25	8 77522	11.22478	8.77600	11.22400	10.00077	9.99923	35
26	77733	22267	77811	22189	00078	99922	34
26 27	77943	22057	78022	21978	00079	99921	33
28	78152	21848	78232	21768	00080	99920	32
29	78360	21640	78441	21559	00080	99920	31
30	8.78568	11.21432	8.78649	11.21351	10.00081	9.99919	30
31	78774	21226	78855	21145	00082	99918	29
82	78979	21021	79061	20939 20734	00083 00083	99917	28 27
33 34	79183 79386	20817 20614	79266 79470	20734	00084	99917 99916	26
35	8.79588	11.20412	8.79673	11.20327	10.00085	9.99915	25
36	79789	20211	79875	20125	00086	99914	24
37	79990	20010	80076	19924	00087	99913	23
38	80189	19811	80277	19723	00087	99913	23 22
39	80388	19612	80476	19524	00088	99912	21
40	8.80585	11.19415	8.80674	11.19326	10.00089	9.99911	20
41	80782	19218	80872	19128	00090	99910	19
42	80978	19022	81068	18932	00091	99909	18
43	81173	18827	81264	18736	00091	99909	17
44	81367	18633	81459	18541	00092	99908	16
45 46	8.81560	11.18440 18248	8.81653 81846	11.18347 18154	10.00093 00094	9.99907 99906	15 14
47	81752 81944	18056	82038	17962	00095	99905	13
48	82134	17866	82230	17770	00096	99904	12
49	82324	17676	82420	17580	00096	99904	îī
50	8.82513	11.17487	8.82610	11.17390	10.00097	9.99903	10
51	82701	17299	82799	17201	00098	99902	9
52	82888	17112	82987	17013	00099	99901	8 7
53	83075	16925	83175	16825	00100	99900	7
54	83261	16739 11.16554	83361	16639	00101	99899	6
55	8.83446	11.16554	8.83547	11.16453	10.00102	9.99898	5 4
56	- 83630	16370	83732	16268	00102	99898	4
57	83813	16187	83916	16084	00103	99897	3 2
58 59	83996 84177	16004 15823	84100 84282	15900 15718	00104 00105	99896 99895	1 1
60	84358	15642	84464	15536	00106	99894	ō
m.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

40			Logar	ithms.			175
м.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	8.84358	11.15642	8.84464	11.15536	10.00106	9.99894	60
11	84539	15461	84646	15354	00107	99893	59
2	84718	15282	84826	15174	00108	99892	58
3	84897 85075	15103	85006	14994	00109	99891 99891	57
4	85075	14925 11.14748	85185	14815 11.14637	00109 10.00110	9.99890	56 55
5	8.85252	11.14748	8.85363 85540	14460	00111	99889	54
7	85429 85605	14395	85717	14283	00112	99888	53
8	85780	14220	85893	14107	00113	99887	52
9	85955	14045	86069	13931	00114	99886	51
10	8.86128	11.13872	8.86243	11.13757	10.00115	9.99885	50
īĭ l	86301	13699	86417	13583	00116	99884	49
12	86474	13526	86591	13409	00117	99883	48
13	86645	13355	86763	13237	00118	99882	47
14	86816	13184	86935	13065	00119	99881	46
15	8.86987	11.13013	8.87106	11.12894	10.00120	9.99880 99879	45 44
16	87156	12844 12675	87277 87447	12723 12553 12384	00121 00121	99879	43
17	87325 87494	12675 12506	87447 87616	12000	00121	99878	42
18	87661	12339	87785	12215	00123	99877	41
30 Ta	8.87829	11.12171	8.87953	11.12047	10.00124	9.99876	40
19 20 21	87995	12005	88120	11880	00125	99875	39
22	88161	11839	88287	11713 11547	00126	99874	38
23	88326	11674	88453	11547	00127	99873	37
24	88490	11510	88618	11382	00128	99872	36
25	8.88654	11.11346	8.88783	11.11217	10.00129	9.99871	35
26	88817	11183	88948	11052	00130	99870	34
26 27 28 29	88980	11020	89111	10889	00131	99869 99868	33 32
28	89142	10858	89274	10726	00132 00133	99868	31
29	89304	10696	89437	10563 11.10402	10.00134	9.99866	31
30 31	8.89464 89625	11.10536 10375	8.89598 89760	10240	00135	99865	30 29
32	89784	10216	89920	10000	00136	99864	28
32 33	89943	10057	90080	09920	00137	99863	27
34	90102	09898	90240	09760	00138	99862	27 26
35	8.90260	11.09740	8.90399	11.09601	10.00139	9.99861	25
86	90417	09583	90557	09443	00140	99860	24
86 37	90574	09426	90715	09285	00141	99859	23 22
38 39	90730	09270	90872	09128	00142	99858	22
39	90885	09115	91029	08971	00143	99857	21
40 I	8.91040	11.08960	8.91185	11.08815	10.00144	9.99856	20
41	91195	08805	91340	08660	00145	99855 99854	19 18
42	91349	08651 08498	91495 91650	08505 08350	00146 00147	99853	17
43 44	91502 91655	08345	91803	08197	00148	99852	16
45	8.91807	11.08193	8.91957	11.08043	10.00149	9.99851	15
46	91959	08041	92110	07890	00150	99850	14
47	92110	07890	92262	07738	00152	99848	13
48	92261	07739 07589	92414	07586	00153	99847	12
49	92411	07589	92565	07435 11.07284	00154	99846	11
50	8.92561	11.07439	8.92716	11.07284	10.00155	9.99845	10
51	92710	07290	92866	07134	00156	99844	9
52 53	92859	07141	93016	06984	00157	99843	8 7 6 5 4 3 2
53	93007	06993	93165	06835 06687	00158 00159	99842 99841	1
54	93154	06846	93313 8.93462	11.06538	10.00160	9.99840	1 5
55 56	8.93301 93448	11.06699 06552	93609	06391	00161	9,99640	1 4
56 57	93594	06406	93756	06244	00162	99838	3
50	93740	06260	93903	06097	00163	99837	1 2
58 59	93885	06115	94049	05951	00164	99836	ī
60	94030	05970	94195	05805	00166	99834	ō
_		Secant.	Cotangent	Tangent.	Cosecant.	Sine.	М.

M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	11
0	8.94030	11.05970	8.94195	11.05805	10.00166	9.99834	
ĭ	94174	05826	94340	05660	00167	99833	
2	94317	05683	94485	05515	00168	99832	14
3	94461	05539	94630	05370	00169	99831	11
4	94603	05397	94773	05227	00170	99830	11
5	8.94746	11.05254	8.94917	11.05083	10.00171	9.99829	13
6	94887	05113	95060	04940	00172	99828	14
7	95029	04971	95202	04798	00173	99827	13
8	95170	04830	95344	04656	00175	99825	
9	95310	04690	95486	04514	00176	99824	1
10	8.95450	11.04550	8.95627	11.04373	10.00177	9.99823 99822	1
12	95589 95728	04411 04272	95767 95908	04233 04092	00178	99821	13
13	95867	04133	96047	03953	00180	99820	1
14	96005	03995	96187	03813	00181	99819	17
15	8.96143	11 03857	8.96325	11.03675	10.00183	9.99817	1
16	96280	11.03857 03720	96464	03536	00184	99816	1.
16 17	96417	03583	96602	03398	00185	99815	1.
18 19	96553	03447	96739	03261	00186	99814	1.
19	96689	03311	96877	03123	00187	99813	14
20 21	8.96825	11.03175	8.97013	11.02987	10.00188	9.99812	1
21	96960	03040	97150	02850	00190	99810	1:
22	97095	02905	97285	02715	00191	99809	:
23 24	97229	02771	97421	02579	00192	99808	
24	97363	02637	97556	02444	00193	99807	13
25 26 27 28	8.97496	11.02504	8.97691	11.02309	10.00194	9.99806	13
20	97629	02371	97825	02175	00196	99804 99803	
27	97762 97894	02238 02106	97959 98092	02041 01908	00197 00198	99802	
20	98026	01974	98225	01775	00199	99801	
29 80	8.98157	11.01843	8.98358	11.01642	10.00200	9.99800	
81	98288	01712	98490	01510	00202	99798	
32	98419	01581	98622	01378	00203	99797	13
83	98549	01451	98753	01247	00204	99796	
34	98679	01321	98884	01116	00205	99795	
85	8.98808	11.01192	8.99015	11.00985	10.00207	9.99793	13
B6	98937	01063	99145	00855	00208	99792	1:
B6 B7 B8 B9	99066	00934	99275	00725	00209	99791	
88	99194	00806	99405	00595	00210	99790	13
39	99322	00678	99534	00466	00212	99788	
10	8.99450	11.00550	8.99662	11.00338	10.00213	9.99787	
11	99577	00423	99791	00209	00214	99786	
12 13	99704	00296	99919	00081	00215	99785 99783	
13 14	99830 99956	00170	9.00046 00174	10.99954 99826	00217 00218	99782	1
14 15	9.00082	10.99918	9.00301	10.99699	10.00218	9.99781	1
16	00207	99793	00427	99573	00220	99780	
17	00332	99668	00427 00553	99447	00222	99778	13
48	00456	99544	00679	99321	00223	99777	Е
49	00581	99419	00805	99195	00224	99777 99776	
50	9.00704	10.99296	9.00930	10.99070	10.00225	9.99775	13
50 51	00828	99172	01055	98945	00227	99773	
52 53 54 55 56 57	00951	99049	01179	98821	00228	99772	1
53	01074	98926	01303	98697	00229	99771	1
54	01196	98804	01427	98573	00231	99769	1
55	9.01318	10.98682	9.01550	10.98450	10.00232	9.99768	
06	01440	98560	01673	98327	00233	99767	1
07	01561	98439	01796	98204	00235 00236	99765 99764	1
58 59	01682	98318 98197	01918	98082 97960	00236	99763	
60 I	01803 01923	98197	02040 02162	97900 97838	00239	99761	
_							- -
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	

6°			Logar	ithms.			173°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.01923	10.98077	9.02162	10.97838	10.00239	9.99761	60
1	02043	97957	02283	97717	00240	99760	59
2	02163	97837	02404	97596	00241	99759	58
2 8 4	02283	97717	02525 02645	97475	00243 00244	99757	57 56
5	02402 9.02520	97598 10.97480	9.02766	97355 10.97234	10.00244	99756 9.99755	55
5 6 7 8 9	02639	97361	02885	97115	00247	99753	54
7	02757	97243	03005	96995	00248	99752	53
8	02874	97126	03124	96876	00249	99751	52
9	02992	97008	03242	96758	00251	99749	51
10	9.03109	10.96891	9.03361	10.96639	10.00252	9.99748	50
11	03226 03342	96774 96658	03479 03597	96521 96403	00253 00255	99747 99745	49
12 13	03458	96542	03714	96286	00256	99744	47
14	03574	96426	03832	96168	00258	99742	46
15	9.03690	10.96310	9.03948	10.96052	10.00259	9.99741	45
16 17	03805	96195	04065	95935 95819	00260	99740	44
17	03920	96080	04181	95819	00262	99738	43
18	04034	95966	04297	95703	00263	99737	42
19	04149	95851	04413	95587	00264	99736	41
19 20 21 22 23 24	9.04262 04376	10.95738 95624	9.04528 04643	10.95472 95357	10.00266 00267	9.99734 99733	39
22	04490	95510	04758	95242	00269	99731	38
23	04603	95397	04873	95127	00270	99730	37
24	04715	95285	04987	95013	00272	99728	36
25	9.04828	10.95172	9.05101	10.94899	10.00273	9.99727	35
25 26 27 28 29 30 81	04940	95060	05214	94786	00274	99726	34
27	05052	94948	05328	94672	0)276	99724	33
20	05164 05275	94836 94725	05441 05553	94559 94447	00277 00279	99723 99721	32
80	9.05386	10.94614	9.05666	10.94334	10.00280	9.99720	30
81	05497	94503	05778	94222	00282	99718	29
32 33 34	05607	94393	05890	94110	00283	99717	29 28
83	05717	94283	06002	93998	00284	99716	27
34	05827	94173	06113	93887	00286	99714	26
85	9.05937	10.94063	9.06224	10.93776	10.00287	9.99713	25
97	06046 06155	93954 93845	06335 06445	93665 93555	00289 00290	99711 99710	24
86 87 88 89	06264	93736	06556	93444	00292	99708	23 22
39	06264 06372	93628	06666	93334	00293	99707	21
40 41	9.06481	10.93519	9.06775	10.93225	10.00295	9.99705	20
41	06589	93411	06885	93115	00296	99704	19
42	06696	93304	06994	93006	00298	99702	18
43 44	06804	93196	07103	92897	00299	99701	17
45	06911 9.07018	93089 10.92982	9.07211 9.07320	92789 10.92680	00301	99699	16
46	07124	92876	07428	92572	10.00302 00304	9.99698 99696	15 14
47	07231	02760	07536	92464	00305	99695	13
48	07337	92663	07643	92357	00307	99693	12
49	07442	92558	07751	92249	00308	99692	11
50 51	9.07548	10.92452	9.07858	10.92142	10.00310	9.99690	10
51	07653	92347	07964	92036	.00311	99689	9
52 53 54	07758 07863	92242	08071	91929	00313	99687	8
54	07868	92137 92032	08177 08283	91823 91717	00314 00316	99686 99684	8
55	9.08072	10.91928	9.08389	10.91611	10.00317	9.99683	8 7 6 5
56	08176	91824	08495	91505	00319	99681	4
57	08280	91720	08600	91400	00320	99680	3
55 56 57 58 59	08383	91617	08705	91295	00322	99678	2
59	08486	91514	08810	91190	00323	99677	3 2 1 0
60	08589 	91411	08914	91086	00325	99675	-
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

7 °				1	172°		
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.08589	10.91411	9.08914	10.91086	10.00325	9.99675	60
1	08692	91308 91205	09019	90981	00326	99674	59
3	08795 08897	91205	09123 09227	90877 90773	00328 00330	99672 99670	58 57
4	08999	91001	09330	90670	00331	99669	56
4 5	9.09101	10.90899	9.09434	10.90566	10.00333 00334	9.99667	55
6	09202	90798	09537	90463	00334	99666	54
6 7 8 9	093/4	90696	09640	90360	00336	99664	53
8	09405 09506	90595 90494	09742 09845	90258 90155	00337 00339	99663 99661	52 51
10	9.09606	10.90394	9.09947	10.90053	10.00341	9.99659	50
11	09707	90293	10049	89951	00342	99658	49
12	09807	90193	10150	89850	00344	99656	48
13	09907	90093	10252	89748	00345	99655	47
14 15	10006 9.10106	89994 10.89894	10353 9.10454	89647 10.89546	00347 10.00349	99653 9.99651	46 45
16	10205	89795	10555	89445	00350	99650	44
17	10304	89696	10656	89344	00352	99648	43
18	10402	89598	10756	89244	00353	99647	42
19	10501	89499	10856 9.10956	89144	00355	99645	41
20 21	9.10599	10.89401	9.10956	10.89044	10.00357	9.99643	40
21	10697 10795	89303 89205	11056 11155	88944 88845	00358 00360	99642 99640	39 38
22 23	10893	89107	11254	88746	00362	99638	37
24	10990	89010	11353	88647	00363	99637	36
25 26	9.11087	10.88913	9.11452	10.88548	10.00365	9.99635	35
26	11184	88816	11551	88419	00367	99633	34
27 28	11281 11377	88719 88623	11649 11747	88351 88253	00368 00370	99632 99630	33 32
29	11474	88526	11845	88155	00371	99629	31
29 30	9.11570	10.88430	9.11943	10.88057	10.00373	9.99627	30
81	11666	88334	12040	87960	00375	99625	29
82	11761	88239	12138	87862	00376	99624	28
83 84	11857 11952	88143 88048	12235 12332	87765	00378 00380	99622 99620	27 26
35	9.12047	10.87953	9.12428	87668 10.87572	10.00382	9.99618	25
86	12142	87858	12525	87475	00383	99617	24
87	12236	87764	12621	87379	00385	99615	23 22
88	12331	87669	12717	87283	00387	99613	
39 40	12425 9.12519	87575 10.87481	12813 9.12909	87187	00388 10.00390	99612 9.99610	21 20
41	12612	87388	13004	10.87091 86996	00392	99608	19
42	12706	87294	13099	86901	00393	99607	18
43	12799	87201	13194	86806	00395	99605	17
44	12892	87108	13289	86711	00397	99603	16
45	9.12985	10.87015	9.13384	10.86616	10.00399	9.99601 99600	15
46 47	13078 13171	86922 86829	13478 13573	86522 86427	00400 00402	99598	14 13
48	13263	86737	13667	86333	00404	99596	12
49	13355	86645	13761	86239	00405	99595	11
50	9.13447	10.86553	9.13854	10.86146	10.00407	9.99593	10
51	13539	86461	13948	86052	00409	99591	9
52 53	13630 13722	86370 86278	14041 14134	85959 85866	00411 00412	99589 9 9 588	8 7
54	13813	86187	14227	85773	00412	99586	6
55	9.13904	10.86096	9.14320	10.85680	10.00416	9.99584	6
55 56	13994	86006	14412	85588	00418	99582	4
57	14085	85915	14504	85496	00419	99581	3
58 59	14175	85825	14597	85403	00421	99579	1
60	14266 14356	85734 85644	14688 14780	85312 85220	00423 00425	99577 99575	ò
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

80			Logar	ithens.			171°
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.14356	10.85644	9.14780	10.85220	10.00425	9.99575	60
1	14445	85555	14872	85128	00426	99574	59
2	14535 14624	85465	14963 15054	85037	00428 00430	99572 99570	58 57
3 4 5 6 7 8 9	14024	85376 85286	15145	84946 84855	00432	99568	56
5	9.14803	10.85197	9.15236	10.84764	10.00434	9.99566	55
6	14891	85109	15327	84673	00435	99565	54
7	14980	85020	15417	84583	00437	99563	53
8	15069	84931 84843	15508	84492 84402	00439 00441	99561 99559	52 51
10	15157 9.15245	10.84755	15598 9.15688	10.84312	10.00443	9.99557	50
11	15333	84667	15777	84223	00444	99556	49
11 12 13	15421	84579	15867	84133	00446	99554	48
13	15508	84492	15956	84044	00448	99552	47
14	15596	84404	16046	83954	00450	99550 9.99548	46
15 16	9.15683 15770	10.84317 84230	9.16135 16224	10.83865 83776	10,00452 00454	9.99548	45 44
17	15857	84143	16312	83688	00455	99545	43
18	15944	84056	16401	83599	00457	99543	42
19	16030	83970	16489	83511	00459	99541	41
20	9.16116	10.83884	9.16577	10.83423	10.00461	9.99539	40
19 20 21 22 23	16203	83797	16665	83335	00463	99537	39
22	16289 16374	83711 83626	16753 16841	83247 83159	00465 00467	99535 99533	38 37
23	16460	83540	16928	83072	00468	99532	36
24 25 26	9.16545	10.83455	9.17016	10.82984	10.00470	9.99530	35
26	16631	83369	17103	82897	00472	99528	34
27 28 29	16716	83284	17190	82810	00474	99526	33
28	16801	83199	17277	82723	00476	99524	32
29	16886	83114	17363	82637	00478	99522 9.99520	31
30 31	9.16970 17055	10.83030 82945	9.17450 17536	10.82550 82464	10.00480 00482	9.99520	30 29
32	17139	82861	17622	82378	00483	99517	28
33	17223	82777	17708	82292	00485	99515	28 27
33 34	17307	82693	17794	82206	00487	99513	26
35	9.17391	10.82609	9.17880	10.82120	10.00489	9.99511	25
36 37	17474	82526 82442	17965	82035 81949	00491 00493	99509 99507	24
37	17558 17641	82442	18051 18136	81864	00493	99507	23 22
38 39	17724	82359 82276	18221	81779	00497	99503	21
40	9.17807	10.82193	9.18306	10.81694	10.00499	9.99501	20
41	17890	82110	18391	81609	00501	99499	19
42	17973	82027	18475	81525	00503	99497	18
43 44	18055 18137	81945	18560	81440 31356	00505 00506	99495 99494	17 16
45	9.18220	81863 10.81780	18644 9.18728	10.81272	10.00508	9.99492	15
46	18302	81698	18812	81188	00510	99490	14
47	18383	81617	18896	81104	00512	99488	13
48	18465	81617 81535	18979	81021	00514	99486	12
49	18547	81453	19063	80937	00516	99484	11
50	9.18628	10.81372	9.19146	10.80854	10.00518	9.99482	10
51 52	18709 18 7 90	81291 81210	19229 19312	80771 80688	00520 00522	99480 99478	9
53	18871	81129	19395	80605	00524	99476	8 7
54.	18952	81048	19478	80522	00526	99474	6
55	9.19033	10.80967	9.19561	10.80439	10.00528	9.99472	5
56 57	19113	80887	19643	80357	00530	99470	4
57	19193	80807	19725	80275	00532	99468	3
58 59	19273 19353	80727 80647	19807 19889	80193 80111	00534 00536	99466 99464	3 2 1
60	19433	80567	19971	80029	00538	99462	ō
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

90			Logar	ithms.			170°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.19433	10.80567	9.19971	10.80029	10.00538	9.99462	60
i	19513	80487	20053	79947	00540	99460	59
2 3	19592	80408	20134	79866	00542	99458	58
3	19672	80328	20216	79784 79703	00544 00546	99456 99454	57 56
4	19751 9.19830	80249 10.80170	20297 9.20378	10.79622	10.00548	9.99452	55
5	19909	80091	20459	79541	00550	99450	54
7	19988	80012	20540	79460	00552	99448	53
7 8	20067	79933	20621	79379	00554	99446	52
9	20145	79855	20701	79299	00556	99444	51
10	9.20223	10.79777	9.20782	10.79218	10.00558	9.99442 99440	50 49
11	20302	79698	20862	79138 79058	00560 00562	99438	48
12 13	20380 20458	79620 79542	20942 21022	78978	00564	99436	47
14	20535	79465	21102	78898	00566	99434	46
15	9.20613	10.79387	9.21182	10.78818	10.00568	9.99432	45
16	20691	79309	21261	78739	00571	99429	44
17	20768	79232	21341	78659	00573	99427	43
18	20845	79155	21420	78580	00575	99425 99423	42
19	20922	79078	21499	78501 10.78422	00577 10.00579	9.99421	40
20	9.20999 21076	10.79001 78924	9.21578 21657	78343	00581	99419	39
21 22 23	21153	78847	21736	78264	00583	99417	38
23	21229	78771	21814	78186	00585	99415	37
24 1	21306	78694	21893	78107	00587	99413	36
25 26	9.21382	10.78618	9.21971	10.78029	10.00589	9.99411	35
26	21458	78542	22049	77951	00591	99409	34 33
27 28	21534	78466	22127 22205	77873 77795	00593 00596	99407 99404	32
29	21610 21685	78390 78315	22283	77717	00598	99402	31
30	9.21761	10.78239	9.22361	10.77639	10.00600	9.99400	30
31	21836	78164	22438	77562	00602	99398	29
32	21912	78088	22516	77484	00604	99396	28
33	21987	78013	22593	77407	00606	99394	27 26
34	22062	77938	22670	77330	00608	99392 9,99390	26 25
35 36 37	9.22137 22211	10.77863	9.22747 22824	10.77253 77176	10.00610 00612	99388	24
30	22211	77789 77714	22901	77099	00615	99385	23
38	22361	77639	22977	77023	00617	99383	22
39	22435	77565	23054	76946	00619	99381	21
40	9.22509	10.77491	9.23130	10.76870	10.00621	9.99379	20
41	22583	77417	23206	76794	00623	99377	19
42	22657	77343	23283	76717	00625	99375 99372	18 17
43	22731	77269	23359 23435	76641 76565	00628 00630	99370	16
44 45	22805 9.22878	77195	9.23510	10.76490	10.00632	9.99368	15
46	22952	10.77122 77048	23586	76414	00634	99366	14
47	23025	76975	23661	76339	00636	99364	13
48	23098	76902	23737	76263	00638	99362	12
49	23171	76829	23812	76188	00641	99359	11 10
50	9.23244	10.76756	9.23887	10.76113	10.00643 00645	9.99357 99355	9
51 52	23317 23390	76683 76610	23962 24037	76038 75963	00645	99353	8
53	23390	76538	24112	75888	00649	99351	8 7
54	23535	76465	24186	75814	00652	99348	6
54 55	9.23607	10.76393	9.24261	10.75739	10.00654	9.99346	5
56 57	23679	76321	24335	75665	00656	99344	4
57	23752	76248	24410	75590	00658	99342	3 2
58	23823	76177	24484	75516	00660	99340 99337	1
59	23895	76105 76033	24558 24632	75442 75368	00663 00665	99335	ı
60	23967	70033				!	- -
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

10°			Logar	ithms.			169°
M.	Sine.	Cosecant.	Tangent.	Cotangent	Secant.	Cosine.	M.
0	9.23967	10.76033	9.24632	10.75368	10.00665	9.99335	60
1	24039	75961	24706	75294	00667	99333	59
2	24110	75890	24779	75221	00669	99331	58
3	24181	75819	24853	75147	00672	99328	57
5	24253 9.24324	75747 10.75676	24926 9.25000	75074 10.75000	00674 10.00676	99326 9.99324	56 55
6	24395	75605	25073	74927	00678	99322	54
7	24466	75534	25146	74854	00681	99319	53
8	24536	75464	25219	74781	00683	99317	52
9	24607	75393	25292	74708	00685	99315	51
10	9.24677	10.75323	9.25365	10.74635	10.00687	9.99313	50
11	24748	75252	25437	74563	00690	99310	49
12 13	24818 24888	75182 75112	25510	74490 74418	00692 00694	99308 99306	48
14	24958	75042	25582 25655	74345	00696	99304	46
15	9.25028	10.74972	9.25727	10.74273	10.00699	9.99301	45
16	25098	74902	25799	74201	00701	99299	44
17	25168	74832	25871	74129	00703	99297	43
18	25237	74763	25943	74057	00706	99294	42
19	25307	74693	26015	73985	00708	99292	41
20	9.25376	10.74624	9.26086	10.73914	10.00710	9.99290	40
21 22	25445	74555	26158	73842	00712	99288	39
22	25514	74486	26229	73771	00715	99285 99283	38
23 24	25583 25652	74417	26301 26372	73699 73628	00717 00719	99283	37
24	9.25721	74348 10.74279	9.26443	10.73557	10.00722	9.99278	35
25 26	25790	74210	26514	73486	00724	99276	34
27 28	25858	74142	26585	73415	00726	99274	33
28	25927	74073	26655	73345	00729	99271	32
29	25995	74005	26726	73274	00731	99269	31
80	9.26063	10.73937	9.26797	10.73203	10.00733	9.99267	30 29
31	26131	73869	26867	73133	00736	99264	29
32	26199	73801	26937	73063	00738	99262	28
33 84	26267	73733	27008	72992 72922	00740	99260 99257	27 26
35	26335 9.26403	73665 10.73597	27078 9.27148	10.72852	00743 10.00745	9.99255	25
86	26470	73530	27218	72782	00748	99252	24
87	26538	73462	27288	72712	00750	99250	23
88	26605	73395	27357	72643	00752	99248	22
39	26672	73328	27427	72573	00755	99245	21
40	9.26739	10.73261	9.27496	10.72504	10.00757	9.99243	20
41	26806	73194	27566	72434	00759	99241	19
42	26873	73127	27635	72365	00762	99238	18
43	26940	73060	27704	72296	00764	99236 99233	17 16
45	27007 9.27073	72993 10.72927	27773 9.27842	72227 10.72158	00767 10.00769	9.99231	15
46	27140	72860	27911	72089	00771	99229	14
47	27206	72794	27980	72020	00774	99226	13
48	27273	72727	28049	71951	00776	99224	12
49	27339	72661	28117	71883	00779	99221	11
50	9.27405	10.72595	9.28186	10.71814	10.00781	9.99219	10
51	27471	72529	28254	71746	00783	99217	9
52	27537	72463	28323	71677	00786	99214	8 7
53 54	27602	72398	28391	71609	00788	99212	6
55	27668	72332	28459	71541	10.00793	99209 9.99207	5
56	9.27734 27799	10.72266 72201	9.28527 28595	10.71473 71405	10.00793 00796	9.99207	4
56 57	27864	72136	28662	71338	00798	99202	3
58	27930	72070	28730	71270	00800	99200	3 2
59	27995	72005	28798	71202	00803	99197	1
60	28060	71940	28865	71135	00805	99195	0
M.	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M.

110			Logar	ithms.			168°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.28060	10.71940	9.28865	10.71135	10.00805	9.99195	60
1	28125	71875	28933	71067	00808	99192	59
2	28190	71810	29000	71000	00810	99190	58
2 3 4	28254	71746	29067	70933	00813	99187	57
4	28319 9.28384	71681 10.71616	29134 9.29201	70866 10.70799	00815 10.00818	99185 9.99182	56 55
5	28448	71552	29268	70732	00820	99180	54
7	28512	71488	29335	70665	00823	99177	
8	28577	71423	29402	70598	00825	99175	53 52
9	28641	71359	29468	70532	00828	99172	51
10	9.28705	10.71295	9.29535	10.70465	10.00830	9.99170	50
11	28769	71231	29601	70399	00833	99167	49
12 13	28833	71167	29668	70332	00835	99165	48
13	28896	71104	29734	70266	00838	99162	47
14 15	28960 9.29024	71040 10.70976	29800 9.29866	70200 10.70134	00840 10.00843	99160 9.99157	46 45
16	29087	70913	29932	70068	00845	99155	44
17	29150	70850	29998	70002	00848	99152	43
18	29214	70786	30064	69936	00850	99150	42
19	29277	70723	30130	69870	00853	99147	41
19 20 21	9.29340	10.70660	9.30195	10.69805	10.00855	9.99145	40
21	29403	70597	30261	69739	00858	99142	39
22 23 24	29466	70534	30326	69674	00860	99140	38
23	29529	70471	30391	69609	00863	99137	37
24	29591	70409	30457	69543	00865	99135	36
25 26 27 28	9.29654	10.70346	9.30522	10.69478	10.00868	9.99132	35
26	29716	70284	30587	69413	00870	99130	34
2/	29779 29841	70221 70159	30652 30717	69348 69283	00873 00876	99127 99124	33 32
29	29903	70097	30782	69218	00878	99122	31
30	9.29966	10.70034	9.30846	10.69154	10.00881	9.99119	80
31	30028	69972	30911	69089	00883	99117	30 29
32	30090	69910	30975	69025	00886	99114	28
33	30151	69849	31040	68960	00888	99112	27
84	30213	69787	31104	68896	00891	99109	26
35 36 37	9.30275	10.69725	9.31168	10.68832	10.00894	9.99106	25
36	30336	69664	31233	68767	00896	99104	24
37	30398	69602	31297	68703	00899	99101	23 22
38	30459	69541	31361	68639	00901	99099	21
39 40	30521 9.30582	69479 10.69418	31425 9.31489	68575 10.68511	00904 10.00907	99096 9.99093	20
41	30643	69357	31552	68448	00909	99091	19
42	30704	69296	31616	68384	00912	99088	18
43	30765	69235	31679	68321	00914	99086	17
44	30826	69174	31743	68257	00917	99083	16
45	9.30887	10.69113	9.31806	10.68194	10.00920	9.99080	15
46	30947	69053	31870	68130	00922	99078	14
47	31008	68992	31933	68067	00925	99075	13
48	31068	68932	31996	68004	00928	99072	12
49	31129	68871 10.68811	32059 9.32122	67941 10.67878	00930 10.00933	99070 9.99067	11 10
50 51	9.31189 31250	68750	32122	67815	00936	9.99067	10
52	31310	68690	32248	67752	00938	99062	8
53	31370	68630	32311	67689	00941	99059	8 7
54	31430	68570	32373	67627	00944	99056	6
55	9.31490	10.68510	9.32436	10.67564	10.00946	9.99054	5
56	31549	68451	32498	67502	00949	99051	5 4
57	31609	68391	32561	67439	00952	99048	3
58	31669	68331	32623	67377	00954	99046	3 2 1
59	31728	68272	32685	67315	00957	99043	1
60	31788	68212	32747	67253	00960	99040	0
M.	Comne.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

12°			Logar	ithms.			167°
M.	Sine.	Cosecant.	Tangent.	Cotangent	Secant.	Cosine.	M.
0	9.31788	10.68212	9.32747	10.67253	10.00960	9.99040	60
ĭ	31847	68153	32810	67190	00962	99038	59
2 3	31907	68093	32872	67190 67128	00965	99035	58
3	31966	68093 68034	32933 32995	67067 67005	00968 00970	99032	57
4	32025	67975	32995	67005	00970	99030	56
5	9.32084	10.67916	9.33057	10.66943	10.00973	9.99027	55
6	32143	67857	33119	66881	00976	99024	54
7	32202	67798	33180	66820	00978	99022	53
8	32261	67739	33242	66758 66697	00981 00984	99019	52
10	32319 9.32378	67681 10.67622	33303 9.33365	10.66635	10.00987	99016 9.99013	51 50
11	32437	67563	33426	66574	00989	99011	49
12	32495	67505	33487	66513	00992	99008	48
13	32553	67447	33548	66452	00995	99005	47
14	32612	67388	33609	66391	00998	99002	46
15	9.32670	10.67330	9.33670	10.66330	10.01000	9.99000	45
16	32728	67272	33731	66269	01003	98997	44
16 17	32786	67214	33792	66208	01006	98994	43
18	32844	67156	33853	66147	01009	98991	42
19	32902	67098	33913	66087	01011	98989	41
20	9.32960	10.67040	9.33974	10.66026	10.01014	9.98986	40
21	33018	66982	34034	65966	01017	98983	39
19 20 21 22 23	33075	66925	34095	65905	01020	98980	38
24	33133 33190	66867	34155 34215	65845	01022 01025	98978 98975	37 36
25	9.33248	66810 10.66752	9.34276	65785 10.65724	10.01028	9.98972	35
25 26	33305	66695	34336	65664	01031	98969	34
7	33362	66638	34396	65604	01033	98967	33
28	83420	66580	34456	65544	01036	98964	32
27 28 29	33477	66523	34516	65484	01039	98961	31
30	9.33534	10.66466	9.34576	10.65424	10.01042	9.98958	30
31 32	33591	66409	34635	65365	01045	98955	29
32	33647	66353	34695	65305	01047	98953	28
33	33704	66296	34755	65245	01050	98950	27
4	33761	66239	34814	65186	01053	98947	26
55	9.33818	10.66182	9.34874	10.65126	10.01056	9.98944	25
35 36 37 38 39	33874	66126	34933	65067 65008	01059	98941	24
57	33931 33987	66069 66013	34992 35051	64949	01062 01064	98938 98936	23 22
20	34043	65957	35111	64889	01067	98933	21
10	9.34100	10.65900	9.35170	10.64830	10.01070	9.98930	20
ii l	34156	65844	35229	64771	01073	98927	19
12	34212	65788	35288	64771 64712	01076	98924	18
43	34268	65732	35347	64653	01079	98921	17
14	34324	65676	35405	64595	01081	98919	16
45	9.34380	10.65620	9.35464	10.64536	10.01084	9.98916	15
16	34436	65564	35523	64477	01087	98913	14
17	34491	65509	35581	64419	01090	98910	13
18	34547	65453	35640	64360	01093	98907	12
19	34602	65398	35698	64302	01096	98904	11
50	9.34658	10.65342	9.35757	10.64243	10.01099	9.98901	10
51	34713 34769	65001	35815 35873	64185 64127	01102 01104	98898 98896	9
12	34824	65287 65231 65176	35931	64069	01104	98893	8 7 6
53	34879	65121	35989	64011	01110	98890	6
55	9.34934	10.65066	9.36047	10.63953	10.01113	9.98887	5
55 56	34989	65011	36105	63895	01116	98884	5 4
7	35044	64956	36163	63837	01119	98881	3
8	35099	64901	36221	63779	01122	98878	1 2
59	35154	64846	36279	63721	01125	98875	1
50	35209	64791	36336	63664	01128	98872	0
	Cosine.	Secant.	Cotangent.	Tangeut.	Cosecant.	Sine.	M.

13°			Logar	ithms.			166°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.35209	10.64791	9.36336	10.63664	10.01128	9.98872	60
1	35263	64737	36394	63606	01131	98869	59
3	35318 35373	64682	36452 36509	63548 63491	01133	98867	58
3	35427	64627 64573	36566	63434	01136 01139	98864 98861	57 56
4 5	9.35481	10.64519	9.36624	10.63376	10.01142	9.98858	55
6	35536	64464	36681	63319	01145	98855	54
7	35590	64410	36738	63262	01148	98852	53
8	35644	64356	36795	63205	01151	98849	52
9	35698	64302	36852	63148	01154	98846	51
10 11	9.35752 35806	10.64248	9.36909	10.63091	10.01157	9.98843	50
12	35860	64194 64140	36966 37023	63034 62977	01160 01163	98840 98837	49 48
13	35914	64086	37080	62920	01166	98834	47
14	35968	64032	37137	62863	01169	98831	46
15	9.36022	10.63978	9.37193	10.62807	10.01172	9.98828	45
16	36075	63925	37250	62750	01175	98825	44
17	36129	63871	37306	62694	01178	98822	43
18	36182	63818	37363	62637	01181	98819	42
19	36236	63764	37419	62581	01184	98816	41
20	9.36289	10.63711	9.37476	10.62524	10.01187	9.98813	40
21 22	36342 36395	63658 63605	37532 37588	62468 62412	01190	98810 98807	39
23	36449	63551	37644	62356	01193 01196	98804	38
24	36502	63498	37700	62356 62300	01199	98801	36
25	9.36555	10.63445	9.37756	10.62244	10.01202	9.98798	35
26	36608	63392	37812	62188	01205	98795	34
27	36660	63340	37868	62132	01208	98792	33
28	36713	63287	37924	62076	01211	98789	32
29	36766	63234	37980	62020	01214	98786	31
30	9.36819	10.63181	9.38035	10.61965	10.01217	9.98783	30
31 32	36871 36924	63129 63076	38091 38147	61909 61853	01220 01223	98780 98777	29 28
33	36976	63024	38202	61798	01225	98774	27
34	37028	62972	38257	61743	01229	98771	26
35	9.37081	10 6:010	9.38313	10.61687	10.01232	9.98768	25
36	37133	62867	38368	61632	01235	98765	24
37	37185	02815	38423	61577	01238	98762	23
38	37237	62763	38479	61521	01241	98759	22
39	37289 9,37341	62711	38534	61466	01244	98756	21
40 41	37393	10.62659 62607	9.38589 38644	10.61411 61356	10.01247 01250	9.98753	20
42	37445	62555	38699	61301	01254	98750 98746	19 18
43	37497	62503	38754	61246	01257	98743	17
44	37549	62451	38808	61192	01260	98740	16
45	9.37600	10.62400	9.38863	10.61137	10.01263	9.98737	15
46	37652 37703	62348 62297	38918	61082	01266	98734	14
47	37703	62297	38972	61028	01269	98731	13
48	37755	62245	39027	60973	01272	98728	12
49	37806 9.37858	62194	39082	60918	01275	98725	11
50 51	37909	10.62142 62091	9.39136 39190	10.60864 60810	10.01278 01281	9.98722 98719	10
52	37960	62040	39245	60755	01285	98715	8
53	38011	61989	39299	60701	01288	98712	8 7
51	38062	61938	39353	60647	01291	98709	6
55	9.38113	10.61887	9.39407	10.60593	10.01294	9.98706	6 5 4
56	38164	61836	39461	60539	01297	98703	4
57	38215	61785 61734	39515	60485	01300	98700	3
58	38266	61734	39569	60431	01303	98697	3 2 1
59 60	38317 38368	61683 61632	39623 39677	60377 60323	01306 01310	98694 98690	0
-00	00000	01032	39077	00023	01910	20020	<u></u>
M.	Cosine,	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.
1039	,						760

140			Logar	ithms.			165°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.38368	10.61632	9.39677	10.60323	10.01310	9.98690	60
1	38418	61582	39731	60269	01313	98687	59
3	38469	61531	39785	60215	01316	98684	58
3	38519	61481	39838	60162	01319	98681	57
4 5	38570 9.38620	61430	39892 9.39945	60108 10.60055	01322 10.01325	98678 9.98675	56 55
6	38670	10.61380 61330	39999	60001	01329	98671	54
6 7 8 9	38721	61279	40052	59948	01332	98668	53
8	38771	61279 61229	40106	59894	01335	98665	52
9	38821	61179	40159	59841	01338	98662	51
10	9.38871	10.61129	9.40212	10.59788	10.01341	9.98659	50
11	38921	61079	40266	59734	01344	98656	49
12 13	38971	61029	40319	59681	01348	98652	48
14	39021 39071	60979 60929	40372 40425	59628 59575	01351 01354	98649 98646	47
15	9.39121	10.60879	9.40478	10.59522	10.01357	9.98643	45
16	39170	60830	40531	59469	01360	98640	44
iř	39220	60780	40584	59416	01364	98636	43
18	39270	60730	40636	59364	01367	98633	42
19 20 21 22 23	39319	60681	40689	59311	01370	98630	41
20	9.39369	10.60631	9.40742	10.59258	10.01373	9.98627	40
21	39418	60582	40795	59205	01377	98623	39
22	39467	60533	40847	59153	01380	98620	38
23 24	39517	60483	40900	59100	01383	98617	37
24	39566 9.39615	60434 10.60385	40952 9.41005	59048 10.58995	01386 10.01390	98614 9.98610	36 35
26	39664	60336	41057	58943	01393	9.98607	34
27	39713	60287	41109	58891	01396	98604	33
28	39762	60238	41161	58839	01399	98601	32
29	39811	60189	41214	58786	01403	98597	31
25 26 27 28 29 30 31 32	9.39860	10.60140	9.41266	10.58734	10.01406	9.98594	30 29
31	39909	60091	41318	58682	01409	98591	29
32	39958	60042	41370	58630	01412	98588	28 27
33 34	40006	59994	41422	58578	01416	98584	27 26
95	40055 9.40103	59945 10,59897	41474	58526 10.58474	01419 10.01422	98581 9.98578	25
35 36 37 38 39	40152	59848	9.41526 41578	58422	01426	98574	24
87	40200	59800	41629	58371	01429	98571	23
38	40249	59751	41681	58319	01432	98568	22
39	40297	59703	41733	58267	01435	98565	21
40	9.40346	10.59654	9.41784	10.58216	10.01439	9.98561	20
41	40394	59606	41836	58164	01442	98558	19
42	40442	59558	41887	58113	01445	98555	18
43 44	40490	59510	41939	58061	01449	98551	17
45	40538 9.40586	59462 10.59414	41990 9.42041	58010 10.57959	01452 10.01455	98548 9.98545	16 15
46	40634	59366	42093	57907	01459	9.98545 98541	14
47	40682	59318	42144	57856	01462	98538	13
48	40730	59270	42195	57805	01465	98535	12
49	40778	59222	42246	57754	01469	98531	11
50	9.40825	10.59175	9.42297	10.57703	10.01472	9.98528	10
51	40873	59127	42348	57652	01475	98525	9
52 53 54 55	40921	59079	42399	57601	01479	98521	8 7
54	40968 41016	59032	42450	57550	01482	98518	7
55	9.41063	58984 10.58937	42501 9.42552	57499	01485	98515 9.98511	6 5
56	41111	58889	9.42552 42603	10.57448	10.01489 01492	9.98511	4
56 57	41158	58842	42653	57397 57347	01492	98505	3
58	41205	58795	42704	57296	01499	98501	2
58 59	41252	58748	42755	57245	01502	98498	Ĩ
60	41300	58700	42805	57195	01506	98494	0
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

15°			Logar	ithms.			164°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.41300	10.58700	9.42805	10.57195	10.01506	9.98494	60
i	41347	58653	42856	57144	01509	98491	59
3	41394	58606	42906	57094	01512 01516	98488 98484	58 57
3	41441 41488	58559 58512	42957 43007	57043 56993	01519	98481	56
5	9.41535	10.58465	9.43057	56993 10.56943	10.01523	9.98477	55
5 6	41582	58418	43108	56892	01526	98474	54
7	41628	58372 58325	43158	56842	01529	98471	53
8	41675 41722	58325	43208 43258	56792 56742	01533 01536	98467 98464	52 51
9 10	9.41768	58278 10.58232	9.43308	10.56692	10.01540	9.98460	50
11	41815	58185	43358	56642	01543	98457	49
12	41861	58139	43408	56592	01547	98453	48
13	41908	58092	43458	56542	01550	98450	47
14	41954	58046	43508	56492	01553	98447 9.98443	46 45
15	9.42001	10.57999	9.43558 43607	10.56442 56393	10.01557 01560	98440	44
16 17	42047 42093	57953 57907	43657	56343	01564	98436	43
18	42140	57860	43707	56293	01567	98433	42
19	42186	57814 10.57768 57722	43756	56244	01571	98429	41
20	9.42232	10.57768	9.43806	10.56194	10.01574	9.98426	40
21	42278	57722	43855	56145	01578	98422 98419	39 38
22 23	42324	57676	43905 43954	56095 56046	01581 01585	98415	37
23	42370 42416	57630 57584	43934	55996	01588	98412	36
25	9.42461	10.57539	9.44053	10.55947	10.01591	9.98409	35
26	42507	57493	44102	55898	01595	98405	34
26 27	42553	57447	44151	55849	01598	98402	33
28	42599	57401	44201	55799	01602	98398 98395	32 31
29 30	42644	57356 10.57310	44250 9.44299	55750	01605 10.01609	9.98391	30
80	9.42690 42735	57265	44348	10.55701 55652	01612	98388	29
31 32	42781	57219	44397	55603	01616	98384	28
33	42826	57174	44446	55603 55554	01619	98381	27
33 34	42872	57128	44495	55505	01623	98377	26
35	9.42917	10.57083	9.44544	10.55456	10.01627	9.98373 98370	25 24
36	42962	57038	44592 44641	55408 55359	01630 01634	98366	23
37 38 39	43008 43053	56992 56947	44690	55310	01637	98363	22
30	43098	56902	44738	55262	01641	98359	21
40	9.43143	10.56857	9.44787	10.55213 55164	10.01644	9.98356	20
41	43188	56812	44836	55164	01648	98352	19
42	43233	56767	44884	55116	01651	98349 98345	18 17
43	43278 43323	56722	44933 44981	55067 55019	01655 01658	98342	16
44 45	9.43367	56677 10,56633	9.45029	10.54971	10.01662	9.98338	15
46	43412	56588	45078	54922	01666	98334	14
47	43457	56543	45126	54874	01669	98331	13 12
48	43502	56498	45174	54826	01673	98327	12 11
49	43546	56454	45222 9.45271	54778	01676	98324 9,98320	10
50	9.43591	10.56409	9.45271	10.54729 54681	10.01680 01683	9.98320	10
51 52	43635 43680	56365 56320	45319 45367	54633	01687	98313	8
53	43724	56276	45415	54585	01691	98309	8 7
54	43769	56231	45463	54537	01694	98306	6 5
55 56 57	9.43813	10.56187	9.45511	10.54489	10.01698	9.98302	5
56	43857	56143	45559	54441	01701	98299 98295	4
57	43901	56099	45606 45654	54394 54346	01705 01709	98290	3 2
58 59	43946 43990	56054 56010	45702	54298	01712	98288	ĩ
60	44034	55966	45750	54250	01716	98284	ō
M.	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M.

16°			Logar	ithms.			163°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine,	M.
0	9.44034	10.55966	9.45750	10.54250	10.01716	9.98284	60
1	44078	55922	45797	54203	01719	98281	59
3	44122	55878	45845	54155	01723	98277	58
3	44166	55834	45892	54108	01723 01727	98273	57
4	44210	55790	45940	54060	01730	98270	56
5	9.44253	10.55747	9.45987	10.54013	10.01734	9.98266	55
6	44297 44341	55703 55659	46035 46082	53965 53918	01738 01741	98262 98259	54 53
7 8	44385	55615	46130	53870	01741	98255 98255	52
9	44428	55572	46177	53823	01749	98251	51
10 I	9.44472	10.55528	9.46224	10.53776	10.01752	9.98248	50
11	44516	55484	46271	53729	01756	98244	49
12	44559	55441	46319	53681	01760 01763	98240	48
13	44602	55398	46366	53634	01763	98237	47
14	44646	55354	46413	53587	01767	98233	46
15	9.44689	10.55311	9.46460	10.53540	10.01771	9.98229	45
16 17	44733 44776	55267 55224	46507 46554	53493 53446	01774 01778	98226 98222	44
18	44819	55181	46601	53399	01789	98218	42
19	44862	55138	46648	53352	01782 01785	98215	41
20	9.44905	10.55095	9.46694	10.53306	10.01789	9.98211	40
21	44948	55052	46741	53259	01793	98207	89
22	44992	55008	46788	53212	01796	98204	38
23	45035	54965	46835	53165	01800	98200	37
24	45077	54923	46881	53119	01804	98196	36
25	9.45120	10.54880	9.46928	10.53072	10.01808	9.98192	35
21 22 23 24 25 26 27 28 29 30	45163 45206	. 54837	46975	53025	01811	98189	34
29	45249	54794 54751	47021 47068	52979 52932	01815 01819	98185 98181	33
29	45292	54708	47114	52886	01823	98177	31
30	9.45334	10.54666	9.47160	10.52840	10.01826	9.98174	30
31	45377	54623	47207	52793	01830	98170	29
82	45419	54581	47253	52747	01834	98166	28
33	45462	54538	47299	52701	01838	98162	27
34 35	45504	54496	47346	52654	01841	98159	26
36	9.45547 45589	10.54453 54411	9.47392 47438	10.52608 52562	10.01845 01849	9.98155	25 24
37	45632	54368	47484	52516	01853	98151 98147	23
38	45674	54326	47530	52470	01856	98144	22
39	45716	54284	47576	52424	01860	98140	21
40	9.45758	10.54242	9.47622	10.52378	10.01864	9.98136	20
41	45801	54199	47668	52332	01868	98132	19
42	45843	54157	47714	52286	01871	98129	18
43	45885	54115	47760	52240	01875	98125	17
44 45	45927 9.45969	54073 10.54031	47806 9.47852	52194 10.52148	01879 10.01883	98121 9.98117	16 15
46	46011	53989	47897	52103	01887	9.98117	14
47	46053	53947	47943	52057	01890	98110	13
48	46095	53905	47989	52011	01894	98106	12
49	46136	53864	48035	51965	01898	98102	11
50	9.46178	10.53822	9.48080	10.51920	10.01902	9.98098	10
51	46220	53780	48126	51874	01906	98094	9
52 53	46262	53738	48171	51829	01910	98090	8
54	46303 46345	53697	48217	51783	01913	98087	1
55	46345 9.46386	53655 10.53614	48262 9.48307	51738 10.51693	01917 10.01921	98083 9.98079	9 8 7 6 5
55 56 57	46428	53572	48353	51647	01925	9.98079	4
57	46469	53531	48398	51602	01929	98071	3
58 59	46511	53489	48443	51557	01933	98067	3 2 1
59	46552	53448	48489	51511	01937	98063	1
60	46594	53406	48534	51466	01940	98060	0
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Coeine,	M
							-
0	9.46594 46635	10.53406 53365	9.48534 48579	10.51466 51421	10.01940 01944	9.98060 98056	60
1 2	46676	53324	48624	51376	01948	98052	58
3	46717	53283	48669	51991	01952	98048	57
4	46758	53242	48714	51331 51286	01956	98044	56
5	9.46800	10.53200	9.48759	10.51241	10.01960	9.98040	56
6	46841	53159	48804	51196	01964	98036	54
5 6 7	46882	53118	48849	51151	01968	98032	53
8	46923	53077	48894	51106	01971	98029	5
9	46964	53036	48939	51061	01975	98025	5
10	9.47005	10.52995	9.48984	10.51016	10.01979	9.98021	50
11	47045	52955	49029	50971	01983	98017	49
12	47086	52914	49073	50927	01987	98013	4
13	47127	52873	49118	50882	01991	98009	4
14	47168	52832	49163	50837	01995	98005	40
15	9.47209	10.52791	9.49207	10.50793	10.01999	9.98001	44
16	47249	52751	49252 49296	50748	02003 02007	97997 9 7993	43
17	47290	52710	49296	50704	02007	97993 97989	4
18 19	47330 47371	52670 52629	49385	50659 50615	02011	97986	4
20	9.47411	10.52589	9.49430	10.50570	10.02018	9.97982	4
21	47452	52548	49474	50526	02022	97978	3
22	47492	52508	49519	50481	02026	97974	3
23	47533	52467	49563	50437	02030	97970	3
24	47573	52427	49607	50393	02034	97966	3
25	9.47613	10.52387	9.49652	10.50348	10.02038	9.97962	3
26	47654	52346	49696	50304	02042	97958	3
27	47694	52306	49740	50260	02046	97954	3
28	47734	52266	49784	50216	02050	97950	3
29	47774	52226	49828	50172	02054	97946	3
30	9.47814	10.52186	9.49872	10.50128	10.02058	9.97942	3 2
31	47854	52146	49916	50084	02062	97938	2
32	47894	52106	49960	50040	02066	97934	2
33	47934	52066	50004	49996	02070	97930	2
34	47974	52026	50048	49952	02074	97926	2
35	9.48014	10.51986	9.50092	10.49908	10.02078	9.97922	
36	48054	51946	50136	49864	02082 02086	97918 97914	2 2
87	48094	51906	50180	49820	02090	97914 97910	2
88 · 89	48133	51867	50223	49777 49733	02094	97906	2
10	48173	51827	50267 9.50311	10.49689	10.02098	9.97902	2
ii	9.48213 48252	10.51787 51748	50355	49645	02102	97898	lī
12	48292	51748	50398	49602	02102	97894	li
13	48332	51668	50442	49558	02110	97890	1 î
14	48371	51629	50485	49515	02114	97886	1 ī
15	9.48411	10.51589	9.50529	10.49471	10.02118	9.97882	ī
16	48450	51550	50572	49428	02122	97878	1.
17	48490	51510	50616	49384	02126	97874	1
18	48529	51471	50659	49341	02130	97870	1
49	48568	51432	50703	49297	02134	97866	1
50	9.48607	10.51393	9.50746	10.49254	10.02139	9.97861	1
51	48647	51353	50789	49211	02143	97857	
52	48686	51314	50833	49167	02147	97853	
3	48725	51275	50876	49124	02151	97849	'
54	48764	51236	50919	49081	02155	97845	
55	9.48803	10.51197	9.50962	10.49038	10.02159	9.97841	
6	48842	51158	51005	48995	02163	97837	1 :
57	48881	51119	51048	48952	02167	97833	
58	48920	51080	51092	48908	02171	97829	
59 60	48959	51041 51002	51135 51178	48865 48822	02175 02179	97825 97821	1
w	48998	51002	511/8	40022	02179	71041	_ _
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M

180			Logar	ithms.			161°
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.48998	10.51002	9.51178	10.48822	10.02179	9.97821	60
1	49037	50963	51221	48779	02183	97817	59
2 3	49076	50924	51264	48736	02188	97812	58
3	49115	50885 50847	51306 51349	48694 48651	02192 02196	97808 97804	57 56
4 5 6	49153 9.49192	10.50808	9.51392	10.48608	10.02200	9.97800	55
6	49231	50769	51435	48565	02204	97796	54
7	49269	50731	51478	48522	02208	97792	53
8	49308	50692	51520	48480	02212	97788	52
9	49347	50653	51563	48437	02216	97784	51
10	9.49385	10.50615	9.51606	10.48394 48352	10.02221 02225	9.97779 97775	50 49
11 12	49424 49462	50576 50538	51648 51691	48309	02229	97771	48
13	49500	50500	51734	48266	02233	97767	47
14	49539	50461	51776	48224	02237	97763	46
15	9.49577	10.50423	9.51819	10.48181	10.02241	9.97759	45
16	49615	50385	51861	48139	02246	97754	44
17	49654	50346	51903	48097	02250	97750	43
18	49692	50308	51946	48054 48012	02254 02258	97746 97742	42
19 20	49730 9.49768	50270 10.50232	51988 9.52031	10.47969	10.02262	9.97738	40
21	49806	50194	52073	47927	02266	97734	39
22	49844	50156	52115	47885	02271	97729	38
23 24	49882	50118	52157	47843	02275	97725	37
24	49920	50080	52200	47800	02279	97721	36
25 26	9.49958	10.50042	9.52242	10.47758	10.02283	9.97717	35
26	49996	50004	52284	47716 47674	02287 02292	97713 97708	34 33
27 28 29	50034 50072	49966 49928	52326 52368	47632	02296	97704	32
29	50110	49890	52410	47590	02300	97700	31
30	9.50148	10.49852	9.52452	10.47548	10.02304	9.97696	30
30 31	50185	49815	52494	47506	02309	97691	29
82	50223	49777	52536	47464	02313	97687	28
33 34	50261	49739	52578	47422	02317 02321	97683	27 26
95	50298 9.50336	49702 10.49664	52620 9.52661	47380 10.47339	10.02326	97679 9.97674	25
35 36 37	50374	49626	52703	47297	02330	97670	24
37	50411	49589	52703 52745	47297 47255 47213	02334	97666	23
38 39	50449	49551	52787	47213	02338	97662	22
39	50486	49514	52829	47171	02343	97657	21
40	9.50523	10.49477	9.52870	10.47130	10.02347	9.97653	20
41	50561	49439	52912 52953	47088 47047	02351 02355	97649 97645	19 18
42	50598 50635	49402 49365	52995	47005	02360	97640	17
44	50673	49327	53037	46963	02364	97636	16
45	9.50710	10.49290	9.53078	10.46922	10.02368	9.97632	15
46	50747	49253	53120	46880	02372	97628	14
47	50784	49216	53161	46839	02377 02381	97623	13
48	50821	49179	53202	46798	02381	97619	12 11
49	50858 9.50896	49142 10.49104	53244 9.53285	46756 10.46715	02385 10.02390	97615 9.97610	10
50 51	50933	49067	53327	46673	02394	97606	9
52	50970	49030	53368	46632	02398	97602	
53	51007	48993	53409	46591	02403	97597	8 7
54	51043	48957	53450	46550	02407	97593	6
55 56 57	9.51080	10.48920	9.53492	10.46508	10.02411	9.97589	5 4
56	51117	48883	53533 53574	46467	02416 02420	97584	4
57	51154 51191	48846 48809	53574 53615	46426 46385	02420	97580 97576	3
58 59	51191 51227	48809	53656	46344	02424	97576 97571	3 2 1
60	51264	48736	53697	46303	02433	97567	ō
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

108*

190			Logar	ithms.	•		160°
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.51264	10.48736	9.53697	10.46303	10.02433	9.97567	60
1	51301	48699	53738	46262	02437	97563	59
3	51338 51374	48662	53779 53820	46221	02442	97558	58
4	51374	48626	53820 53861	46180	02446	97554	57
5	51411 9.51447	48589 10.48553	9.53902	46139 10.46098	02450 10.02455	97550 9.97545	56 55
5 6	51484	48516	53943	46057	02459	97541	54
7	51520	48480	53984	46016	02464	07596	53
8	51557	48443	54025	45975	02468	97532	52
9	51593	48407	54065	45935	02472	9/528	51
10 11	9.51629	10.48371 48334	9.54106 54147	10.45894 45853	10.02477 02481	9.97523	50
12	51666 51702	48298	54187	45813	02481	97519 97515	49 48
13	51738	48262	54228	45772	02490	97510	47
14	51774	48226	54269	45731	02494	97506	46
15	9.51811	10.48189	9.54309	10.45691	10.02499	9.97501	45
16	51847	48153	54350	45650	02503	97497	44
17	51883	48117 48081	54390	45610	02508	97492	43
18 19 20 21 22 23	51919 51955	48045	54431 54471	45569 45529	02512 02516	97488 97484	42
20	9.51991	10.48009	9.54512	10.45488	10.02521	9.97479	40
21	52027	47973	54552	45448	02525	97475	39
22	52063	47937	54593	45407	02530	97470	38
23	52099	47901	54633	45367	02534	97466	37
24	52135	47865	54673	45327	02539	97461	36
25 26	9.52171	10.47829	9.54714	10.45286	10.02543	9.97457	35
20	52207 52242	47793 47758	54754 54794	45246 45206	02547 02552	97453 97448	34
28	52278	47722	54835	45165	02556	97444	32
29	52314	47686	54875	45125	02561	97439	31
27 28 29 30 31	9.52350	10.47650	9.54915	10.45085	10.02565	9.97435	.30
31	52385	47615	54955	45045	02570	97430	29
32 33 34	52421 52456	47579 47544	54995	45005	02574	97426	28 27
94	52490 52492	47508	55035 55075	44965 44925	02579 02583	97421 97417	26
35	9.52527	10.47473	9.55115	10.44885	10.02588	9.97412	25
36	52563	47437	55155	44845	02592	97408	24
37	52598	47402	55195	44805	0:2597	97403	23 22
38 39	52634	47366	55235 55275	44765	02601	97399	22
40	52669	47331 10.47295	552/5	44725	02606	97394	21
41	9.52705 52740	47260	9.55315 55355	10.44685 44645	10.02610 02615	9.97390 97385	20 19
42	52775	47225	55395	44605	02619	97381	18
43	52811	47189	55434	44566	02624	97376	17
44	52846	47154	55474	44526	02628	97372	16
45	9.52881	10.47119	9.55514	10.44486	10.02633	9.97367	15
46 47	52916	47084	55554	44446	02637	97363	14
48	52951 52986	47049 47014	55593 55633	44407 44367	02642 02647	97358 97353	13 12
49	53021	46979	55673	44307	02651	97349	111
50	9.53056	10.46944	9.55712	10.44288	10.02656	9.97344	10
51	53092	46908	55752	44248	02660	97340	9
52	53126	46874	55791	44209	02665	97335	8 7
53 54	53161	46839	55831	44169	02669	97331	7
55	53196 9.53231	46804 10.46769	55870 9.55910	44130 10.44090	02674 10.02678	97326 9.97322	6 5 4
55 56	53266	46734	55949	44051	02683	9.97322	1 4
57	53301	46699	55989	44011	02688	97312	3
58	53336	46664	56028	43972	02692	97308	3 2 1
59	53370	46630	56067	43933	02697	97303	
60	53405	46595	56107	43893	02701	97299	0
M.	Cosine,	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

20 °			Logari	ithms.			159°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.53405	10.46595	9.56107	10.43893	10.02701	9.97299	60
1	53440	46560	56146	43854	02706	97294	59
2	53475	46525	56185	43815	02711	97289	58
3	53509	46491	56224	43776	02715	97285	57
4 5	53544 9.53578	46456 10.46422	56264 9.56303	43736	02720 10.02724	97280 9.97276	56 55
6	53613	46387	56342	10.43697 43658	02729	97271	54
6	53647	46353	56381	43619	02734	97266	53
8	53682	46318	56420	43580	02738	97262	52
9	53716	46284	56459	43541	02743	97257	51
10	9.53751	10.46249	9.56498	10.43502	10.02748	9.97252	50
11	53785	46215	56537	43463	02752	97248	49
12	53819	46181	56576	43424	02757	97243 97238	48
13 14	53854 53888	46146 46112	56615 56654	43385 43346	02762 02766	97234	47 46
15	9.53922	10.46078	9.56693	10.43307	10.02771	9.97229	45
16	53957	46043	56732	43268	02776	97224	44
17	53991	46009	56771	43229	02780	97220	43
18	54025	45975	56810	43190	02785	97215	42
19 20	54059	45941	56849	43151	02790	97210	41
20	9.54093	10.45907	9.56887	10.43113	10.02794	9.97206	40
21 22	54127	45873	56926	43074	02799	97201	39
22	54161	45839	56965	43035	02804	97196	38
23 24	54195 54229	45805 45771	57004 57042	42996 42958	02808 02813	97192 97187	37 36
25	9.54263	10.45737	9.57081	10.42919	10.02818	9.97182	35
26	54297	45703	57120	42880	02822	97178	34
27	54331	45669	57158	42842	02827	97173	33
28	54365	45635	57197	42803	02832	97168	32
29	54399	45601	57235	42765	02837	97163	31
30	9.54433	10.45567	9.57274	10.42726	10.02841	9.97159	30 29
31	54466	45534	57312	42688	02846	97154	29
32 33	54500 54534	45500 45466	57351 57389	42649	02851 02855	97149 97145	28 27
34	54567	45433	57428	42611 42572	02860	97140	26
35	9.54601	10.45399	9.57466	10.42534	10.02865	9.97135	25
35 36 37	54635	45365	57504	42496	02870	97130	24
37	54668	45332	57543	42457	02874	97126	23
38	54702	45298	57581	42419	02879	97121	22
39	54735	45265	57619	42381	02884	97116	21
40	9.54769	10.45231	9.57658	10.42342	10.02889	9.97111	20
41 42	54802	45198	57696	42304	02893	97107	19
43	54836 54869	45164 45131	57734 57772	42266 42228	02898 02903	97102 97097	18
44	54903	45097	57810	42190	02908	97092	16
45	9.54936	10.45064	9.57849	10.42151	10.02913	9.97087	15
46	54969	45031	57887	42113	02917	97083	14
47	55003	44997	57925	42075	02922	97078	13
48	55036	44964	57963	42037	02927	97073	12
49	55069	44931	58001	41999	02932	97068	11
50	9.55102	10.44898	9.58039	10.41961	10.02937	9.97063	10
51	55136	44864	58077	41923	02941	97059	9
52 53	55169 55202	44831 44798	58115 58153	41885 41847	02946 02951	97054 97049	8 7 6 5
54	55235	44765	58191	41809	02956	97049	6
55	9.55268	10.44732	9.58229	10.41771	10.02961	9.97039	5
55 56 57	55301	44699	58267	41733	02965	97035	4
57	55334	44666	58304	41696	02970	97030	3
58	55367	44633	58342	41658	02975	97025	3 2 1
59	55400	44600	58380	41620	02980	97020	1
60	55433	44567	58418	41582	02985	97015	0
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

21°			Logar	ithms.		1	158°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.55433	10.44567	9.58418	10.41582	10.02985	9.97015	60
1	55466	44534	58455	41545	02990	97010	59
2	55499	44501	58493	41507	02995	97005	58
3	55532	44468	58531	41469	02999	97001	57
4 5 6	55564 9.55597	44436 10.44403	58569 9.58606	41431 10.41394	03004 10.03009	96996 9.96991	56 55
6	55630	44370	58644	41356	03014	96986	54
7	55663	44337	58681	41319	03019	96981	53
7 8 9	55695	44305	58719	41281	03024	96976	52
9	55728	44272	58757	41243	03029	96971	51
10	9.55761	10.44239	9.58794	10.41206	10.03034	9.96966	50
11	55793	44207	58832	41168	03038	96962	49
12	55826	44174	58869	41131	03043	96957	48
13	55858	44142	58907	41093	03048	96952	47
14 15	55891 9.55923	44109	58944	41056	03053	96947	46
16	55956	10.44077 44044	9.58981 59019	10.41019 40981	10.03058 03063	9.96942 96937	45
17	55988	44012	59056	40944	03068	96932	43
18	56021	43979	59094	40906	03073	96927	42
10	56053	43947	59131	40869	03078	96922	41
20 21 22	9.56085	10.43915	9.59168	10.40832	10.03083	9.96917	40
21	56118	43882	59205	40795	03088	96912	39
22	56150	43850	59243	40757	03093	96907	38
23	56182·	43818	59280	40720	03097	96903	37
24	56215	43785	59317	40683	03102	96898	36
25	9.56247	10.43753	9.59354	10.40646	10.03107	9.96893	35
26	56279	43721	59391	40609	03112	96888	34
27	56311	43689 43657	59429	40571	03117	96883	33 32
20	56343	43625	59466 59503	40534 40497	03122 03127	96878 96873	31
28 29 30	56375 9.56408	10.43592	9.59540	10.40460	10.03132	9.96868	30
31	56440	43560	59577	40423	03137	96863	29
32	56472	43528	59614	40386	03142	96858	28
93	56504	43496	59651	40349	03147	96853	27
34	56536	43464	59688	40312	03152	96848	26
35	9.56568	10.43432	9.59725	10.40275	10.03157	9.96843	25
36	56599	43401	59762	40238	03162	96838	24
37	56631	43369	59799	40201	03167	96833	23
38 39	56663	43337	59835	40165	03172	96828	22
40	56695 9.56727	43305 10.43273	59872	40128	03177	96823 9,96818	21 20
41	56759	43241	9.59909 59946	10.40091 40054	10.03182 03187	9.90515	19
42	56790	43210	59983	40017	03192	96808	18
43	56822	43178	60019	39981	03197	96803	17
44	56854	43146	60056	39944	03202	96798	16
45	9.56886	10.43114	9.60093	10.39907	10.03207	9.96793	15
46	56917	43083	60130	39870	03212	96788	14
47	56949	43051	60166	39834	03217	96783	13
48	56980	43020	60203	39797	03222	96778	12
49	57012	42988	60240	39760	03228	96772	11
50	9.57044	10.42956	9.60276	10.39724	10.03233	9.96767	10
51 52	57075 57107	42925	60313	39687	03238 03243	96762	9
53	57107 57138	42893 42862	60349 60386	39651 39614	03243	96757 96752	8 7
54	57169	42831	60422	39578	03253	96747	6
55	9.57201	10 42799	9.60459	10.39541	10.03258	9.96742	6
56	57232	42768	60495	39505	03263	96737	4
56 57	57264	42736	60532	39468	03268	96732	3
58	57295	42705	60568	39432	03273	96727	3 2 1
59	57326	42674	60605	39395	03278	96722	1
60	57358	42642	60641	39359	03283	96717	0
М.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

22 °			Logar	ithms.			157°
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.57358	10.42642	9.60641	10.39359	10.03283	9.96717	60
1	57389	42611	60677	39323	03289	96711	59
2	57420	42580	60714	39286	03294	96706	58
2 3 4 5 6 7	57451	42549 42518	60750	39250 39214	03299 03304	96701 96696	57 56
4	57482 9.57514	10.42486	60786 9.60823	10.39177	10.03309	9.96691	55
8	57545	42455	60859	. 39141	03314	96686	54
7	57576	42424	60895	39105	03319	96681	53
8	57607	42393	60931	39069	03324	96676	52
9 10	57638	42362	60967	39033	03330	96670	51
10	9.57669	10.42331	9.61004	10.38996	10.03335	9.96665	50
11	57700	42300	61040	38960	03340 03345	96660 96655	49 48
12 13	57731	42269 42238	61076 61112	38924 38888	03350	96650	47
14	57762 57793	42207	61148	38852	03355	96645	46
15	9.57824	10.42176	9.61184	10.38816	10.03360	9.96640	45
16	57855	42145	61220	38780	03366	96634	44
17	57885	42115	61256	38744	03371	96629	43
18	57916	42084	61292	38708	03376	96624	42
19	57947	42053	61328	38672	03381	96619	41
20	9.57978	10.42022	9.61364	10.38636	10.03386 03392	9.96614 96608	40 39
21 22	58008	41992 41961	61400 61436	38600 38564	03392	96603	38
23	58039 58070	41930	61472	38528	03402	96598	37
24	58101	41899	61508	38492	03407	96593	36
24 25 26	9.58131	10.41869	9.61544	10.38456	10.03412	9.96588	35
26	58162	41838	61579	38421	03418	96582	34
27 I	58192	41808	61615	38385	03423	96577	33
28 29	58223	41777	61651	38349	03428	96572	32
29 30	58253	41747 10.41716	61687 9.61722	38313 10.38278	03433 10.03438	96567 9,96562	31 30
31	9.58284 58314	41686	61758	38242	03444	96556	29
32	58345	41655	61794	38206	03449	96551	28
83	58375	41625	61830	38170	03454	96546	27
33 34	58406	41594	61865	38135	03459	96541	26
85	9.58436	10.41564	9.61901	10.38099	10.03465	9.96535	25
86	58467	41533	61936	38064	03470	96530	24 23
37	58497	41503	61972	38028 37992	03475 03480	96525 96520	22
38 39	58527 58557	41473 41443	62008 62043	37957	03486	96514	21
40	9.58588	10.41412	9.62079	10.37921	10.03491	9.96509	20
41	58618	41382	62114	37886	03496	96504	19
42	58648	41352	62150	37850	03502	96498 *	18
43	58678	41322	62185	37815	03507	96493	17
44	58709	41291	62221	37779	03512	96488	16
45	9.58739	10.41261	9.62256	10.37744	10.03517 03523	9.96483 96477	15 14
46	58769	41231 41201	62292 62327	37708 37673	03528	96472	13
47 48	58799 58829	41171	62362	37638	03533	96467	12
49	58859	41141	62398	37602	03539	96461	ii
50	9.58889	10.41111	9.62433	10.37567	10.03544	9.96456	10
51	58919	41081	62468	37532	03549	96451	9
52	58949	41051	62504	37496	03555	96445	8 7
53	58979	41021	62539	37461	03560	96440	7
54	59009	40991	62574	37426 10.37391	03565 10.03571	96435 9.96429	6 5
56 56	9.59039 59069	10.40961 40931	9.62609 62645	37355	03576	9.96429	4
57	59098	40902	62680	37320	03581	96419	
58	59128	40872	62715	37285	03587	96413	3 2 1
59	59158	40842	62750	37250	03592	96408	1
60	59188	40812	62785	37215	03597	96403	ō
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

23°			Logar	ithms.			156°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.59188	10.40812	9.62785	10.37215	10.03597	9.96403	60
1	59218	40782	62820	37180	03603	96397	59
3	59247	40753	62855	37145	03608	96392	58
3	59277	40723	62890 62926	37110 37074	03613 03619	96387 96381	57
4 5 6	59307 9.59336	40693 10.40664	9.62961	10.37039	10.03624	9.96376	56 55
8	59366	40634	62996	37004	03630	96370	54
7	59396	40604	63031	36969	03635	96365	53
8	59425	40575	63066	36934	03640	96360	52
9	59455	· 40545	63101	36899	03646	96354	51
10	9.59484	10.40516	9.63135	10.36865	10.03651	9.96349	50
11 12	59514	40486	63170	36830	03657	96343	49
12	59543	40457	63205	36795	03662	96338 96333	48
13 14	59573 59602	40427 40398	63240 63275	36760 36725	03667 03673	96327	46
15	9.59632	10.40368	9.63310	10.36690	10.03678	9.96322	45
16	59661	40339	63345	36655	03684	96316	44
17	59690	40310	63379	36621	03689	96311	43
18	59720	40280	63414	36586	03695	96305	42
19	59749	40251	63449	36551	03700	96300	41
20	9.59778	10.40222	9.63484	10.36516	10.03706	9.96294	40
21	59808	40192	63519	36481 36447	03711	96289 96284	39
22 23	59837 59866	40163 40134	63553 63588	36412	03716 03722	96278	38 37
24	59895	40105	63623	36377	03727	96273	36
25	9.59924	10.40076	9.63657	10.36343	10.03733	9.96267	35
26	59954	40046	63692	36308	03738	96262	34
27	59983	40017	63726	36274	03744	96256	33
28	60012	39988	63761	36239	03749	96251	32
29	60041	39959	63796	36204	03755	96245	31
30	9.60070	10.39930	9.63830 63865	10.36170 36135	10.03760 03766	9.96240 96234	30 29 28
31 32	60099 60128	39901 39872	63899	36101	03771	96229	29
33	60157	39843	63934	36066	03777	96223	27
84	60186	39814	63968	36032	03782	96218	26
35	9.60215	10.39785	9.64003	10.35997	10.03788	9.96212	25
36	60244	39756	64037	35963	03793	96207	24
37	60273	39727	64072	35928	03799	96201	23
38	60302	39698	64106	35894	03804	96196	22
39	60331	39669	64140	35860 10.35825	03810 10.03815	96190 9.96185	21 20
40 41	9.60359 60388	10.39641 39612	9.64175 64209	35791	03821	96179	19
42	60417	39583	64243	35757	03826	96174	18
43	60446	39554	64278	35722	03832	96168	17
44	60474	39526	64312	35688	03838	96162	16
45	9.60503	10.39497	9.64346	10.35654	10.03843	9.96157	15
46	60532	39468	64381	35619	03849	96151	14
47	60561	39439	64415	35585 35551	03854	96146	13
48	60589	39411	64449	35551	03860	96140 96135	12
49 50	60618 9.60646	39382 10.39354	64483 9.64517	35517 10.35483	03865 10.03871	9.96129	11 10
51	60675	39325	64552	35448	03877	96123	9
52	60704	39296	64586	35414	03882	96118	8
53	60732	39268	64620	35380	03888	96112	8 7
54	60761	39239	64654	35346	03893	96107	6
55	9.60789	10.39211	9.64688	10.35312	10.03899	9.96101	5
56 57	60818	39182	64722	35278	03905	96095	4
57	60846	39154	64756	35244	03910	96090	3
58	60875	39125	64790	35210	03916	96084	3 2 1
59 60	60903 60931	39097 59069	64824 64858	35176 35142	03921 03927	96079 96073	0
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

24°			Logar	thms.			155°
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.60931	10.39069	9.64858	10.35142	10.03927	9.96073	60
1	60960	39040	64892	35108	03933	96067	59
3	60988	39012	64926	35074	03938	96062	28
3	61016	38984 38955	64960 64994	35040 35006	03944 03950	96056 96050	57 56
4	61045 9.61073	10.38927	9.65028	10.34972	10.03955	9.96045	55
6	61101	38899	65062	34938	03961	96039	54
4 5 6 7	61129	38871	65096	34904	03966	96034	53
8	61158	38842	65130	34870	03972	96028	52
9	61186	38814	65164	34836	03978	96022	51
10	9.61214	10.38786	9.65197	10.34803	10.03983 03989	9.96017 96011	50 49
11 12	61242 61270	38758 38730	65231 65265	34769 34735	03995	96005	48
13	61298	38702	65299	34701	04000	96000	47
14	61326	38674	65333	34667	04006	95994	46
15	9.61354	10.38646	65333 9.65366	10.34634	10.04012	9.95988	45
16	61382	38618	65400	34600	04018	95982	44
17	61411	38589	65434	34566	04023	95977 95971	43
18 19	61438 61466	38562 38534	65467 65501	34533 34499	04029 04035	95965	41
20	9.61494	10.38506	9.65535	10.34465	10.04040	9.95960	40
21	61522	38478	65568	34432	04046	95954	39
21 22	61550	38450	65602	34398	04052	95948	38
23	61578	38422	65636	34364	04058	95942	37
23 24 25 26 27 28	61606 9.61634	38394	65669	34331	04063	95937	36
25	9.61634 61662	10.38366 38338	9.65703 65736	10.34297 34264	10.04069 04075	9.95931 95925	35 34
20	61689	38311	65770	34230	04080	95920	33
28	61717	38283	65803	34197	04086	95914	32
29	61745	38255	65837	34163	04092	95908	31
29 30 31 32 33	9.61773	10.38227	9.65870	10.34130	10.04098	9.95902	30 29
31	61800	38200	65904	34096	04103	95897	29
32	61828	38172	65937	34063 34029	04109 04115	95891 95885	28 27
33 34	61856 61883	38144 38117	65971 66004	33996	04121	95879	26
85	9.61911	10.38089	9.66038	10.33962	10.04127	9.95873	25
35 36 37	61939	38061	66071	33929	04132	95868	24
37	61966	38034	66104	33896	04138	95862	23
38 39	61994	38006	66138	33862	04144	95856	22
39	62021	37979	66171	33829 10.33796	04150 10.04156	95850 9.95844	21 20
40 41	9.62049 62076	10.37951 37924	9.66204 66238	33762	04161	95839	19
42	62104	37896	66271	33729	04167	95833	18
43	62131	37869	66304	33696	04173	95827	17
44	62159	37841	66337	33663	04179	95821	16
45	9.62186	10.37814	9.66371	10.33629	10.04185	9.95815	15
46	62214	37786	66404	33596	04190	95810 95804	14 13
47 48	62241 62268	37759 37732	66437 66470	33563 33530	04196 04202	95798	12
49	62296	37704	66503	33497	04208	95792	ii
50	9.62323	10.37677	9.66537	10.33463	10.04214	9.95786	10
51 52	62350	37650	66570	33430	04220	95780	9
52	62377	37623	66603	33397	04225	95775	8 7
53 54 55 56 57 58 59	62405	37595	66636	33364	04231 04237	95769	7
55	62432 9.62459	37568 10.37541	9.66702	33331 10.33298	10.04243	95763 9.95757	6 5
56	62486	37514	66735	33265	04249	95751	4
57	62513	37487	66768	33232	04255	95745	
58	62541	37459	66801	33199	04261	95739	3 2 1
59	62568	37432	66834	33166	04267	95733	
60	62595	37405	66867	33133	04272	95728	0
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

25°			Logari	ithms.			154°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.62595	10.37405	9.66867	10.33133	10.04272	9.95728	60
1	62622	37378 37351	66900	33100	04278	95722	59
2	62649	37351	66933	33067	04284	95716	58
3	62676	37324	66966	33034	04290	95710	57
4	62703 9.62730	37297 10.37270	66999 9.67032	33001 10.32968	04296 10.04302	95704 9.95698	56
5 6	62757	37243	67065	32935	04308	95692	55 54
7	62784	37216	67098	32902	04314	95686	53
8	62811	37189	67131	32869	04320	95680	52
8	62838	37162	67163	20227	04326	95674	51
10	9.62865	10.37135	9.67196	10.32804	10.04332	9.95668	50
11	62892	37108	67229	32771	04337	95663	49
12 13	62918	37082	67262	32738	04343	95657	48
13	62945	37055 37028	67295	32705	04349 04355	95651	47
14 15	62972 9.62999	10.37001	67327	32673 10.32640	10.04361	95645 9.95639	46
16	63026	36974	9.67360 67393	32607	04367	95633	45
17	63052	36948	67426	32574	04373	95627	43
18	63079	36921	67458	32542	04379	95621	42
18 19	63106	36894	67491	32509	04385	95615	41
20	9.63133	10.36867	9.67524	10.32476	10.04391	9.95609	40
20 21 22 23 24	63159	36841	67556	32444	04397	95603	39
22	63186	36814	67589	32411	04403	95597	38 37
23	63213	36787	67622	32378	04409	95591	37
24	63239	36761	67654	32346	04415	95585	36
25 26 27 28 29	9.63266	10.36734	9.67687	10.32313	10.04421	9.95579	35
20	63292 63319	36708 36681	67719 67752	32281 32248	04427 04433	95573 95567	34 33
28	63345	36655	67785	32215	04439	95561	32
29	63372	36628	67817	32183	04445	95555	31
30	9.63398	10.36602	9.67850	10.32150	10.04451	9.95549	30
31	63425	36575	67882	32118	04457	95543	30 29
32 33	63451	36549	67915	32085	04463	95537	28
33	63478	36522	67947	32053	04469	95531	27
84	63504	36496	67980	32020	04475	95525	26
35 36 37	9.63531	. 10.36469	9.68012	10.31988	10.04481	9.95519	25
36	63557 63583	36443 36417	68044 68077	31956 31923	04487 04493	95513 95507	24
90	63610	36390	68109	31891	04500	95500	23 22
38 39	63636	36364	68142	31858	04506	95494	21
40	9.63662	10.36338	9.68174	10.31826	10.04512	9.95488	20
41	63689	36311	68206	31794	04518	95482	19
42	63715	36285	68239	31761	04524	95476	18
43	63741	36259	68271	31729	04530	95470	17
44	63767	36233	68303	31697	04536	95464	16
45	9.63794	10.36206	9.68336	10.31664	10.04542	9.95458	15
46 47	63820 63846	36180 36154	68368	31632	04548	95452	14
48	63872	36128	68400 68432	31600 31568	04554 04560	95446 95440	13 12
49	63898	36102	68465	31535	04566	95434	111
50	9.63924	10.36076	9.68497	10.31503	10.04573	9.95427	10
50 51	63950	36050	68529	31471	04579	95421	9
52	63976	36024	68561	31439	04585	95415	8 7
53	64002	35998	68593	31407	04591	95409	7
54	64028	35972	68626	31374	04597	95403	6
55 56 57	9.64054	10.35946	9.68658	10.31342	10.04603	9.95397	5
56	64080	35920	68690	31310	04609	95391	4
58	64106	35894	68722	31278	04616	95384	8
59	64132 64158	35868 35842	68754 68786	31246 31214	04622 04628	95378 95372	8 2 1
60	64184	35816	68818	31182	04634	95366	ō
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

26°			Logar	ithms.			153°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.64184	10.35816	9.68818	10.31182	10.04634	9.95366	60
1	64210 64236	35790 35764	68850 68882	31150	04640	95360	59
2 3	64262	35764 35738	68914	31118 31086	04646 04652	95354 95348	58 57
4	64288	35738 35712	68946	31054	04659	95341	56
4 5 6	9.64313	10.35687	9.68978	10.31022	10.04665	9.95335	55
6	64339	35661	69010	30990	04671	95329	54
7 8 9	64365	35635	69042	30958	04677	95323	53
8	64391 64417	35609 35583	69074 69106	30926 30894	04683 04690	95317 95310	52 51
10	9.64442	10.35558	9.69138	10.30862	10.04696	9.95304	50
11	64468	35532	69170	30830	04702	95298	49
12 13	64494	35506	69202	30798	04708	95292	48
13	64519	35481	69234	30766	04714	95286	47
14	64545	35455 10.35429	69266	30734 10.30702	04721	95279	46
15 16	9.64571 64596	35404	9.69298 69329	30671	10.04727 04733	9.95273 95267	44
17	64622	35378	69361	30639	04739	95261	43
18	64647	35353	69393	30607	04746	95254	42
19	64673	35327	69425	30575	04752	95248	41
20	9.64698	10.35302	9.69457	10.30543	10.04758	9.95242	40
21	64724	35276 35251	69488	30512	04764	95236	39
22 23	64749 64775	35251 35225	69520 69552	30480 30448	04771 04777	95229 95223	38
24	64800	35220	69584	30416	04777	95217	36
25	9.64826	10.35174	9.69615	10.30385	10.04789	9.95211	35
25 26	64851	35149	69647	30353	04796	95204	34
27 28 29	64877	35123	69679	30321	04802	95198	33
28	64902	35098	69710	30290	04808	95192	32
29	64927 9.64953	35073 10.35047	69742 9.69774	30258 10.30226	04815	95185 9.95179	31 30
30 31	64978	35022	69805	30195	10.04821 04827	9.95179	29
32	65003	34997	69837	30163	04833	95167	28
83	65029	34971	69868	30132	04840	95160	27
34	65054	34946	69900	30100	04846	95154	26
35	9.65079	10.34921	9.69932	10.30068	10.04852	9.95148	25
36 37	65104 65130	34896 34870	69963	30037 30005	04859	95141	24
38	65155	34845	69995 70026	29974	04865 04871	95135 95129	23
38 39	65180	34820	70058	29942	04878	95122	21
40	9.65205	10.34795	9.70089	10.29911	10.04884	9.95116	20
41	65230	34770	70121	29879	04890	95110	19
42	65255	34745	70152	29848	04897	95103	18
43 44	65281	34719 34694	70184 70215	29816	04903	95097 95090	17 16
45	65306 9.65331	10.34669	9.70247	29785 10.29753	04910 10.04916	9.95084	15
46	65356	34644	70278	29722	04922	95078	14
47	65381	34619	70309	29691	04929	95071	13
48 4 9	65406	34594	70341	29659	04935	95065	12
49	65431	34569	70372	29628	04941	95059	11
50	9.65456	10.34544	9.70404	10.29596	10.04948	9.95052	10
51 52	65481 65506	34519 34494	70435 70466	29565 29534	04954 04961	95046 95039	8
53	65531	34469	70498	29502	04967	95033	7
54	65556	34444	70529	29471	04973	95027	7 6
55	9.65580	10.34420	9.70560	10.29440	10.04980	9.95020	5 4
56 57	65605	34395	70592	29408	04986	95014	4
57	65630	34370	70623	29377	04993	95007	3 2
58 59	65665 65680	34345 34320	70654 70685	29346 29315	04999 05005	95001 94995	1
60	65705	34295	70717	29283	05012	94988 94988	Ŏ
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

27°			Logar	ithms.	•		152°
M.	Sine.	Cosecant.	Tangent.	Cotangent	Secant.	Cosine.	M.
0	9.65705	10.34295	9.70717	10.29283	10.05012	9.94988	60
1	65729	34271	70748	29252	05018	94982	59
3	65754	34246	70779	29221	05025	94975	58
3	65779	34221	70810	29190	05031	94969	57
5	65804 9.65828	34196 10.34172	70841 9.70873	29159 10.29127	05038 10.05044	94962 9.94956	56
8	65853	34147	70904	29096	05051	94949	55 54
6	65878	34122	70935	29065	05057	94943	53
8	65902	34098	70966	29034	05064	94936	52
9	65927	34073	70997	29003	05070	94930	51
10	9.65952	10.34048	9.71028	10.28972	10.05077	9.94923	50
11 12	65976	34024	71059	28941	05083	94917	49
12	66001	33999	71090	28910	05089	94911	48
13 14	66025 66050	33975 33950	71121 71153	28879 28847	05096 05102	94904 94898	47
15	9.66075	10.33925	9.71184	10.28816	10.05102	9.94891	46 45
16	66099	33901	71215	28785	05115	94885	44
17	66124	33876	71246	28754	05122	94878	43
18	66148	33852	71277	28723	05129	94871	42
19	66173	33827	71308	28692	05135	94865	41
20 21 22	9.66197	10.33803	9.71339	10.28661	10.05142	9.94858	40
21	66221	33779	71370	28630	05148	94852	39
22	66246	33754	71401	28599	05155	94845	38
23	66270	33730	71431	28569	05161	94839	37
25	66295 9.66319	33705 10.33681	71462	28538 10,28507	05168	94832 9.94826	36
20	66343	33657	9.71493 71524	28476	10.05174 05181	9.94826	35
26 27 28 29	66368	33632	71555	28445	05187	94813	34 33
28	66392	33608	71586	28414	05194	94806	32
29	66416	33584	71617	28383	05201	94799	31
30	9.66441	10.33559	9.71648	10.28352	10.05207	9.94793	30
31	66465	33535	71679	28321	05214	94786	29
32	66489	33511	71709	28291	05220	94780	28
33	66513	33487	71740	28260	05227	94773	27
34	66537	33463	71771	28229	05233	94767	26
35 36 37	9.66562	10.33438	9.71802	10.28198	10.05240	9.94760	25
97	66586 66610	33414 33390	71833 71863	28167 28137	05247 05253	94753 94747	24 23
38	66634	33366	71894	28106	05260	94740	22
38 39	66658	33342	71925	28075	05266	94734	21
40	9.66682	10.33318	9.71955	10.28045	10.05273	9.94727	20
41	66706	33294	71986	28014	05280	94720	19
42	66731	33269	72017	27983	05286	94714	18
43	66755	33245	72048	27952	05293	94707	17
44	66779	33221	72078	27922	05300	94700	16
45	9.66803	10.33197	9.72109	10.27891	10.05306	9.94694	15
46 47	66827 66851	33173 33149	72140	27860 27830	05313 05320	94687	14
48	66875	33125	72170 72201	27799	05320	94680 94674	13 12
49	66899	33101	72231	27769	05333	94667	n
50	9.66922	10.33078	9.72262	10.27738	10.05340	9.94660	10
50 51	66946	33054	72293	27707	05346	94654	9
52	66970	33030	72323	27677	05353	94647	8
53	66994	33006	72354	27646	05360	94640	7
54	67018	32982	72384	27616	05366	94634	6
55 56 57	9.67042	10.32958	9.72415	10.27585	10.05373	9.94627	5
56	67066	32934	72445	27555	05380	94620	4
57	67090	32910	72476	27524	05386	94614	3 2
58 59	67113	32887 32863	72506	27494 27463	05393	94607 94600	1 2
60	67137 67161	32839	72537 72567	27403	05400 05407	94593	0
M.	Cosine,	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

28°			Logar	ithms.			151°
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.67161	10.32839	9.72567	10.27433	10.05407	9.94593	60
1	67185	32815	72598	27402	05413	94587	59
3	67208	32792	72628	27372	05420	94580	58
3	67232	32768	72659	27341	05427	94578	57
4	67256	32744 10.32720	72689	27311	05433 10.05440	94567	56
2	9.67280 67303	32697	9.72720 72750	10.27280 27250	05447	9.94560 94553	54
7	67327	32673	72780	27220	05454	94546	53
Ŕ	67350	32650	72811	27189	05460	94540	55 54 53 52
4 5 6 7 8 9	67374	32626	72841	27159	05467	94533	51
0	9.67398	10.32602	9.72872	10.27128	10.05474	9.94526	50
1	67421	32579	72902	27098	05481	94519	49
2	67445	32555	72932	27068	05487	94513	48
3	67468	32532	72963	27037	05494	94506	47
4	67492	32508	72993	27007	05501	94499	46
5	9.67515 67539	10.32485 32461	9.73023 73054	10.26977 26946	10.05508 05515	9.94492 94485	45 44
9	67562	32438	73084	26916	05521	94479	43
6 7 8 9 0 1 2 3	67586	32414	73114	26886	05528	94472	42
9	67609	32391	73144	26856	05535	94465	41
ŏ l	9.67633	10.32367	9.73175	10.26825	10.05542	9.94458	40
1	67656	32344	73205	26795	05549	94451	39
2	67680 ·	32320	73235	26765	05555	94445	38 37
3	67703	32297	73265	26735	05562	94438	37
	67726	32274	73295	26705	05569	94431	36
!	9.67750	10.32250	9.73326	10.26674	10.05576	9.94424	35 34
?	67773 67796	32227 32204	73356 73386	26644 26614	05583	94417 94410	99
5 6 7 8 9	67820	32180	73416	26584	05590 05596	94404	33 32
1	67843	32157	73446	26554	05603	94397	31
	9.67866	10.32134	9.73476	10.26524	10.05610	9.94390	30
1	67890	32110	73507	26493	05617	94383	29
1	67913	32087	73537	26463	05624	94376	30 29 28 27 26 25
- 1	67936	32064	73567	26433	05631	94369	27
	67959	32041	73597	26403	05638	94362	26
5	9.67982 68006	10.32018	9.73627	10.26373	10.05645	9.94355	25
7	68029	31994 31971	73657 73687	26343 26313	05651 05658	94349 94342	124
8	68052	31948	73717	26283	05665	94335	23 22 21
8	68075	31925	73747	26253	05672	94328	21
0	9.68098	10.31902	73747 9.73777	26253 10.26223	05672 10.05679	9.94321	20
l I	68121	31879	73807	26193	05686	94314	19
2	68144	31856	73837	26163	05693	94307	18
3	68167	31833	73867	26133	05700	94300	17
1	68190	31810	73897	26103	05707	94293	16
5	9.68213 68237	10.31787 31763	9.73927 73957	10.26073 26043	10.05714 05721	9.94286 94279	15 14
7	68260	31740	73987	26013	05721	94279	19
śΙ	68283	31717	74017	25983	05734	94266	13 12
9	68305	31695	74047	25953	05741	94259	ii
0	9.68328	10.31672	9.74077	10.25923	10.05748	9.94252	10
0 1 2	68351	31649	74107	25893	05755 05762	94245	9
2	68374	31626	74137	25863	05762	94238	8
3	68397	31603	74166	25834	05769	94231	7
1	68420	31580	74196	25804	05776	94224	6
5	9.68443 68466	10.31557	9.74226 74256	10.25774 25744	10.05783	9.94217	5
	68489	31534 31511	74286	25744 25714	05790 05797	94210 94203	4
	68512	31488	74316	25684	05804	94203 94196	1 3
3	68534	31466	74345	25655	05811	94189	8 7 6 5 4 3 2
δĺ	68557	31443	74375	25625	05818	94182	ō
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29°			Logar	ithms.			150°
M.	Sine.	Cosecant.	Tangent.	Cotangent	Secant.	Cosin e.	M.
0	9.68557	10.31443	9.74375	10.25625	10.05818	9.94182	60
1	68580	31420	74405	25595	05825	94175	59
2	68603	31397	74435	25565	05832	94168	58
3	68625	31375	74465	25535	05839	94161	57
5	68648 9.68671	31352 10.31329	74494 9.74524	25506 10.25476	05846 10.05853	94154 9.94147	56 55
6	68694	31306	74554	25446	05860	94140	54
6	68716	31284	74583	25417	05867	94133	53
8	68739	31261	74613	25387	05874	94126	52
	68762	31238	74643	25357	05881	94119	51
10	9.68784	10.31216	9.74673	10.25327	10.05888	9.94112	50
11	68807	31193	74702	25298	05895	94105	49
12	68829	31171	74732	25268	05902	94098	48
13 14	68852	31148	74762	25238	05910	94090	47
15	68875 9,68897	31125 10.31103	74791 9.74821	25209 10.25179	05917 10.05924	94083 9.94076	46 45
16	68920	31080	74851	25149	05931	94069	44
17	68942	31058	74880	25120	05938	94062	43
18	68965	31035	74910	25090	05945	94055	42
19	68987	31013	74939	25061	05952	94048	41
19 20 21 22 23 24	9.69010	10.30990	9.74969	10.25031	10.05959	9.94041	40
21	69032	30968	74998	25002	05966	94034	39
22	69055	30945	75028	24972	05973	94027	38
23	69077	30923	75058	24942	05980	94020	37
24	69100	30900	75087	24913	05988	94012	36
25 26	9.69122	10.30878	9.75117	10.24883	10.05995	9.94005	35 34
20	69144 69167	30856 30833	75146 75176	24854 24824	06002 06009	93998 93991	33
28	69189	30811	75205	24795	06016	93984	32
29	69212	30788	75235	24765	06023	93977	31
27 28 29 30	9.69234	10.30766	9.75264	10.24736	10.06030	9.93970	30
31	69256	30744	75294	24706	06037	93963	29
32 33 34	69279	30721	75323	24677	06045	93955	28
33	69301	30699	75353	24647	06052	93948	27
34	69323	30677	75382	24618	06059	93941	26
85	9.69345	10.30655	9.75411	10.24589	10.06066	9.93934	25
36	69368	30632 30610	75441	24559	06073	93927	24
37 38 39	69390 69412	30588	75470 75500	24530 24500	06080 06088	93920 93912	23 22
80	69434	30566	75529	24471	06095	93905	21
40	9.69456	10.30544	9.75558	10.24442	10.06102	9.93898	20
41	69479	30521	75588	24412	06109	93891	19
42	69501	30499	75617	24383	06116	93884	18
43	. 69523	30477	75647	24353	06124	93876	17
44	69545	30455	75676	24324	06131	93869	16
45	9.69567	10.30433	9.75705	10.24295	10.06138	9.93862	15
46	69589	30411 30389	75735	24265	06145	93855	14
47 48	69611 69633	30367	75764 75793	24236 24207	06153	93847 93840	13 12
49	69655	30345	75822	24178	06160	93833	111
50	9.69677	10.30323	9.75852	10.24148	06167 10.06174	9.93826	10
51	69699	30301	75881	24119	06181	93819	1 9
52	69721	30279	75910	24090	06189	93811	8
53 54	69743	30257	75939	24061	06196	93804	7
54	69765	30235	75969	24031	06203	93797	7 6 5
55 I	9.69787	10.30213	9.75998	10.24002	10.06211	9.93789	5
56	69809	30191	76027	23973	06218	93782	4
57	69831	30169	76056	23944	06225 06232	93775	3
58 59	69853 69875	30147 30125	76086 76115	23914 23885	06232	93768 93760	1 2
60	69897	30103	76144	23856	06247	93753	ő
M.	Cosine,	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

30°			Logar	ithms.			1490
M.	Sine.	Cosecant.	Tangent.	Cotangent	Secant.	Cosine.	M.
0	9.69897	10.30103	9.76144	10.23856	10.06247	9.93753	60
1	69919	30081	76173	23827	06254	93746	59
3	69941	30059	76202	23798	06262	93738	58
3	69963 69984	30037 30016	76231 76261	23769 23739	06269 06276	93731 93724	57 56
4 5	9.70006	10.29994	9.76290	10.23710	10.06283	9.93717	55
6	70028	29972	76319	23681	06291	93709	54
6 7	70050	29950	76348	23652	06298	93702	53
8	70072	29928	76377	23623	06305	93695	52
9 10	70093	29907	76406	23594	06313	93687	51
10	9.70115	10.29885	9.76435	10.23565	10.06320	9.93680	50
11	70137 70159	29863- 29841	76464 76493	23536 23507	06327 06335	93673 93665	49
12 13	70189	29820	76522	23478	06342	93658	47
14	70202	29798	76551	23449	06350	93650	46
15	9.70224	10.29776	9.76580	10.23420	10.06357	9.93643	45
16	70245	29755	76609	23391	06364	93636	44
17	70267	29733	76639	23361	06372	93628	43
18	70288	29712	76668	23332	06379	93621	42
19	70310	29690	76697	23303	06386	93614	41
20	9.70332	10.29668	9.76725	10.23275	10.06394	9.93606 93599	40
21 22	· 70353 70375	29647 29625	76754 76783	23246 23217	06401 06409	93599	39
23	70375	29604	76812	23188	06416	93584	38 37
24	70418	29582	76841	23159	06423	93577	36
	9.70439	10.29561	9.76870	10.23130	10.06431	9.93569	35
25 26 27 28	70461	29539	76899	23101	06438	93562	34
27	70482	29518	76928	23072	06446	93554	33
28	70504	29496	76957	23043	06453	93547	32
29	70525	29475	76986	23014	06461	93539	31
30 31	9.70547 70568	10.29453 29432	9.77015 77044	10.22985 22956	10.06468 06475	9.93532 93525	30 29
82	70590	29410	77073	22927	06483	93517	28
33	70611	29389	77101	22899	06490	93510	27
34	70633	29367	77130	22870	06498	93502	26
35	9.70654	10.29346	9.77159	10,22841	10.06505	9.93495	25
36	70675	29325	77188	22812	06513	93487	24
37	70697	29303	77217	22783	06520	93480	23
38 39	70718	29282 29261	77246	22754	06528	93472	22
40	70739 9.70761	10.29239	77274 . 9.77303	22726 10,22697	06535 10.06543	93465 9.93457	21 20
41	70782	29218	77332	22668	06550	93450	19
42	70803	29197	77361	22639	06558	93442	18
43	70824	29176	77390	22610	06565	93435	17
44	70846	29154	77418	22582	06573	93427	16
45	9.70867	10.29133	9.77447	10.22553	10.06580	9.93420	15
46	70888	29112	77476	22524	06588	93412	14
47 48	70909 70931	29091 29069	77505 77533	22495 22467	06595 06603	93405 93397	13
49	70952	29048	77562	22438	06610	93390	12 11
50	9.70973	10.29027	9.77591	10.22409	10.06618	9.93382	10
5ĭ	70994	29006	77619	22381	06625	93375	19
52	71015	28985	77648	22352	06633	93367	š
53 54	71036	28964	77677	22323	06640	93360	8 7
54	71058	28942	77706	22294	06648	93352	6
55	9.71079	10.28921	9.77734	10.22266	10.06656	9.93344	6 5 4
56	71100	28900 28879	77763	22237 22209	06663	93337	4
57	71121 71142	28879	77791 77820	22209	06671 06678	93329 93322	3
58 59	71163	28837	77849	22151	06686	93314	3 2 1
60	71184	28816	77877	22123	06693	93307	ō
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

31°			Logar	ithms.			148°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.71184	10.28816	9.77877	10.22123	10.06693	9.93307	60
1 2 3	71205	28795	77906	22094	06701 06709	93299	59
2	71226	28774	77935	22065	06709	93291	58
3	71247 71268	28753 28732	77963 77992	22037 22008	06716	93284	57
· 4	9.71289	10.28711	9.78020	10.21980	06724 10.06731	93276 9.93269	56 55
6	71310	28690	78049	21951	06739	93261	54
6 7	71331	28669	78077	21923	06747	93253	53
8	71352	28648	78106	21894	06754	98246	52
9	71373	28627	78135	21865	06762	93238	51
10	9.71393	10.28607	9.78163	10.21837	10.06770	9.93230	50
11	71414	28586	78192	21808	06777	93223	49
12 13	71435 71456	28565 28544	78220 78249	21780 21751	06785	93215	48
14	71456	28523	78277	21723	06793 06800	93207 93200	47 46
15	9.71498	10.28502	9.78306	10.21694	10.06808	9.93192	45
16	71519	28481	78334	21666	06816	93184	44
Ĩ7	71539	28461	78334 78363	21637	06823	93177	43
18	71560	28440	78391	21609	06831	93169	42
19	71581	28419	78419	21581	06839	93161	41
20	9.71602	10.28398	9.78448	10.21552	10.06846	9.93154	40
21	71622	28378	78476	21524	06854	93146	39
22	71643	28357	78505	21495	06862	93138	38
23	71664	28336 28315	78533 78562	21467 21438	06869 06877	93131 93123	37
24	71685 9.71705	10.28295	9.78590	10.21410	10.06885	9.93115	36 35
26	71726	28274	78618	21382	06892	93108	34
27	71726 71747	28253	78647	21353	06900	93100	33
28	71767	28233	78675	21325	06908	93092	32
24 25 26 27 28 29 30	71788	28212	78704	21296	06916	93084	31
30	9.71809	10.28191	9.78732	10.21268	10.06923	9.93077	30 29
31	71829	28171	78760	21240	06931	93069	29
32	71850	28150	78789	21211	06939	93061	28
33	71870	28130	78817	21183	06947	93053	27
34 35	71891 9.71911	28109 10.28089	78845 9.78874	21155 10.21126	06954 10.06962	93046 9.93038	26 25
36	71932	28068	78902	21098	06970	93030	24
37	71952	28048	78930	21070	06978	93022	23
38	71973	28027	78959	21041	06986	93014	22
39	71994	28006	78987	21013	06993	93007	21
40	9.72014	10.27986	9.79015	10.20985	10.07001	9.92999	20
41	72034	27966	79043	20957	07009	92991	19
42	72055	27945	79072	20928	07017	92983	18
43	72075	27925	79100	20900	07024	92976	17
44 45	72096 9.72116	27904 10.27884	79128 9.79156	20872 10.20844	07032 10.07040	92968 9,92960	16 15
46	72137	27863	79185	20815	07048	9.92960	14
47	72157	27843	79213	20787	07056	92944	13
48	72177	27823	79241	20759	07064	92936	12
49	72198	27802	79269	20731	07071	92929	111
50	9.72218	10.27782	9.79297	10.20703	10.07079	9.92921	10
51	72238	27762	79326	20674	07087	92913	9
52	72259	27741	79354	20646	07095	92905	8 7
53	72279	27721	79382	20618	07103	92897	7
54	72299	27701	79410	20590	07111	92889	6
55	9.72320 72340	10.27680	9.79438 79466	10.20562	10.07119	9.92881 92874	5 4
56 57	72340 72360	27660 27640	79466	20534 20505	07126 07134	92874	9
58	72381	27619	79523	20477	07142	92858	3 2
59	72401	27599	79551	20449	07150	92850	í
60	72421	27579	79579	20421	07158	92842	Ō
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

32°	Logarithms.						1479
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.72421	10.27579	9.79579	10.20421	10.07158	9.92842	60
1	72441	27559	79607	20393	07166	92834	59
2	72461	27539	79635	20365	07174	92826	58
3 4	72482 72502	27518 27498	79663 79691	20337 20309	07174 07182 07190	92818 92810	57
5	9.72522	10.27478	9.79719	10.20281	10.07197	9.92803	56 55
5	72542	27458	79747	20253	07205	92795	54
7	72562	27438	79776	20224	07213	92787	53
7 8 9	72582	27418 27398	79804	20196	07221 07229	92779	52
9	72602	27398	79832	20168	07229	92771	51
10 11 12	9.72622	10.27378	9.79860	10.20140	10.07237	9.92763	50 49
112	72643 72663	27357 27337	79888 79916	20112 20084	07245 07253	92755 92747	48
13	72683	27317	79944	20056	07261	92739	40
14	72703	27297	79972	20028	07269	92731	47 46
15	9.72723	10.27277	9.80000	10.20000	10.07277	9.92723	45
16	72743	27257	80028	19972	07285	92715	44
17	72763	27237	80056	19944	07293	92707	43
18	72783 72803	27217 27197	80084	19916	07301 07309	92699	42
19	72803	27197	80112	19888	07309	92691	41
20	9.72823 72843	10.27177 27157	9.80140	10.19860 19832	10.07317	9.92683 92675	40
20 21 22 23 24	72843 72863	27137	80168 80195	19832	07325 07333	92667	39
23	72883	27117	80223	19777	07341	92659	38 37
24	72902	27098	80251	19749	07349	92651	36
25	9.72922	27098 10.27078	9,80279	10.19721	10.07357	9.92643	35
26	72942	27058	80307	19693	07365	92635	34 33
27	72962	27038	80335	19665	07373	92627	33
27 28 29	72982	27018	80363	19637	07381	92619	32
29	73002	26998	80391	19609	07389 10,07397	92611	31
30 31 32 33 34	9.73022 73041	10.26978 26959	9.80419 80447	10.19581 19553	07405	9.92603 92595	30 29 28 27
32	73061	26939	80474	19526	07413	92587	28
33	73081	26919	80502	19498	07421	92579	27
34	73101	26899	80530	19470	07429	92571	26
35 36 37	9.73121	10.26879	9.80558	10.19442	10.07437	9.92563	25
36	73140	26860	80586	19414	07445	92555	24
87	73160	26840	80614	19386	07454	92546	23
38 39	73180	26820	80642	19358	07462	92538	22 21
40	73200 9.73219	26800	80669	19331 10.19303 19275	07470 10.07478	92530 9.92522	20
41	73239	10.26781 26761	80725	19275	07486	92514	19
42	73259	26741	9.80697 80725 80753	19247	07494	92506	18
43	73278	26722	80781	19219	07502	92498	18 17 16
44	73298	26702	80808	19192	07510	92490	16
45	9.73318	10.26682	9.80836	10.19164	10.07518	9.92482	15
46	73337 73357	26663	80864	19136	07527	92473	14
47 48	73377	26643 26623	80892 80919	19108 19081	07535 07543	92465 92457	13 12
49	73396	26604	80947	19053	07551	92449	11
50	9.73416	10.26584	9.80975	10.19025	10.07559	9.92441	10
51	73435	26565	81003	18997	10.07559 07567	92433	9
50 51 52 53 54 55 56 57 58	73455	26565 26545	81003 81030	18970	07575 07584	92425	9 8 7 6 5 4 3 2 1
53	73474	26526	81058	18942	07584	92416	7
54	73494	26506	81086	18914	07592	92408	6
55	9.73513	10.26487	9.81113	10.18887	10.07600	9.92400	5
50	73533 73552	26467 26448	81141 81169	18859 18831	07608 07616	92392 92384	1 4
58	73572	26428	81196	18804	07616	92376	1 3
59	73591	26409	81224	18776	07633	92367	l î
60	73611	26389	81252	18748	07641	92359	ō
M.	Cosine,	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

33°			Logari	thms.			146°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.73611	10.26389	9.81252	10.18748	10.07641	9.92359	60
1	73630	26370	81279	18721	07649	92351	59
3	73650	26350	81307	18693	07657	92343	58
.3	73669	26331	81335 81362	18665 18638	07665 07674	92335	57
5	73689 9.73708	26311 10.26292	9.81390	10.18610	10.07682	92326 9.92318	56 55
6	73727	26273	81418	18582	07690	92310	54
4 5 6 7	73747	26253	81445	18555	07698	92302	
8	73766	26234	81473	18527	07707	92293	53 52
.9	73785	26215	81500	18500	07715	92285	51
10 11	9.73805 73824	10.26195	9.81528	10.18472 18444	10.07723	9.922/7	50
12	73843	26176 26157	81556 81583	18417	07731 07740	92269 92260	49 48
13	73863	26137	81611	18389	07748	92252	47
14	73882	26118	81638	18362	07756	92244	46
15	9.73901	10.26099	9.81666	10.18334	10.07765	9.92235	45
16	73921	26079	81693	18307	07773	92227	44
17	73940	26060	91721	18279	07781	92219	43
18 19	73959 73978	26041 26022	81748	18252 18224	07789 07798	92211 92202	42 41
20	9.73997	10.26003	81776 9.81803	10.18197	10.07806	9.92194	40
21	74017	25983	81831	18169	07814	92186	39
21 22	74036	25964	81858	18142	07823	92177	38
23	74055	25945	81886	18114	07831	92169	37
24	74074	25926	81913	18087	07839	92161	36
25 26	9.74093	10.25907	9.81941	10.18059	10.07848	9.92152	35
20	74113 74132	25887 25868	81968 81996	18032 18004	07856 07864	92144 92136	34 33
27 28	74151	25849	82023	17977	07873	92127	32
29	74170	25830	82051	17949	07881	92119	31
30	9.74189	10.25811	9.82078	10.17922	10.07889	9.92111	30
31	74208	25792	82106	17894	07898	92102	29 28
32	74227	25773	82133	17867	07906	92094	28
33 34	74246 74265	25754 25735	82161 82188	17839 17812	07914 07923	92086 92077	27 26
35	9.74284	10.25716	9.82215	10.17785	10.07931	9.92069	25
36	74303	25697	82243	17757	07940	92060	24
37	74322	25678	82270	17730	07948	92052	23
38	74341	25659	82298	17730 17702	07956	92044	22
39	74360	25640	82325	17675	07965	92035	21
40 41	9.74379 74398	10.25621	9.82352 82380	10.17648	10.07973 07982	9.92027 92018	20 19
42	74417	25602 25583	82407	17620 17593	07990	92010	19
43	74436	25564	82435	17565	07998	92002	18 17
44	74455	25545	82462	17565 17538	08007	91993	16
45	9.74474	10.25526	9.82489	10.17511	10.08015	9.91985	15
46	74493	25507	82517	17483	08024	91976	14
47 48	74512	25488	82544 82571	17456 17429	08032 08041	91968	13
48 49	74531 74549	25469 25451	82571 82599	17429	08041	91959 91951	12 11
50	9.74568	10.25432	9.82626	10.17374	10.08058	9.91942	10
51	74587	25413	82653	17347	08066	91934	9
52	74606	25394	82681	17319	08075	91925	8 7
53	74625	25375	82708	17292	08083	91917	7
54 55	74644	25356	82735	17265	08092	91908	6
56	9.74662 74681	10.25338 25319	9.82762 82790	10.17238	10.08100 08109	9.91900 91891	4
57	74700	25300	82817	17210 17183 17156	08117	91883	3
58	74719	25281	82844	17156	08126	91874	1 2
59	74737	25263	82871	17129	08134	91866	1
60	74756	25244	82899	17101	08143	91857	0
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

M. 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14	8ine. 9.74756 74775 74775 74794 74812 74831 9.74860 74868 74867 74906 74904 9.74943 74961 74980 74999 75017 9.75036 75054	10.25244 25225 25226 25286 25188 25189 10.25150 25132 25113 25094 25076 10.25067 25039 25020 25020 25020 24983 10.24984	9.82899 82926 82926 82926 82980 83008 9.83035 83062 83062 83117 83144 9.83171 83198 83225 83252 83252	10.17101 17074 17047 17040 16992 10.16965 16938 16911 16883 16856 10.16829 16802 16775	8ecant. 10.08143 08151 08160 08168 08177 10.08185 08194 08202 08211 108228 08227 08236	Cosine. 9.91857 91849 91840 91832 91823 9.91815 91798 91789 91781 9.91772 91763 91755	M. 60 59 58 57 56 55 54 53 52 51 50 49
1 2 3 4 5 6 7 8 9 10 11 12 13	74775 747794 74812 74831 9.74850 74868 74887 74906 74924 9.74943 74961 74980 74999 75017 9.75036 75054 75078	25225 25206 25188 25169 10.25150 25132 25113 25094 25076 10.25057 25039 25020 25001 24983 10.24964	82926 82953 82980 83008 9.83035 83062 83089 83117 83144 9.83171 83198 83225 83252	17074 17047 17020 16992 10.16965 16938 16911 16883 16856 10.16829 16802 16775	08151 08160 08168 08177 10.08185 08194 08202 08211 08219 10.08228 08237	91849 91840 91832 91823 9.91815 91806 91798 91789 91781 9.91772 91763	59 58 57 56 55 54 53 52 51 50 49
2 3 4 5 6 7 8 9 10 11 12 13	74775 747794 74812 74831 9.74850 74868 74887 74906 74924 9.74943 74961 74980 74999 75017 9.75036 75054 75078	25206 25188 25169 10.25150 25132 25113 25094 25076 10.25057 25039 25020 25001 24983 10.24964	82926 82953 82980 83008 9.83035 83062 83089 83117 83144 9.83171 83198 83225 83252	17074 17047 17020 16992 10.16965 16938 16911 16883 16856 10.16829 16802 16775	08151 08160 08168 08177 10.08185 08194 08202 08211 08219 10.08228 08237	91849 91840 91832 91823 9.91815 91806 91798 91789 91781 9.91772 91763	59 58 57 56 55 54 53 52 51 50 49
5 6 7 8 9 10 11 12 13	74812 74831 9.74850 74868 74867 74906 74924 9.74943 74961 74980 74999 75017 9.75036 75054 75073	25188 25169 10.25150 25132 25132 25094 25076 10.25057 25039 25020 25020 24983 10.24964	82980 83008 9.83035 83062 83089 83117 83144 9.83171 83198 83225 83225	17047 17020 16992 10.16965 16938 16911 16883 16856 10.16829 16802 16775	08168 08177 10.06185 08194 08202 08211 08219 10.08228 08237	91832 91823 9.91815 91806 91798 91789 91781 9.91772 91763	56 55 54 53 52 51 50 49
5 6 7 8 9 10 11 12 13	74831 9.74850 74868 74868 74906 74924 9.74943 74961 74980 75017 9.75036 75054 75073	25169 10.25150 25132 25113 25094 25076 10.25057 25039 25020 25001 24983 10.24964	83008 9.83035 83062 83089 83117 83144 9.83171 83198 83225 83225	10.16965 16938 16911 16883 16856 10.16829 16802 16775	08177 10.08185 08194 08202 08211 08219 10.08228 08237	91823 9.91815 91806 91798 91789 91781 9.91772 91763	56 55 54 53 52 51 50 49
10 11 12 13	9.74850 74868 74887 74906 74924 9.74943 74941 74980 74999 75017 9.75036 75054 75073	10.25150 25132 25113 25094 25076 10.25057 25039 25020 25001 24983 10.24964	9.83035 83062 83089 83117 83144 9.83171 83198 83225 83225	10.16965 16938 16911 16883 16856 10.16829 16802 16775	10.08185 08194 08202 08211 08219 10.08228 08237	9.91815 91806 91798 91789 91781 9.91772 91763	55 54 53 52 51 50 49
10 11 12 13	74868 74887 74906 74924 9.74943 74961 74980 74999 75017 9.75036 75054 75073	25132 25113 25094 25076 10.25057 25039 25020 25001 24983 10.24964	83062 83089 83117 83144 9.83171 83198 83225 83252	16938 16911 16883 16856 10.16829 16802 16775	08194 08202 08211 08219 10.08228 08237	91806 91798 91789 91781 9.91772 91763	54 53 52 51 50 49
10 11 12 13	74887 74906 74924 9.74943 74961 74980 74999 75017 9.75036 75054 75073	25113 25094 25076 10.25057 25039 25020 25001 24983 10.24964	83089 83117 83144 9.83171 83198 83225 83252	16911 16883 16856 10.16829 16802 16775	08202 08211 08219 10.08228 08237	91798 91789 91781 9.91772 91763	53 52 51 50 49
10 11 12 13	74906 74924 9.74943 74961 74980 74999 75017 9.75036 75054 75073	25094 25076 10.25057 25039 25020 25001 24983 10.24964	83117 83144 9.83171 83198 83225 83252	16883 16856 10.16829 16802 16775	08211 08219 10.08228 08237	91789 91781 9.91772 91763	52 51 50 49
10 11 12 13	74924 9.74943 74961 74980 74999 75017 9.75036 75054 75073	25076 10.25057 25039 25020 25001 24983 10.24964	83144 9.83171 83198 83225 83252	16856 10.16829 16802 16775	08219 10.08228 08237	91781 9.91772 91763	51 50 49
10 11 12 13	9.74943 74961 74980 74999 75017 9.75036 75054 75073	10.25057 25039 25020 25001 24983 10.24964	9.83171 83198 83225 83252	10.16829 16802 16775	10.08228 08237	9.91772 91763	50 49
11 12 13	74961 74980 74999 75017 9.75036 75054 75073	25039 25020 25001 24983 10.24964	83198 83225 83252	16802 16775	08237	91763	49
12 13	74980 74999 75017 9.75036 75054 75073	25020 25001 24983 10.24964	83225 83252	16775			
13	75017 9.75036 75054 75073	25001 24983 10.24964	83252	10740			48
14	9.75036 75054 75073	10.24964	00000	16748	08254	91746	47
	75054 75073		1 83280	16720	08262	91738	46
15	75073		9.83307	16720 10.16693	10.08271	9.91729	45
16 17 18		24946	83334	16666	08280	91720	44
17		24927	83361	16639	08288	91712	43
18	75091	24909	83388	16612	08297	91703	42
19	. 75110	24890	83415	16585	08305	91695	41
20 21	9.75128	10.24872	9.83442	10.16558	10.08314	9.91686	40
22	75147 75165	24853 24835	83470	16530	08323	91677	39
23	75184	24835	83497 83524	16503 16476	08331 08340	91669 91660	38
24	75202	24798	83551	16449	08349	91651	36
25	9.75221	10.24779	9.83578	10.16422	10.08357	9.91643	35
26	75239	24761	83605	16395	08366	91634	34
27	75258	24742	83632	16368	08375	91625	33
28	75276	24724	83659	16341	08383	91617	32
25 26 27 28 29 30 31 82 83 34	75294	24706	83686	16314	08392	91608	31
30	9.75313	10.24687	9.83713	10.16287	10.08401	9.91599	30
31	75331	24669	83740	16260	08409	91591	29
82	75350	24650	83768	16232	08418	91582	28
83	75368	24632	83795	16205	08427	91573	27
34	75386	24614	83822	16178	08435	91565	26
96	9.75405 75423	10.24595 24577	9.83849	10.16151	10.08444	9.91556	25
35 36 37 38 39	75441	24559	83876	16124 16097	08453 08462	91547	24
38	75459	24541	83903 83930	16070	08462	91538 91530	23 22
39	75478	24522	83957	16043	08479	9152 1	21
40	9.75496	10.24504	9.83984	10.16016	10.08488	9.91512	20
41	75514	24486	84011	15989	08496	91504	19
42	75533	24467	84038	15962	08505	91495	18
43	75551	24449	84065	15935	08514	91486	17
44	75569	24431	84092	15908	08523	91477	16
45	9.75587	10.24413	9.84119	10.15881	10.08531	9.91469	15
46	75605	24395	84146	15854	08540	91460	14
47	75624	24376	84173	15827	08549	91451	13
48	75642	24358	84200	15800	08558	91442	12
49	75660	24340	84227	15773	08567	91433	11
51	9.75678	10.24322	9.84254	10.15746	10.08575	9.91425	10
49 50 51 52 53 54 55 56 57	75696 75714	24304 24286	84280 84307	15720 15693	08584	91416	9 8 7 6 5
53	75733	24267	84334	15666	08593 08602	91407	8
54	75751	24249	84361	15639	08602 08611	91398 91389	6
55	9.75769	10.24231	9.84388	10.15612	10.08619	9.91381	6
56	75787	24213	84415	15585	08628	91372	4
57	75805	24195	84442	15558	08637	91363	3
58 59	75823	24177	84469	15531	08646	91354	2
59	75841	24159	84496	15504	08655	91345	3 2 1
60	75859	24141	84523	15477	08664	91336	Ō
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine,	M.

35°			144°				
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.75859	10.24141	9.84523	10.15477	10.08664	9.91336	60
1	75877	24123	84550	15450	08672	91328	59
3	75895	24105	84576	15424	08681	91319	58
3	75913	24087 24069	84603 84630	15397 15370	08690 08699	91310 91301	57 56
4 5 6 7	75931 9.75949	10.24051	9.84657	10.15343	10.08708	9.91292	55
6	75967	24033	84684	15316	08717	91283	54
7	75985	24015	84711	15289	08726	91274	53
8 9	76003	23997	84738	15262	08734	91266	52
.9	76021	23979	84764	15236	08743 10.08752	91257 9.91248	51 50
10 11	9.76039 76057	10.23961 23943	9.84791 84818	10.15209 15182	08761	91239	49
12	76075	23925	84845	15155	08770	91230	48
13	76093	23907	84872	15128	08779	91221	47
14	76111	23889	84899	15101	08788	91212	46
15	9.76129	10.23871	9.84925	10.15075	10.08797	9.91203	45
16	76146	23854	84952	15048	08806 08815	91194 91185	44 43
17 18	76164 76182	23836 23818	84979 85006	15021 14994	08824	91176	42
19	76200	23800	85033	14967	08833	91167	41
20	9.76218	10.23782	9.85059	10.14941	10.08842	9.91158	40
21	76236	23764	85086	14914	08851	91149	39
22	76253 76271	23747	85113	14887	08859	91141	38
23	76271	23729	85140	14860	08868	91132	37
24	76289	23711	85166	14834	08877	91123 9.91114	36 35
25 26	9.76307 76324	10.23693 23676	9.85193 85220	10.14807 14780	10.08886 08895	91105	34
20	76342	23658	85247	14753	08904	91096	33
27 28 29	76360	23640	85273	14727	08913	91087	32
29	76378	23622	85300	14727 14700	08922	91078	31
30	9.76395	10.23605	9.85327	10.14673	10.08931	9.91069	30
31	76413	23587	85354	14646	08940	91060	29
32	76431	23569 23552	85380 85407	14620 14593	08949 08958	91051 91042	28 27
33 34	76448 76466	23534	85434	14566	08967	91033	26
35	9.76484	10.23516	9.85460	10.14540	10.08977	9.91023	25
36	76501	23499	85487	14513	08986	91014	24
37	76519	23481	85514	14486	08995	91005	23
38	76537	23463	85540	14460	09004	90996	22
39	76554	23446	85567	14433	09013	90987	21 20
40 41	9.76572 76590	10.23428 23410	9.85594 85620	10.14406 14380	10.09022 09031	9.90978 90969	19
42	76607	23393	85647	14353	09040	90960	18
43	76625	23375	85674	14326	09049	90951	17
44	76642	23358	85700	14300	09058	90942	16
45	9.76660	10.23340	9.85727	10.14273	10.09067	9.90933	15
46	76677	23323	85754	14246	09076	90924	14 13
47	76695	23305 23288	85780 85807	14220 14193	09085 09094	90915 90906	12
48 49	76712 76730 -	23270	85834	14166	09104	90896	iĩ
50	9.76747	10.23253	9.85860	10.14140	10.09113	9.90887	10
51	76765	23235	85887	14113	09122	90878	9
52	76782	23218	85913	14087	09131	90869	8
53	76800	23200	85940	14060	09140	90860	7
54	76817	23183	85967	14033	09149 10.09158	90851 9,90842	6 5
55	9.76835	10.23165	9.85993 86020	· 10.14007 13980	09168	9.90842	4
56 57	76852 76870	23148 23130	86046	13954	09177	90823	3
58	76887	23113	86073	13927	09186	90814	2
59	76904	23096	86100	13900	09195	90805	1
60	76922	23078	86126	13874	09204	90796	0
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

36 °		Logarithms.						
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.	
0	9.76922	10.23078	9.86126	10.13874	10.09204	9.90796	60	
ĭ	76939	23061	86153	13847	09213	90787	59	
2	76957	23043	86179	13821	09223	90777	58	
3	76974	23026	86206	13794 13768	09232	90768	57	
5	76991	23009	86232	13768	09241	90759	56	
5	9.77009	10.22991	9.86259	10.13741	10.09250 09259	9.90750 90741	55 54	
6	77026	22974 22957	86285 86312	13715 13688	09269	90731	53	
7	77043 77061	22939	86338	13662	09278	90722	52	
8	77078	22922	86365	13635	09287	90713	51	
10	9.77095	10.22905	9.86392	10.13608	10.09296	9.90704	50	
ii	77112	22888	86418	13582	09306	90694	49	
12	77130	22870	86445	13555	09315	90685	48	
12 13	77147	22853	86471	13529	09324	90676	47	
14	77164	22836	86498	13502	09333	90667	46	
15	9.77181	10.22819	9.86524	10.13476	10.09343	9.90657	45	
16	77199	22801	86551	13449	09352	90648	44	
17	77216	22784	86577	13423	09361	90639	43	
18	77233	22767	86603	13397 13370	09370 09380	90630 90620	42	
19	77250 9.77268	22750 10.22732	86630 9.86656	10.13344	10.09389	9.90611	40	
20 21	9.77285	22715	86683	13317	09398	90602	39	
25	77302	22698	86709	13291	09408	90592	38	
22 23	77210	22681	86736	13264	09417	90583	37	
24	77336	22664	86762	13238	09426	90574	36	
25	9.77353	10.22647	9.86789	10.13211	10.09435	9.90565	35	
25 26 27 28 29	77370	22630	86815	13185	09445	90555	34	
27	77387	22613	86842	13158	09454	90546	3 3	
28	77405	22595	86868	13132	09463	90537	32	
29	77422	22578	86894	13106	09473	90527 9.90518	31	
30	9.77439	10.22561	9.86921	10.13079	10.09482 09491	90509	30 29	
31	77456	22544 22527	86947 86974	13053 13026	09501	90499	28	
32 33 34 35	77473 77490	22510	87000	13000	09510	90490	27	
24	77507	22493	87027	12973	09520	90480	26	
35	9.77524	10.22476	9.87053	10.12947	10.09529	9.90471	25	
36	77541	22459	87079	12921	09538	90462	24	
36 37	77558	22442	87106	12894	09548	90452	23	
38 39	77575	22425	87132	12868	09557	90443	22	
39	77592	22408	87158	12842	09566	90434	21	
40	9.77609	10.22391	9.87185	10.12815	10.09576	9.90424	20	
41	77626	22374	87211	12789	09585	90415	19	
42	77643	22357	87238	12762	09595	90405	18	
43	77660	22340 22323	87264	12736	09604 09614	90396 90386	17 16	
44	77677	10.22306	87290 9.87317	12710 10.12683	10.09623	9.90377	15	
45 46	9.77694 77711	22289	87343	12657	09632	90368	14	
47	77728	22272	87369	12631	09642	90358	13	
48	77744	22256	87396	12604	09651	90349	12	
49	77761	22239	87422	12578	09661	90339	11	
50	9.77778	10.22222	9.87448	10.12552	10.09670	9.90330	10	
50 51	77795	22205	87475	12525	09680	90320	9	
52 L	77812	22188	87501	12499	09689	90311	8	
53	77829	22171	87527	12473	09699	90301	7	
53 54 55	77846	22154	87554	12446	09708	90292	7 6 5	
55	9.77862	10.22138	9.87580	10.12420	10.09718	9.90282 90273	3	
56 57	77879	22121	87606 87633	12394 12367	09727 09737	90273	9	
5/	77896 77013	22104 22087	87659	12367	09746	90254	2	
58 59	77913 77930	22087	87685	12315	09756	90244	3 2 1 0	
60	77946	22054	87711	12289	09765	90235	ō	
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.	

37°	Logarithms.								
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.		
0	9.77946	10.22054	9.87711	10.12289	10.09765	9.90235	60		
1 2	77963	22037	87738	12262	09775	90225	59		
2	77980	22020	87764	12236	09784	90216	58		
3 4 5 6 7	77997 78013	22003 21987	87790 87817	12210 12183	09794 09803	90206 90197	57 56		
5	9.78030	10.21970	9.87843	10 12157	10.09813	9.90187	55		
6	78047	21953	87869	10.12157 12131	09822	90178	54		
7	78063	21937	87895	12105	09832	90168	53		
8	78080	21920	87922	12078	09841	.90159	52		
.9	78097	21903	87948	12052	09851	90149	51		
10 11	9.78113 78130	10.21887 21870	9.87974 88000	10.12026 12000	10.09861	9.90139 90130	50 49		
12	78147	21853	88027	11973	09880	90120	48		
13	78163	21837	88053	11947	09889	90111	47		
14	78180	21820	88079	11921	- 09899	90101	46		
15	9.78197	10.21803	9.88105	10.11895	10.09909	9.90091	45		
16	78213	21787 21770	88131	11869	09918	90082	44		
17	78230 78246	21770	88158	11842 11816	09928 09937	90072 90063	43		
18 19	78246 78263	21737	88184 88210	11790	09947	90053	41		
20	9.78280	10.21720	9.88236	10.11764	10.09957	9.90043	40		
21	78296	21704	88262	11738	09966	90034	39		
22	78313	21687	88289	11711	09976	90024	38		
23	78329	21671	88315	11685	09986	90014	37		
24	78346	21654	88341	11659	09995	90005	36		
25	9.78362 78379	10.21638 21621	9.88367 88393	10.11633 11607	10.10005 10015	9.89995 89985	35 34		
26 27 28 29	78395	21605	88420	11580	10013	89976	33		
28	78412	21588	88446	11554	10034	89966	32		
29	78428	21572	88472	11528	10044	89956	31		
80	9.78445	10.21555 21539	9.88498	10.11502 11476	10.10053	9.89947	30		
81	78461	21539	88524	11476	10063	89937	29		
32 33	78478	21522	88550	11450	10073 10082	89927 89918	28 27		
33 34	78494 78510	21506 21490	88577 88603	11423 11397	10092	88808	26		
35	9.78527	10.21473	9.88629	10.11371	10.10102	9.89898	25		
36	78543	21457	88655	11345	10112	89888	24		
37	78560	21440	88681	11319	10121	89879	23		
38	78576	21424	88707	11293	10131	89869	22		
39 40	78592	21408	88733	11267	10141	89859	21 20		
41	9.78609 78625	10.21391 21375	9.88759 88780	10.11241 11214	10.10151 10160	9.89849 89840	19		
42	78642	21358	88812	11188	10170	89830	18		
43	78658	21342	88838	11162	10180.	89820	17		
44	78674	21326	88864	11136	10190	89810	16		
45	9.78691	10.21309 21293	9.88890	10.11110	10.10199	9.89801	15		
46	78707	21293	88916	11084	10209	89791	14		
47 48	78723 7873 9	21277 21261	88942 88968	11058 11032	10219 10229	89781 89771	13		
49	78756	21244	88994	11006	10239	89761	ii		
50	9.78772	10.21228	9.89020	10.10980	10.10248	9.89752	10		
51	78788	21212	89046	10954	10258	89742	9		
52	78805	21195	89073	10927	10268	89732	8 7		
53	78821	21179	89099	10901	10278	89722	7		
54 55	78837 9.78853	21163 10.21147	89125 9.89151	10875 10.10849	10288 10.10298	89712 9.89702	6		
56	78869	21131	89177	10.10849	10.10298	9.89702 89693	5		
57	78886	21114	89203	10797	10317	89683	3		
58	78902	21098	89229	10771	10327	89673	3 2 1		
59	78918	. 21082	89255	10745	10337	89663	1		
60	78934	21066	89281	10719	10347	89653	0		
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.		

3 8º			Logar	ithms.			141°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.78934	10.21066	9.89281	10.10719	10.10347	9.89653	60
1	78950	21050	89307	10693	10357	89643	59
2	78967	21033 21017	89333 89359	10667 10641	10367 10376	89633 89624	58 57
2 3 4 5	78983 78999	21017	89385	10615	10376	89614	56
5	9.79015	10,20985	9.89411	10.10589	10.10396	9.89604	55
6	79031	20969	89437	10563	10406	89594	54
7	79047	20953	89463	10537	10416	89584	53
8	79063	20937 20921	89489	10511	10426	89574 89564	52 51
- 10	79079 9.79095	10.20905	89515 9.89541	10485 10.10459	10436 10.10446	9.89554	50
11	79111	20889	89567	10433	10456	89544	49
12 13	79128	20872	89593	10407	10466	89534	48
13	79144	20856	89619	10381	10476	89524	47
14	79160 9.79176	20840 10.20824	9.89645 9.89671	10355	10486 10,10496	89514 9.89504	46 45
15 16	79176	20808	89697	10.10329 10303	10.10496	9.89304 89495	44
17	79208	20792	89723	10277	10515	89485	43
18	79224	20776	89749	10251	10525	89475	42
19 20	79240	20760	89775	10225	10535	89465	41
20	9.79256 79272	10.20744	9.89801 89827	10.10199 10173	10.10545 10555	9.89455 89445	40 39
21 22	79288	20728 20712	89853	10173	10565	89435	38
23	79304	20696	89879	10121	10575	89425	37
24	79319	20681	89905	10095	10585	89415	36
25 26	9.79335	10.20665	9.89931	10.10069	10.10595	9.89405	35
26	79351 79367	20649	89957 89983	10043	10605	89395 89385	34
27 28 29 30	79367 79383	20633 20617	90009	10017 09991	10615 10625	89375	32
29	79399	20601	90035	09965	10636	89364	31
30	9.79415	10.20585	9.90061	10.09939	10.10646	9.89354	30
31	79431	20569	90086	09914	10656	89344	29
32 33	79447 79463	20553 20537	90112 90138	09888 09862	10666 10676	89334 89324	28 27
34	79478	20522	90164	09836	10686	89314	26
35	9.79494	10.20506	9.90190	10.09810	10.10696	9.89304	25
36	79510	20490	90216	09784	10706	89294	24
37	79526	20474	90242	09758	10716	89284	23 22
38 39	79542 79558	20458 20442	90268 90294	09732 09706	10726 10736	89274 89264	21
40	9.79573	10.20427	9.90320	10.09680	10.10746	9.89254	20
41	79589	20411	90346	09654	10756	89244	19
42	79605	20395	90371	09629	10767	89233	18
43	79621	20379	90397	09603	10777	89223	17
44 45	79636 9.79652	20364 10.20348	90423 9.90449	09577 10.09551	10787 10.10797	89213 9.89203	16 15
46	79668	20332	90475	09525	10807	89193	14
47	79684	20316	90501	. 09499	10817	89183	13
48	79699	20301	90527	09473	10827	89173	12
49	79715	20285	90553	09447	10838	89162	11
50 51	9.79731 79746	10.20269	9.90578 90604	10.09422 09396	10.10848 10858	9.89152 89142	10
52	79762	20238	90630	09370	10868	89132	8
53 54	79778	20222	90656	09344	10878	89122	7
54	79793	20207	90682	09318	10888	89112	7 6 5 4 3 2
55	9.79809	10.20191	9.90708	10.09292	10.10899	9.89101	5
56 57	79825 79840	20175 20160	90734 90759	09266 09241	10909 10919	89091 89081	9
58	79840 79856	20160	90785	09241	10919	89071	2
59	79872	20128	90811	09189	10940	89060	1
60	79887	20113	90837	09163	10950	89050	0
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

39°				140°			
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.79887	10.20113	9.90837	10.09163	10.10950	9.89050	60
1	79903	20097	90863	09137	10960	89040	59
2 3	79918	20082	90889	09111	10970	89030	58
3	79934	20066	90914	09086	10980	89020	57
4 5 6	79950 9.79965	20050 10.20035	90940 9.90966	09060 10.09034	10991 10.11001	89009 9.88999	56 55
6	79981	20019	90992	09008	11011	88989	54
7	79996	20004	91018	08982	11022	88978	53
8	80012	19988	91043	08957	11032	88968	52
8	80027	19973	91069	08931	11042	88958	51
10	9.80043	10.19957	9.91095	10.08905	10.11052	9.88948	50
11	80058	19942	91121	08879	11063	88937	49
12	80074	19926	91147	08853	11073	88927	48
13	80089	19911	91172	08828	11083	88917	47 46
14 15	80105 9.80120	19895 10.19880	91198 9.91224	08802 10.08776	11094 10.11104	88906 9.88896	45
16	80136	19864	91250	08750	11114	88886	44
17	80151	19849	91276	08724	11125	88875	43
18	80166	19834	91301	08699	11135	88865	42
19	80182	19818	91327	08673	11145	88855	41
20	9.80197	10.19803	9.91353	10.08647	10.11156	9.88844	40
21	80213	19787	91379	08621	11166	88834	39
22	80228	19772	91404	08596	11176	88824	38
23	80244	19756	91430	08570	11187	88813	37
24	80259	19741	91456	08544	11197	88803	36
25 26	9.80274	10.19726	9.91482	10.08518	10.11207	9.88793	35
20	80290 80305	19710 19695	91507 91533	08493 08467	11218 11228	88782 88772	34 33
27 28	80320	19680	91559	08441	11239	88761	32
29	80336	19664	91585	08415	11249	88751	31
30	9.80351	10.19649	9.91610	10.08390	10.11259	9.88741	30
31	80366	19634	91636	08364	11270	88730	29
32	80382	19618	91662	08338	11280	88720	28
33	80397	19603	91688	08312	11291	88709	. 27
34	80412	19588	91713	08287	11301	88699	26
35 36 37	9.80428	10.19572	9.91739	10.08261	10.11312	9.88688	25
36	80443	19557	91765	08235	11322	88678	24 23
38	80458 80473	19542 19527	91791 91816	08209 08184	11332 11343	88668 88657	22
39	80489	19527	91842	08158	11353	88647	21
40	9.80504	10.19496	9.91868	10.08132	10.11364	9.88636	20
41	80519	19481	91893	08107	11374	88626	19
42	80534	19466	91919	08081	11385	88615	18
43	80550	19450	91945	08055	11395	88605	17
44	80565	19435	91971	08029	11406	88594	16
45	9.80580	10.19420	9.91996	10.08004	10.11416	9.88584	15
46	80595	19405	92022	07978	11427	88573	14
47 48	80610	19390	92048	07952	11437	88563	13 12
48	80625 80641	19375 19359	92073 92099	07927 07901	11448 11458	88552 88542	11
50	9.80656	10.19344	9.92125	10.07875	10.11469	9.88531	10
50 51	80671	19329	92150	07850	11479	88521	9
52	80686	19314	92176	07824	11490	88510	8
53	80701	19299	92202	07798	11501	88499	7
54	80716	19284	92227	07773	11511	88489	6
55	9.80731	10.19269	9.92253	10.07747	10.11522	9.88478	5
56	80746	19254	92279	07721	11532	88468	4
57	80762	19238	92304	07696	11543	88457	3 2
58	80777	19223	92330	07670	11553	88447	2
59 60	80792 80807	19208 19193	92356 92381	07644 07619	11564 11575	88436 88425	1 0
- M.	Cosine.		Cotangent.		Cosecant.	Sine,	M.

40°			Logar	ithms.			139°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine,	M.
0	9.80807	10.19193	9.92381	10.07619	10.11575	9.88425	60
1	80822	19178	92407	07593	11585	88415	59
3	80837	19163	92433	07567	11596	88404	58
3	80852	19148	92458	07542	11606	88394	57
4 5 6	80867 9.80882	19133 10.19118	92484 9.92510	07516 10.07490	11617 10.11628	88383 9.88372	56 55
6	80897	19103	9.92510	07465	11638	88362	54
7	80912	19088	92561	07439	11649	88351	53
8	80927	19073	92587	07413	11660	88340	52
ğ	80942	19058	92612	07388	11670	88330	51
10	9.80957	10.19043	9.92638	10.07362	10.11681	9.88319	50
11	80972	19028	92663	07337	11692	88308	49
12	80987	19013	92689	07311	11702	88298	48
13	81002	18998	92715	07285	11713	88287	47
14	81017 9.81032	18983 10.18968	92740 9.92766	07260 10.07234	11724 10.11734	88276 9.88266	46
15 16	81047	18953	9.92700	07208	11745	88255	44
17	81061	18939	92817	07183	11756	88244	43
18	81076	18924	92843	07157	11766	88234	42
19	81091	18909	92868	07132	11777	88223	41
20	9.81106	10.18894	9.92894	10.07106	10.11788	9.88212	40
21	81121	18879	92920	07080	11799	88201	39
22	81136	18864	92945	07055	11809	88191	38
23	81151	18849	92971	07029	11820	88180	37
24	81166	18834	92996	07004	11831	88169	36
25	9.81180	10.18820 18805	9.93022	10.06978	10.11842	9.88158	35
25 26 27	81195	18805	93048 93073	06952 06927	11852	88148	34
27	81210 81225	18775	93073	06901	11863 11874	88137 88126	33
20	81240	18760	93124	06876	11885	88115	31
28 29 30	9.81254	10.18746	9.93150	10.06850	10.11895	9.88105	30
31	81269	18731	93175	06825	11906	88094	29
32	81284	18716	93201	06799	11917	88083	28
33	81299	18701	93227	06773	11928	88072	27
34	81314	18686	93252	06748	11939	88061	26
35 36	9.81328	10.18672	9.93278	10.06722	10.11949	9.88051	25
36	81343	18657	93303	06697	11960	88040	24
87	81358 81372	18642 18628	93329 93354	06671 06646	11971 11982	88029 88018	23 22
38 39	81387	18613	93380	06620	11993	88007	21
40	9.81402	10.18598	9.93406	10.06594	10.12004	9.87996	20
41	81417	18583	93431	06569	12015	87985	19
42	81431	18569	93457	06543	12025	87975	18
43	81446	18554	93482	06518	12036	87964	17
44	81461	18539	93508	06492	12047	87953	16
45	9.81475	10.18525	9.93533	10.06467	10.12058	9.87942	15
46	81490	18510	93559	06441	12069	87931	14
47	81505	18495	93584	06416	12080	87920	13
48 49	81519 81534	18481 18466	93610 93636	06390 06364	12091 12102	87909 87898	12 11
50	9.81549	10.18451	9,93661	10.06339	10.12113	9.87887	10
51	81563	18437	93687	06313	12123	87877	9
52	81578	18422	93712	06288	12134	87866	8
53	81592	18408	93738	06262	12145	87855	7
54	81607	18393	93763	06237	12156	87844	6
55	9.81622	10.18378	9.93789	10.06211	10.12167	9.87833	5
56	81636	18364	93814	06186	12178	87822	4
57	81651	18349	93840	06160	12189	87811	3 2
58	81665	18335	93865	06135	12200	87800	2
59	81680	18320	93891	06109	12211	87789	Ī
60	81694	18306	93916	06084	12222	87778	0
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

410			Logar	Logarithms.			138°	
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.	
0.	9.81694	10.18306	9.93916	10.06084	10.12222	9.87778	60	
1	81709	18291 18277	93942	06058	12233	87767	59	
2	81723	18277	93967	06033	12244	87756	58	
3 4 5 6 7 8	81738 81752	18262 18248	93993 94018	06007 05982	12255	87745	57	
5	9.81767	10.18233	9.94044	10.05956	12266 10.12277	87734 9.87723	56 55	
6	81781	18219	94069	05931	12288	87712	54	
7	81796	18204	94095	05905	12299	87701	53	
8	81810	18190	94120	05880	12310	87690	52	
9	81825	18175	94146	05854	12321	87679	51	
10	9.81839	10.18161	9.94171	10.05829	10.12332	9.87668	50	
11	81854	18146	94197	05803	12343	87657	49	
12 13	81868 81882	18132 18118	94222 94248	05778	12354	87646	48	
14	81897	18103	94273	05752 05727	12365 12376	87635 87624	47	
15	9.81911	10.18089	9.94299	10.05701	10.12387	9.87613	45	
16	81926	18074	94324	05676	12399	87601	44	
17	81940	18060	94350	05650	12410	87590	43	
18	81955	18045	94375	05625	12421	87579	42	
19	81969	18031	94401	05599	12432	87568	41	
20	9.81983	10.18017	9.94426	10.05574	10.12443	9.87557	40	
21 22 23	81998	18002	94452	05548	12454	87546	39	
22	82012	17988	94477	05523	12465	87535	38	
24	82026 82041	17974 17959	94503 94528	05497 05472	12476	87524	37	
25	9.82055	10.17945	9.94554	10.05446	12487 10.12499	87513 9.87501	36 35	
26	82069	17931	94579	05421	12510	87490	34	
27	82084	17916	94604	05396	12521	87479	33	
28	82098	17902	94630	05370	12532	87468	32	
29	82112	17888	94655	05345 10.05319	12543	87457	31	
30	9.82126	10.17874	9.94681	10.05319	10.12554	9.87446	30	
31	82141	17859	94706	05294	12566	87434	29	
32 33	82155	17845	94732	05268	12577	87423	28	
34	82169 82184	17831 17816	94757 94783	05243 05217	12588 12599	87412	27 26	
35	9.82198	10.17802	9.94808	10.05192	10.12610	87401 9.87390	25	
36	82212	17788	94834	05166	12622	87378	24	
37	82226	17774	94859	05141	12633	87367	23	
38	82240	17760	94884	05116	12644	87356	22	
39	82255	17745 10.17731 17717	94910	05090 10.05065	12655	87345	-21	
40	9.82269	10.17731	9.94935	10.05065	10.12666	9.87334	20	
41	82283	17717	94961	05039	12678	87322	19	
42 43	82297 82311	17703	94986	05014	12689	87311	18	
44	82326	17689 17674	95012 95037	04988 04963	12700	87300 87288	17 16	
45	9.82340	10.17660	9.95062	10.04938	12712 10.12723	9.87277	15	
46	82354	17646	95088	04912	12734	87266	14	
47	82368	17632	95113	04887	12745	87255	13	
48	82382	17618	95139	04861	12757	87243	12 11	
49	82396	17604	95164	04836	12768 10.127 7 9	87232		
50 51	9.82410	10.17590	9.95190	10.04810	10.12779	9.87221	10	
52	82424	17576 17561	95215	04785	12791	87209	9	
53	82439 82453	17501	95240 95266	04760 04734	12802 12813	87198 87187	8 7	
54	82467	17547 17533 10.17519	95291	04709	12825	87175	6	
55	9,82481	10.17519	9.95317	10.04683	10.12836	9.87164	6 5 4 8 2	
56	82495	17505	95342	04658	12847	87153	4	
57	82509	17491	95368	04632	12859	87141	8	
58	82523	17477	95393	04607	12870	87130	2	
59	82537	17463	95418	04582	12881	87119		
60	82551	17449	95444	04556	12893	87107	0	
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.	

M. Sine Cosecant Tangent Cotangent Secant Cosine M.	42 °			Logar	ithms.			137°
1 82565 17435 95469 04505 12915 87085 58 3 82593 17407 95520 04480 12927 87085 58 5 9,82621 10.17379 9,95515 10.04429 10.12850 987020 56 5 9,82621 10.17379 9,95571 10.04429 10.12850 987020 56 7 82649 17351 96627 04378 12948 87016 52 8 82663 17387 96647 04353 12984 87016 52 9 82677 17323 96672 04328 12995 87005 51 10 9,82691 10.17309 9,95698 10.04302 10.13007 9,86993 50 11 82705 17226 95774 04226 13041 86959 47 14 82749 17223 95825 10.04175 10.13064 9,86936 45 16	M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
2 82579 17421 95495 04505 12915 87085 58 3 82598 17407 95520 04490 12951 87085 58 5 9.82621 10.17379 9.55571 10.04429 10.12950 9.7050 55 6 8.82635 17386 95596 04404 12961 87089 54 7 82649 17351 95622 04378 12972 87028 53 8 82663 17337 95647 04338 12972 87028 53 10 9.82691 10.17309 9.95682 10.4032 11.3907 9.8593 50 11 82705 17295 95723 04277 13018 86982 49 12 82719 17281 95748 04252 13030 88970 48 13 82733 17267 95774 04226 13041 86959 47 14 82747 17225 95799 04201 13053 86947 46 16 82775 17225 95855 04125 13087 86947 46 16 82775 17225 95855 04125 13087 86924 41 17 82788 17112 95875 04125 13087 86924 41 18 82802 17198 95901 04099 13098 86902 42 19 82816 17184 95926 04074 13110 86890 41 20 9.82830 10.17107 9.96782 10.0498 13138 86882 29 21 82844 17156 95977 04028 13138 86892 42 22 82858 17112 96002 36998 13145 86890 41 23 82872 17128 9602 36998 13145 86890 41 24 82845 17115 96053 03947 13168 86892 42 24 82885 10.17107 96104 03896 13141 86899 934 24 82885 10.17107 96104 03896 13141 86899 934 25 9.82899 10.17101 9.96078 10.03892 13158 86867 39 26 82913 17087 96104 03896 13141 86899 934 27 82927 17073 96129 03871 13168 86832 36 28 82931 17087 96104 03896 13191 86869 934 38 83010 16990 96281 03749 13169 86869 934 38 83010 16990 96281 03749 13224 86786 32 39 82898 10.17001 9.96078 10.03922 10.13237 9.86763 30 9.82968 10.17032 9.96205 10.03951 10.13237 9.86763 30 9.82986 10.17045 96180 03896 13191 86869 934 34 83023 16979 96307 03698 13248 86752 29 39 83095 10.6894 9.96357 03648 10.13319 9.86670 16 41 83120 16898 96357 03640 13306 86670 22 41 83180 16899 96357 03640 13306 86670 22 42 82885 10.1768 996180 03896 13341 86659 21 43 838078 16892 96686 03344 13269 86604 16 45 9.83174 10.16826 9.96586 10.03791 10.3351 13.3458 86572 12 59 82995 10.03641 10.13313 9.8667 9510 10.3899 13.3458 86672 25 39 83092 16908 96357 03640 13306 8660 16 46 833878 16662 96966 03344 10.13411 9.86699 15 50 9.83310 10.16690 99615 03851 10.13528 986472 55 50 9.83310 10.16690 99686 10.03641 10.13528 98667 12 50 9.83324 10.16789 96666 03344 13.1368					10.04556			
4 82607 17383 95545 04455 12388 87062 56 82621 1017379 95571 10.04429 10.12950 87039 54 7 82649 17351 95622 04378 12972 87028 54 8 82631 17337 95647 04333 12984 87016 52 9 82677 17323 95672 04328 12995 8705 51 10 9.82691 10.17309 9.5682 10.04302 10.13007 9.8693 51 11 82705 17285 95723 04277 13018 86982 49 12 82719 17281 95748 04252 13041 86959 47 14 82747 17253 95799 04201 13053 86947 44 15 9.82761 10.1729 9.95850 04155 13046 9.8636 45 16 82774 17225 958	1	82565	17435	95469	04531	12904	87096	
4 82607 17383 95545 04455 12388 87062 56 82621 1017379 95571 10.04429 10.12950 87039 54 7 82649 17351 95622 04378 12972 87028 54 8 82631 17337 95647 04333 12984 87016 52 9 82677 17323 95672 04328 12995 8705 51 10 9.82691 10.17309 9.5682 10.04302 10.13007 9.8693 51 11 82705 17285 95723 04277 13018 86982 49 12 82719 17281 95748 04252 13041 86959 47 14 82747 17253 95799 04201 13053 86947 44 15 9.82761 10.1729 9.95850 04155 13046 9.8636 45 16 82774 17225 958	2	82579	17421		04505	12915	87085	58
5 9,82621 10,17379 9,95571 10,04429 10,12350 9 87050 55 7 82649 17351 96522 04378 12972 87028 53 8 82663 17337 95672 04328 12995 87065 51 10 9.82691 10,17309 9,3688 10,04302 10,13007 9,86933 50 11 82705 17285 95723 04277 13018 86982 42 12 82719 17281 95748 04252 13030 86970 48 13 82733 17267 95774 04226 13041 86954 46 15 9,82761 10,17239 9,9825 0,4175 10,13064 9,86936 46 17 82788 17212 95875 04125 13087 86913 43 18 82202 17188 95926 04074 13110 86964 44 19	3		17907	95520	04455	12927	87073 87069	
8 82663 17337 95647 04353 12984 87016 52 10 9.82691 10.17309 9.95698 10.04302 10.13007 9.86993 50 11 82705 17285 95728 04272 13018 86982 49 12 82719 17281 95748 04252 13030 86970 48 13 82733 17267 95774 04252 13041 86959 46 14 82747 17253 95895 10.04175 10.13064 9.86936 45 15 9.82761 10.17239 9.58825 10.04175 10.13064 9.86936 45 16 82775 17225 95850 04150 13076 86924 44 17 82788 17212 95856 04074 13110 86890 41 19 82361 17184 95920 04049 10.13321 86876 39 21	5		10 17370					
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8 82663 17337 95647 04353 12984 87016 52 10 9.82691 10.17309 9.95698 10.04302 10.13007 9.86993 50 11 82705 17285 95728 04272 13018 86982 49 12 82719 17281 95748 04252 13030 86970 48 13 82733 17267 95774 04252 13041 86959 46 14 82747 17253 95895 10.04175 10.13064 9.86936 45 15 9.82761 10.17239 9.58825 10.04175 10.13064 9.86936 45 16 82775 17225 95850 04150 13076 86924 44 17 82788 17212 95856 04074 13110 86890 41 19 82361 17184 95920 04049 10.13321 86876 39 21	7	82649	17351	95622	04378		87028	53
11 82705 17285 99723 04277 13018 86982 49 13 82733 17267 95774 04226 13041 86959 4 14 82747 17253 95799 04201 13053 86947 4 15 9.82761 10.17239 9.95825 10.04175 10.13064 9.86936 45 16 82775 17225 95850 04150 13076 86913 43 17 82788 17212 95875 04125 13087 86913 43 18 82202 17198 95901 04099 13098 86902 42 19 82516 17184 95926 04074 13110 86893 41 20 9.82830 10.17170 9.95952 10.04048 10.13121 9.86879 40 21 82844 17156 95977 04023 13133 868673 38 22 8285	8	82663	17337	95647	04353		87016	52
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15 9.82761 10.17239 9.95825 10.04175 10.13064 9.86936 445 17 82788 17212 95875 04125 13087 88913 43 18 82802 17198 95901 04099 13098 86902 42 19 82816 17184 95926 04074 13110 86890 41 20 9.82830 10.17170 9.95952 10.04048 10.13121 9.86879 42 21 82844 17156 95977 04023 13133 86867 39 22 82858 17112 96002 03998 13145 86855 38 24 82885 17115 96038 03947 13168 86852 36 25 9.82899 10.17101 9.96078 10.03922 10.13179 9.86821 35 26 82913 17087 96155 03845 13214 86786 32 27	12	82700 82719	17290		04252			
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18 82202 17198 95901 04099 13098 86902 42 19 82816 17184 95926 04074 13110 86902 42 20 9.82830 10.17170 9.95952 10.04048 10.13121 9.86879 40 21 82844 17156 95977 04023 13133 86867 38 22 82858 17142 96002 03972 13156 86844 37 24 82885 17115 96053 03947 13166 86844 37 25 9.82899 10.17101 9.96078 10.03922 10.13179 9.86821 35 26 8.2913 17087 96104 03896 13191 86809 34 27 8.2927 17073 96155 03845 13214 86786 32 28 82941 17059 96155 03845 13214 86786 32 29 8	16		17225					
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27 82927 17073 96129 03871 13202 86798 32 28 82941 17059 96155 03845 13214 86798 32 29 82955 17045 96180 03820 13225 86775 31 30 9.82968 10.17032 9.96205 10.03795 10.13237 9.86763 30 31 82982 17014 96256 03744 13260 86740 28 32 82996 17004 96256 03744 13260 86740 28 33 83010 16990 96281 03719 13272 86722 27 34 83023 16977 96307 03693 13283 86717 26 36 83051 16949 96357 03643 13306 86694 24 37 83065 16935 96383 03617 13318 86622 23 38 83078	24		17115	96053				36
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35 9.83037 10.16963 9.96332 10.03668 10.13295 9.86705 25 36 83061 16949 96357 03643 13306 86694 24 37 83065 16935 96383 03617 13318 86682 23 38 83078 16922 96408 03592 13341 86670 22 40 9.83106 10.16894 996459 10.03541 10.13353 9.86647 20 41 83120 16880 96484 03516 13365 86635 19 42 83133 16867 96510 03490 13376 86624 18 43 83161 16839 995560 03440 13400 86600 16 45 9.83174 10.16826 996586 10.0341 10.13411 9.86589 15 46 83188 16812 96611 03389 13423 86577 14 47	20		17087					34
35 9.83037 10.16963 9.96332 10.03668 10.13295 9.86705 25 36 83061 16949 96357 03643 13306 86694 24 37 83065 16935 96383 03617 13318 86682 23 38 83078 16922 96408 03592 13341 86670 22 40 9.83106 10.16894 996459 10.03541 10.13353 9.86647 20 41 83120 16880 96484 03516 13365 86635 19 42 83133 16867 96510 03490 13376 86624 18 43 83161 16839 995560 03440 13400 86600 16 45 9.83174 10.16826 996586 10.0341 10.13411 9.86589 15 46 83188 16812 96611 03389 13423 86577 14 47	28		17050		03845	19014		39
35 9.83037 10.16963 9.96332 10.03668 10.13295 9.86705 25 36 83061 16949 96357 03643 13306 86694 24 37 83065 16935 96383 03617 13318 86682 23 38 83078 16922 96408 03592 13341 86670 22 40 9.83106 10.16894 996459 10.03541 10.13353 9.86647 20 41 83120 16880 96484 03516 13365 86635 19 42 83133 16867 96510 03490 13376 86624 18 43 83161 16839 995560 03440 13400 86600 16 45 9.83174 10.16826 996586 10.0341 10.13411 9.86589 15 46 83188 16812 96611 03389 13423 86577 14 47	29		17045	96180	03820	13225	86775	31
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35 9.83037 10.16963 9.96332 10.03668 10.13295 9.86705 25 36 83061 16949 96357 03643 13306 86694 24 37 83065 16935 96383 03617 13318 86682 23 38 83078 16922 96408 03592 13341 86670 22 40 9.83106 10.16894 996459 10.03541 10.13353 9.86647 20 41 83120 16880 96484 03516 13365 86635 19 42 83133 16867 96510 03490 13376 86624 18 43 83161 16839 995560 03440 13400 86600 16 45 9.83174 10.16826 996586 10.0341 10.13411 9.86589 15 46 83188 16812 96611 03389 13423 86577 14 47	31			96231	03769	10240		29
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38 83078 16922 96408 03592 13341 86670 22 39 83092 16908 96438 03567 13341 86659 21 40 9.83106 10.16894 9.96459 10.03541 10.13353 9.86647 20 41 83120 16880 96484 03516 13385 9.86647 20 42 83133 16867 96510 03490 13376 86624 18 43 83161 16839 96586 03460 13400 866012 17 44 83161 16839 995560 03440 13400 86601 16 45 9.83174 10.16826 9.96586 10.03414 10.13411 9.86589 15 46 83188 16812 96611 03344 10.13411 9.86565 13 48 83215 16785 99682 03383 13445 86565 13 49	95	0 83025	10 16063			10 13295	9 86705	
38 83078 16922 96408 03592 13341 86670 22 39 83092 16908 96438 03567 13341 86659 21 40 9.83106 10.16894 9.96459 10.03541 10.13353 9.86647 20 41 83120 16880 96484 03516 13385 9.86647 20 42 83133 16867 96510 03490 13376 86624 18 43 83161 16839 96586 03460 13400 866012 17 44 83161 16839 995560 03440 13400 86601 16 45 9.83174 10.16826 9.96586 10.03414 10.13411 9.86589 15 46 83188 16812 96611 03344 10.13411 9.86565 13 48 83215 16785 99682 03383 13445 86565 13 49	36	83051						24
38 83078 16922 96408 03592 13341 86670 22 39 83092 16908 96438 03567 13341 86659 21 40 9.83106 10.16894 9.96459 10.03541 10.13353 9.86647 20 41 83120 16880 96484 03516 13385 9.86647 20 42 83133 16867 96510 03490 13376 86624 18 43 83161 16839 96586 03460 13400 866012 17 44 83161 16839 995560 03440 13400 86601 16 45 9.83174 10.16826 9.96586 10.03414 10.13411 9.86589 15 46 83188 16812 96611 03344 10.13411 9.86565 13 48 83215 16785 99682 03383 13445 86565 13 49	37				03617	13318		
40 9.83106 10.16894 9.96459 10.03541 10.13353 9.86647 20 41 83120 16880 96484 03516 13365 86635 19 42 83137 16853 96530 03490 13376 86624 18 43 83147 16853 96535 03465 13388 86612 17 44 83161 16839 96580 03440 13400 86600 16 45 9.83174 10.16826 996586 10.03414 10.13411 9.86589 15 46 83188 16812 96611 03389 13423 86577 14 47 83202 16798 96636 03364 13435 86565 13 48 83215 16785 96662 03338 13445 86542 11 50 9.83242 10.16758 9.96712 10.03288 10.13470 9.86330 10 51	38	83078	16922		03592		86670	
42 83133 16867 96510 03490 13376 86624 18 43 83147 16853 96536 03465 13388 86612 17 44 83161 16839 96560 03440 13400 86600 16 45 9.83174 10.16826 9.96586 10.03414 10.13411 9.86589 15 46 83188 16812 96611 03389 13423 86577 14 47 83202 16798 96636 03364 13435 86565 13 48 83215 16785 96662 03338 13446 86554 12 49 83229 16771 96687 03313 13458 86542 11 50 9.83242 10.16758 9.96712 10.03288 10.13470 9.86530 10 51 83256 16744 96738 03202 13482 86518 9 52 8327	39	83092	16908		03567	13341	86659	
42 83133 16867 96510 03490 13376 86624 18 43 83147 16853 96536 03465 13388 86612 17 44 83161 16839 96560 03440 13400 86600 16 45 9.83174 10.16826 9.96586 10.03414 10.13411 9.86589 15 46 83188 16812 96611 03389 13423 86577 14 47 83202 16798 96636 03364 13435 86565 13 48 83215 16785 96662 03338 13446 86554 12 49 83229 16771 96687 03313 13458 86542 11 50 9.83242 10.16758 9.96712 10.03288 10.13470 9.86530 10 51 83256 16744 96738 03202 13482 86518 9 52 8327	40	9.83106	10.16894		10.03541	10.13353	9.86647	20
43 83147 16853 96585 03465 13388 86612 17 44 83161 16839 96560 03440 13400 86600 16 45 9.83174 10.16826 9.96586 10.03414 10.13411 9.86589 15 46 83188 16812 96611 03384 10.13411 9.86589 15 47 83202 16778 99636 03364 13435 86565 13 48 83215 16785 96662 03338 13446 86554 12 49 83229 16771 96687 03313 13458 86542 11 50 9.83242 10.16788 9.96712 10.03288 10.13470 9.86330 10 51 83256 16744 96738 03237 13493 86507 8 52 83270 16730 96763 03237 13493 86507 8 54	41	83120	16880	96484	03516	13300	86635	19
44 83161 16839 96560 03440 13400 86600 16 45 9.83174 10.16826 9.96586 10.03414 10.13411 9.86589 15 46 83188 16812 96611 03389 13423 86577 14 47 83202 16798 96636 03364 13435 86565 13 48 83215 16785 96662 03338 13446 86554 12 49 83229 16771 96687 03313 13458 86542 11 50 9.83242 10.16758 9.96712 10.03288 10.13470 9.86530 10 51 83256 16744 96788 03222 13492 86518 9 52 83270 16730 96763 03237 13493 86507 8 53 83283 16717 96788 03212 13505 86495 7 54 83297<	42		16853			13388	86619	
45 9.83174 10.16826 9.96586 10.03414 10.13411 9.85589 15 46 83188 16812 96611 03389 13435 86577 14 47 83202 16778 96636 03364 13435 86565 13 48 83215 16785 96662 03338 13446 86554 12 49 83229 16771 96687 03313 13458 86542 21 50 9.83242 10.16758 9.96712 10.03288 10.13470 9.86530 10 51 83256 16744 96738 03237 13493 86507 8 52 83270 16730 96763 03237 13493 86507 8 53 83283 16717 96788 03212 13505 86495 7 54 83297 16703 98614 03186 13517 86483 6 56 83324 </td <td>44</td> <td></td> <td>16839</td> <td></td> <td>03440</td> <td></td> <td></td> <td></td>	44		16839		03440			
47 83202 16798 96636 03364 13435 86565 13 48 83215 16785 96662 03338 13446 86554 12 49 83229 16771 9687 03313 13458 86542 11 50 9.83242 10.16758 9.96712 10.03288 10.13470 9.86500 10 51 83256 16744 96783 03262 13482 86518 9 52 83270 16730 96763 03237 13493 86507 8 53 83283 16717 96788 03212 13505 86495 7 54 83297 16703 96814 03186 13517 86483 6 55 9.83310 10.16690 9.96839 10.03161 10.13528 9.86472 5 56 83324 16676 96864 03136 13540 86460 4 57 83338	45	9.83174	10.16826	9.96586	10.03414	10.13411	9.86589	
47 83202 16798 96636 03364 13435 86565 13 48 83215 16785 96662 03338 13446 86554 12 49 83229 16771 9687 03313 13458 86542 11 50 9.83242 10.16758 9.96712 10.03288 10.13470 9.86500 10 51 83256 16744 96783 03262 13482 86518 9 52 83270 16730 96763 03237 13493 86507 8 53 83283 16717 96788 03212 13505 86495 7 54 83297 16703 96814 03186 13517 86483 6 55 9.83310 10.16690 9.96839 10.03161 10.13528 9.86472 5 56 83324 16676 96864 03136 13540 86460 4 57 83338	46	83188	16812		03389	13423	86577	
49 83229 16771 96687 03313 13458 86542 11 50 9.83242 10.16758 9.96712 10.03288 10.13470 9.86530 11 51 83256 16734 96763 03262 13482 86518 9 52 83270 16730 96763 03237 13493 86507 8 53 83283 16717 96788 03212 13505 86495 7 54 83297 16703 96814 03186 12517 86483 6 55 9.83310 10.16690 9.96839 10.03161 10.13528 9.86472 5 56 83324 16676 96890 03110 13552 86460 4 57 83338 16662 96890 03110 13552 86448 3 58 83351 16649 96915 03085 13564 86436 2 59 83365	47		16798					
51 83256 16744 96738 03262 13482 86518 9 52 83270 16730 96768 03237 13493 86507 9 53 83283 16717 96788 03212 13505 86495 7 54 83297 16703 96814 03186 13517 86483 6 55 9.83310 10.16690 9.96839 10.03161 10.13528 9.8472 5 56 83324 16676 96864 03136 13540 86460 4 57 83338 16662 96890 03110 13552 86448 2 58 83351 16649 96915 03085 13564 86436 2 59 83365 16635 96940 03060 13575 86425 1 60 83378 16622 96966 03034 13587 86413 0			16785					
51 83256 16744 96738 03262 13482 86518 9 52 83270 16730 96768 03237 13493 86507 9 53 83283 16717 96788 03212 13505 86495 7 54 83297 16703 96814 03186 13517 86483 6 55 9.83310 10.16690 9.96839 10.03161 10.13528 9.8472 5 56 83324 16676 96864 03136 13540 86460 4 57 83338 16662 96890 03110 13552 86448 2 58 83351 16649 96915 03085 13564 86436 2 59 83365 16635 96940 03060 13575 86425 1 60 83378 16622 96966 03034 13587 86413 0	49	88229	10 16771		10 02288	10 12470		
54 83297 16703 96814 03186 13517 86483 6 55 9.83310 10.16690 9.96839 10.03161 10.15528 9.86472 5 56 83324 16676 96864 03136 13540 86460 4 57 83338 16662 96890 03110 13552 86448 3 58 83351 16649 96915 03085 13564 86436 2 59 83365 16635 96940 03060 13575 86425 1 60 83378 16622 96966 03034 13587 86413 0	51	83256	16744	9.90712	03262			10
54 83297 16703 96814 03186 13517 86483 6 55 9.83310 10.16690 9.96839 10.03161 10.15528 9.86472 5 56 83324 16676 96864 03136 13540 86460 4 57 83338 16662 96890 03110 13552 86448 3 58 83351 16649 96915 03085 13564 86436 2 59 83365 16635 96940 03060 13575 86425 1 60 83378 16622 96966 03034 13587 86413 0	52	83270	16730	96763	03237		86507	8
54 83297 16703 96814 03186 13517 86483 6 55 9.83310 10.16690 9.96839 10.03161 10.15528 9.86472 5 56 83324 16676 96864 03136 13540 86460 4 57 83338 16662 96890 03110 13552 86448 3 58 83351 16649 96915 03085 13564 86436 2 59 83365 16635 96940 03060 13575 86425 1 60 83378 16622 96966 03034 13587 86413 0	53	83283	16717	96788	03212	13505	86495	ž
56 83324 16676 96864 03136 13540 86460 4 57 83338 16662 96890 03110 13552 86448 3 58 83351 16649 96915 03085 13564 86436 2 59 83365 16635 96940 03060 13575 86425 1 60 83378 16622 96966 03034 13587 86413 0	54	83297	16703	96814	03186	13517	86483	6
58 83351 16649 96915 03085 13564 86436 2 59 83365 16635 96940 03060 13575 86425 1 60 83378 16622 96966 03034 13587 86413 0	55		10.16690		10.03161	10.13528		5
58 83351 16649 96915 03085 13564 86436 2 59 83365 16635 96940 03060 13575 86425 1 60 83378 16622 96966 03034 13587 86413 0	56	83324	16676		03136		86460	4
59 83365 16635 96940 03060 13575 86425 1 60 83378 16622 96966 03034 13587 86413 0	5/	83338						3
60 83378 16622 96966 03034 13587 86413 0	50		16625					1
M. Cosine. Secant. Cotangent, Tangent. Cosecant. Sine. M.			16622					
	M.	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine,	M.

430			Logar	:	136°		
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.83378	10.16622	9.96966	10.03034	10.13587	9.86413	60
1	83392	16608	96991	03009	13599	86401	59
2	83405	16595	97016	02984	13611	86389	58
3	83419	16581	97042	02958	13623	86377	57
4	83432 9.83446	16568 10.16554	97067 9.97092	02933 10.02908	13634 10.13646	86366 9.86354	56 55
5 6 7	83459	16541	97118	02882	13658	86342	54
7	83473	16527	97143	02857	13670	86330	53
8	83486	16514	97168	02832	13682	86318	52
9	83500	16500	97193	02807	13694	86306	51
10	9.83513	10.16487	9.97219	10.02781	10.13705	9.86295	50
11	83527	16473	97244	02756	13717	86283	49
12 13	83540	16460	97269	02731	13729	86271 86259	48
13	83554 83567	16446 16433	97295 97320	02705 02680	13741 13753	86247	46
15	9.83581	10.16419	9.97345	10.02655	10.13765	9.86235	45
16	83594	16406	97371	02629	13777	86223	44
17	83608	16392	97396	02604	13789	86211	43
18	83621	16379	97421	02579	13800	86200	42
19	83634	16366	97447	02553	13812	86188	41
20 21 22 23	9.83648	10.16352	9.97472	10.02528	10.13824	9.86176	40
21	83661	16339	97497	02503	13836	86164	39
22	83674	16326	97523	02477 02452	13848 13860	86152 86140	38
23	83688 83701	16312 16299	97548 97573	02452	13860	86128	36
24	9.83715	10.16285	9.97598	10.02402	10.13884	9.86116	35
26	83728	16272	97624	02376	13896	86104	34
27	83741	16259	97649	02376 02351	13908	86092	33
25 26 27 28 29	83755	16245	97674	02326	13920	86080	32
29	83768	16232	97700	02300	13932	86068	31
30	9.83781	10.16219	9.97725	10.02275	10.13944	9.86056	30
31	83795	16205	97750	02250	13956	86044	29
32 33	83808	16192	97776	02224 02199	13968 13980	86032 86020	28 27
34	83821 83834	*16179 16166	97801 97826	02199	13992	86008	26
35	9.83848	10.16152	9.97851	10.02149	10.14004	9.85996	25
36	83861	16139	97877	02123	14016	85984	24
36 37	83874	16126	97902	02098	14028	85972	23
38 39	83887	16113	97927	02073	14040	85960	22
39	83901	16099	97953	02047	14052	85948	21
40	9.83914	10.16086	9.97978	10.02022	10.14064	9.85936	20
41 42	83927 83940	16073 16060	98003 98029	01997 01971	14076 14088	85924 85912	19 18
43	83954	16046	98054	01946	14100	85900	17
44	83967	16033	98079	01921	14112	85888	16
45	9.83980	10.16020	9.98104	10.01896	10.14124	9.85876	15
46	83993	16007	98130	01870	14136	85864	14
47	84006	15994	98155	01845	14149	85851	13
48	84020	15980	98180	01820	14161	85839	12
49	84033	15967	98206	01794	14173	85827	11 10
50 51	9.84046	10.15954 15941	9.98231 98256	10.01769 01744	10.14185 14197	9.85815 85803	10
52	84059 84072	15928	98281	01719	14209	85791	
53	84085	15915	98307	01693	14205	85779	8 7 6 5 4
54	84098	15902	98332	01668	14234	85766	6
55	9.84112	10.15888	9.98357	10.01643	10.14246	9.85754	5
56 57	84125	15875	98383	01617	14258	85742	
57	84138	15862	98408	01592	14270	85730	3
58	84151	15849	98433	01567	14282	85718	1
59 60	84164 84177	15836 15823	98458 98484	01542 01516	14294 14307	85706 85693	0
M.	Cosine.	Secant.	Cotangent,		Cosecant.	Sine.	M.

440			Logar	ithms.			1359
M.	Sin e.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.84177	10.15823	9.98484	10.01516	10.14307	9.85693	60
1	84190	15810	98509	01491	14319	85681	59
2 3	84203	15797	98534	01466	14331	85669	58 57
4	84216 84229	15784 15771	98560 98585	01440 01415	14343 14355	85657 85645	56
5	9.84242	10.15758	9.98610	10.01390	10.14368	9.85632	56 55
6	84255	15745	98635	01365	14380	85620	54
7	84269	15731	98661	01339	14392	85608	53
8	84282	15718	98686	01314	14404	85596	52
9 10	84295 9.84308	15705 10.15692	98711 9.98737	01289 10.01263	14417 10.14429	85583 9.85571	51 50
11	84321	15679	98762	01238	14441	85559	49
12	84334	15666	98787	01213	14453	85547	48
13	84347	15653	98812	01188	14466	85534	47
14	84360	15640	98838	01162	14478	85522	46
15	9.84373	10.15627	9.98863	10.01137	10.14490	9.85510	45
16 17	84385 84398	15615 15602	98888 98913	01112 01087	14503 14515	85497 85485	44
18	84411	15589	98939	01061	14527	85473	42
19	84424	15576	98964	01036	14540	85460	41
	9.84437	10.15563	9.98989	10.01011	10.14552	9.85448	40
20 21 22 23	84450	15550	99015	00985	14564	85436	39
22	84463	15537	99040	00960	14577	85423	38 37
23	84476	15524	99065	00935	14589	85411	37
24	84489 9.84502	15511 10.15498	99090 9.99116	00910	14601	85399 9.85386	36 35
25 26 27 28	84515	15485	99141	10.00884 00859	10.14614 14626	85374	34
27	84528	15472	99166	00834	14639	85361	33
28	84540	15460	99191	00809	14651	85349	32
29 30	84553	15447	99217	00783	14663	85337	33 32 31
30	9.84566	10.15434	9.99242	10.00758	10.14676	9.85324	30 29 28 27 26
31	84579	15421	99267	00733	14688	85312	29
32 33	84592 84605	15408 15395	99293 99318	00707 00682	14701 14713	85299 85287	28
34	84618	15382	99343	00657	14726	85274	26
35	9.84630	10.15370	9.99368	10.00632	10.14738	9.85262	25
35 36	84643	15357	99394	00606	14750	85250	25 24
37	84656	15344	99419	00581	14763	85237	23 22 21
38 39	84669	15331	99444	00556	14775	85225	22
40	84682 9.84694	15318	99469 9.99495	00531 10.00505	14788 10.14800	85212 9.85200	20
41	84707	10.15306 15293	99520	00480	14813	85187	19
42	84720	15280	99545	00455	14825	85175	18
43	84733	15267	99570	00430	14838	85162	18 17
44	84745	15255	99596	00404	14850	85150	16
45	9.84758	10.15242	9.99621	10.00379	10.14863	9.85137	15
46	84771 84784	15229 15216	99646	00354	14875 14888	85125	14 13
47 48	84796	15204	99672 99697	00328 00303	14900	85112 85100	12
49	84809	15191	99722	00278	14913	85087	iī
49 50 51	9.84822	10.15178	9.99747	10.00253	10.14926	9.85074	10
51	84835	15165	99773	00227	14938	85062	9
52	84847	15153	99798	00202	14951	85049	8 7
53 54	84860	15140 15127	99823	00177	14963 14976	85037	6
55	84873 9.84885	10.15115	99848 9.99874	00152 10.00126	10.14988	85024 9.85012	5
56	84898	15102	99899	00101	15001	84999	4
57 I	84911	15089	99924	00076	15014	84986	3
58	84923	15077	99949	00051	15026	84974	2
59	84936	15064	99975	00025	15039	84961	1
60	84949	15051	10.00000	00000	15051	84949	- 0
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine,	M.

00		Na	tural T	igonom	etrical l	Function	15.	12	— 79°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.00000	1.0000	Infinite.	.00000	Infinite.	1.0000	.00000	1.0000	60
1	. 0029	.99971	3437.7	. 0029	3437.7	.0000	. 0000	.0000	59
2	. 0058	9942	1718.9	. 0058	1718.9	.0000	. 0000	.0000	58
3 4	. 0087	9913	1145.9 859.44	. 0087	1145.9	.0000	. 0000	.0000	57
5	.00145	99854	687.55	.00145	859.44 687.55	1.0000	.0000	.0000 1.0000	56 55
6	. 0174	9825	572.96	. 0174	572.96	.0000	. 0000	.0000	54
7	. 0204	9796	491.11	. 0204	491.11	.0000	. 0000	.0000	53
8	. 0233	9767	429.72	. 0233	429.72	.0000	. 0000	.0000	52
9	. 0262	9738	381.97	. 0262	381.97	.0000	. 0000	.0000	51
10	.00291	.99709	343.77	.00291	343.77	1.0000	.00000	.99999	50
11	. 0320	9680	312.52	. 0320	312.52	.0000	. 0000	. 9999	49
12 13	. 0349	. 9651 . 9622	286.48 64.44	. 0349	286.48 64.44	.0000	. 0001	. 9999	48 47
14	. 0407	9593	45.55	. 0407	45.55	.0000	. 0001	. 9999	46
15	.00436	.99564	229.18	.00436	229.18	1.0000	.00001	.99999	45
16	. 0465	9534	14.86	. 0465	14.86	.0000	. 0001	. 9999	44
17	. 0494	. 9505	02.22	. 0494	02.22	.0000	. 0001	. 9999	43
18	. 0524	. 9476	190.99	. 0524	190.98	.0000	. 0001	. 9999	42
19	. 0553	. 9447	80.93	. 0553	80.93	.0000	. 0001	. 9998	41
20	.00582	.99418	171.89	00582	171.88	1.0000	.00002	.99998	40
21	. 0611	. 9389	63.70	. 0611	63.70	.0000	. 0002	. 9998	39
22 23	. 0640	. 9360	56.26 49.47	. 0640	56.26 49.46	.0000	. 0002	9998	38
24	. 0669 . 0698	9331	43.24	. 0698	49.46	.0000	. 0002	. 9997	37 36
25	.00727	.99273	137.51	.00727	137.51	1.0000	.00003	.99997	35
26	. 0756	9244	32.22	. 0756	32.22	.0000	. 0003	. 9997	34
27	. 0785	. 9215	27.32	. 0785	27.32	.0000	. 0003	. 9997	33
28	. 0814	. 9185	22.78	. 0814	22.77	.0000	. 0003	. 9997	33 32
29	. 0843	. 9156	18.54	. 0844	18.54	.0000	. 0003	. 9996	31
30	.00873	.99127	114.59	.00873	114.59	1.0000	.00004	.99996	30
31	. 0902	. 9098	10.90	. 0902	10.89	.0000	. 0004	. 9996	29
32	. 0931	. 9069	07.43	. 0931	07.43	.0000	. 0004	. 9996 . 9995	28 27
33 34	. 0989	. 9040	04.17 01.11	. 0989	04.17 01.11	.0000	. 0005	. 9995	26
35	.01018	.98982	98.223	.01018	98.218	1.0000	.00005	.99995	25
36	. 1047	. 8953	5.495	. 1047	5.489	.0000	. 0005	. 9994	24
37	. 1076	8924	2.914	. 1076	2.908	.0000	. 0006	. 9994	23
38	. 1105	. 8895	0.469	. 1105	0.463	.0001	. 0006	. 9994	22
39	. 1134	. 8865	88.149	. 1134	88.143	.0001	. 0006	. 9993	21
40	.01163	.98836	85.946	.01164	85.940	1.0001	.00007	.99993	20
41	. 1193	. 8807	3.849	. 1193	3.843	.0001	. 0007	. 9993	19
42 43	. 1222 . 1251	. 8778 . 8749	1.853 79.950	. 1222 . 1251	1.847 79.943	.0001	. 0007	. 9992	18 17
44	. 1280	8720	8.133	. 1280	8.126	.0001	. 0008	9992	16
45	.01309	.98691	76.396	.01309	76.390	1.0001	.00008	.99991	15
46	. 1338	. 8662	4.736	. 1338	4.729	.0001	. 0009	. 9991	14
47	. 1367	. 8633	3.146	1367	3.139	.0001	. 0009	. 9991	13
48	. 1396	. 8604	1.622	. 1396	1.615	.0001	. 0010	. 9990	12
49	. 1425	. 8575	0.160	. 1425	0.153	.0001	. 0010	. 9990	11
50	.01454	.98546	68.757	.01454	68.750	1.0001	.00010	.99989	10
51	. 1483	8516	7.409	. 1484	7.402	.0001	. 0011	. 9989	9
52 53	. 1512 . 1542	. 8487 . 8458	6.113 4.866	. 1513 . 1542	6.105 4.858	.0001	. 0011	. 9988	8 7
54	. 1542	. 8429	3.664	. 1571	3.657	.0001	. 0012	. 9988	6
55	.01600	.98400	62.507	.01600	62.499	1.0001	.00013	.99987	5
56	. 1629	. 8371	1.391	. 1629	1.383	.0001	. 0013	. 9987	4
57	. 1658	. 8342	0.314	. 1658	0.306	.0001	. 0014	. 9987	3
58	. 1687	. 8313	59.274	. 1687	59.266	.0001	. 0014	. 9986	1 2
59	. 1716	. 8284	8.270	. 1716	8.261	.0001	. 0015	9985	1
60	. 1745	. 8255	7.299	. 1745	7.290	.0001	. 0015	. 9985	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

10		Na	tural Tr	igonom	etrical l	Punction	15.	13	78°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.01745	.98255	57.299	.01745	57.290	1.0001	.00015	.99985	60
1	. 1774	. 8226	6.359	. 1775	6.350	.0001	. 0016	. 9984	59
2	. 1803	. 8196	5.450	. 1804	5.441	.0001	. 0016	. 9984	58 57
3	. 1832	8167	4.570 3.718	. 1833 . 1862	4.561 3.708	.0002	. 0017	. 9983	56
4 5	. 1861 .01891	.98109	52.891	.01891	52.882	1.0002	.00018	.99982	55
6	. 1920	. 8080	2.090	. 1920	2.081	.0002	. 0018	. 9981	54
7	. 1949	. 8051	1.313	. 1949	1.303	.0002	. 0019	. 9981	53
8	. 1978	. 8022	0.558	. 1978	0.548	.0002	. 0019	. 9980	52
9	. 2007	. 7993	49.826	. 2007	49.816	.0002	. 0020	. 9980	51
10	.02036	.97964	49.114	.02036	49.104	1.0002	.00021	.99979	50 49
11 12	2065	. 7935 . 7906	8.422 7.750	2066	8.412 7.739	.0002	. 0021	9979	48
13	. 2123	. 7877	7.096	2124	7.085	.0002	. 0022	9977	47
14	2152	7847	6.460	2153	6.449	.0002	. 0023	9977	46
15	.02181	.97818	45.840	.02182	45.829	1.0002	.00024	.99976	45
16	. 2210	. 7789	5.237	. 2211	5.226	.0002	. 0024	. 9975	44
17	. 2240	7760	4.650	. 2240	4.638	.0002	. 0025	. 9975	43
18	. 2269	7731	4.077	. 2269	4.066	.0002	. 0026	. 9974	42
19	. 2298	7702	3.520 42.976	.02327	3.508 42,964	1.0003	.0026	9974	41 40
20 21	. 2356	. 7644	2,445	2357	2.433	1.0003 .0003	. 0028	. 9972	39
22	2385	7615	1.928	2386	1.916	.0003	. 0028	9971	38
23	2414	7586	1.423	2415	1.410	.0003	. 0029	9971	37
24	. 2443	7557	0.930	. 2444	0.917	.0003	. 0030	9970	36
25 26	.02472	.97528	40.448	.02473	40.436	1.0003	.00030	.99969	35
26	. 2501	. 7499	39.978	2502	39.965	.0003	. 0031	. 9969	34
27	. 2530	. 7469	9.518	2531	9.506	.0003	. 0032	. 9968	33 32
28 29	. 2559	. 7440	9.069 8.631	. 2560 . 2589	9.057 8.618	.0003	. 0033	. 9967	31
30	.02618	.97382	38.201	.02618	38.188	1.0003	.00034	.99966	30
81	. 2647	. 7353	7.782	. 2648	7.769	.0003	. 0035	. 9965	30 29
32	. 2676	. 7324	7.371	. 2677	7.358	.0003	. 0036	. 9964	128
83	. 2705	. 7295	6.969	. 2706	6.956	.0004	. 0036	. 9963	27
34	. 2734	. 7266	6.576	. 2735	6.563	.0004	. 0037	. 9963	26
85	.02763	.97237	36.191	.02764	36.177	1.0004	. 00038	. 9961	25 24
36 87	. 2792 . 2821	. 7208	5.814 5.445	. 2793 . 2822	5.800 5.431	.0004	. 0039	. 9960	24
38	2850	7150	5.084	2851	5.069	.0004	. 0041	9959	23 22
39	. 2879	7121	4.729	2880	4.715	.0004	. 0041	. 9958	21
40	.02908	.97091	34.382	.02910	34.368	1.0004	.00042	.99958	20
41	. 2937	. 7062	4.042	. 2939	4.027	.0004	. 0043	. 9957	19
42	. 2967	. 7033	3.708	. 2968	3.693	.0004	. 0044	. 9956	18
43	. 2996	. 7004	3.381	. 2997	3.366	.0004	0045	9955	17
44 45	.03054	. 6975 .96946	3.060 32.745	. 3026	3.045 32,730	.0004	.0046	. 9954	16 15
46	. 3083	. 6917	2.437	. 3084	2.421	1.0005 .0005	. 0047	. 9952	14
47	3112	6888	2.134	. 3113	2.118	.0005	. 0048	. 9951	13
48	. 3141	. 6859	1.836	. 3143	1.820	.0005	. 0049	. 9951	12
49	. 3170	. 6830	1.544	. 3172	1.528	.0005	. 0050	9950	11
50	.03199	.96801	31.257	.03201	31.241	1.0005	.00051	.99949	10
51	. 3228	. 6772	0.976	. 3230	0.960	.0005	. 0052	. 9948	9
52 53	. 3257 . 3286	6743	0.699 0.428	. 3259	0.683 0.411	.0005	. 0053	. 9947 . 9946	8 7
53 54	. 3315	. 6684	0.161	. 3200	0.145	.0005	. 0055	. 9945	6
55	.03344	.96655	29.899	.03346	29.882	1.0005	.00056	.99944	5
56	. 3374	. 6626	9.641	. 3375	9.624	.0006	. 0057	9943	4
57	. 3403	. 6597	9.388	. 3405	9.371	.0006	. 0058	. 9942	3
58	. 3432	. 6568	9.139	. 3434	9.122	.0006	. 0059	. 9941	2
59	. 3461	6539	8.894	. 3463	8.877	.0006	. 0060	. 9940	1
60	. 3490	. 6510	8.654	. 3492	8.636	.0006	. 0061	. 9939	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

2 °		Na	tural Tr	igonom	etrical	Punction	15.	13	7 7 °
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.03490	.96510	28.654	.03492	28.636	1.0006	.00061	.99939	60
1 2	. 3519	. 6481	8.417	. 3521	8.399	.0006	. 0062	. 9938	59
3	. 3548 . 3577	. 6452 . 6423	8.184 7.955	. 3550 . 3579	8.166 7.937	.0006	. 0063	. 9937 . 9936	58 57
4	. 3606	6394	7.730	. 3608	7.712	.0006	. 0065	. 9935	56
5	.03635	.96365	27.508	.03638	27.490	1.0007	.00066	.99934	55
6	. 3664	. 6336	7.290	. 3667	7.271	.0007	. 0067	. 9933	54
7	. 3693	. 6306	7.075	. 3696	7.056	.0007	. 0068	. 9932	56 55 54 53 52
8	. 3722	6277	6.864	. 3725	6.845	.0007	. 0069	. 9931	52
9 10	. 3751 .03781	. 6248	6.655 26.450	. 3754	6.637 26.432	.0007 1.0007	.0070	. 9930	51 50
11	. 3810	. 6190	6.249	. 3812	6.230	.0007	. 0073	. 9927	49
12	3839	6161	6.050	3842	6.031	.0007	. 0074	. 9926	48
13	. 3868	6132	5.854	. 3871	5.835	.0007	. 0075	. 9925	47
14	. 3897	. 6103	5.661	. 3900	5.642	.0008	. 0076	. 9924	46
15	.03926	.96074	25.471	.03929	25.452	1.0008	.00077	.99923	45
16	. 3955 . 3984	. 6045 . 6016	5.284 5.100	. 3958 . 3987	5.264 5.080	.0008 .0008	. 0078	. 9922	44 43
17 18	. 4013	. 5987	4.918	. 4016	4.898	.0008	. 0080	. 9919	42
19	. 4042	5958	4.739	4045	4.718	.0008	. 0082	9918	41
20	.04071	.95929	24.562	.04075	24.542	1.0008	.00083	.99917	40
20 21	. 4100	. 5900	4.388	. 4104	4.367	.0008	. 0084	. 9916	39
22	. 4129	. 5870	4.216	. 4133	4.196	.0008	. 0085	. 9915	38 37
23	. 4158 . 4187	. 5841	4.047 3.880	. 4162	4.026	.0009	. 0086	9913	36
24	.04217	. 5812 .95783	23.716	. 4191	3.859 23.694	1.0009	.00089	.99911	35
26	. 4246	5754	3.553	4249	3.532	.0009	. 0090	. 9910	34
27	4275	5725	3,393	4279	3.372	.0009	. 0091	. 9908	33 32
28	. 4304	. 5696	3.235	. 4308	3.214	.0009	. 0093	. 9907	32
ม ม สมมัย มมัสมมัย มมัสม	. 4333	. 5667	3.079	. 4337	3.058	.0009	. 0094	. 9906	31
30	.04362	.95638	22,925	.04366	22.904	1.0009	.00095	.99905	30 29 28 27 26 25
31 32	. 4391	. 5609 . 5580	2.774 2.624	. 4395 . 4424	2.752 2.602	.0010 .0010	. 0096	. 9903	99
33	4449	5551	2,476	4453	2.454	.0010	. 0099	. 9901	27
33 34	. 4478	5522	2,330	4483	2,308	.0010	. 0100	. 9900	26
35	.04507	.95493	22.186	.04512	22.164	1.0010	.00102	.99898	25
36	. 4536	. 5464	2.044	. 4541	2.022	.0010	. 0103	. 9897	24
37	4565	. 5435	1.904	4570	1.881	.0010	. 0104	. 9896	23
38 39	. 4594 . 4623	. 5405 . 5376	1.765 1.629	. 4599 . 4628	1.742 1.606	.0011	. 0107	. 9893	22 21 20 19
40	.04652	.95347	21.494	.04657	21.470	1.0011	.00108	.99892	20
41	. 4681	. 5318	1.360	4687	1.337	.0011	. 0110	9890	19
42	. 4711	. 5289	1.228	. 4716	1.205	.0011	. 0111	. 9889	18
43	. 4740	. 5260	1.098	. 4745	1.075	.0011	. 0112	. 9888	17
44	. 4769	. 5231	0.970	. 4774	0.946	.0011	.0114	. 9896 .99885	16 15
45 46	. 4827	.95202	20.843 0.717	.04803	20.819 0.693	1.0011 .0012	. 0116	. 9883	14
47	. 4856	5144	0.593	. 4862	0.569	.0012	. 0118	9882	13
48	. 4885	5115	0.471	. 4891	0.446	.0012	. 0119	. 9881	12
49	. 4914	. 5086	0.350	. 4920	0.325	.0012	. 0121	. 9879	11
50	.04943	.95057	20.230	.04949	20.205	1.0012	.00122	.99878	10
51	. 4972	. 5028	0.112	. 4978	0.087	.0012	. 0124	. 9876	9
52 53	. 5001 . 5030	. 4999	19.995 9.880	. 5007	19.970 9.854	.0012	. 0125	. 9875 . 9873	8 7
54	. 5059	4941	9.766	5066	9.740	.0013	. 0128	9872	6
55	.05088	.94912	19.653	.05095	19.627	1.0013	.00129	99870	5
56	. 5117	. 4883	9.541	. 5124	9.515	.0013	. 0131	. 9869	4
57	. 5146	. 4853	9.431	. 5153	9.405	.0013	. 0132	. 9867	3
58	. 5175	. 4824	9.322	. 5182	9.296	.0013	. 0134	. 9866	1
59 60	. 5204	. 4795 . 4766	9.214 9.107	. 5212 . 5241	9.188 9.081	.0013 .0014	. 0135	. 9864 . 9863	ō
					l				-
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

6801

6859

6888

6918

6947

6976

3198

3140

3111

3082

3053

3024

.93169

4.702

4.578

4.517

4.456

4.395

4.335

Cosine. Vrs. sin. || Secant. | Cotang. ||

14.640

51

55 .06830

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30 Natural Trigonometrical Functions. 1760 M. M. Vrs. cos. Cosec'nt Tang. Cotang. Secant. Vrs. sin. Cosine. Sine. .05234 .94766 .05241 19.081 1.0014 00137 99863 60 19.107 . 5270 . 0138 5263 4737 9.002 8.975 .0014 9861 59 1 9860 58 8.897 5299 8.871 .0014 0140 2 5292 4708 . 5328 . 0142 $\tilde{3}$ 5321 4679 8.794 8,768 .0014 9858 57 . 0143 9857 . 5357 4 5350 4650 8.692 8.665 .0014.94621 18.591 .05387 18.564 1.0014 .00145 .99855 55 .05379 54 53 . 5416 9854 5408 4592 8.491 8.464 .0015 . 0146 6 5445 8.365 9852 4563 8.393 .0015 0148 7 5437 8 5466 4534 8.295 . 5474 . 5503 8.268 .0015 . 0149 9850 52 0151 9849 51 .0015 g 5495 4505 8.198 8.171 .05524 .94476 18.103 .05532 18.075 1.0015 .00153 .99847 50 10 . 5562 . 0154 9846 49 11 5553 4447 8.008 7.980 .0015 . 0156 5582 5591 7.886 .0016 9844 48 7.914 12 4418 13 5611 . 4389 7.821 . 5620 7.793 7.701 .0016 . 0157 9842 47 . 0159 9841 46 4360 7.730 5649 .0016 14 5640 .94331 17.610 1.0016 .00161 .99839 45 .05669 17.639 .05678 15 . 0162 . 5707 7.520 9837 44 16 5698 4302 7.549 .0016 7.431 7.343 7.256 7.460 5737 . 0164 9836 43 5727 4273 .0016 17 9834 4244 7.372. 5766 .0017 . 0166 42 18 5756 7.285 .0017 0167 9832 41 4214 5795 19 5785 .94185 .05824 .00169 .99831 20 .05814 17.198 17.169 1.0017 40 . 0171 . 5853 9829 39 21 5843 4156 7.113 7.084 .0017 22 5872 5902 4127 7.028 5883 6.999 .0017 . 0172 9827 38 . 0174 37 9826 23 4098 6.944. 5912 6.915 .0017 0176 9824 36 5931 6.861 5941 6.832 .0018 24 4069 .99822 .00178 35 25 .05960 .94040 16.779 .05970 16.750 1.0018 . 0179 9820 34 33 26 5989 4011 6.698 5999 6.668 .0018 , 0181 6.617 6029 6.587 .0018 9819 27 6018 3982 6.507 .0018 . 0183 9817 32 28 6047 3953 6.538 6058 3924 9815 29 6.459 6087 6.428 .00180185 31 6076 .99813 .00186 30 16.380 .06116 16.350 1.0019 30 .06105 .93895 . 0188 31 3866 6.303 6145 6.272 .0019 9812 29 6134 9810 28 . 6175 32 6163 3837 6.2266.195 .0019 . 0190 . 0192 27 26 6.150 6204 6.119 .0019 9808 3808 33 6192 9806 6.075 6233 6.043 .0019 0194 34 6221 3777 1.0019 .99804 25 .06262 15.969 .00195 35 .06250 .93750 16.000 24 23 36 6279 3721 5.926 . 6291 5.894 .0020 . 0197 9803 0199 9801 .0020 37 6308 3692 5.853 6321 5.821 $\tilde{2}\tilde{2}$ 38 6337 3663 5.780 6350 5.748 .0020 . 0201 9799 9797 21 39 6366 3634 5.708 6379 5.676 .00200203 .06408 .99795 15,605 1.0020 .00205 20 40 .06395 .93605 15.637 9793 41 6424 3576 5.566 . 6437 5.534 .0021 . 0206 19 . 0208 5.464 .0021 9791 18 5.496 6467 42 6453 3547 6482 5.427 . 6496 5.394 .0021 0210 9790 17 3518 43 5.325 0212 9788 16 44 6511 3489 5.358 6525 .0021 15.257 .00214 .99786 15 45 .93460 15.290 .06554 1.0021 .06540 14 5.222 . 6583 5.189 .00220216 9784 46 6569 3431 5.155 5.122 .0022 0218 9782 13 6613 47 6598 3402 . 0220 9780 12 48 6627 3373 5.089 6642 5,056 .00224.990 0022 0222 9778 11 49 6656 3343 5.023 6671 .00224 .99776 .06685 .93314 14.958 .06700 14,924 1.0022 10 50 . 0226 4.893 . 6730 4.860 .0023 9774 51 6714 3285 3256 .0023 0228 9772 4.829 6759 4.795 52 6743 . 6788 0230 9770 7 53 3227 4.765 4.732 .0023

86ª 930

6817

6876

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6993

.06846

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4.482

4.421

4.361

4.301

Tang.

14.606

.0023

.0024

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Cosec'nt | Vrs. cos.

1.0023

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0237

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.00233

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9764 4

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9760 2

9758

. 9756

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40		Na	tural Tr	igonom	etrical l	15.	175°		
М.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. siu.	Cosine.	M.
0	.06976	.93024	14.335	.06993	14.301	1.0024	.00243	.99756	60
1	7005	. 2995	4.276	. 7022	4.241	.0025	. 0246	. 9754	59
2 3	. 7034 . 7063	. 2966 . 2937	4.217 4.159	. 7051 . 7080	4.182 4.123	.0025	. 0248	. 9752 . 9750	58 57
4	7092	2908	4.101	7110	4.065	.0025	. 0252	9748	56
5	.07121	.92879	14.043	.07139	14.008	1.0025	.00254	.99746	55
6	7150	2850	3.986	. 7168	3.951	.0026	. 0256	. 9744	54
7 8	. 7179 . 7208	2821	3.930 3.874	. 7197 . 7226	3.894 3.838	.0026	. 0258	9742	53 52
ş i	7237	2763	3.818	. 7256	3.782	.0026	. 0262	9738	51
10	.07266	92734	13.763	.07285	13.727	1.0026	.00264	.99736	50
11	. 7295	. 2705	3.708	. 7314	3.672	.0027	. 0266	9733	49
12	. 7324	. 2676	3.654	. 7343	3.617	.0027	. 0268	. 9731	48
13 14	. 7353 . 7382	. 2647	3.600 3.547	. 7873 . 7402	3.563 3.510	.0027	. 0271	9729	47
15	.07411	.92589	13.494	.07431	13,457	1.0027	.00275	.99725	45
16	. 7440	. 2560	3.441	. 7460	3.404	.0028	. 0277	. 9723	44
17	. 7469	. 2531	3.389	. 7490	3.351	.0028	. 0279	. 9721	43
18	. 7498	. 2502	8.337	. 7519	3.299	.0028	. 0281	9718	42
19 20	. 7527 .07556	. 2473 .92444	3.286 13.235	. 7548 .07577	3.248 13.197	.0028 1.0029	.0284	9716	41
21	. 7585	. 2415	3.184	. 7607	3.146	.0029	. 0288	.99714	40 39
22	. 7614	. 2386	3.134	7636	3.096	.0029	. 0290	9710	38
23	. 7643	. 2357	3.084	. 7665	3.046	.0029	. 0292	. 9707	37
24	. 7672	. 2328	3.034	. 7694	2.996	.0029	. 0295	9705	36
25 26	. 7730	.92299	12.985 2.937	.07724	12.947 2.898	1.0030	.00297	.99703	35 34
27	7759	2241	2.888	7782	2.849	.0030	0301	. 9701 . 9698	33
28	. 7788	. 2212	2.840	7812	2.801	.0030	. 0304	9696	33 32
29	. 7817	. 2183	2.793	. 7841	2.754	.0031	. 0306	. 9694	131
80	.07846	.92154	12.745	.07870	12.706	1.0031	.00308	.99692	30 29 28
81 82	. 7875 . 7904	. 2125	2.698 2.652	. 7899 . 7929	2.659 2.612	.0031	. 0310	. 9689	29
83	7933	2067	2.606	7958	2.566	.0032	. 0313	. 9687 . 9685	27
84	7962	2038	2.560	. 7987	2.520	.0032	. 0317	. 9682	26
85	.07991	.92009	12.514	.08016	12.474	1.0032	.00320	.99680	26 25
86	. 8020	1980	2.469	. 8046	2.429	.0032	. 0322	. 9678	24
37 3 8	. 8049 . 8078	. 1951 . 1922	2.424 2.379	. 8075 . 8104	2.384 2.339	.0032	. 0324	. 9675 . 9673	23 22
39	. 8107	1893	2.335	. 8134	2.295	.0033	. 0329	. 9671	21
40	.08136	.91864	12.291	.08163	12.250	1.0033	.00331	.99668	20
41	. 8165	. 1835	2.248	. 8192	2.207	.0033	. 0334	. 9666	19
42	. 8194 . 8223	. 1806	2.204 2.161	. 8221 . 8251	2.163	.0034	. 0336	. 9664	18
43 44	. 8252	1777	2.161	. 8280	2.120 2.077	.0034	. 0339	. 9661 . 9659	17 16
45	.08281	.91719	12.076	.08309	12.035	1.0034	.00343	.99656	15
46	. 8310	. 1690	2.034	. 8339	1.992	.0035	. 0346	. 9654	14
47	. 8339	. 1661	1.992	. 8368	1.950	.0035	. 0348	. 9652	13
48	. 8368	. 1632	1.950	. 8397	1.909	.0035	. 0351	. 9649	12
49 50	. 8397	. 1603	1.909 11.868	. 8426 .08456	1.867 11.826	.0035 1.0036	.0353	. 9647 .99644	11 10
51	. 8455	. 1545	1.828	. 8485	1.785	.0036	. 0358	. 9642	9
52	. 8484	. 1516	1.787	. 8514	1.745	.0036	. 0360	9639	8
53	. 8513	. 1487	1.747	. 8544	1.704	.0036	. 0363	. 9637	8
54	. 8542	1458	1.707	. 8573	1.664	.0037	. 0365	. 9634	6
55 56	.08571	. 91429	11.668 1.628	.08602 . 8632	11.625	1.0037	.00368	. 9629	5
57	. 8629	. 1371	1.589	. 8661	1.546	.0037	. 0373	. 9629	9
58	8658	. 1342	1.550	. 8690	1.507	.0038	. 0375	. 9624	2
59	. 8687	. 1313	1.512	. 8719	1.468	.0038	. 0378	. 9622	1
8 0	. 8715	. 1284	1.474	. 8749	1.430	.0038	. 0380	. 9619	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

5°		Na	turel Tr	igonom	etrical l	15.	174°		
M.	Sine.	Vrs. 208.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.08715	.91284	11.474	.08749	11.430	1.0038	.00380	.99619	60
1	. 8744	. 1255 . 1226	1.436 1.398	8778	1.392	.0038	. 0383	. 9617	59
2 3	. 8773 . 8802	1197	1.360	. 8807 . 8837	1.354 1.316	.0039	. 0388	. 9614	58 57
4	. 8831	1168	1.323	. 8866	1.279	.0039	. 0391	. 9609	56
5	.08860	.91139	11.286	.08895	11.242	1.0039	.00393	.99607	55
6	. 8889	. 1110	1.249	8925	1.205	.0040	. 0396	. 9604	54
7 8	. 8918 . 8947	. 1082 . 1053	1.213 1.176	. 8954 . 8983	1.168 1.132	.0040	. 0398	. 9601	53
9	. 8976	1024	1.140	. 9013	1.095	.0040	. 0401	. 9599 . 9596	52 51
10	.09005	90995	11.104	.09042	11.059	1.0041	.00406	.99594	50
11	. 9034	. 0966	1.069	. 9071	1.024	.0041	. 0409	. 9591	49
12	. 9063	. 0937	1.033	. 9101	0.988	.0041	. 0411	. 9588	48
13 14	. 9092	0908	0.998 0.963	. 9130 . 9159	0.953	.0041	. 0414	. 9586 . 9583	47
15	.09150	.90850	10.929	.09189	0.918 10.883	1.0042	.00419	.99580	46
16	. 9179	. 0821	0.894	. 9218	0.848	.0042	. 0422	. 9578	44
17	. 9208	. 0792	0.860	. 9247	0.814	.0043	. 0425	. 9575	43
18	. 9237	. 0763	0.826	. 9277	0.780	.0043	. 0427	9572	42
19 20	. 9266	. 0734 .90705	0.792 10.758	. 9306 .09335	0.746 10.712	.0043 1.0043	.0430	. 9570 .99567	41
21	. 9324	. 0676	0.725	. 9365	0.678	.0044	. 0436	. 9564	39
22	9353	. 0647	0.692	. 9394	0.645	.0044	. 0438	. 9562	38
23	. 9382	. 0618	0.659	. 9423	0.612	.0044	. 0441	. 9559	37
24	. 9411	. 0589	0.626	. 9453	0.579	.0044	. 0444	. 9556	36
25 26	.09440	.90560 . 0531	10.593 0.561	.09482	10.546 0.514	1.0045 .0045	.00446	.9553 . 9551	35 34
27	. 9498	. 0502	0.529	9541	0.481	.0045	. 0452	. 9548	33
28	. 9527	. 0473	0.497	9570	0.449	.0046	. 0455	9545	32
29	. 9556	. 0444	0.465	. 9599	0.417	.0046	. 0458	. 9542	31
30	.09584	.90415	10.433	.09629	10.385	1.0046	.00460	.99540	30
31 32	. 9613	. 0386	0.402 0.371	. 9658 . 9688	0.354 0.322	.0046 .0047	. 0463	. 9537 . 9534	29 28
33	9671	0328	0.340	. 9717	0.322	.0047	. 0469	9531	27
34	9700	. 0300	0.309	. 9746	0.260	.0047	. 0472	9528	26
35	.09729	.90271	10.278	.09776	10.229	1.0048	.00474	.99525	25
36	9758	. 0242	0.248	. 9805	0.199	.0048	. 0477	. 9523	24
3 7	. 9787 . 9816	. 0213	0.217 0.187	. 9834 . 9864	0.168 0.138	.0048	. 0480	9520	23 22
39	9845	. 0155	0.157	9893	0.108	.0049	. 0486	9514	21
40	.09874	.90126	10.127	.09922	10.078	1.0049	.00489	.99511	20
41	. 9903	. 0097	0.098	. 9952	0.048	.0049	. 0491	. 9508	19
4 2 4 3	. 9932	. 0068	0.068	. 9981	0.019 9.9893	.0050	. 0494	. 9505 . 9503	18
44	. 9991	. 0039	0.039	. 0010	.9601	.0050	. 0500	9503	17 16
45	.10019	.89981	9.9812	.10069	9.9310	1.0050	.00503	.99497	15
46	. 0048	. 9952	.9525	. 0099	.9021	.0051	. 0506	. 9494	14
47	. 0077	9923	.9239	. 0128	.8734	.0051	. 0509	. 9491	13
48	. 0106	. 9894 . 9865	.8955 .8672	. 0158	.8448	.0051 .0052	. 0512	. 9488	12
49 50	.10163	.89836	9.8391	. 0187 .10216	.8164 9.7882	1.0052	.0515	. 9485 .99482	11 10
51	. 0192	. 9807	.8112	. 0246	.7601	.0052	. 0521	. 9479	9
52	. 0221	. 9779	.7834	. 0275	.7322	.0053	. 0524	. 9476	8
53	. 0250	9750	.7558	. 0305	.7044	.0053	. 0527	. 9473	7
54	. 0279	9721	.7283	. 0334	.6768	.0053	. 0530	. 9470	6
55 56	. 10308	.89692 . 9663	9.7010 .6739	.10363 . 0393	9.6493 .6220	1.0053 .0054	.00533	.99467	5
57	. 0366	9634	.6469	. 0422	.5949	.0054	. 0539	9461	3
58	. 0395	. 9ა05	.6200	. 0452	.5679	.0054	. 0542	9458	3 2 1
59	. 0424	9576	.5933	. 0481	.5411	.0055	. 0545	. 9455	
60	. 0453	. 9547	.5668	. 0510	.5144	.0055	. 0548	. 9452	0
M.	Cosine.	Vrs. sir.	Secant.	Cotang.	Tang.	Cosec'nt;	Vrs. cos.	Sine.	M.

95° 84°

6°		Na	tural Tr	igonom	etrical l	Punction	15.	12	73°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.10453	.89547	9.5668	.10510	9.5144	1.0055	.00548	.99452	60
1	. 0482	. 9518	.5404	. 0540	.4878	.0055	. 0551	. 9449	59
2	. 0511	9489	.5141	. 0569	.4614	.0056	. 0554	. 9446	58
3	. 0540	. 9460	.4880	. 0599	.4351	.0056	. 0557	. 9443	57
4	. 0568	. 9431	.4620	. 0628	.4090	.0056	. 0560	. 9440	56
5	.10597	.89402	9.4362	.10657	9.3831	1.0057	.00563	.99437	55
6	. 0626	9373	.4105	. 0687	.3572	.0057	. 0566	. 9434	54
7 8	. 0655 . 0684	. 9345 . 9316	.3850 .3596	. 0716	.3315	.0057 .0057	. 0569	. 9431 . 9428	53 52
8	. 0713	9287	.3343	. 0775	.2806	.0058	. 0575	. 9424	51
9 10	.10742	.89258	9.3092	.10805	9.2553	1.0058	.00579	.99421	50
11 /	. 0771	9229	.2842	. 0834	.2302	.0058	. 0582	. 9418	49
12	. 0800	. 9200	.2593	. 0863	.2051	.0059	. 0585	. 9415	48
13	. 0829	. 9171	.2346	. 0893	.1803	.0059	. 0588	. 9412	47
14	. 0858	. 9142	.2100	. 0922	.1555	.0059	. 0591	. 9409	46
15	.10887	.89113	9.1855	.10952	9.1309	1.0060	.00594	.99406	45
16	. 0916	. 9084	.1612	. 0981	.1064	.0060	. 0597	. 9402	44
17	. 0944	. 9055	.1370	. 1011	.0821	.0060	. 0601	. 9399	43
18 19	. 0973	. 9026	.1129	. 1040	.0579	.0061	. 0604	. 9396	42
19	. 1002	. 8998 .88969	.0890	. 1069 .11099	.0338 9.0098	1.0061 1.0061	. 0607	. 9393	41
20 21 22 23	. 1060	. 8940	9.0651 .0414	. 1128	8.9860	.0062	.00610	. 9386	39
22	. 1089	8911	.0179	. 1158	.9623	.0062	. 0617	9383	38
23	. 1118	8882	8.9944	. 1187	.9387	.0062	. 0620	. 9380	37
24	. 1147	8853	.9711	. 1217	.9152	.0063	. 0623	9377	36
25	.11176	.88824	8.9479	.11246	8.8918	1.0063	.0623	.99373	35
26	. 1205	. 8795	.9248	. 1276	.8686	.0063	. 0630	9370	34
27	. 1234	. 8766	.9018	. 1305	.8455	.0064	. 0633	. 9367	33
28	. 1262	8737	.8790	. 1335	.8225	.0064	. 0636	. 9364	32
24 25 26 27 28 29 30	. 1291	. 8708	.8563	. 1364	.7996	.0064	. 0639	. 9360	31
30	.11320	.88680	8.8337	.11393	8.7769	1.0065	.00643	.99357	30 29
31 32	. 1349 . 1378	. 8651 . 8622	.8112 .7888	. 1423 . 1452	.7542 .7317	.0065	. 0646	9354	28
33	. 1407	8593	.7665	1482	.7093	.0066	. 0653	. 9347	27
34	. 1436	8564	.7444	. 1511	.6870	.0066	. 0656	. 9344	26
35	.11465	.88535	8.7223	.11541	8.6648	1.0066	.00659	.99341	25
26	. 1494	. 8506	.7004	. 1570	.6427	.0067	. 0663	. 9337	24
37 38	. 1523	. 8477	.6786	. 1600	.6208	.0067	. 0666	. 9334	23 22
38	. 1551	. 8448	.656 9	. 1629	.5989	.0067	. 0669	, 9330	22
39	. 1580	. 8420	.6353	. 1659	.5772	.0068	. 0673	. 9327	21
40	.11609	.88391	8.6138	.11688	8.5555	1.0068	.00676	.99324	20
41	. 1638	. 8362	.5924	. 1718	.5340	.0068	. 0679	. 9320	19
42 43	. 1667 . 1696	8304	.5711 .5499	. 1747 . 1777	.5126 .4913	.0069	. 0683	. 9317	18 17
44	. 1725	8272	.5289	. 1806	.4701	.0069	. 0690	. 9310	16
45	.11754	.88246	8.5079	.11836	8.4489	1.0070	.00693	.99307	15
46	. 1783	. 8217	.4871	. 1865	.4279	.0070	. 0696	. 9303	14
47	. 1811	. 8188	.4663	. 1895	.4070	.0070	. 0700	9300	13
48	. 1840	. 8160	.4457	. 1924	.3862	.0071	. 0703	9296	12
49	. 1869	. 8131	.4251	. 1954	.3655	.0071	. 0707	. 9293	11
50	.11898	.88102	8.4046	.11983	8.3449	1.0071	.00710	.99290	10
51	. 1927	. 8073	.3843	. 2013	.3244	.0072	. 0714	. 9286	9
52 53	. 1956	8044	.3640	. 2042	.3040	.0072	. 0717	. 9283	8 7
54	. 1985	7986	.3439 .3238	. 2072 . 2101	.2837 .2635	.0073	. 0721	. 9279	1 %
55	.12042	.87957	8.303 9	.12131	8.2434	1.0073	.00728	.9276	6 5
56	. 2071	7928	.2840	. 2160	.2234	.0074	. 0731	. 9269	4
56 57	. 2100	7900	.2642	2190	.2035	.0074	. 0735	9265	3
58	. 2129	7871	.2446	. 2219	.1837	.0074	. 0738	9262	۱ž
59	. 2158	. 7842	.2250	. 2249	.1640	.0075	. 0742	9258	1
60	2187	. 7813	.2055	. 2278	.1443	.0075	. 0745	. 9255	Õ
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

7°		Na	tural Tr	igonom	etrical l	Punction	15.	13	7 2 °
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.12187	.87813	8.2055	.12278	8.1443	1.0075	.00745	.99255	60
1	. 2216	. 7787	.1861	. 2308	.1248	.0075	. 0749	. 9251	59
2	. 2245	. 7755	.1668	. 2337	.1053	.0076	. 0752	. 9247	58
3	. 2273	7726	.1476	. 2367	.0860	.0076	. 0756	. 9244	57
4	. 2302	. 7697	.1285	. 2396	.0667	.0076	. 0760	. 9240	56
5	.12331	.87669	8.1094	.12426	8.0476	1.0077	.00763	.99237	55
6	. 2360	. 7640	.0905	. 2456	.0285	.0077	. 0767	. 9233	54
7 8	. 2389	7611	.0717	. 2485	.0095	.0078	. 0770	. 9229	53
ŝ	. 2418 . 2447	. 7582	.0529	. 2515	7.9906	.0078	. 0774	. 9226	52
10	.12476	. 7553 .87524	.0342 8.0156	. 2544 .12574	.9717 7.9530	.0078	. 0778	. 9222	51
iĭ	. 2504	. 7495	7.9971	. 2603	.9344	1.0079	.00781	.99219	50 49
12	2533	7467	.9787	2633	.9158	.0079	. 0788	. 9213	48
13	2562	7438	.9604	2662	.8973	.0080	. 0792	9208	47
14	2591	7409	.9421	2692	.8789	.0080	. 0792	9204	46
15	.12620	.87380	7.9240	.12722	7.8606	1.0080	.00799	.99200	45
16	. 2649	. 7351	.9059	2751	.8424	.0081	. 0803	. 9197	44
17	. 2678	7322	.8879	2781	.8243	.0081	. 0807	9193	43
18	2706	7293	.8700	2810	.8062	.0082	. 0810	9189	42
19	. 2735	. 7265	.8522	. 2840	.7882	.0082	. 0814	. 9186	41
20	.12764	.87236	7.8344	.12869	7.7703	1.0082	.00818	.99182	40
21	. 2793	. 7207	.8168	. 2899	.7525	.0083	. 0822	. 9178	39
22	. 2822	. 7178	.7992	. 2928	.7348	.0083	. 0825	. 9174	38
23	. 2851	. 7149	.7817	. 2958	.7171	.0084	. 0829	. 9171	38 37
24	. 2879	. 7120	.7642	. 2988	.6996	.0084	. 0833	. 9167	36
25 26	.12908	.87091	7.7469	.13017	7.6821	1.0084	.00837	.99163	35
26	. 2937	. 7063	.7296	. 3047	.6646	.0085	. 0840	. 9160	34
27	. 2966	. 7034	.7124	. 3076	.6473	.0085	. 0844	. 9156	33
28	. 2995	. 7005	.6953	. 3106	.6300	.0085	. 0848	. 9152	32
29	. 3024	. 6976	.6783	. 3136	.6129	.0086	. 0852	. 9148	33 32 31
30 31	.13053	.86947	7.6613	.13165	7.5957	1.0086	.00855	.99144	1 30
32	. 3081	. 6918	.6444	. 3195	.5787	.0087	. 0859	. 9141	29 28 27 26
33	3110	. 6890	.6276	. 3224	.5617	.0087	. 0863	9137	28
34	. 3168	. 6861	.6108	. 3254	.5449	.0087	. 0867	. 9133	27
85	.13197	. 6832 .86803	.5942 7.5776	. 3284	.5280	.0088	. 0871	9129	26
36	. 3226	. 6774	.5611	. 3343	7.5113	1.0088 .0089	.00875	.99125	25
36 37	3254	. 6745	.5446	3372	.4780	.0089	. 0878	9121	24
38	3283	6717	.5282	. 3402	.4615	.0089	. 0886	9114	24 23 22 21
39	. 3312	. 6688	.5119	3432	.4451	.0090	. 0890	. 9110	22
40	.13341	.86659	7.4957	.13461	7.4287	1.0090	.00894	.99106	20
41	. 3370	. G630	.4795	. 3491	.4124	.0090	. 0898	9102	19
42	. 3399	. 6601	.4634	3520	.3961	.0091	. 0902	. 9098	18
43	. 3427	. 6572	.4474	. 3550	.3800	.0091	. 0905	. 9094	17
44	. 3456	. 6544	.4315	. 3580	.3639	.0092	. 0909	9090	16
45	.13485	.86515	7.4156	.13609	7.3479	1.0092	.00913	.99086	15
46	. 3514	. 6486	.3998	. 3639	.3319	.0092	. 0917	. 9083	14
47	. 3543	6457	.3840	. 3669	.3160	.0093	. 0921	. 9079	13
48	. 3571	6428	.3683	. 3698	.3002	.0093	. 0925	. 9075	12
49	. 3600	6400	3527	. 3728	.2844	.0094	. 0929	. 9070	11
50	.13629	.86371	7.3372	.13757	7.2687	1.0094	.00933	.99067	10
51 52	. 3658	. 6342	.3217	. 3787	.2531	.0094	. 0937	. 9063	9
53	. 3687 . 3716	6313	.3063	. 3817	.2375	.0095	. 0941	. 9059	8
54 54	. 3744	6284	.2909	. 3846	.2220	.0095	. 0945	. 9055	7
55	.13773	. 6255 .86227	.2757	3876	.2066	.0096	. 0949	. 9051	6
56	. 3802		7.2604	.13906	7.1912	1.0096	.00953	.99047	5
57	. 3831	. 6198	.2453	. 3935	.1759	.0097	. 0957	. 9043	4
58	. 3860	6140	.2302	3965	.1607	.0097	. 0961	. 9039	3 2
59	. 3888	6111	.2152	. 3995 . 4024	.1455	.0097	. 0965	. 9035	2
60	. 3917	. 6083	.1853	. 4024	.1304 .1154	.0098	. 0969	9031	0
_			.1000	. 1001	.1104	.0098	. 0973	. 9027	١٧
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos	Sine.	M.
						, COOCC AL		DILLO.	144.

80		Na	tural T	igonom	etrical l	Punction	ns.	1:	71°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.13917	.86083	7.1853	.14054	7.1154	1.0098	.00973	.99027	60
1	. 3946	. 6054	.1704	. 4084	.1004	.0099	. 0977	. 9023	59
2	. 3975	. 6025 . 5996	.1557	. 4113 . 4143	.0854	.0099	. 0981	. 9019	58
4	. 4032	5967	.1409 .1263	. 4173	.0558	.0099	. 0989	. 9015 . 9010	57 56
5	.14061	85939	7.1117	.14202	7.0410	1.0100	.00993	.99006	55
6	. 4090	. 5910	.0972	. 4232	.0264	.0101	. 0998	. 9002	54
7	. 4119	. 5881	.0827	. 4262	.0117	.0101	. 1002	8998	53
8	. 4148 . 4176	. 5852 . 5823	.0683	. 4291 . 4321	6.9972	.0102	. 1006	8994	52
10	.14205	.85795	7.0396	.14351	.9827 6.9682	.0102 1.0102	.01014	. 8990 .98986	51 50
ii	. 4234	. 5766	.0254	. 4380	.9538	.0103	. 1018	. 8982	49
12	. 4263	. 5737	.0112	. 4410	.9395	.0103	. 1022	8978	48
13	. 4292	. 5708	6.9971	. 4440	.9252	.0104	. 1026	. 8973	47
14 15	. 4320 .14349	. 5679 .85651	.9830 6.9690	. 4470 .14499	.9110	.0104	. 1031	. 8969 .98965	46
16	. 4378	. 5622	.9550	. 4529	6.8969 .8828	1.0104 .0105	. 1039	. 8961	45 44
17	4407	. 5593	.9411	4559	.8687	.0105	. 1043	8957	43
18	. 4436	. 5564	.9273	. 4588	.8547	.0106	. 1047	8952	42
19	. 4464	. 5536	.9135	. 4618	.8408	.0106	. 1052	. 8948	41
20	.14493 . 4522	.85507	6.8998	.14648	6.8269	1.0107	.01056	.98944	40
21 22	. 4551	. 5478 . 5449	.8861 .8725	. 4677 . 4707	.8131 .7993	.0107 .0107	. 1060 . 1064	. 8940 . 8936	39 38
23	4579	5420	.8589	4737	.7856	.0108	1068	. 8931	37
24	. 4608	. 5392	.8454	. 4767	.7720	.0108	. 1073	. 8927	36
25	.14637	.85363	6.8320	.14796	6.7584	1.0109	.01077	.98923	35
26	. 4666	. 5334	.8185	. 4826	.7448	.0109	. 1081	. 8919	34
27 28	. 4695 . 4723	. 5305 . 5277	.8052 .7919	. 4856 . 4886	.7313 .7179	.0110 .0110	. 1085	. 8914 . 8910	33 32
29	4752	5248	.7787	4915	.7045	.0111	1094	. 8906	31
80	.14781	.85219	6.7655	.14945	6.6911	1.0111	.01098	.98901	30
31	. 4810	. 5190	.7523	. 4975	.6779	.0111	. 1103	. 8897	29
32 33	4838	. 5161	.7392	. 5004	.6646	.0112	. 1107	. 8893	28 27
34	. 4867 . 4896	. 5133 . 5104	.7262 .7132	. 5034 . 5064	.6514 .6383	.0112 .0113	. 1111	. 8889 . 8884	26
35	.14925	85075	6.7003	.15094	6.6252	1.0113	.01120	.98880	25
36	. 4953	. 5046	.6874	. 5123	.6122	.0114	. 1124	. 8876	24
87	. 4982	. 5018	.6745	. 5153	.5992	.0114	. 1129	. 8871	23
38	. 5011	4989	.6617	. 5183	.5863	.0115	. 1133	. 8867	22
39 40	. 5040 .15068	. 4960 .84931	.6490 6.6363	. 5213 .15243	.5734 6.5605	.0115 1.0115	. 1137	. 8862 .98858	21 20
41	. 5097	. 4903	.6237	. 5272	.5478	.0116	. 1146	. 8854	19
42	. 5126	. 4874	.6111	. 5302	.5350	.0116	. 1151	. 8849	18
43	. 5155	. 4845	.5985	. 5332	.5223	.0117	. 1155	. 8845	17
44	. 5183	4816	.5860	. 5362	.5097	.0117	. 1159	. 8840	16
45 46	.15212 . 5241	.84788 . 4759	6.5736 .5612	.15391 . 5421	6.4971 .4845	1.0118 .0118	. 1168	.98836 . 8832	15 14
47	5270	4730	.5488	. 5451	.4720	.0119	. 1173	. 8827	13
48	. 5298	. 4701	.5365	. 5481	.4596	.0119	. 1177	. 8823	12
49	. 5328	. 4672	.5243	. 5511	.4472	.0119	. 1182	. 8818	11
50	.15356	.84644	6.5121	.15540	6.4348	1.0120	.01186	.98814	10
51 52	. 5385 . 5413	. 4615 . 4586	.4999	. 5570 . 5600	.4225 .4103	.0120	. 1190 . 1195	. 8809 . 8805	8
53	. 5442	4558	.4757	. 5630	.3980	.0121	1199	. 8800	7
54	. 5471	. 4529	.4637	. 5659	.3859	.0122	. 1204	. 8796	6
55	.15500	.84500	6.4517	.15689	6.3737	1.0122	.01208	.98791	5
56	. 5528	. 4471	.4398	. 5719	.3616	.0123	. 1213	. 8787	4
57 58	. 5557 . 5586	. 4448	.4279	. 5749 . 5779	.3496 .3376	.0123	. 1217	. 8782 . 8778	3 2
59	5615	. 4385	.4042	. 5809	.3257	.0124	1227	8773	î
60	. 5643	. 4356	.3924	. 5838	.3137	.0125	. 1231	. 8769	ō
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Sine.	Vrs. cos.	M.

2 . 57 3 . 57 4 . 57 5 .157 6 . 58 7 . 58 8 . 58	543 572 701 730 758	Vrs. cos. .84356 . 4328 . 4299 . 4270 . 4242 .84213 . 4184 . 4155 . 4127 . 4098	Cosec'nt 6.3924 .3807 .3690 .3574 .3458 6.3343 .2228 .3113	Tang15838 . 5868 . 5898 . 5928 . 5958 .15987 . 6017	Cotang. 6.3137 .3019 .2901 .2783 .2665	Secant. 1.0125 .0125 .0125 .0126	Vrs. sin. .01231 . 1236 . 1240	.98769 . 8764	M. 60 59
1 . 56 2 . 57 3 . 57 4 . 57 5 .157 6 . 58 7 . 58 8 . 58	572 701 730 758 787 816 844 873 902	. 4328 . 4299 . 4270 . 4242 .84213 . 4184 . 4155 . 4127	.3807 .3690 .3574 .3458 6.3343 .2228 .3113	. 5868 . 5898 . 5928 . 5958 .15987	.3019 .2901 .2783 .2665	.0125 .0125	. 1236		
2 . 57 3 . 57 4 . 57 5 .157 6 . 58 7 . 58 8 . 58	701 730 758 787 816 844 873 902	. 4299 . 4270 . 4242 .84213 . 4184 . 4155 . 4127	.3690 .3574 .3458 6.3343 .2228 .3113	. 5898 . 5928 . 5958 .15987	.2901 .2783 .2665	.0125		. 8764	I EA
3 . 57 4 . 57 5 .157 6 . 58 7 . 58 8 . 58	730 758 787 316 344 373 302 331	. 4270 . 4242 .84213 . 4184 . 4155 . 4127	.3574 .3458 6.3343 .2228 .3113	. 5928 . 5958 .15987	.2783 .2665	0125	1 1740		
4 . 57 5 .157 6 . 58 7 . 58 8 . 58	758 787 316 344 373 902 931	. 4242 .84213 . 4184 . 4155 . 4127	.3458 6.3343 .3228 .3113	. 5958 .15987	.2665		1245	8760	58 57
5 .157 6 . 58 7 . 58 8 . 58	787 316 344 373 902 931	.84213 . 4184 . 4155 . 4127	6.3343 .2228 .3113	.15987		.0126	1249	. 8755 . 8750	56
7 . 58 8 . 58	316 344 373 302 31	. 4184 . 4155 . 4127	.2228 .3113		6. 2548	1.0127	.01254	.98746	55
7 . 58 8 . 58	373 302 331	. 4127	.3113		.2432	.0127	. 1259	. 8741	54
8 . 58	002			. 6047	.2316	.0128	. 1263	. 8737	53
0 50	31		.2999	6077	.2200	.0128 .0129	1268	. 8732	52
		.84069	.2885 6.2772	. 6107 .16137	6.1970	1.0129	.01277	. 8727 .98723	51 50
11 . 59		. 4041	.2659	6167	.1856	.0130	1282	. 8718	49
12 . 59	88	. 4012	.2546	. 6196	.1742	.0130	. 1286	. 8714	48
13 . 60	017	. 3983	.2434	. 6226	.1628	.0131	. 1291	. 8709	47
14 . 60)45	. 3954	.2322	. 6256	.1515	.0131	. 1296	. 8704	46
15 .160		.83926	6.2211	.16286	6.1402	1.0132	.01300	.98700	45
16 · 61 17 · 61	32	. 3897 . 3868	.2100 .1990	. 6316 . 6346	.1290	.0132 .0133	. 1305 . 1310	. 8695 . 8690	44
	60	3840	.1880	6376	.1066	.0133	1314	8685	42
	89	. 3811	1770	6405	.0955	.0134	1319	. 8681	41
20 .162		.83782	6.1661	.16435	6.0844	1.0134	.01324	.98676	40
21 . 62	246	. 3753	.1552	. 6465	.0734	.0135	. 1328	. 8671	39
22 . 62	275	. 3725	.1443	. 6495	.0624	.0135	. 1333	. 8667	38
	304 333	. 3696 . 3667	.1335 .1227	. 6525 . 6555	.0514	.0136	1338	. 8662	37
24 . 63 25 .163		.83639	6.1120	.16585	6.0296	.0136 1.0136	. 1343	. 8657 .98652	36 35
	390 l	3610	.1013	. 6615	.0188	.0137	. 1352	. 8648	34
	119	. 3581	.0906	. 6644	.0080	.0137	. 1357	. 8643	33
28 . 64	147	. 3553	.0800	. 6674	5.9972	.0138	. 1362	. 8638	32
	176	. 3524	.0694	. 6704	.9865	.0138	. 1367	. 8633	31
80 .165	533	.83495	6.0588	.16734	5.9758	1.0139	.01371	.98628	30
	562	. 3466 . 3438	.0483	6764	.9651 .9545	.0139 .0140	. 1376 . 1381	. 8624 . 8619	29 28
	591	. 3409	.0274	6824	.9439	.0140	1386	. 8614	27
	319	3380	.0170	6854	.9333	.0141	1391	. 8609	26
35 .166		.83352	6.0066	.16884	5.9228	1.0141	.01395	.98604	25
	377	. 3323	5.9963	. 6914	.9123	.0142	. 1400	. 8600	24
	705	. 3294	.9860	. 6944	.9019	.0142	. 1405	. 8595	23 22
	734 763	3237	.9758	. 6973 . 7003	.8915 .8811	.0143 .0143	. 1410 . 1415	. 8590 . 8585	21
40 .167		.83208	5.9554	.17033	5.8708	1.0144	.01420	.98580	20
	320	. 3180	.9452	. 7063	.8605	.0144	. 1425	. 8575	19
42 . 68	349	. 3151	.9351	. 7093	.8502	.0145	. 1430	. 8570	18
	378	. 3122	.9250	. 7123	.8400	.0145	. 1434	8565	17
	906	. 3094	.9150	. 7153	.8298	.0146	. 1439	. 8560	16 15
45 .169 46 .69	964	.83065	5.9049 .8950	.17183 . 7213	5.8196 .8095	1.0146 .0147	. 1449	.98556 . 8551	14
47 69	992	3008	.8850	7243	.7994	.0147	. 1454	. 8546	13
	21	. 2979	.8751	7273	.7894	.0148	. 1459	. 8541	12
	050	. 2950	.8652	. 7303	.7793	.0148	. 1464	. 8536	11
50 .170		.82922	5.8554	.17333	5.7694	1.0149	.01469	.98531	10
	107	. 2893	.8456	. 7363	.7594	.0150	. 1474	. 8526	9
	136	. 2864 . 2836	.8358	. 7393 . 7423	.7495 .7396	.0150 .0151	. 1479 . 1484	. 8521 . 8516	8 7
	164 193	2807	.8261 .8163	7453	.7390	.0151	. 1489	. 8511	6
55 .172		.82778	5.8067	.17483	5.7199	1.0152	.01494	.98506	5
56 . 72	250	2750	.7970	. 7513	.7101	.0152	. 1499	. 8501	4
57 . 72	279	. 2721	.7874	. 7543	.7004	.0153	. 1504	. 8496	3
	307	. 2692	.7778	. 7573	.6906	.0153	. 1509	. 8491	2
	336 365	. 2664 . 2635	.7683 .7588	. 7603 . 7633	.6809 .6713	.0154 .0154	. 1514 . 1519	. 8486 . 8481	0
M. Cos	ine.	Vrs. sip.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

100	,	Na	tural Ti	rigonom	etrical l	Function	ns.	10	59°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0)	.17365	.82635	5.7588	.17633	5.6713	1.0154	.01519	.98481	60
1	. 7393	2606	.7493	. 7663 . 7693	.6 616	.0155	. 1524	. 8476	59
2 3	. 7422	. 2578	.7398	. 7693	.6520	.0155	. 1529	. 8471	58 57
4	. 7451 . 7479	. 2549 . 2521	.7304	. 7723 . 7753	.6425	.0156	. 1534	. 8465	57
5	.17508	.82492	.7210 5.7117	.17783	.6329 5.6234	.0156 1.0157	.01544	. 8460 .98455	56 55
5 6 7 8	. 7537	. 2463	.7023	7813	.6140	.0157	. 1550	8450	54
7	7565	2435	.6930	7843	.6045	.0158	. 1555	. 8445	53
8	. 7594	. 2406	.6838	. 7873	.5951	.0158	. 1560	. 8440	52
9	. 7622	. 2377	.6745	. 7903	.5857	.0159	. 1565	. 8435	51
10	.17651	.82349	5.6653	.17933	5.5764	1.0159	.01570	.98430	50
11 12	. 7680 . 7708	. 2320	.6561	. 7963	.5670	.0160	. 1575	. 8425	49
13	7737	. 2291 . 2263	.6470 .6379	. 7993 . 8023	.5578 .5485	.0160 .0161	. 1580 . 1585	. 8419 . 8414	48 47
14	7766	2234	.6288	8053	.5393	.0162	. 1591	. 8409	46
15	.17794	.82206	5.6197	.18083	5.5301	1.0162	.01596	.98404	45
16	. 7823	. 2177	.6107	. 8113	.5209	.0163	. 1601	. 8399	44
17	. 7852	. 2148	.6017	. 8143	.5117	.0163	. 1606	. 8394	43
18	. 7880	. 2120	.5928	. 8173	.5026	.0164	. 1611	. 8388	42
19	. 7909	. 2091	.5838	. 8203	.4936	.0164	. 1617	. 8383	41
20 21	.17937 . 7966	.82062	5.5749	.18233	5.4845	1.0165	.01622	.98378	40
22	. 7995	2034	.5660 .5572	. 8263 . 8293	.4755 .4665	.0165	. 1627 . 1632	. 8373 . 8368	39 38
23	8023	1977	.5484	8323	.4575	.0166 .0166	. 1638	8362	37
23 24	8052	. 1948	.5396	. 8353	.4486	.0167	. 1643	8357	36
25	.18080	.81919	5.5308	.18383	5.4396	1.0167	.01648	98352	36 35
26 27	. 8109	. 1891	.5221	. 8413	.4308	.0168	. 1653	. 8347	34
27	. 8138	. 1862	.5134	. 8444	.4219	.0169	. 1659	. 8341	33 32 31
28	. 8166	. 1834	.5047	. 8474	.4131	.0169	. 1664	. 8336	32
29 30	. 8195 .18223	. 1805 .81776	.4960	. 8504	.4043	.0170	. 1669	. 8331	31
31	. 8252	. 1748	5.4874 .4788	.18534 .8564	5.3955 .3868	1.0170 .0171	.01674	. 98325	30 29
32	8281	1719	.4702	. 8594	.3780	.0171	. 1685	. 8315	123
33	8309	1691	.4617	. 8624	.3694	.0172	1690	8309	28 27 26 25
34	8338	. 1662	.4532	. 8654	.3607	.0172	. 1696	. 8304	26
35	.18366	.81633	5.4447	.18684	5.3521	1.0173	.01701	.98299	25
36	. 8395	. 1605	.4362	. 8714	.3434	.0174	. 1706	. 8293	1 124
87	. 8424	. 1576	.4278	. 8745	.3349	.0174	. 1712	8288	23 22 21
38 39	. 8452 . 8481	. 1548	.4194 .4110	. 8775	.3263	.0175	. 1717	8283	22
40	.18509	.81490	5.4026	. 8805	.3178 5.3093	.0175 1.0176	. 1722	. 8277 .98272	20
41	8538	. 1462	.3943	. 8865	.3008	.0176	1733	8267	19
42	. 8567	. 1433	.3860	8895	.2923	.0177	1739	8261	18
43	. 8595	. 1405	.3777	8925	.2839	.0177	1744	8256	17
44	. 8624	. 1376	.3695	. 8955	.2755	.0178	. 1749	8250	16
45	.18652	.81348	5.3612	.18985	5.2671	1.0179	.01755	.98245	15
46	8681	. 1319	.3530	. 9016	.2588	.0179	. 1760	8240	14
47 48	. 8709 . 8738	. 1290 . 1262	.3449	. 9046	.2505	.0180	. 1766	. 8234 . 8229	13
49	8767	1233	.3367	. 9076	.2422	.0180 .0181	1771	8229	12 11
50	.18795	.81205	5.3205	.19136	5.2257	1.0181	.01782	.98218	10
51	. 8824	. 1176	.3124	. 9166	.2174	.0182	. 1788	8212	9
52	. 8852	. 1147	.3044	. 9197	.2092	.0182	1793	8207	8
53	. 8881	. 1119	.2963	. 9227	.2011	.0183	. 1799	. 8201	8 7
54	. 8909	. 1090	.2883	. 9257	.1929	.0184	. 1804	. 8196	6
55	.18938	.81062	5.2803	.19287	5.1848	1.0184	.01810	98190	5
56	8967	. 1033	.2724	. 9317	.1767	.0185	. 1815	8185	4
57 58	. 8995 . 9024	. 1005	.2645	. 9347 . 9378	.1686	.0185	. 1821	8179	3
59	9052	. 0976	.2566	9408	.1606 .1525	.0186 .0186	. 1826 . 1832	8174	1
60	9081	. 0919	.2408	. 9438	.1445	.0187	. 1837	. 8163	ő
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'ut	Vrs. cos.	Sine.	M.

110	•	Na	tural Tr	igonom	etrical	168°			
M.	Sine.	Vrs. cos.	Cosec 'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.19081	.80919	5.2408	.19438	5.1445	1.0187	.01837	.98163	60
1	. 9109	0890	.2330	. 9468	.1366	.0188	. 1843	. 8157	59
2	. 9138	. 0862	.2252	. 9498	.1286	.0188	. 1848	. 8152	58
3	. 9166	. 0833	.2174	. 9529	.1207	.0189	. 1854	8146	57
4 5	. 9195 .19224	. 0805 .80776	.2097 5.2019	. 9559 .19589	.1128 5.1049	.0189 1.0190	. 1859	. 8140	56 55
6	9252	. 0748	.1942	. 9619	.0970	.0191	. 1871	8129	54
7	9281	. 0719	1865	. 9649	.0892	.0191	1876	8124	53
8	9309	. 0691	.1788	. 9680	.0814	.0192	. 1882	. 8118	52
9	. 9338	. 0662	.1712	. 9710	.0736	.0192	. 1887	. 8112	51
10	.19366	.80634	5.1636	.19740	5.0658	1.0193	.01893	.98107	50
11	. 9395	. 0605	.1560	. 9770	.0581	.0193	. 1899	. 8101	49
12	. 9423	. 0576	.1484	. 9800	.0504	.0194	. 1904	. 8095	48
13 14	. 9452 . 9480	. 0548	.1409	. 9831 . 9861	.0427	.0195 .0195	. 1910	8090 8084	47
15	.19509	.80491	5.1258	.19891	.0350 5.0273	1.0196	. 1916	.98078	45
16	. 9537	. 0462	.1183	9921	.0197	.0196	. 1927	8073	44
17	9566	. 0434	.1109	9952	.0121	.0197	. 1933	8067	43
18	. 9595	. 0405	.1034	. 9982	.0045	.0198	. 1938	. 8061	42
19	. 9623	. 0377	.0960	.20012	4.9969	.0198	. 1944	. 8056	41
20	.19652	.80348	5.0886	.20042	4.9894	1.0199	.01950	.98050	40
21 22	. 9680	. 0320	.0812	. 0073	.9819	.0199	. 1956	. 8044	39
22	. 9709	. 0291	.0739	. 0103	.9744	.0200	. 1961	. 8039	38 37
23 24	. 9737	. 0263	.0666	. 0133	.9669 .9594	.0201	. 1967	8033	37
25	.19794	.80206	.0593 5.0520	.20194	4.9520	.0201 1.0202	. 1973	.98021	36 35
26	. 9823	. 0177	.0447	. 0224	.9446	.0202	. 1984	. 8016	34
27	. 9851	. 0149	.0375	0254	.9372	.0203	1990	. 8010	33
27 28	. 9880	. 0120	.0302	0285	.9298	.0204	. 1996	. 8004	32
29 30	. 9908	. 0092	.0230	. 0315	.9225	.0204	. 2002	. 7998	31
30	.19937	.80063	5.0158	.20345	4.9151	1.0205	.02007	.97992	30 29
31	. 9965	. 0035	.0087	. 0375	.9078	.0205	. 2013	. 7987	29
32	. 9994	. 0006	.0015	. 0406	.9006	.0206	. 2019	. 7981	28 27
33 34	. 0051	. 79978	4.9944 .9873	. 0436 . 0466	.8933 .8860	.0207 .0207	. 2025 . 2031	. 7975 . 7969	26
35	.20079	.79921	4.9802	.20497	4.8788	1.0208	.02037	.97963	25
36	. 0108	. 9892	.9732	. 0527	.8716	.0208	2042	7957	24
37	. 0136	. 9863	.9661	0557	.8644	.0209	. 2048	7952	23
38	. 0165	. 9835	.9591	. 0588	.8573	.0210	2054	7946	23 22
39	. 0193	. 9807	.9521	. 0618	.8501	.0210	. 2060	. 7940	21 20
40	.20222	.79778	4.9452	.20648	4.8430	1.0211	.02066	.97934	20
41	. 0250	9750	.9382	. 0679	.8359	.0211	. 2072	. 7928	19
42 43	. 0279	. 9721	.9313	0709	.8288	.0212	2078	. 7922	18
44	. 0336	. 9664	.9243	0739	.8217 .8147	.0213	. 2084	. 7916 . 7910	17 16
45	.20364	.79636	4.9106	.20800	4.8077	1.0214	.02095	.97904	15
46	. 0393	9607	.9037	. 0830	.8007	.0215	. 2101	. 7899	14
47	. 0421	9579	.8969	. 0861	.7937	.0215	. 2107	. 7893	13
48	. 0450	9550	.8901	. 0891	.7867	.0216	. 2113	. 7887	12
49	. 0478	9522	.8833	. 0921	.7798	.0216	. 2119	. 7881	11
50	.20506	.79493	4.8765	.20952	4.7728	1.0217	.02125	.97875	10
51 52	. 0535	9465	.8697	. 0982	.7659	.0218	. 2131	. 7869	9
53	. 0563	9436	.8630 .8563	. 1012	.7591 .7522	.0218 .0219	. 2137 . 2143	. 7863 . 7857	8
54	. 0620	9379	.8496	. 1043	.7453	.0219	2143	7851	6
55	.20649	79351	4.8429	.21104	4.7385	1.0220	.02155	.97845	6 5
56	. 0677	9323	.8362	. 1134	.7317	.0221	. 2161	7839	4
57	0706	9294	.8296	. 1164	.7249	.0221	. 2167	. 7833	3
58	. 0734	. 9266	.8229	. 1195	.7181	.0222	. 2173	. 7827	3 2 1
59	. 0763	. 9237	.8163	. 1225	.7114	.0223	. 2179	. 7821	
60	. 0791	. 9209	.8097	. 1256	.7046	.0223	. 2185	. 7815	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

120	•	Na	tural Tr	igonom	etrical l	Punction	15.	10	6 7°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.20791	.79209	4.8097	.21256	4.7046	1.0223	.02185	.97815	60
1	. 0820	. 9180	.8032	. 1286	.6979	.0224	. 2191	. 7809	59
2	. 0848	. 9152	.7966	. 1316	.6912	.0225	. 2197	. 7803	58
3	. 0876	9123	.7901	. 1347	.6845	.0225	. 2203	. 7806 . 7790	57 56
4	. 0905	9105	.7835 4.7770	. 1377 .21408	.6778 4.6712	1.0226	.02215	.97784	55
5 6	.20933	.79066 . 9038	.7706	. 1438	.6646	.0227	. 2222	7778	54
7	. 0990	9010	.7641	. 1468	.6580	.0228	2228	7772	53
8	. 1019	8981	.7576	. 1499	.6514	.0228	. 2234	. 7766	52 51
9	. 1047	. 8953	.7512	. 1529	.6448	.0229	2240	. 7760	51
10	.21076	.78924	4.7448	.21560	4.6382	1.0230	.02246	.97754	50
11	. 1104	8896	.7384	. 1590	.6317	.0230	. 2252	. 7748	49
12	. 1132	8867	.7320	. 1621	.6252	.0231	. 2258 . 2264	. 7741	48 47
13	. 1161	. 8839 . 8811	.7257 .7193	. 1651 . 1682	.6187 .6122	.0232	2204	. 7735 . 7729	46
14 15	. 1189 .21218	78782	4.7130	.21712	4.6057	1.0233	.02277	.97723	45
16	. 1246	8754	.7067	. 1742	.5993	.0234	2283	7717	44
17	1275	8725	.7004	. 1773	.5928	0234	2289	7711	43
18	. 1303	8697	.6942	. 1803	.5864	.0235	. 2295	. 7704	42
19	. 1331	. 8668	.6879	. 1834	.5800	.0235	. 2302	. 7698	41
20	.21360	.78640	4.6817	.21864	4.5736	1.0236	.02308	.97692	40
21 22	. 1388	8612	.6754	. 1895	.5673	.0237	. 2314	. 7686	39
22	. 1417	8583	.6692	. 1925	.5609	.0237	. 2320	7680	38 37 36 35 34
23	. 1445	. 8555 . 8526	.6631 .6569	. 1956 . 1986	.5546 .5483	.0238	. 2326	. 7673 . 7667	37
24 25	. 1473	78508	4.6507	.22017	4.5420	1.0239	.02339	.97661	25
26 26	. 1530	. 8470	.6446	2047	.5357	.0240	. 2345	7655	34
27	1559	8441	.6385	2078	.5294	.0241	. 2351	7648	33
27 28	. 1587	8413	.6324	. 2108	.5232	.0241	. 2358	. 7642	32
29	. 1615	. 8384	.6263	. 2139	.5169	.0242	. 2364	. 7636	33 32 31
30	.21644	.78356	4.6202	.22169	4.5107	1.0243	.02370	.97630	30 29 28 27 26 25 24
31	. 1672	8328	.6142	. 2200	.5045	.0243	. 2377	. 7623	29
32	. 1701	. 8299	.6081	. 2230	.4983	.0244	. 2383	. 7617	28
33	. 1729	8271 8242	.6021	. 2261	.4921 .4860	.0245	. 2389	. 7611 . 7604	27
84 35	. 1757 .21786	.78214	4.5901	.22322	4.4799	1.0246	.02402	.97598	26
36	. 1814	8186	.5841	. 2353	.4737	.0247	. 2408	. 7592	24
37	. 1843	8154	.5782	2383	.4676	.0247	. 2415	7585	23 22 21
38	. 1871	8129	.5722	. 2414	.4615	.0248	. 2421	. 7579	22
39	. 1899	8100	.5663	. 2444	.4555	.0249	. 2427	. 7573	21
40	.21928	.78072	4.5604	.22475	4.4494	1.0249	.02434	.97566	20
41	. 1956	8043	.5545	. 2505	.4434	.0250	. 2440	7560	19
42	. 1985	8015	.5486	. 2536 . 2566	.4373	.0251	. 2446	. 7553 . 7547	18 17
43 44	. 2013	. 7987 . 7959	.5369	2597	.4253	.0252	. 2459	. 7541	16
45	.22070	77930	4.5311	.22628	4.4194	1.0253	.02466	.97534	15
46	2098	7902	.5253	. 2658	.4134	.0253	. 2472	. 7528	14
47	2126	7873	.5195	. 2689	.4074	.0254	. 2479	7521	13
48	2155	. 7845	.5137	. 2719	.4015	.0255	. 2485	. 7515	12
49	. 2183	. 7817	.5079	. 2750	.3956	.0255	. 2491	. 7508	11
50	.22211	.77788	4.5021	.22781	4.3897	1.0256	.02498	.97502	10
51	. 2240 •	7760	.4964	. 2811	.3838	.0257	. 2504	. 7495	9
52	. 2268	7732	.4907	. 2842	.3779	.0257	. 2511 . 2517	. 7489	8
53	. 2297	7703	.4850 .4793	. 2872 . 2903	.3721	.0258	. 2517	. 7483 . 7476	6
54 55	.22353	.77647	4.4736	.22934	4.3604	1.0260	.02530	.97470	5
56	. 2382	. 7618	.4679	. 2964	.3546	.0260	. 2537	7463	1 4
57	. 2410	7590	.4623	2995	.3488	.0261	. 2543	. 7457	3
58	2438	. 7561	.4566	. 3025	.3430	.0262	. 2550	. 7450	3 2 1
59	. 2467	. 7533	.4510	. 3056	.3372	.0262	. 2556	. 7443	
60	. 2495	. 7505	.4454	. 3087	.3315	.0263	. 2563	. 7437	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

13°	•	Na	tural Tr	igonom	ns.	. 166°			
M.	Sine,	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.22495	.77505	4.4454	.23087	4.3315	1.0263	.02563	.97437	60
1	2523	. 7476 . 7448	.4398	. 3117	.3257 .3200	.0264	. 2569 . 2576	. 7430	59
2	. 2552	7448	.4342	. 3148	.3200	.0264	. 2576	. 7424	58
2 3 4 5 6 7 8 9 10	. 2580 . 2608	. 7420 . 7391	.4287 .4231	. 3179 . 3209	.3143 .3086	.0265 .0266	. 2583 . 2589	. 7417	57 56
5	.22637	77363	4.4176	.23240	4.3029	1,0266	.02596	.97404	55
6	2665	7335	.4121	. 3270	.2972	.0267	. 2602	. 7398	54
7	2693	7306	.4065	. 3301	.2916	.0268	2609	. 7391	53
8	2722	. 7278	.4011	. 3332	.2859	.0268	. 2616	. 7384	52
9	. 2750	. 7250	.3956	. 3363	.2803	.0269	. 2622	. 7378	51
10	.22778	.77221	4.3901	.23393	4.2747	1.0270	.02629	.97371	50
11 12	2807	. 7193	.3847	. 3424	.2691	.0271	. 2635	. 7364	49
13	. 2835 . 2863	. 7165 . 7136	.3792	. 3455	.2635	.0271	. 2642	7358	48
14	. 2892	. 7136	.3738 .3684	. 3485 . 3516	.2579 .2524	.0272	. 2649 . 2655	. 7351 . 7344	47 46
15	.22920	.77080	4.3630	.23547	4.2468	1.0273	.02662	.97338	45
16	. 2948	7052	.3576	3577	.2413	.0274	. 2669	7331	44
1 7	2977	7023	3522	3608	.2358	.0275	2675	7324	43
18	3005	. 6995	.3469	. 3639	.2303	.0276	2682	. 7318	42
19	. 3033	. 6967	.3415	. 3670	.2248	.0276	. 2689	. 7311	41
20	.23061	.76938	4.3362	.23700	4.2193	1.0277	.02695	.97304	40
21	. 3090	6910	.3309	3731	.2139	.0278	. 2702	. 7298	39
22	. 3118	. 6882	.3256	. 3762	.2084	.0278	. 2709	. 7291	38
23	. 3146	. 6853	.3203	. 3793	.2030	.0279	2716	. 7284	37
24	. 3175 .23203	. 6825 .76797	.3150	. 3823 .23854	.1976 4.1921	.0280 1.0280	.02729	. 7277 .97271	36 35
25 26	. 3231	6769	4.3098 .3045	. 3885	.1867	.0281	. 2736	. 7264	34
97	3260	6740	.2993	. 3916	.1814	.0282	2743	7257	33
28	3288	6712	.2941	. 3946	.1760	.0283	2749	7250	32
29	. 3316	. 6684	.2888	3977	1706	.0283	2756	7244	31
28 29 30	.23344	.76655	4.2836	.24008	.1706 4.1653	1.0284	.02763	.97237	30
31	. 3 373	. 6627	.2785	4039	.1600	.0285	. 2770	. 7230	29
82	. 3401	. 6599	.2733	. 4069	.1546	.0285	. 2777	. 7223	28 27
83	. 3429	. 6571	.2681	. 4100	.1493	.0286	. 2783	. 7216	27
34	. 3458	6542	.2630	4131	.1440	.0287	. 2790	. 7210	26
35	.23486 . 3514	.76514	4.2579	.24162	4.1388	1.0288	.02797	.97203	25
36 37	. 3542	. 6486 . 6457	.2527 .2476	. 4192 . 4223	.1335 .1282	.0288	. 2804 . 2811	. 7196 . 7189	24 23
38	3571	6429	.2425	. 4254	.1230	.0290	2818	7182	22
89	3599	6401	.2375	. 4285	.1178	.0291	2824	7175	21
40	.23627	.76373	4.2324	.24316	4.1126	1.0291	.02831	.97169	20
41	. 3655	. 6344	.2273	. 4346	.1073	.0292	. 2838	. 7162	19
42	. 3684	. 6316	.2223	. 4377	.1022	.0293	. 2845	. 7155	18
43	. 3712	. 6288	.2173	. 4408	.0970	.0293	. 2852	. 7148	17
44	. 3740	. 6260	.2122	. 4439	.0918	.0294	. 2859	. 7141	16
45 46	.23768	.76231	4.2072 .2022	.24470	4.0867	1.0295	.02866	.97134	15
47	. 3825	6203	.1972	. 4501 . 4531	.0815 .0764	.0296	. 2873 . 2880	7127	14 13
48	. 3853	6147	.1923	. 4562	.0713	.0297	2886	7113	12
49	. 3881	6118	.1873	4593	.0662	.0298	2893	. 7106	ii
50	.23910	.76090	4.1824	24624	4.0611	1.0299	.02900	.97099	10
51	. 3938	. 6062	.1774	. 4655	.0560	.0299	2907	. 7092	8
52	. 3966	. 6034	.1725	. 4686	.0509	.0300	. 2914	. 7086	8 7
53	. 3994	. 6005	.1676	. 4717	.0458	.0301	. 2921	. 7079	7
54	. 4023	. 5977	.1627	. 4747	.0408	.0302	. 2928	. 7072	6
55	.24051	.75949	4.1578	.24778	4.0358	1.0302	.02935	.97065	5
56	. 4079	5921	.1529	. 4809	.0307	.0303	. 2942	. 7058	4
57 58	. 4107 . 4136	. 5892 . 5864	.1481 .1432	4840	.0257 .0207	.0304	. 2949	. 7051	3
59	. 4164	. 5836	.1384	. 4871 . 4902	.0207	.0305	. 2956	. 7044	1
60	4192	. 5808	.1336	4933	.0108	.0306	2970	7029	ō
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

140	Natural Trigonometrical Functions.								
M.	Sine.	Vrs. cos.	Cosec 'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.24192	.75808	4.1336	.24933	4.0108	1.0306	.02970	.97029	60
1	. 4220	. 5779	.1287	. 4964	.0058	.0307	. 2977	. 7022	59
2	. 4249	. 5751	.1239	. 4995	.0009	.0308	. 2984	. 7015	58
3	. 4277	5723	.1191	. 5025	3.9959	.0308	. 2991	. 7008	57
4	. 4305	. 5695	.1144	. 5056	.9910	.0309	.03006	. 7001 .96994	56 55
5 6	. 4361	.75667 . 5638	4.1096 .1048	. 25087	3.9861 .9812	1.0310 .0311	. 3013	. 6987	54
7	. 4390	5610	.1001	. 5149	.9763	.0311	3020	. 6980	53
8	. 4418	. 5582	.0953	. 5180	.9714	.0312	3027	. 6973	53 52
9	. 4446	. 5554	.0906	5211	.9665	.0313	3034	. 6966	51
10	.24474	.75526	4.0859	.25242	3.9616	1.0314	.03041	.96959	50
11	. 4502	. 5497	.0812	. 5273	.9568	.0314	. 3048	. 6952	49
12	. 4531	. 5469	.0765	. 5304	.9520	.0315	. 3055	. 6944	48
13	. 4559	. 5441	.0718	. 5335	.9471	.0316	. 3063	. 6937 . 6930	47
14	4587	5413	.0672	. 5366	.9423	.0317	. 3070	.96923	46
15 16	.24615 . 4643	.75385	4.0625 .0579	.25397	3.9375 .9327	1.0317 .0318	. 3084	. 6916	44
17	4672	5328	.0532	5459	.9279	.0319	. 3091	. 6909	43
18	4700	5300	.0486	5490	9231	.0320	. 3098	. 6901	42
19	4728	. 5272	.0440	. 5521	.9184	.0320	. 3106	. 6894	41
20	.24756	.75244	4.0394	.25552	3.9136	1.0321	.03113	.96887	40
20 21 22 23	. 4784	. 5215	.0348	. 5583	.9089	.0322	. 3120	. 6880	39
22	. 4813	. 5187	.0302	. 5614	.9042	.0323	. 3127	. 6873	38
23	. 4841	. 5159	.0256	. 5645	.8994	.0323	. 3134	. 6865	37
24	. 4869	. 5131	.0211	. 5676	.8947	.0324	. 3142	. 6858	36
20	.24897	.75103	4.0165	.25707	3.8900	1.0325	.03149	.96851	35
25 26 27 28 29	. 4925 . 4953	. 5075 . 5046	.0120	. 5738 . 5769	.8853 .8807	.0326	. 3156	. 6844	34 33
20	. 4982	5018	.0029	. 5800	.8760	.0327	3171	. 6829	32
29	. 5010	. 4990	3.9984	. 5831	.8713	.0328	3178	. 6822	31
30	.25038	.74962	3.9939	.25862	3.8667	1.0329	.03185	.96815	30
31	. 5066	. 4934	.9894	. 5893	.8621	.0330	. 3192	. 6807	29
32	. 5094	. 4906	.9850	. 5924	.8574	.0330	. 3200	. 6800	28
33	. 5122	. 4877	.9805	. 5955	.8528	.0331	. 3207	. 6793	27
34	. 5151	. 4849	.9760	. 5986	.8482	.0332	. 3214	. 6785	26
35	.25179	.74821	3.9716	.26017	3.8436	1.0333	.03222	.96778	25 24
36 37	. 5207 . 5235	. 4793 . 4765	.9672 .9627	. 6048	.8390 .8345	.0334	. 3229	. 6771 . 6763	23
38	. 5263	4737	.9583	6110	.8299	.0335	. 3244	6756	22
39	5291	4709	.9539	6141	.8254	.0336	3251	. 6749	21
40	.25319	.74680	3.9495	.26172	3.8208	1.0337	.03258	.96741	20
41	. 5348	. 4652	.9451	. 6203	.8163	.0338	. 3266	. 6734	19
42	. 5376	. 4624	.9408	. 6234	.8118	.0338	. 3273	. 6727	18
43	. 5404	. 4596	.9364	. 6266	.8073	.0339	. 3281	. 6719	17
44	. 5432	4568	.9320	. 6297	.8027	.0340	3288	. 6712	16
45	.25460	.74540	3.9277	.26328	3.7983	1.0341	.03295	.96704	15
46 47	. 5488 . 5516	. 4512 . 4483	.9234	. 6359 . 6390	.7938 .7893	.0341	. 3303	. 6690	14 13
48	. 5544	. 4455	.9147	6421	.7848	.0342	. 3318	. 6682	12
49	. 5573	. 4427	.9104	6452	.7804	.0344	. 3325	. 6675	iĩ
50	.25601	.74399	3.9061	.26483	3.7759	1.0345	.03332	.96667	10
51	. 5629	. 4371	.9018	. 6514	.7715	.0345	. 3340	. 6660	9
52	. 5657	. 4344	.8976	. 6546	.7671	.0346	. 3347	. 6652	8
53	. 5685	. 4315	.8933	. 6577	.7627	.0347	. 3355	. 6645	7
54	. 5713	. 4287	.8890	. 6608	.7583	.0348	. 3362	. 6638	6
55 56 57	.25741	.74259	3.8848	.26639	3.7539	1.0349	.03370	.96630	5
56	. 5769	. 4230	.8805	. 6670	.7495	.0349	. 3377	6623	4.
50	. 5798 . 5826	. 4202	.8763 .8721	. 6701 . 6732	.7451	.0350 .0351	. 3385	. 6615 . 6608	3
58 59	. 5854	4174	.8679	6764	.7407 .7364	.0352	. 3400	. 6600	1
60	. 5882	. 4118	.8637	6795	.7320	.0353	3407	. 6592	ō
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M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Taug.	Cosec'nt	Vrs. cos.	Sine.	M.

150	•	Na	tural Tı	rigonom	etrical l	unction	15.	10	640
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.25882	.74118	3.8637	.26795	3.7320	1.0353	.03407	.96592	60
1 2	. 5910	. 4090	.8595	. 6826	.7277	.0353	. 3415	. 6585	59
2	. 5938	. 4062	.8553	. 6857	.7234	.0354	. 3422	. 6577	58 57
8	. 5966	. 4034	.8512 .8470	. 6888 . 6920	.7191 .7147	.0355 .0356	. 3430	. 6570 . 6562	56
4 5	. 5994	. 4006 .73978	3.8428	.26951	3.7104	1.0357	.03445	.96555	55
6	. 6050	3949	.8387	. 6982	.7062	.0358	. 3453	6547	54
7	6078	3921	.8346	. 7013	.7019	.0358	. 3460	6540	54 53
8	6107	8893	.8304	. 7044	.6976	.0359	. 3468	. 6532	52
9	. 6135	. 3865	.8263	. 7076	.6933	.0360	. 3475	. 6524	51
10	.26163	.73837	3.8222	.27107	3.6891	1.0361	.03483	.96517	50
11	. 6191	8809	.8181	. 7138	.6848	.0362	. 3491	. 6509	49
12	. 6219	. 3781	.8140	. 7169	.6806	.0362	. 3498	. 6502	48
13	. 6247	. 3753	.8100	. 7201	.6764	.0363	. 3506 . 3514	. 6494 . 6486	47 46
14	. 6275 .26303	. 3725 .73697	.8059	. 7232 .27263	.6722 3.6679	1.0365	.03521	.96479	45
15 16	. 6331	0000	3.8018 .7978	. 7294	.6637	.0366	. 3529	. 6471	44
17	. 6359	. 3641	7937	7326	.6596	.0367	3536	. 6463	43
18	6387	3613	.7897	7357	.6554	.0367	. 3544	6456	42
19	6415	3585	.7857	7388	.6512	.0368	. 3552	. 6448	41
20	.26443	.73556	3.7816	.27419	3.6470	1.0369	.03560	.96440	40
21	. 6471	. 3528	.7776	. 7451	.6429	.0370	. 3567	. 6433	39
22	. 6499	3500	.7736	. 7482	.6387	.0371	. 3575	. 6425	38
23 24	. 6527	3472	.7697	. 7513	.6346	.0371	. 3583	. 6417	37
24	6556	. 3444	.7657	. 7544	.6305	.0372	. 3590	. 6409 .96402	36 35
25 26	.26584	.73416 . 8388	3.7617	.27576 . 7607	3.6263 .6222	1.0373 .0374	. 3606	. 6394	34
27	. 6612 . 6640	. 3360	.7577 .7538	. 7638	.6181	.0375	. 3614	6386	33
28	. 6668	3332	.7498	7670	.6140	.0376	3621	. 6378	32
28 29	. 6696	3304	.7459	7701	.6100	.0376	. 3629	. 6371	31
30	.26724	.73276	3.7420	.27732	3.6059	1.0377	.03637	.96363	30
31	. 6752	. 3248	.7380	. 7764	.6018	.0378	. 3645	6355	29
32	. 6780	. 3220	.7341	. 7795	.5977	.0379	. 3652	. 6347	28 27
83	. 6808	3192	.7302	. 7826	.5937	.0380	. 3660	. 6340	26
34	. 6836	3164	.7263 3.7224	. 7858 .27889	.5896 3.5856	.0381 1.0382	. 3668	. 6332	25
35 36	. 6892	.73136 . 3108	.7186	. 7920	.5816	.0382	. 3684	. 6316	24
30 37	. 6920	3080	.7147	7952	.5776	.0383	3691	6308	23
38	6948	3052	.7108	7983	.5736	.0384	3699	. 6301	22
89	. 6976	3024	.7070	. 8014	.5696	.0385	. 3707	. 6293	21
40	27004	.72996	3.7031	.28046	3.5656	1.0386	.03715	.96285	20
41	. 7032	. 2968	.6993	. 8077	.5616	.0387	. 3723	. 6277	19
42	. 7060	2940	.6955	. 8109	.5576	.0387	. 3731	. 6269	18
43	. 7088	. 2912	.6917	. 8140	.5536	.0388	3739	. 6261	17
44	. 7116	2884	.6878	. 8171 .28203	.5497 3.5457	.0389 1.0390	. 3746	. 6253 .96245	16 15
45	.27144	.72856 . 2828	3.6840 .6802	. 8234	.5418	.0391	. 3762	6238	14
46 47	7200	2800	.6765	8266	.5378	.0392	3770	6230	13
48	7228	2772	.6727	8297	.5339	.0393	3778	6222	12
49	7256	2744	.6689	8328	.5300	.0393	. 3786	. 6214	11
50	.27284	.72716	3.6651	.28360	3.5261	1.0394	.03794	.96206	10
51	. 7312	2688	6614	. 8391	.5222	.0395	. 3802	. 6198	9
52	. 7340	2660	.6576	. 8423	.5183	.0396	. 3810	. 6190	8 7
53	. 7368	. 2632	.6539	. 8454	.5144	.0397	. 3818	. 6182	7
54	7396	. 2604	.6502	. 8486	.5105	.0398 1.0399	. 3826	. 6174	6
55	.27424	.72576	3.6464	.28517	3.5066 .5028	.0399	. 3842	.96166 . 6158	4
56	. 7452	2548	.6427 .6390	. 8549 . 8580	.4989	.0399	. 3850	. 6150	3
57 58	. 7480 . 7508	2492	.6353	. 8611	.4951	.0401	3858	6142	2
59	. 7536	2464	.6316	. 8643	4912	.0402	3866	6134	l î
60	. 7564	2436	.6279	. 8674	.4874	.0403	. 3874	. 6126	ō
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec 'nt	Vrs. cos.	Sine.	M.

160	•	Na	tural Tr	igonom	etrical i	15.	163°		
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.27564	.72436	3.6279	.28674	3.4874	1.0403	.03874	.96126	60
1	. 7592	. 2408	.6243	. 8706	.4836	.0404	. 3882	. 6118	59
2	. 7620	. 2380	.6206	. 8737	.4798	.0405	. 3890	. 6110	58 57
3	. 7648	. 2352	.6169	. 8769	.4760	.0406	. 3898	. 6102	57
5	. 7675 .27703	.72296	.6133 3.6096	. 8800 .28832	3.4684	.0406 1.0407	. 3906	.96086	56 55
6	7731	2268	.6060	. 8863	.4646	.0408	3922	6078	54
6 7	7759	2240	.6024	. 8895	.4608	.0409	. 3930	6070	1 53
8	. 7787	. 2213	.5987	8926	.4570	.0410	. 3938	. 6062	52
9	. 7815	. 2185	.5951	. 8958	.4533	.0411	. 3946	. 6054	51
10	.27843	.72157	3.5915	.28990	3.4495	1.0412	.03954	.96045	50
11 12	. 7871 . 7899	. 2129 . 2101	.5879 .5843	. 9021 . 9053	.4458 .4420	.0413	. 3962	6037	49 48
13	7927	2073	.5807	9084	.4383	.0414	3979	6021	47
14	7955	2045	.5772	. 9116	.4346	.0415	3987	6013	46
15	.27983	.72017	3.5736	.29147	3.4308	1.0416	.03995	.96005	45
16	. 8011	. 1989	.5700	. 9179	.4271	.0417	. 4003	. 5997	44
17	. 8039	. 1961	.5665	. 9210	.4234	.0418	. 4011	. 5989	43
18	. 8067 . 8094	. 1933 . 1905	.5629 .5594	9242	.4197	.0419	. 4019 . 4028	. 5980 . 5972	42 41
19 20	28122	.71877	3.5559	.29305	.4160 3.4124	1.0420	.04036	.95964	40
21	. 8150	1849	.5523	9337	.4087	.0421	4044	5956	39
22	. 8178	. 1822	.5488	. 9368	.4050	.0422	4052	. 5948	38
23	. 8206	. 1794	.5453	. 9400	.4014	.0423	. 4060	. 5940	37
24	8234	. 1766	.5418	. 9432	.3977	.0424	. 4069	. 5931	36
25 26	. 28262	.71738	3,5383	.29463	3.3941	1.0425	.04077	.95923	35
26 27	8318	. 1710 . 1682	.5348 .5313	9495	.3904 .3868	.0426	. 4085 . 4093	5907	34 33
28	8346	1654	.5279	9558	.3832	.0428	4101	5898	32
29	8374	. 1626	.5244	9590	.3795	.0428	4110	. 5890	31
80	.28401	.71608	3.5209	.29621	3.3759	1.0429	.04118	.95882	30
31	. 8429	. 1570	.5175	. 9653	.3723	.0430	. 4126	. 5874	29
82	8457	. 1543	.5140	9685	.3687	.0431	. 4134	. 5865	28
33 34	8485 8513	. 1515 . 1487	.5106	9716	.3651	.0432	. 4143 . 4151	. 5857 . 5849	27 26
35	.28541	.71459	3.5037	29780	3.3580	1.0434	.04159	.95840	25
36	8569	. 1431	.5003	9811	.3544	.0435	. 4168	. 5832	24
37	. 8597	. 1403	.4969	. 9843	.3509	.0436	. 4176	. 5824	23
38	. 8624	. 1375	.4935	. 9875	.3473	.0437	. 4184	. 5816	22
39	. 8652	. 1347	.4901	. 9906	.3438	.0438	. 4193	. 5807	21
40	.28680 . 8708	.71320	3.4867	.29938	3.3402	1.0438 .0439	.04201	.95799	20
41 42	8736	1264	.4833 .4799	30001	.3367	.0439	4218	. 5791 . 5782	19 13
43	8764	1236	.4766	. 0033	3296	.0411	4226	5774	17
44	. 8792	. 1208	.4732	. 0065	.3261	.0442	. 4234	. 5765	16
45	.28820	.71180	3.4698	.30096	3.3226	1.0443	.04243	.95757	15
46	. 8847	. 1152	.4665	. 0128	.3191	.0144	. 4251	. 5749	11
47	. 8875 . 8903	. 1125	.4632	. 0160 . 0192	.3156	.0445	. 4260 . 4268	. 5740 . 5732	13
48 49	8931	1069	.4598 .4565	0192	.3121	.0446	4208	5723	12 11
50	28959	.71041	3.4532	30255	3.3052	1.0448	.04285	.95715	15
51	8987	. 1013	.4498	0287	.3017	.0448	. 4293	. 5707	9
52	. 9014	. 0985	.4465	. 0319	.2983	.0449	. 4302	. 5698	
53	. 9042	. 0958	.4432	. 0350	.2948	.0450	. 4310	. 5690	8 7
54	9070	. 0930	.4399	. 0382	.2914	.0451	4319	. 5681	6
55 56	.29098	.70902	3.4366 .4334	.30414	3.2879 .2845	1.0452	. 4335	.95673	5
56 57	. 9126	. 0846	.4334	. 0446	.2845	.0453 .0454	. 4333	. 5656	3
58	9181	0818	.4268	. 0509	2777	.0455	4352	5647	1 3
59	9209	. 0791	.4236	. 0541	.2742	.0456	. 4361	5639	1
60	. 9237	. 0763	.4203	. 0573	.2708	.0457	. 4369	. 5630	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

179	•	Na	tural T	igonom	etrical l	Function	ns.	10	6 2 °
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.29237	.70763	3.4203	.30573	3.2708	1.0457	.04369	.95630	60
1	. 9265	. 0735	.4170	. 0605	.2674	.0458	. 4378	. 5622	59
2	. 9293	0707	.4138	. 0637	.2640	.0459	. 4386	. 5613	58
3	. 9321	. 0679	.4106	. 0668	.2607	.0460	. 4395	. 5605 . 5596	57
4 5	. 9348	. 0651 .70624	.4073 3.4041	. 0700 .30732	.2573 3.2539	.0461 1.0461	.04412	.95588	56 55
6	. 9404	. 0596	.4009	. 0764	.2505	.0462	. 4421	5579	54
7	9432	. 0568	.3977	0796	.2472	.0463	. 4426	. 5571	54 53
8	. 9460	. 0540	.3945	. 0828	.2438	.0464	. 4438	. 5562	52
9	. 9487	. 0512	.3913	. 0859	.2405	.0465	. 4446	. 5554	51
10	.29515	.70485	3.3881	.30891	3.2371	1.0466	.04455	.95545	50
11	. 9543	0457	.3849	. 0923	.2338	.0467	. 4463	. 5536	49
12	. 9571	0429	.3817	. 0955	2305	.0468	. 4472 . 4481	. 5528 . 5519	48 47
13 14	9598	. 0401	.3785 .3754	. 1019	.2271	.0469	. 4489	. 5511	46
15	.29654	.70346	3.3722	.31051	3.2205	1.0471	.04498	95502	45
16	. 9682	. 0318	.3690	. 1083	.2172	.0472	. 4507	. 5493	44
17	9710	0290	.3659	. 1115	.2139	.0473	. 4515	. 5485	43
18	9737	. 0262	.3627	. 1146	.2106	.0474	. 4524	5476	42
19	. 9765	. 0235	.3596	. 1178	.2073	.0475	. 4532	. 5467	41
20	.29793	.70207	3.3565	.31210	3.2041	1.0476	.04541	.95459	40
21	9821	. 0179	.3534	. 1242	.2008	.0477	. 4550	5450	39 38 37
22	. 9848	. 0151	3502	. 1274	.1975	.0478	4558	. 5441	38
23 24	9876	. 0124	.3471	1306	.1942 .1910	.0478	. 4567 . 4576	5424	36
24	.29932	.70068	.3440 3.3409	. 1338 .31370	3.1877	1.0480	.04585	.95415	35
25 26	9959	.0040	.3378	. 1402	.1845	.0481	4593	5407	35 34
27	9987	. 0013	.3347	. 1434	.1813	.0482	4602	5398	33 32
28	.30015	.69982	.3316	. 1466	.1780	.0483	. 4611	. 5389	32
27 28 29	. 0043	. 9957	.3286	. 1498	.1748	.0484	. 4619	. 5380	31
30	.30070	.69929	3.3255	.31530	3.1716	1.0485	.04628	.95372	31 30 29 28 27 26 25 24
31	. 0098	. 9902	.3224	. 1562	.1684	.0486	. 4637	• 5363	29
32	. 0126	. 9874	.3194	. 1594	.1652	.0487	. 4646	• 5354	123
33 34	. 0154	9846	.3163	. 1626 . 1658	.1620 .1588	.0488	. 4654	5345	26
35	.30209	.69791	3.3102	.31690	3.1556	1.0490	.04672	95328	25
36	0237	9763	.3072	. 1722	.1524	.0491	. 4681	5319	124
37	0265	9735	3042	1754	1492	.0492	4690	5310	23 22 21 20 19
38	0292	. 9707	.3011	. 1786	.1460	.0493	. 4698	. 5301	22
39	. 0320	. 9680	.2981	. 1818	.1429	.0494	. 4707	. 5293	21
40	.30348	.69652	3.2951	.31850	3.1397	1.0495	.04716	.95284	20
41	0375	. 9624	.2921	. 1882	.1366	.0496	4725	. 5275	119
42	. 0403	9597	.2891	. 1914	,1334	.0497	4734	• 5266	18
43 44	. 0431 . 0459	. 9569 . 9541	.2861 .2831	. 1946 . 1978	.1303	.0498	. 4743	. 5257 . 5248	17 16
45	.30486	.69513	3.2801	.32010	3.1240	1.0500	.04760	.95239	15
46	. 0514	9486	.2772	. 2042	.1209	.0501	. 4769	5231	114
47	. 0542	9458	.2742	2074	.1177	.0502	4778	5222	14 13
48	. 0569	9430	.2712	. 2106	.1146	.0503	. 4787	. 5213	12
49	. 0597	9403	.2683	. 2138	.1115	.0504	. 4796	. 5204	11
50	.30625	.69375	3.2653	.32171	3.1084	1.0505	.04805	.95195	10
51	. 0653	9347	.2624	. 2203	.1053	.0506	. 4814	. 5186	9
52 53	. 0680	9320	.2594	. 2235	.1022	.0507	. 4823 . 4832	. 5177	8 7
54 54	. 0708	9292	.2565 .2535	. 2267	.0960	.0508	. 4840	. 5159	6
55	.30763	.69237	3.2506	.32331	3.0930	1.0510	.04849	.95150	6 5
55 56	. 0791	9209	.2477	. 2363	.0899	.0511	4858	. 5141	4
57	. 0819	9181	.2448	2395	.0868	.0512	4867	5132	3
58	. 0846	. 9154	.2419	2428	.0838	.0513	. 4876	. 5124	3 2 1
59	. 0874	, 9126	.2390	. 2460	.0807	.0514	. 4885	. 5115	1
60	. 0902	. 9098	.2361	. 2492	.0777	.0515	. 4894	. 5106	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

m. | Cosine. | Vrs. sin. | Secant. | Cotang. | | Tang. | Cosec nt | | Vrs. cos. | Sine. | m.

189	,	Na	tural T	rigonon	etrical	161°			
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.30902	.69098	3.2361	.32492	3.0777	1.0515	.04894	.95106	60
1	. 0929	. 9071	.2332	2524	.0746	.0516	. 4903	. 5097	59
2	. 0957	. 9043	.2303	2556	.0716	.0517	. 4912	. 5088	58
2 3 4	0985	. 9015	.2274	2588	.0686	.0518	. 4921	5079	57
5	. 1012 .31040	. 8988 .68960	.2245 3.2216	. 2621 .32653	.0655 3.0625	.0519 1.0520	. 4930	. 5070 .95061	56 55
6	. 1068	. 8932	2188	2685	.0595	.0521	. 4948	. 5051	54
5 6 7 8 9	. 1095	8905	.2159	2717	.0565	.0522	4957	. 5042	53
8	. 1123	8877	.2131	. 2749	.0535	.0523	. 4966	. 5033	52
9	. 1150	. 8849	.2102	. 2782	.0505	.0524	. 4975	. 5024	51
10 11 12	.31178	.68822	3.2074	.32814	3.0475	1.0525	.04985	.95015	50
12	. 1206 . 1233	. 8794 . 8766	.2045	. 2846 . 2878	.0445	.0526	. 4994	. 5006 . 4997	49 48
13	1261	8739	.1989	2910	.0385	.0528	5012	. 4988	47
14	. 1289	8711	.1960	2943	.0356	.0529	. 5021	4979	46
15 16	.31316	.68684	3.1932	.32975	3.0326	1.0530	.05030	.94970	45
16	. 1344	8656	.1904	. 3007	.0296	.0531	. 5039	. 4961	44
17 18	. 1372	8628	.1876	. 3039	.0267	.0532	5048	. 4952	43
19	. 1399 . 1427	. 8601 . 8573	.1848 .1820	. 3072 . 3104	.0237	.0533	. 5057	. 4942 . 4933	42 41
20	.31454	.68545	3.1792	.33136	3.0178	1 0535	.05076	.94924	40
21	. 1482	8518	.1764	. 3169	.0149	1.0535 .0536	. 5085	4915	39
22	. 1510	. 8490	.1736	. 3201	.0120	.0537	. 5094	. 4906	38
23	. 1537	. 8463	.1708	. 3233	.0090	.0538	. 5103	. 4897	37
24	. 1565	. 8435	.1681	. 3265	.0061	.0539	. 5112	. 4888	36
20	.31592 . 1620	.68407 .8380	3.1653 .1625	.33298 . 3330	3.0032 .0003	1.0540 .0541	.05121	.94878 . 4869	35 34
27	. 1648	8352	.1598	3362	2.9974	.0542	5140	. 4860	33
28	. 1675	8325	.1570	3395	.9945	.0543	5149	. 4851	82
2222442222	. 1703	. 8297	.1548	. 3427	.9916	.0544	. 5158	. 4841	31
80	.31730	.68269	3.1515	.33459	2.9887	1.0545	.05168	.94832	30 29
31 32 33	. 1758	. 8242	.1488	. 3492	.9858	.0546	. 5177	. 4823	29
92	. 1786 . 1813	8214	.1461 .1433	. 3524 . 3557	.9829	.0547 .0548	. 5186 . 5195	. 4814 . 4805	28 27
84	. 1841	8159	.1406	3589	.9772	.0549	. 5205	4795	26
35	.31868	.68132	8.1379	.33621	2.9743	1.0550	.05214	.94786	25
35 36 37 38	. 1896	8104	.1352	. 3654	.9714	.0551	. 5223	. 4777	24
87	. 1923	8076	.1325	. 3686	.9686	.0552	. 5232	. 4767	23
39	1951	8049	.1298 .1271	. 3718	.9657	.0553	. 5242	. 4758	22
40	. 1978 .32006	. 8021 .67994	3.1244	. 3751 .33783	.9629 2.9600	.0554 1.0555	. 5251	. 4749 .94740	21 20
41	2034	7966	.1217	. 3816	.9572	.0556	5270	. 4730	19
42	. 2061	. 7939	.1190	. 3848	.9544	.0557	5279	. 4721	18
43	2089	. 7911	.1163	. 3880	.9515	.0558	. 5288	. 4712	17
44	2116	7884	.1137	. 3913	.9487	.0559	. 5297	. 4702	16
45 46	.32144	.67856 . 7828	3.1110 .1083	.33945 .3978	2.9459 .9431	1.0560 .0561	.05307 .5316	.94693 . 4684	15 14
47	2199	7801	.1057	4010	.9403	.0562	5326	. 4674	13
48	2226	7773	.1030	. 4043	.9375	.0563	5335	. 4665	12
49	. 2254	. 7746	.1004	. 4075	.9347	.0565	. 5344	. 4655	11
50	.32282	.67718	3.0977	.34108	2.9319	1.0566	.05354	.94646	10
51 52	2309	7691	.0951	. 4140	.9291	.0567	. 5363	4637	9
53	. 2337 . 2364	. 7663 . 7636	.0925	. 4173 . 4205	.9263 .9235	.0568	. 5373	. 4627 . 4618	8
54	2392	7608	.0872	. 4238	.9208	.0570	. 5391	. 4608	9 8 7 6 5
55	.32419	.67581	3.0846	.34270	2.9180	1.0571	.05401	.94599	Š
56 57	. 2447	. 7553	.0820	. 4303	.9152	.0572	. 5410	. 4590	4
57	. 2474	. 7526	.0793	. 4335	.9125	.0573	. 5420	. 4580	3
58 59	2502	7498	.0767	. 4368	.9097	.0574	. 5429	. 4571	1
60	. 2529 . 2557	. 7471	.0741 .0715	. 4400 . 4433	.9069 .9042	.0575	. 5439	. 4561 . 4552	0
_	- 2001	110	.0710				. 0110	. 1004	_
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

, 19º	•	Na	tural Tr	igonom	etrical l	160°			
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.32557	.67443	3.0715	.34433	2.9042	1.0576	.05448	.94552	60
1	. 2584	. 7416	.0690	. 4465	.9015	.0577	. 5458	. 4542	59
2	. 2612	7388	.0664	. 4498	.8987	.0578	. 5467	. 4533	58 57
3	. 2639 . 2667	. 7361 . 7333	.0638 .0612	. 4530 . 4563	.8960 .8933	.0579 .0580	. 5476 . 5486	. 4523 . 4514	57 56
Ē	.32694	.67306	3.0586	.34595	2.8905	1.0581	.05495	.94504	55
2 3 4 5 6 7	2722	7278	.0561	4628	.8878	.0582	. 5505	. 4495	54
7	. 2749	. 7251	.0535	. 4661	.8851	.0584	. 5515	. 4485	53 52 51
8	. 2777	. 7223	.0509	. 4693	.8824	.0585	. 5524	. 4476	52
9 10	. 2804	. 7196 .67168	.0484 3.0458	. 4726 .34758	.8797 2.8770	.0586 1.0587	. 5534	. 4466 .94457	51 50
ii	. 2859	7141	.0433	. 4791	.8743	.0588	. 5553	. 4447	49
12	. 2887	7113	.0407	4824	.8716	.0589	. 5562	. 4438	48
13	. 2914	. 7086	.0382	. 4856	.8689	.0590	. 5572	. 4428	47
14	. 2942	7058	.0357	. 4889	.8662	.0591	5581	. 4418	46
15 16	.32969	. 7003	3.0331 .0306	.34921	2.8636 .8609	1.0592 .0593	.05591	.94409	45
17	3024	6976	.0281	4987	.8582	.0594	. 5610	4390	43
18	. 3051	6948	.0256	. 5019	.8555	.0595	. 5620	4380	42
19	. 3079	. 6921	.0231	. 5052	.8529	.0596	. 5629	. 4370	41
20	.33106	.66894	3.0206	.35085	2.8502	1.0598	.05639	.94361	40
21 22	. 3134 . 3161	. 6866	.0181 .0156	. 5117 . 5150	.8476 .8449	.0599	. 5649	. 4351 . 4341	39 38 37 36 35 34 33 32
23	3189	6811	.0131	5183	.8423	.0601	. 5668	4332	37
24	. 3216	. 6784	.0106	. 5215	.8396	.0602	. 5678	. 4322	36
25	.33243	.66756	3.0081	.35248	2.8370	1.0603	.05687	.94313	35
26	. 3271	6729	.0056	. 5281	.8344	.0604	5697	4303	34
27 28	. 3298	. 6701 . 6674	.0031	. 5314 . 534 6	.8318 .8291	.0605	. 570 7 . 5716	. 4293 . 4283	33
29	. 3353	6647	2.9982	5379	.8265	.0607	5726	4274	31
30	.33381	.66619	2.9957	.35412	2.8239	1.0608	.05736	.94264	30
81	. 3408	. 6592	.9933	. 5445	.8213	.0609	. 5745	. 4254	30 29 28 27 26 25 24
32	. 3435	. 6564	.9908	. 5477	.8187	.0611	. 5755	. 4245	28
33 34	. 3463	. 6537 . 6510	.9884 .9859	. 5510 . 5543	.8161 .8135	.0612	. 5765	. 4235	27
35	.33518	.66482	2.9835	.35576	2.8109	1.0614	.05784	.94215	25
36	. 3545	. 6455	.9810	. 5608	.8083	.0615	. 5794	. 4206	24
37	. 3572	. 6427	.9786	. 5641	.8057	.0616	. 5804	. 4196	23 22 21
38	. 3600	. 6400	.9762	. 5674	.8032	.0617	. 5814	4186	22
39 40	. 3627 .33655	. 6373 .66345	.9738 2.9713	. 5707 .3573 9	.8006 2.7980	.0618 1.0619	. 5823	. 4176 .94167	20
41	3682	. 6318	.9689	5772	.7954	.0620	. 5843	4157	19
42	. 3709	. 6290	.9665	. 5805	.7929	.0622	. 5853	. 4147	18
43	. 3737	. 6263	.9641	. 5838	.7903	.0623	. 5863	. 4137	17
44	. 3764	. 6236	.9617	. 5871	.7878	.0624	. 5872	. 4127	16
45 46	.33792	.66208 .6181	2.9593 .9569	.35904	2.7852 .7827	1.0625 .0626	.05882	. 94118	15 14
47	. 3846	6153	.9545	. 5969	7801	.0627	5902	4098	13
48	. 3874	. 6126	.9521	. 6002	.7776	.0628	5912	. 4088	12
49	. 3901	. 6099	.9497	. 6035	.7751	.0629	5922	. 4078	11
50	.33928	.66071	2.9474	.36068	2.7725	1.0630	.05932	.94068	10
51 52	. 3956 . 3983	. 6044	.9450 .9426	. 6101 . 6134	.7700 .7675	.0632	. 5941	. 4058 . 4049	9
53	. 4011	. 5989	.9402	6167	.7650	.0634	. 5961	4039	8 7
54	. 4038	. 5962	.9379	. 6199	.7625	.0635	. 5971	. 4029	6
55	.34065	.65935	2.9355	.36232	2.7600	1.0636	.05981	.94019	1 5
56	. 4093	. 5907	.9332	6265	.7574	.0637	. 5991	. 4009	4
57 58	. 4120	. 5880 . 5853	.9308 .9285	. 6298 . 6331	.7549 .7524	.0638	. 6001	. 3999	3
59	. 4175	. 5825	.9261	. 6364	.7524	.0639	. 6021	. 3979	3 2 1
60	. 4202	. 5798	.9238	. 6397	.7475	.0642	. 6031	. 3969	ō
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

109° 70°

20°	•	Na	tural Tr	igonom	etrical l	Punction	15.	13	59°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.34202	.65798	2.9238	.36397	2.7475	1.0642	.06031	.93969	60
1	. 4229	. 5771	.9215	. 6430	.7450	.0643	. 6041	. 3959	Į 59
2 3	. 4257	5743	.9191	. 6463	.7425	.0644	. 6051	. 3949	58 57
3	. 4284	. 5716	.9168	. 6496	.7400	.0645	. 6061	. 3939	57
4	. 4311	. 5689	.9145	. 6529	.7376	.0646	. 6071	. 3929	56
5	.34339	.65661	2.9122	.36562	2.7351	1.0647	.06080	.93919	55
6	. 4366 . 4393	. 5634 . 5607	.9098 .9075	. 6595 . 6628	.7326 .7302	.0648 .0650	. 6090 . 6100	3909 3899	1 54
7 8	. 4421	5579	.9052	. 6661	.7277	.0651	. 6110	. 3889	54 53 52
9	. 4448	5552	.9029	6694	.7252	.0652	6121	. 3879	51
ιŏΙ	.34475	.65525	2.9006	.36727	2.7228	1.0653	.06131	.93869	50
ĭ	4502	. 5497	.8983	. 6760	.7204	.0654	. 6141	3859	49
2	4530	. 5470	.8960	. 6793	.7179	.0655	. 6151	. 3849	48
13	. 4557	. 5443	.8937	. 6826	.7155	.0656	. 6161	3839	47
4	. 4584	. 5415	.8915	. 6859	.7130	.0658	. 6171	. 3829	46
15	.34612	.65388	2.8892	.36892	2.7106	1.0659	.06181	.93819	45
6	. 4639	. 5361	.8869	. 6925	.7082	.0660	. 6191	. 3809	44
7	. 4666	. 5334	.8846	. 6958	.7058	.0661	. 6201	. 3799	43
8	. 4693 . 4721	5306	.8824	. 6991	.7033	.0662	. 6211	. 3789	42
9	.34748	. 5279 .65252	.8801 2.8778	. 7024 .37057	.7009 2.6985	.0663	. 6221 .06231	. 3779	41 40
21	. 4775	. 5225	.8756	. 7090	.6961	.0664 .0666	6241	.93769 . 3758	39
22	4803	5197	.8733	. 7123	.6937	.0667	6251	3748	38
23	. 4830	5170	.8711	. 7156	.6913	.0668	6262	3738	37
Ã	4857	. 5143	.8688	7190	.6889	.0669	6272	3728	38 37 36
5	.34884	.65115	2.8666	.37223	2.6865	1.0670	.06282	.93718	35
26	. 4912	. 5088	.8644	. 7256	.6841	.0671	. 6292	. 3708	34
27	. 4939	. 5061	.8621	. 7289	.6817	.0673	. 6302	. 3698	33
8	. 4966	. 5034	.8599	. 7322	.6794	.0674	. 6312	. 3687	32
19	. 4993	5006	.8577	. 7355	.6770	.0675	. 6323	. 3677	35 34 33 32 31 30 29 28 27 26 25 24 23 22 21 20 19
10	.35021	.64979	2.8554	.37388	2.6746	1.0676	.06333	.93667	30
2	. 5048 . 5075	. 4952 . 4925	.8532	. 7422	.6722	.0677	. 6343	. 3657	25
3	5102	4897	.8510 .8488	. 7455 . 7488	.6699	.0678 .0679	. 6353	. 3647 . 3637	28
4	. 5130	4870	.8466	7521	.6652	.0681	. 6373	. 3626	26
5	.35157	.64843	2.8444	.37554	2.6628	1.0682	.06384	.93616	25
36	. 5184	. 4816	.8422	. 7587	.6604	.0683	. 6394	3606	24
7	. 5211	. 4789	.8400	7621	.6581	.0684	. 6404	3596	23
8	. 5239	. 4761	.8378	7654	.6558	.0685	. 6414	3585	22
19	. 5266	. 4734	.8356	. 7687	.6534	.0686	. 6425	. 3575	21
0	35293	.64707	2.8334	.37720	2.6511	1.0688	.06435	.93565	20
1	. 5320	. 4680	.8312	. 7754	.6487	.0689	. 6445	3555	19
12	. 5347	. 4652	.8290	. 7787	.6464	.0690	. 6456	. 3544	18 17
3	. 5375	. 4625	.8269	. 7820	.6441	.0691	. 6466	. 3534	117
14 15	. 5402	. 4598 .64571	.8247 2.8225	. 7853 .37887	.6418	.0692	6476	3524	16
6	. 5456	. 4544	.8204	. 7920	2.6394 .6371	1.0694 .0695	. 6497	.93513	15 14
7	5483	4516	.8182	. 7953	.6348	.0696	6507	3493	13
18	. 5511	4489	.8160	7986	.6325	.0697	6517	. 3482	12
19	5538	. 4462	.8139	. 8020	.6302	.0698	6528	. 3472	lii
50	.35565	.64435	2.8117	.38053	2.6279	1.0699	.06538	93462	10
51	. 5592	. 4408	.8096	. 8086	.6256	.0701	. 6548	. 3451	9
52	. 5619	. 4380	.8074	. 8120	.6233	.0702	. 6559	. 3441	8
53	. 5647	. 4353	.8053	. 8153	.6210	.0703	. 6569	. 3431	7
54	. 5674	. 4326	.8032	. 8186	.6187	.0704	. 6579	. 3420	6 5
55	.35701	.64299	2.8010	.38220	2.6164	1.0705	.06590	.93410	5
6	. 5728	. 4272	.7989	. 8253	.6142	.0707	. 6600	. 3400	4
7	. 5755	. 4245	.7968	. 8286	.6119	.0708	. 6611	. 3389	3
8	. 5782	. 4217 . 4190	.7947	. 8320	.6096	.0709	6621	. 3379	3 2 1
59 50	. 5810 . 5837	. 4163	.7925 .7904	. 8353 . 8386	.6073 .6051	.0710 .0711	. 6631	. 3368 . 3358	1 6
	. 0001	1 . 2100	11204	. 0000	10001	.0/11	. 0042	. 2000	1 0
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219	•	Na	tural Tı	igonom	etrical	158°			
M.	Sine.	Vrs. cos.	Cosec 'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.35837	.64163	2.7904	.38386	2.6051	1.0711	.06642	.93358	60
1	. 5864	4136	.7883	. 8420 . 8453	.6028 .6006	.0713 .0714	. 6652	. 3348	59
3	. 5891 . 5918	. 4109 . 4082	.7862 .7841	. 8486	.5983	.0715	6673	3327	58 57
4	. 5945	4055	.7820	. 8520	.5960	.0716	6684	. 3316	56
4 5	.35972	.64027	2.7799	.38553	2.5938	1.0717	.06694	.93306	55
6	. 6000	4000	.7778	. 8587	.5916	.0719 .0720	. 6705	. 3295	54
6 7 8 9	. 6027 . 6054	. 3973 . 3946	.7757 .7736	. 8620 . 8654	.5893 .5871	.0720	6715	. 3285 . 3274	53 52 51
8	6081	3919	.7715	. 8687	.5848	.0722	6736	. 3264	51
1ŏ	.36108	63892	2.7694	.38720	2.5826	1.0723	.06747	.93253	50
11	. 6135	. 3865	.7674	. 8754	.5804	.0725	. 6757	. 3243	49
12 13	. 6162	. 3837	.7653	. 8787 . 8821	.5781 .5759	.0726 .0727	6768	. 3232 . 3222	48
13	. 6189 . 6217	. 3810 . 3783	.7632 .7611	. 8854	.5737	.0728	6789	3211	47 46
15	36244	.63756	2.7591	38888	2.5715	1.0729	.06799	.93201	45
16	6271	. 3729	.7570	. 8921	.5693	.0731	. 6810	. 3190	44
17	. 6298	. 3702	.7550	. 8955	.5671	.0732	. 6820	. 3180	43
18	6325	. 3675	.7529 .7509	. 8988 . 9022	.5640	.0733 .0734	. 6831 . 6841	. 3169 . 3150	42 41
19	. 6352 .36379	. 3648 .63621	2,7488	.39055	.5627 2.5605	1.0736	.06852	.93148	40
20 21 22 23	. 6406	3593	.7468	. 9089	.5583	.0737	. 6863	3137	. 32
22	. 6433	. 3566	.7447	. 9122	.5561	.0738	. 6873	. 3127	31 31
23	. 6460	3539	.7427	. 9156	.5539	.0739	. 6884	. 3116	31
24 25	. 6488 .36515	. 3512 .63485	.7406 2.7386	. 9189 .39223	.5517 2.5495	.0740 1.0742	.6894	. 3105 .93095	3(
26	. 6542	3458	.7366	. 9257	.5473	.0743	. 6916	. 3084	3ŧ 34
27	6569	3431	.7346	. 9290	.5451	.0744	. 6926	. 3074	35
28	6596	. 3404	.7325	. 9324	.5430	.0745	. 6937	. 3063	33
27 28 29 30	6623	3377	.7305	9357	.5408	.0747	. 6947	3052	31
30 31	.36650 .6677	.63350	2.7285 .7265	.39391 . 9425	2.5386 .5365	1.0748 .0749	.06958	.93042	36 29 28
32	6704	3296	7245	9458	.5343	.0750	6979	3020	28
33	. 6731	. 3269	.7225	. 9492	.5322	.0751	. 6990	. 3010	. 27
34 35	. 6758	. 3242	.7205	. 9525	.5300	.0753	. 7001	. 2999	26 25
35	.36785	.63214	2.7185	.39559	2.5278	1.0754	.07012	.92988 . 2978	25 24
36 37	. 6812 . 6839	3187	.7165 .7145	. 9593 . 9626	.5257 5236	.0755 .0756	7033	2967	23
38	. 6866	3133	7125	. 9660	.5236 .5214	.0758	7044	2956	22
39	6893	. 3106	.7105	. 9694	.5193	.0759 l	. 7054	. 2945	22 21
40	.36921	.63079	2.7085	.39727	2.5171	1.0760	.07065	.92935	20
41	. 6948 . 6975	3052	.7065 .7045	. 9761 . 9795	.5150 .5129	.0761 .0763	7076 7087	. 2924 . 2913	19
42 43	7002	2998	.7026	9828	.5128	.0764	7097	2902	18 17
44	7029	. 2971	.7006	9862	.5086	.0765	. 7108	. 2892	16
45	.37056	.62944	2.6986	.39896	2.5065	1.0766	.07119	.92881	15
46	. 7083	. 2917	.6967	. 9930	.5044	.0768	. 7130	. 2870 . 2859	14
47 48	. 7110 . 7137	. 2890 . 2863	.6947 .6927	. 9963	.5023 .5002	.0769 .0770	. 7141 . 7151	2848	13 12
49	7164	2836	.6908	.40031	.4981	.0771	7162	2838	iĩ
50	37191	.62809	2.6888	.40065	2.4960	1.0773	.07173	.92827	10
51	. 7218	. 2782	.6869	. 0098	.4939	.0774	. 7184	. 2816	9
52	7245	. 2755	.6849	. 0132	.4918	.0775 .0776	. 7195	. 2805	8 7
53 54	, 7272 , 7299	2728 2701	.6830 .6810	. 0166	.4897 .4876	.0778	. 7205 . 7216	. 2794	6
55	37326	.62674	2.6791	.40233	2.4855	1.0779	.07227	.92773	6 5
56 57	7353	. 2647	.6772	. 0267	.4834	.0780	. 7238	. 2762	4
57	. 7380	. 2620	.6752	. 0301	.4813	.0781	. 7249	. 2751	3
58	. 7407	2593	.6733	. 0335	.4792	.0783	. 7260 . 7271	2740	3 2 1
59 60	. 7434 . 7461	. 2566	.6714	. 0369	.4772 .4751	.0784 .0785	7271	. 2729 . 2718	Q
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М.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	V rs. cos.	Sine.	M.

220	,	N-	tural Tr	icono	etalcal l	Paraett		41	57°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
									-
0	.27461	.62539	2.6695	.40403	2.4751	1.0785	.07282	.92718	60
1	. 7488 . 7514	2512	.6675 .6656	. 0436 . 0470	.4730 .4709	.0787 .0788	. 7292	. 2707 . 2696	59 58
2 3 4 5	7541	2458	.6637	. 0504	.4689	.0789	. 7314	2686	57
4	7568	2431	.6618	. 0538	4668	.0790	7325	2675	56
5	.37595	.62404	2.6599	.40572	2.4647	1.0792	.07336	.92664	55
6	. 7622	. 2377	.6580	. 0606	.4627	.0793	. 7347	. 2653	55 54
6 7	. 7649	. 2351	.6561	. 0640	.4606	.0794	. 7358	. 2642	53 52
8	• 7676	2324	.6542	. 0673	.4586	.0795	. 7369	. 2631	52
9	. 7703 .37730	. 2297 .62270	.6523 2.6504	. 0707	.4565	.0797	. 7380	. 2620 .92609	51
10	. 7757	. 2243	.6485	.40741 . 0775	2.4545 .4525	1.0798 .0799	. 7402	. 2598	50 49
11 12	7784	2216	.6466	. 0809	.4504	.0801	7413	2587	48
13	7811	2189	.6447	. 0843	.4484	.0802	7424	. 2576	47
14	. 7838	. 2162	.6428	. 0877	.4463	.0803	. 7435	. 2565	46
14 15	.37865	.62135	2.6410	.40911	2.4443	1.0804	.07446	.92554	45
16	. 7892	. 2108	.6391	. 0945	.4423	.0806	. 7457	. 2543	44
17	. 7919	. 2081	.6372	. 0979	.4403	.0807	. 7468	. 2532	43
. 18 19	. 7946 . 7972	2054	.6353	. 1013 . 1047	.4382	.0808	. 7479 . 7490	. 2521 . 2510	42 41
19	.37999	.62000	.6335 2.6316	.41081	.4362 2.4342	.0810 1.0811	.07501	.92499	40
20 21 22 23	. 8026	. 1974	.6297	. 1115	.4322	.0812	. 7512	. 2488	39
22	8053	1947	.6279	. 1149	.4302	.0813	7523	. 2477	38
23	. 8080	. 1920	.6260	. 1183	.4282	.0815	. 7534	. 2466	38 37
24	. 8107	. 1893	.6242	. 1217	.4262	.0816	. 7545	. 2455	136
25	.38134	.61866	2.6223	.41251	2.4242	1.0817	.07556	.92443	35
26	. 8161	. 1839	.6205	. 1285	.4222	.0819	. 7567	2432	34
25 26 27 28 29 30 31	. 8188 . 8214	. 1812 . 1785	.6186	. 1319	.4202	.0820	. 7579	. 2421	34 33 32
28	8214	1758	.6168 .6150	. 1353 . 1387	.4182 .4162	.0821	. 7590 . 7601	. 2399	32
ซึก	.38268	.61732	2.6131	.41421	2.4142	1.0824	.07612	.92388	31 30 29 28
31	8295	. 1705	.6113	. 1455	.4122	.0825	. 7623	. 2377	29
32 33	. 8322	. 1678	.6095	. 1489	.4102	.0826	. 7634	. 2366	28
33	. 8349	. 1651	.6076	. 1524	.4083	.0828	. 7645	2354	27 26 25
34	. 8376	. 1624	.6058	. 1558	.4063	.0829	. 7657	. 2343	26
35	.38403	.61597	2.6040	.41592	2.4043	1.0830	.07668	.92332 . 2321	24
36 37	. 8429 . 8456	. 1570 . 1544	.6022 .6003	. 1626 . 1660	.4023 .4004	.0832	. 7679 . 7690	2310	99
38	8483	1517	.5985	. 1694	.3984	.0834	7701	2299	23 22 21
3 9	. 8510	1490	.5967	1728	.3964	.0836	7712	2287	21
40	.38537	.61463	2.5949	.41762	2.3945	1.0837	.07724	.92276	20
41	8564	. 1436	.5931	. 1797	.3925	.0838	. 7735	. 2265	19
42	. 8591	. 1409	.5913	. 1831	.3906	.0840	. 7746	. 2254	18
43	. 8617	. 1382	.5895	. 1865	.3886	.0841	. 7757	. 2242	17
44 45	.8644	. 1356	.5877 2.5859	. 1899	.3867 2.3847	.0842 1.0844	. 7769 .07780	. 2231	16 15
46	0000	. 1302	.5841	.41933 . 1968	.3828	.0845	. 7791	.92220	14
47	8698	. 1275	.5823	. 2002	.3808	.0846	7802	2197	13
48	8751	1248	.5805	2036	.3789	.0847	. 7814	. 2186	13 12
49	. 8778	. 1222	.5787	2070	.3770	.0849	. 7825	. 2175	11
50	.38805	.61195	2.5770	.42105	2.3750	1.0850	.07836	92164	10
51	. 8832	. 1168	.5752	. 2139	.3731	.0851	1.7847	. 2152	9
52	. 8859	. 1141	.5734	. 2173	.3712	.0853	. 7859	. 2141	8
53	. 8886	. 1114	.5716	. 2207	.3692	.0854	. 7870 . 7881	. 2130 . 2118	6
54 55	. 8912	. 1088	.5699 2.5681	. 2242 .42276	.3673 2.3654	.0855 1.0857	.07893	.92107	5
56	. 8966	. 1034	.5663	. 2310	.3635	.0858	. 7904	. 2096	4
56 57	. 8993	1007	.5646	2344	3616	.0859	7915	2084	3
58	9019	. 0980	.5628	. 2379	.3597	.0861	. 7927	. 2073	3 2 1
59	. 9046	. 0954	.5610	. 2413	.3577	.0862	. 7938	. 2062	
60	. 9073	. 0927	.5593	. 2447	.3558	.0864	. 7949	. 2050	0

M. Cosine. Vrs. sin. Secant. Cotang. Tang. Cosec'nt Vrs. cos.

23	•	Na	tural Tr	igonom	etrical l	Punction	ns.	1.	56°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.39073	.60927	2.5593	.42447	2.3558	1.0864	.07949	.92050	60
0 1 2	9100	. 0900	.5575	. 2482	.3539	.0865	. 7961	. 2039	59 58 57
2	>9126	. 0873	.5558	. 2516 . 2550	.3520	.0866	7972 7984	. 2028	57
3	. 9153 . 9180	. 0846	.5540	2585	.3501 .3482	.0868	7995	2005	56
- 5	.39207	.60793	2.5506	.42619	2.3463	1.0870	.08006	.91993	56 55
6	9234	. 0766	.5488	. 2654	.3445	.0872	. 8018	. 1982	1.54
7	9260	. 0739	.5471	. 2688	.3426	.0873	. 8029	. 1971	53 52
8	. 9287	. 0713	.5453	. 2722	.3407	.0874	. 8041	. 1959	52
	. 9314	. 0686	.5436	. 2757	.3388	.0876	. 8052	. 1948	51
10 11	.39341	.60659	2.5419	.42791	2.3369 .3350	1.0877 .0878	.08063	.91936 . 1925	50 49
12	. 9394	. 0632	.5402 .5384	. 2860	.3332	.0880	8086	. 1913	48
13	. 9421	. 0579	.5367	2894	.3313	.0881	8098	1902	47
14	9448	. 0552	.5350	. 2929	.3294	.0882	. 8109	. 1891	46
15	.39474	.60526	2.5333	.42963	2.3276	1.0884	.08121	.91879	45
16	. 9501	. 0499	.5316	. 2998	.3257	.0885	. 8132	. 1868	44
17	. 9528	. 0472	.5299	. 3032	.3238	.0886	8144	. 1856	43
18	. 9554	. 0445	.5281	. 3067	.3220	.0888	. 8155	. 1845	42
19 20	. 9581 .39608	.60392	.5264 2.5247	. 3101 .43136	.3201 2.3183	.0889 1.0891	. 8167 .08178	. 1833 .91822	41 40
21	. 9635	. 0365	.5230	. 3170	.3164	.0892	. 8190	. 1810	39
22	9661	. 0339	.5213	3205	.3145	.0893	8201	. 1798	38
23	9688	. 0312	.5196	3239	.3127	.0895	8213	. 1787	37
24	. 9715	. 0285	.5179	. 3274	.3109	.0896	. 8224	. 1775	36
25 26	.39741	.60258	2.5163	.43308	2.3090	1.0897	.08236	.91764	36 35 34 33 32
26	9768	. 0232	.5146	. 3343	.3072	.0899	. 8248	. 1752	34
27 28	. 9795	. 0205	.5129	. 3377	.3053	.0900	. 8259	. 1741 . 1729	33
29	. 9821 . 9848	. 0178	.5112 .5095	. 3412	.3035	.0902	. 8271 . 8282	. 1718	91
30	.39875	.60125	2.5078	.43481	2.2998	1.0904	.08294	.91706	31 30 29 28 27 26 25 24
31	9901	. 0098	.5062	. 3516	.2980	.0906	. 8306	. 1694	29
32	. 9928	. 0072	.5045	. 3550	.2962	.0907	. 8317	. 1683	28
33	9955	. 0045	.5028	. 3585	.2944	.0908	. 8329	. 1671	27
84	. 9981	. 0018	.5011	. 3620	.2925	.0910	8340	. 1659	26
35 36	.40008	.59992	2.4995	. 3689	2.2907	1.0911 .0913	.08352	.91648 . 1636	25
37	. 0035	• 9965 • 9938	.4978 .4961	. 3723	.2871	.0913	. 8375	. 1625	24
38	. 0088	9912	.4945	. 3758	.2853	.0915	8387	. 1613	23 22 21
39	. 0115	9885	4928	. 3793	.2835	.0917	8399	. 1601	21
40	.40141	.59858	2.4912	.43827	2.2817	1.0918	.08410	.91590	20 19
41	. 0168	. 9832	.4895	. 3862	.2799	.0920	. 8422	. 1578	19
42	. 0195	. 9805	.4879	. 3897	.2781	.0921	. 8434	. 1566	18
43	. 0221	9778	.4862	. 3932	.2763	.0922	8445	. 1554	17
44 45	. 0248	. 9752 .59725	.4846 2.4829	. 3966 .44001	.2745 2.2727	.0924 1.0925	. 8457	. 1543 .91531	16 15
46	. 0301	. 9699	.4813	. 4036	2.2729	.0927	. 8480	. 1519	14
47	. 0328	. 9672	.4797	. 4070	.2691	.0928	. 8492	. 1508	13
48	. 0354	. 9645	.4780	. 4105	.2673	.0929	. 8504	. 1496	12
49	. 0381	. 9619	.4764	. 4140	.2655	.0931	. 8516	. 1484	11
50	.40408	.59592	2.4748	.44175	2.2637	1.0932	.08527	.91472	10
51	. 0434	. 9566	.4731	. 4209	.2619	.0934	. 8539	. 1461	9
52 53	. 0461	. 9539	.4715	. 4244	.2602	.0935	8551	. 1449	8 7
54	. 0487	. 9512	.4699 .4683	. 4279 . 4314	.2584	.0936	. 8563 . 8575	. 1437 . 1425	6
55	.40541	.59459	2.4666	. 4314	2.2548	1.0939	.08586	.91414	5
56	. 0567	. 9433	.4650	. 4383	.2531	.0941	. 8598	. 1402	4
56 57	. 0594	. 9406	.4634	. 4418	.2513	.0942	8610	. 1390	3
58	. 0620	. 9379	.4618	. 4453	.2495	.0943	. 8622	. 1378	2
59	. 0647	. 9353	.4602	. 4488	.2478	.0945	. 8634	. 1366	1
60	. 0674	. 9326	.4586	. 4523	.2460	.0946	. 8645	. 1354	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

113° 24 66

24°)	Na	tural Tr	igonom	gonometrical Punctions.				
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.40674	.59326	2.4586	.44523	2.2460	1.0946	.08645	.91354	60
1	. 0700	9300	.4570	4558	.2443	.0948	. 8657	. 1343	59
3	. 0727 . 0753	9273	.4554 .4538	. 4593 . 4627	.2425 .2408	.0949 .0951	. 8669 . 8681	. 1331	58 57
4	. 0780	9220	.4522	4662	.2390	.0952	. 8693	1307	56
5	.40806	.59193	2.4506	.44697	2.2373	1.0953	.08705	.91295	55
6	. 0833	. 9167	.4490	. 4732	.2355	.0955	. 8716	. 1283	54
	. 0860	9140	.4474	. 4767	.2338	.0956	8728	. 1271	53
8 9	. 0886	9114	.4458 .4442	. 4802 . 4837	.2320 .2303	.0958 .0959	. 8740 . 8752	. 1260 . 1248	52 51
10	.40939	.59061	2.4426	.44872	2.2286	1.0961	.08764	.91236	50
ii	. 0966	9034	.4411	. 4907	.2268	.0962	. 8776	1224	49
12	. 0992	. 9008	.4395	. 4942	.2251	.0963	. 8788	. 1212	48
13	. 1019	. 8981	.4379	. 4977	.2234	.0965	. 8800	. 1200	47
14	. 1045	8955	.4363 2.4347	. 5012	.2216 2.2199	.0966 1.0968	. 8812	. 1188	46 45
15 16	.41072 . 1098	. 58928	.4332	. 5082	.2182	.0969	. 8836	. 1164	44
17	. 1125	8875	.4316	5117	.2165	.0971	. 8848	1152	43
18	. 1151	. 8848	.4300	. 5152	.2147	.0972	. 8860	. 1140	42
19	. 1178	. 8822	.4285	. 5187	.2130	.0973	. 8872	. 1128	41
20	.41204	.58795	2.4269	.45222	2.2113	1.0975	.08884	.91116	40 39
21	. 1231 . 1257	. 8769 . 8742	.4254 .4238	. 5257 . 5292	.2096 .2079	.0976	. 8896	1104	38
20 21 22 23	. 1284	8716	.4222	5327	.2062	.0979	8920	1080	38 37
24	. 1310	. 8689	.4207	. 5362	.2045	.0981	. 8932	. 1068	36
25	.41337	.58663	2.4191	.45397	2.2028	1.0982	.08944	.91056	35
26	. 1363	. 8636	.4176	. 5432	.2011	.0984	. 8956	1044	34
25 26 27 28	. 1390 . 1416	. 8610 . 8584	.4160 .4145	. 5467	.1994	.0985	. 8968	1032	36 35 34 33 32 31
29	1443	8557	.4130	. 5537	.1960	.0988	. 8992	1008	31
30	.41469	.58531	2.4114	.45573	2.1943	1.0989	.09004	.90996	30 29 28 27 26 25 24
31	. 1496	. 8504	.4099	. 5608	.1926	.0991	. 9016	. 0984	29
32	. 1522	. 8478	.4083	. 5643	.1909	.0992	. 9028	. 0972	28
83 84	. 1549 . 1575	. 8451 . 8425	.4068 .4053	. 5678 . 5713	1875	.0995	9052	. 0948	26
85	41602	.58398	2.4037	.45748	2.1859	1.0997	.09064	.90936	25
36	. 1628	. 8372	.4022	. 5783	.1842	.0998	. 9076	. 0924	24
37	. 1654	. 8345	.4007	. 5819	.1825	.1000	9088	. 0911	23 22 21
38	. 1681	. 8319	.3992	. 5854 . 5889	.1808 .1792	.1001	. 9101 . 9113	. 0899	22
39 40	. 1707	. 8292 .58266	.3976 2.3961	.45924	2.1775	1.1003	.09125	.90875	20
41	. 1760	. 8240	.3946	. 5960	.1758	.1005	. 9137	. 0863	19
42	. 1787	. 8213	.3931	. 5995	.1741	.1007	. 9149	. 0851	18
43	. 1813	. 8187	.3916	. 6030	.1725	.1008	. 9161	. 0839	17
44	. 1839	. 8160	.3901	. 6065	.1708 2.1692	.1010 1.1011	. 9173	. 0826	16 15
45 46	. 1892	.58134	2.3886 .3871	.46101 .6136	.1675	.1013	. 9198	. 0802	14
47	1919	8081	.3856	6171	.1658	.1014	9210	. 0790	13
48	. 1945	. 8055	.3841	. 6206	.1642	.1016	9222	. 0778	12
49	. 1972	. 8028	.3826	. 6242	.1625	.1017	. 9234	. 0765	11
50	.41998	.58002	2.3811	.46277	2.1609 .1592	1.1019	.09247	.90753	10
51 52	. 2024	. 7975 . 7949	.3796 .3781	6312	.1576	.1020 .1022	9259	. 0741	8
53	2077	7923	.3766	6383	.1559	.1023	9283	0717	8 7
54	. 2103	. 7896	.3751	. 6418	.1543	.1025	9296	. 0704	6
55	.42130	.57870	2.3736	.46454	2.1527	1.1026	.09308	.90692	5
56	. 2156	. 7844	.3721	. 6489	.1510	.1028	. 9320	. 0680	4 3 2 1
57 58	2183	7817	.3706 .3691	. 6524	.1494 .1478	.1029	9332	. 0668	1 3
59	2235	7764	.3677	6595	.1461	.1032	9357	. 0643	۱ĩ
60	. 2262	. 7738	.3662	. 6631	.1445	,1034	. 9369	. 0631	ō
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

1140

250	,	Na	tural Ti	Trigonometrical Punctions. 1					
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.42262	.57738	2.3662	.46631	2.1445	1.1034	.09369	.90631	60
1	. 2288	. 7712	.3647	. 6666	.1429	.1035	. 9381	. 1618	59
2 3 4 5 6 7	. 2314	. 7685	.3632	. 6702	.1412	.1037	. 9394	. 0606	58 57 56 55 54 53 52 51
3	. 2341	. 7659	.3618	. 6737	.1396	.1038	. 9406	. 0594	57
4	. 2367	. 7633	.3603	. 6772	.1380	.1040	. 9418	. 0581	56
6	. 42394	.57606 .7580	2.3588 .3574	.46808 . 6843	2.1364 .1348	1.1041 .1043	.09431	. 0557	54
7	. 2446	7554	.3559	6879	.1331	1044	9455	0544	53
Ŕ	2473	7527	.3544	6914	.1315	.1046	9468	0532	52
8	. 2499	. 7501	.3530	6950	.1299	.1047	. 9480	. 0520	51
10	.42525	.57475	2.3515	.46985	2.1283	1.1049	.09492	.90507	50
ii	. 2552	. 7448	.3501	. 7021	.1267	.1050	9505	. 0495	49
12	2578	. 7422	.3486	. 7056	.1251	.1052	. 9517	. 0483	48
13	. 2604	. 7396	.3472	. 7092	.1235	.1053	. 9530	. 0470	47
14	. 2630	. 7369	.3457	. 7127	.1219	.1055	. 9542	. 0458	46
15	.42657 . 2683	. 57343	2.3443 .3428	.47163 . 7199	2.1203	1.1056 .1058	.09554	. 0433	45 44
16 17	2709	7290	.3414	7234	.1187	.1059	9579	. 0421	43
18	2736	7264	.3399	7270	.1155	.1061	9592	. 0408	42
19	2762	7238	.3385	7305	.1139	.1062	9604	. 0396	41
20	.42788	.57212	2,3371	.47341	2.1123	1.1064	.09617	.90383	40
21	. 2815	. 7185	.3356	. 7376	.1107	.1065	. 9629	. 0371	39
22	. 2841	. 7159	.3342	. 7412	.1092	.1067	. 9641	. 0358	38
23	. 2867	. 7133	.3328	. 7448	.1076	.1068	. 9654	. 0346	37
24	. 2893	. 7106	.3313	. 7483	.1060	.1070	. 9666	. 0333	36
25	.42920	.57080	2.3299	.47519	2.1044	1.1072	.09679	.90321	35
20	2946	7054	.3285	7555	.1028	.1073	9691	0308	39 38 37 36 35 34 33 32 31 30 29 28 27 26 25 24 23 22 21 20 19
2/	. 2972	. 7028 . 7001	.3271	. 7590 . 7626	.1013	.1075 .1076	9704	. 0296	33
20	3025	6975	.3242	7662	.0997	.1078	9710	0203	91
18 19 20 21 22 23 24 25 26 27 28 29 81	.43051	.56949	2.3228	47697	2.0965	1.1079	.09741	.90258	1 80
81	. 3077	6923	.3214	7733	.0950	.1081	. 9754	. 0246	29
32 83 34	3104	. 6896	.3200	7769	.0934	.1082	. 9766	. 0233	28
83	. 3130	. 6870	.3186	. 7805	.0918	.1084	9779	. 0221	27
34	. 3156	. 6844	.3172	. 7840	.0903	.1085	. 9792	. 0208	26
35 86	.43182	.56818	2.3158	.47876	2.0887	1.1087	.09804	.90196	25
86	. 3208	. 6791	.3143	. 7912	.0872	.1088	. 9817	. 0183	24
37 38	. 3235	. 6765	.3129	. 7948	.0856	.1090	. 9829	. 0171	23
39	. 3287	6713	.3115 .3101	. 7983 . 8019	.0840	.1092 .1093	9842	0158	22
40	.43313	.56686	2.3087	.48055	2.0809	1.1095	.09867	.90133	20
41	. 3340	. 6660	.3073	. 8091	.0794	.1096	9880	. 0120	119
42	. 3366	. 6634	.3059	. 8127	.0778	.1098	9892	. 0108	18
43	. 3392	. 6608	.3046	. 8162	.0763	.1099	. 9905	. 0095	18 17
44	. 3418	. 6582	.3032	. 8198	.0747	.1101	. 9917	. 0082	16
45	.43444	.56555	2.3018	.48234	2.0732	1.1102	.09930	.90070	15
46	. 3471	. 6529	.3004	. 8270	.0717	.1104	9943	. 0057	14
47 48	. 3497	. 6503	.2990	. 8306	.0701	.1106	. 9955	. 0044	13
49	. 3523 . 3549	. 6477	.2976	. 8342 . 8378	.0686	.1107	. 9968	. 0032	12
50	.43575	.56424	2.2949	.48414	.0671 2.0655	.1109 1.1110	. 9981	. 0019	11 10
51	3602	6398	.2935	. 8449	.0640	.1112	.10006	.89994	9
52	3628	6372	.2921	8485	.0625	.1113	. 0019	. 9981	
53	3654	. 6346	.2907	. 8521	.0609	.1115	0031	. 9968	8 7
54	. 3680	6320	.2894	. 8557	.0594	.1116	. 0044	9956	6
55	.43706	.56294	2.2880	.48593	2.0579	1.1118	.10057	.89943	5
56	. 3732	. 6267	.2866	. 8629	.0564	.1120	. 0070	. 9930	4
57	. 3759	. 6241	.2853	. 8665	.0548	.1121	. 0082	. 9918	3
58	. 3785	. 6215	.2839	8701	.0533	.1123	. 0095	. 9905	2
59 60	. 3811	. 6189	.2825	8737	.0518	.1124	. 0108	. 9892	1
	. 3837	. 6163	.2812	8773	.0503	.1126	. 0121	. 9879	0
M.	Cosine.	vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

26 °	•	Na	tural Tr	igonom	etrical l	153°			
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.43837	.56163	2.2812	.48773	2.0503	1.1126	.10121	.89879	60
1	. 3863	. 6137	.2798	. 8809	.0488	.1127	. 0133	. 9867	59
2	. 3889	. 6111	.2784	. 8845	.0473	.1129	. 0146	. 9854	58 57
4	. 3915 . 3942	. 6084 . 6058	.2771	. 8881 . 8917	.0458	.1131	. 0159	. 9841	57
5	.43968	.56032	2.2744	. 48953	.0443 2.0427	.1132 1.1134	. 0172	. 9828 .89815	56
6	. 3994	. 6006	.2730	8989	.0412	.1135	. 0197	9803	55 54
7	. 4020	. 5980	.2717	. 9025	.0397	.1137	0210	9790	53
6 7 8 9	. 4046	. 5954	.2703	. 9062	.0382	.1139	. 0223	. 9777	53 52 51
	. 4072	. 5928	.2690	. 9098	.0367	.1140	. 0236	. 9764	51
10 11	.44098	.55902	2.2676	.49134	2.0352	1.1142	.10248	.89751	50
12	. 4124 . 4150	. 5875 . 5849	.2663 .2650	9170	.0338	.1143	. 0261	9739	49
13	4177	. 5823	.2636	. 9206 . 9242	.0323	.1145 .1147	. 0274	9726	48 47
14	4203	5797	.2623	9278	.0293	.1148	. 0300	9700	46
15	.44229	.55771	2.2610	.49314	2.0278	1.1150	.10313	.89687	45
16	. 4255	. 5745	.2596	. 9351	.0263	.1151	. 0326	9674	44
17	. 4281	. 5719	.2583	. 9387	.0248	.1153	. 0338	9661	43
18	. 4307	. 5693	.2570	. 9423	.0233	.1155	0351	. 9649	42
19 20	. 4333 .44359	. 5667 .55641	.2556 2.2543	. 9459	.0219	.1156	. 0364	. 9636	41
20	. 4385	. 5615	.2530	.49495 . 9532	2.0204	1.1158 .1159	.10377	.89623 . 9610	40
21 22	. 4411	5589	.2517	. 9568	.0174	.1161	. 0403	9597	39
23	. 4437	5562	.2503	9604	.0159	.1163	. 0416	9584	38 37
24 25	. 4463	. 5536	.2490	. 9640	.0145	.1164	. 0429	. 9571	36
25	.44489	.55510	2.2477	.49677	2.0130	1.1166	.10442	.89558	36 35
26	 4516 	. 5484	.2464	. 9713	.0115	.1167	. 0455	. 9545	34
27 28 29	. 4542	. 5458	.2451	. 9749	.0101	.1169	. 0468	. 9532	33 32 31
28	. 4568 . 4594	. 5432 . 5406	.2438 .2425	. 9785 . 9822	.0086	.1171	. 0481	. 9519	32
30	.44620	.55380	2.2411	. 49858	2.0058	.1172 1.1174	. 0493	. 9506 .89493	21
31	. 4646	. 5354	.2398	. 9894	.0042	.1176	. 0519	. 9480	30 29
32	. 4672	5328	.2385	. 9931	.0028	.1177	. 0532	9467	28
33	. 4698	. 5302	.2372	. 9967	.0013	.1179	. 0545	. 9454	28 27
34	. 4724	. 5276	.2359	.50003	1.9998	.1180	. 0558	. 9441	26 25
35	.44750	.55250	2.2346	.50040	1.9984	1.1182	.10571	.89428	25
36 37	. 4776	. 5224	.2333	. 0076	.9969	.1184	. 0584	. 9415	24
38	. 4802 . 4828	. 5198 . 5172	.2320	. 0113	.9955	.1185	. 0598	. 9402	23 22 21
39	. 4854	. 5146	.2294	. 0145	.9940	.1187 .1189	. 0624	. 9376	22
40	.44880	.55120	2.2282	50222	1.9912	1.1190	.10637	.89363	20
41	. 4906	. 5094	.2269	. 0258	.9897	.1192	. 0650	9350	19
42	. 4932	. 5068	.2256	. 0295	.9883	.1193	. 0663	. 9337	18
43	. 4958	. 5042	.2243	. 0331	.9868	.1195	. 0676	. 9324	17
44	. 4984	. 5016	.2230	. 0368	.9854	.1197	. 0689	. 9311	16
45 46	.45010 . 5036	.54990 . 4964	2.2217 .2204	.50404 . 0441	1.9840 .9825	1.1198	.10702	.89298 . 9285	15
47	. 5062	4938	.2192	. 0477	.9823	.1200 .1202	. 0715	9272	14 13
48	5088	4912	.2179	. 0514	.9797	.1202	0741	9258	12
49	. 5114	4886	.2166	. 0550	.9782	.1205	0754	9245	iī
50	.45140	.54860	2.2153	.50587	1.9768	1.1207	.10768	.89232	10
51	. 5166	. 4834	.2141	. 0623	.9754	.1208	. 0781	. 9219	9
52	. 5191	4808	.2128	. 0660	.9739	.1210	. 0794	. 9206	8
53	. 5217	. 4782	.2115	. 0696	.9725	.1212	. 0807	. 9193	7
54 55	. 5243 .45269	. 4756 .54730	.2103 2,2090	. 0733	.9711 1.9697	.1213 1.1215	. 0820	.89166	9 8 7 6 5 4 3 2
56	. 5295	. 4705	.2077	. 0806	.9683	.1215	. 0846	. 9153	1
57	. 5321	4679	.2065	. 0843	.9668	.1218	. 0860	9140	3
58	5347	. 4653	.2052	. 0879	.9654	.1220	0873	9127	Ž
59	. 5373	. 4627	.2039	. 0916	.9640	.1222	. 0886	. 9114	
60	. 5399	. 4601	.2027	. 0952	.9626	.1223	. 0899	. 9101	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

27 °	Natural Trigonometrical Functions. 152°								
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.45399	.54601	2.2027	.50952	1.9626	1.1223	.10899	.89101	60
i	. 5425	. 4575	.2014	. 0989	.9612	.1225	. 0912	. 9087	59
2	. 5451	. 4549 . 4523	.2002 .1989	. 1026	.9598	.1226 .1228	. 0926	. 9074	58
8	. 5477 . 5503	. 4497	.1977	. 1062	.9584 .9570	.1220	. 0939	. 9061 . 9048	57 56
5 1	.45528	.54471	2.1964	.51136	1.9556	1.1231	.10965	.89034	55
6	. 5554	. 4445	.1952	. 1172	.9542	.1233	. 0979	9021	55 54 53
7 8 9	5580	. 4420	.1939	. 1209	.9528	.1235	. 0992	. 9008	53
8	· 5606	. 4394	.1927	. 1246	.9514	.1237	1005	8995	52 51
10	. 5632 .45658	. 4368	.1914 2.1902	. 1283 .51319	.9500 1.9486	.1238 1.1240	.1018	. 8981 .88968	50
ii	5684	. 4316	.1889	. 1356	.9472	.1242	. 1045	. 8955	49
12	. 5710	. 4290	.1877	. 1393	.9458	.1243	. 1058	. 8942	48
13	• 5736	. 4264	.1865	. 1430	.9444	.1245	. 1072	. 8928	47
14 !	. 5761	. 4238	.1852	1466	.9430	.1247	. 1085	. 8915	46
15 16	.45787 .5813	.54213	2.1840 .1828	.51503	1.9416	1.1248	.11098	.88902	45
17	5839	. 4187 . 4161	.1815	. 1540 . 1577	.9402 .9388	.1250 .1252	. 1112	. 8888 . 8875	44 43
18	. 5865	4135	.1803	1614	.9375	.1253	1138	. 8862	42
18 19	. 5891	. 4109	.1791	. 1651	.9361	.1255	1152	8848	41
20	.45917	.54083	2.1778	.51687	1.9347	1.1257	.11165	.88835	40
21	. 5942	. 4057	.1766	. 1724	.9333	.1258	. 1178	. 8822	39 38 37
22	. 5968	. 4032	.1754	. 1761	.9319	.1260	. 1192	. 8808	38
23	. 5994 . 6020	. 4006	.1742 .1730	. 1798 . 1835	.9306 .9292	.1262 .1264	. 1205 . 1218	. 8795 . 8781	37
95	.46046	.53954	2.1717	.51872	1.9278	1.1265	.11232	.88768	36 35
26	6072	. 3928	.1705	. 1909	.9264	.1267	. 1245	8755	34
27	6097	. 3902	.1693	. 1946	.9251	.1269	1259	. 8741	33
28	. 6123	. 3877	.1681	. 1983	.9237	.1270	. 1272	. 8728	32
29	. 6149	3851	.1669	. 2020	.9223	.1272	. 1285	8714	31
20 21 22 23 24 25 26 27 28 29 80 31	.46175 .6201	.53825	2.1657	.52057	1.9210	1.1274	.11299	.88701	30 29 28 27
91	. 6226	. 3799 . 3773	.1645 .1633	. 2094	.9196 .9182	.1275 .1277	1312	. 8688 . 8674	239
32 33	6252	3748	.1620	. 2168	.9169	.1279	1339	. 8661	27
34	6278	3722	.1608	. 2205	.9155	.1281	1353	. 8647	26
35 36 37	.46304	.53696	2.1596	.52242	1.9142	1.1282	.11366	.88634	26 25
36	. 6330	. 3670	.1584	2279	.9128	.1284	. 1380	. 8620	24 23 22 21 20
37 38	. 6355 . 6381	. 3645	.1572	. 2316	.9115	.1286	. 1393	. 8607	23
39	6407	. 3619	.1560 .1548	. 2353	.9101 .9088	.1287 .1289	. 1407	. 8593 . 8580	22
40	.46433	.53567	2.1536	.52427	1.9074	1.1291	.11434	.88566	20
41	. 6458	. 3541	.1525	. 2464	.9061	.1293	. 1447	8553	19
42	. 6484	. 3516	.1513	. 2501	.9047	.1294	. 1461	. 8539	18
43	. 6510	. 3490	.1501	2538	.9034	.1296	. 1474	. 8526	17
44	6536	3464	.1489	. 2575	.9020	.1298	. 1488	. 8512	16
45 46	.46561 .6587	.53438	2.1477 .1465	.52612 . 2650	1.9007 .8993	1.1299 .1301	. 1515	.88499 . 8485	15 14
47	6613	3387	.1453	2687	.8980	.1301	. 1528	8472	13
48	. 6639	. 3361	.1441	2724	.8967	.1305	. 1542	. 8458	12
49	. 6664	. 3336	.1430	. 2761	.8953	.1306	. 1555	. 8444	11
50	.46690	.53310	2.1418	.52798	1.8940	1.1308	.11569	.88431	10
51	. 6716	. 3284	.1406	. 2836	.8927	.1310	. 1583	. 8417	ነ 9
52 53	. 6741 . 6767	. 3258	.1394	. 2873 . 2910	.8913 .8900	.1312 .1313	. 1596 . 1610	. 8404 . 8390	8 7
54	. 6793	. 3233	.1382	. 2910	.8887	.1315	. 1623	. 8376	1 6
55	.46819	.53181	2.1359	.52984	1.8873	1.1317	.11637	.88363	6 5
56 57	. 6844	. 3156	.1347	. 3022	.8860	.1319	. 1651	. 8349	4
57	. 6870	. 3130	.1335	. 3059	.8847	.1320	. 1664	. 8336	3 2 1
58	. 6896	. 3104	.1324	. 3096	.8834	.1322	. 1678	. 8322	2
59 60	. 6921	. 3078	.1312	. 3134	.8820 .8807	.1324	. 1691	8308	0
_	. 054/	. 3003	.1300	. 3171	.0007	.1326	. 1700	. 0230	<u> </u>
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec 'nt	Vrs. cos.	Sine.	M.

117° 62°

2 8°		Na	tural Tr	trical Functions.			1510		
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.46947	.53053	2.1300	.53171	1.8807	1.1326	.11705	.88295	60
1	. 6973 . 6998	. 3027	.1289	. 3208 . 3245	.8794 .8781	.1327 .1329	. 1719 . 1732	. 8281 . 8267	59 58
2 3 4 5 6	. 7024	2976	.1266	3283	.8768	.1331	1746	8254	57
4	. 7050	2950	.1254	. 3320	.8768 .8754	.1333	. 1760	. 8240	56
5	.47075	.52924	2.1242	.53358	1.8741	1.1334	.11774	.88226	55
6	. 7101	. 2899 . 2873	.1231 .1219	. 3395	.8728 .8715	.1336 .1338	. 1787 . 1801	. 8213 . 8199	54
7 8 9	. 7127 . 7152	. 2847	.1208	. 3470	.8702	.1340	. 1815	. 8185	5\$ 52
9	. 7178	2822	.1196	. 3507	.8689	.1341	. 1828	. 8171	51
10	.47204	.52796	2.1185	.53545	1.8676	1.1343	.11842	.88158	50
11	. 7229	2770	.1173	. 3582	.8663	.1345	. 1856	. 8144	49
12 13	. 7255 . 7281	2745	.1162 .1150	. 3619 . 3657	.8650	.1347 .1349	. 1870 . 1883	. 8130 . 8117	48
14	7306	2694	.1139	. 3694	.8637 .8624	1350	1897	8103	46
15 16	.47332	.52668	2.1127	.53732	1.8611	1.1352	.11911	*88089	45
16	. 7357	. 2642	.1116	. 3769	.8598	.1354	. 1925	8075	44
17 18	. 7383 . 7409	. 2617 . 2591	.1104	. 3807	.8585	.1356 .1357	. 1938 . 1952	. 8061 . 8048	43
19	. 7434	2565	.1093 .1082	. 3882	.8572 .8559	.1359	1966	8034	41
20	.47460	.52540	2.1070	.53919	1.8546	1.1361	.11980	.88020	40
21	. 7486	. 2514	.1059	. 3957	.8533	.1363	. 1994	. 8006	39
20 21 22 23	. 7511	. 2489	.1048	. 3995	.8520	.1365	. 2007	. 7992 . 7979	38 37
23	. 7537 . 7562	. 2463 . 2437	.1036 .1025	. 4032	.8507 .8495	.1366	. 2021 . 2035	7979	36
25	.47588	.52412	2.1014	.54107	1.8482	.1368 1.1370	.12049	.87951	35
26	. 7613	. 2386	.1002	. 4145	.8469	.1372	. 2063	. 7937	34
25 26 27 28	. 7639	. 2361	.0991	. 4183	.8456	.1373	. 2077	. 7923	33 32
28 29	. 7665 . 7690	2335	.0980	. 4220 . 4258	.8443 .8430	.1375 .1377	. 2090 . 2104	. 7909 . 7895	31
80	.47716	.52284	2.0957	.54295	1.8418	1.1379	.12118	.87882	30
31	. 7741	. 2258	.0946	. 4333	.8405	.1381	. 2132	. 7868	29 28
32	. 7767	. 2233	.0935	. 4371	.8392	.1382	. 2146	. 7854	28
33	. 7792 . 7818	. 2207	.0924	. 4409 . 4446	.8379	.1384 .1386	. 2160 . 2174	. 7840 . 7826	27 26 25
34 35	. 7818	.52156	2.0901	.54484	1.8367 1.8354	1.1388	.12188	.87812	25
3 6	. 7869	2131	.0890	4522	.8341	.1390	. 2202	. 7798	24
87	. 7895	. 2105	.0879	. 4559	.8329	.1391	. 2216	. 7784	23 22 21 20
38	. 7920	2080	.0868	4597	.8316	.1393	. 2229	. 7770 . 7756	22
89 4 0	. 7946 .47971	. 2054	.0857 2.0846	. 4635 .54673	.8303 1.8291	.1395 1.1397	.12257	.87742	20
41	. 7997	2003	.0835	4711	.8278	.1399	. 2271	. 7728	119
42	. 8022	. 1978	.0824	. 4748	.8265	.1401	. 2285	. 7715	18 17
43	. 8048	1952	.0812	. 4786	.8253	.1402	. 2299	. 7701 . 7687	17 16
44 45	. 8073 .48099	. 1927 .51901	.0801 2.0790	. 4824	.8240 1.8227	.1404 1.1406	. 2313	.87673	15
46	8124	. 1876	.0779	. 4900	.8215	.1408	. 2341	. 7659	14
47	. 8150	. 1850	.0768	. 4937	.8202	.1410	. 2355	. 7645	113
48	, 8175	. 1825	.0757	. 4975	.8190	.1411	. 2369	. 7631	12 11 10
49 50	. 8201	. 1799	.0746 2.0735	. 5013	.8177 1.8165	.1413 1.1415	. 2383	. 7617 .87603	110
51	. 8252	. 1748	.0725	. 5089	.8152	.1417	. 2411	7588	9
52	. 8277	1723	.0714	. 5127	.8140	.1419	. 2425	. 7574	8
53	. 8303	. 1697	.0703	5165	.8127	.1421	2439	7560	9 8 7 6 5 4 3 2
54 55	. 8328 .48354	. 1672	.0692 2.0681	. 5203	.8115 1.8102	.1422 1.1424	. 2453	. 7546 .87532	þ
56	. 8379	.51646 . 1621	.0670	5279	.8090	.1424	. 12468	. 7518	4
57	. 8405	1595	.0659	5317	.8078	.1428	. 2496	. 7504	3
58	. 8430	. 1570	.0648	. 5355	.8065	.1430	. 2510	. 7490	2
59	. 8455	. 1544	.0637	. 5393	.8053	.1432	2524	. 7476 . 7462	0
60	. 8481	. 1519	.0627	. 5451	.8040	.1433	. 2000	. /402	
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

118° 61°

2 9°	Natural Trigonometrical Functions. 150°								
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.48481	.51519	2.0627	.55431	1.8040	1.1433	.12538	.87462	60
1	. 8506 . 8532	. 1493	.0616	. 5469 . 5507	.8028 .8016	.1435 .1437	. 2552 . 2566	. 7448 . 7434	59
3	. 8557	. 1443	.0594	. 5545	.8003	.1439	2580	. 7420	58 57
4	. 8583	. 1417	.0583	. 5583	.7991	.1441	2594	. 7405	156
5	.48608	.51392	2.0573	.55621	1.7979	1.1443	.12609	.87391	55
6	. 8633	. 1366	.0562	. 5659	.7966	.1445	. 2623	. 7377	54
4 5 6 7 8 9	. 8659 . 8684	. 1341	.0551	. 5697 . 5735	.7954 .7942	.1446 .1448	. 2637 . 2651	. 7363 . 7349	55 54 53 52
9	. 8710	1290	.0530	5774	.7930	.1450	2665	7335	51
10	.48735	.51265	2.0519	.55812	1.7917	1.1452	.12679	.87320	50
11	. 8760	. 1239 . 1214	.0508	. 5850	.7905	.1454	. 2694	. 7306	49
12	. 8786	. 1214	.0498	. 5888	.7893	.1456	2708	. 7292 . 7278	48
13 14	. 8811 . 8837	. 1189	.0487	. 5926 . 5964	.7881 .7868	.1458 .1459	. 2722 . 2736	7264	47 46
15	.48862	.51138	2.0466	.56003	1.7856	1.1461	.12750	.87250	45
16	. 8887	. 1112	.0455	. 6041	.7844	.1463	. 2765	. 7235	44
17	. 8913	. 1087	.0444	. 6079	.7832	.1465	. 2779	. 7221	43
18	. 8938	. 1062	.0434	. 6117	.7820	.1467	. 2793	. 7207	42
19	. 8964 .48989	. 1036	.0423 2.0413	. 6156 .56194	.7808 1.7795	.1469 1.1471	. 2807	. 7193 .87178	41 40
21	. 9014	. 0986	.0402	. 6232	.7783	.1473	. 2836	. 7164	39
22222425 2522222 252222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 25222 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 252 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 252 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 252 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 2522 252 2522 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252 252	. 9040	. 0960	.0392	6270	.7771	.1474	2850	. 7164 . 7150	38 37
23	. 9065	. 0935	.0381	. 6309	.7759	.1476	. 2864	. 7136	37
24	9090	. 0910	.0370	. 6347	.7747	.1478	. 2879	. 7121	36 35
20 96	.49116 . 9141	. 0859	2.0360	.56385 . 6424	1.7735 .7723	1.1480 .1482	.12893	.87107 . 7093	35
27	. 9166	. 0834	.0339	. 6462	.7711	.1484	2921	7078	34 33
28	. 9192	. 0808	.0329	6500	.7699	.1486	2936	7064	132
29	. 9217	. 0783	.0318	. 6539	.7687	.1488	. 2950	. 7050	31
30	.49242	.50758	2.0308	.56577	1.7675	1.1489	.12964	.87035	30 29 28 27
31 82	. 9268 . 9293	. 0732	.0297 .0287	. 6616 . 6654	.7663 .7651	.1491 .1493	. 2979	. 7021 . 7007	29
83	. 9318	. 0682	.0276	. 6692	.7639	.1495	3007	6992	27
84	. 9343	. 0656	.0266	6731	.7627	.1497	3022	. 6978	26
85	.49369	.50631	2.0256	.56769	1.7615	1.1499	.13036	.86964	26 25 24 23 22 21 20
36 37	. 9394	. 0606	.0245	. 6808	.7603	.1501	. 3050	. 6949	24
88	. 9419 . 9445	. 0580	.0235	. 6846 . 6885	.7591 .7579	.1503 .1505	. 3065	. 6935 . 6921	20
89	. 9470	. 0530	.0214	6923	.7567	.1507	. 3094	. 6906	21
40	.49495	.50505	2.0204	.56962	1.7555	1.1508	.13108	.86892	20
41	. 9521	. 0479	.0194	. 7000	.7544	.1510	. 3122	. 6877	19
42	. 9546	0454	.0183	. 7039	.7532	.1512	. 3137	. 6863	18
4 3 4 4	. 9571 . 9596	. 0429	.0173 .0163	. 7077 . 7116	.7520 .7508	.1514 .1516	. 3151	. 6849 . 6834	17 16
45	.49622	.50378	2.0152	.57155	1.7496	1.1518	.13180	.86820	15
46	. 9647	. 0353	.0142	. 7193	.7484	.1520	. 3194	. 6805	14
47	. 9672	. 0328	.0132	. 7232	.7473	.1522	. 3209	. 6791	13
48	. 9697	. 0303	.0122	. 7270	.7461	.1524	. 3223	. 6776	12
49 50	. 9723 .49748	.50252	.0111 2.0101	. 7309 .57348	.7449 1.7437	.1526 1.1528	. 3238	. 6762 .86748	11 10
51	. 9773	. 0227	.0091	. 7386	.7426	.1530	. 3267	. 6733	9
52 53	. 9798	. 0202	.0081	. 7425	.7414	.1530 .1531 .1533	3281	. 6719	8
53	. 9823	. 0176	.0071	. 7464	.7402	.1533	. 3296	. 6704	7
54	. 9849	. 0151	.0061	. 7502	.7390	.1535	. 3310	. 6690	6 5 4 3 2 1
55 56	. 49874	.50126 . 0101	2.0050	.57541 . 7580	1.7379 .7367	1.1537 .1539	.13325	.86675 . 6661	4
56 57	9924	. 0076	.0030	7619	.7355	.1541	. 3354	. 6646	3
58	. 9950	. 0050	.0020	7657	.7344	.1543	. 3368	6632	2
59	. 9975	. 0025	.0010	. 7696	.7332	.1545	. 3383	. 6617	1
60	.50000	. 0000	.0000	. 7735	.7320	.1547	. 3397	. 6602	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

30 °	•	Na	tural Tr	igonom	etrical l	1490			
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.50000	.50000	2.0000	.57735	1.7320	1.1547	.13397	.86602	60
. 1	. 0025	.49975	1.9990	. 7774	.7309	.1549	. 3412	. 6588	59
2	. 0050	9950	.9980	. 7813	.7297	.1551	. 3426	6573	58
- 3 4	. 0075	9924	.9970	. 7851 . 7890	.7286 .7274	.1553 .1555	. 3441	. 6559 . 6544	57 56
5	. 0101	.49874	1.9950	.57929	1.7262	1.1557	.13470	.86530	55
6	. 0151	. 9849	.9940	7968	.7251	.1559	3485	6515	54
7	. 0176	9824	.9930	. 8007	.7239	.1561	. 3499	. 6500	53
8	. 0201	9799	.9920	. 8046	.7228	.1562	. 3514	. 6486	52
9	. 0226	. 9773 .49748	.9910 1.9900	. 8085 .58123	.7216 1.7205	.1564 1.1566	. 3529	. 6471 .86457	51 50
10 11	. 0277	9723	.9890	. 8162	.7193	.1568	. 3558	6442	49
12	0302	9698	.9880	8201	.7182	.1570	3572	6427	48
13	. 0327	. 9673	.9870	. 8240	.7170	.1572	. 3587	. 6413	47
14	. 0352	9648	.9860	. 8279	.7159	.1574	. 3602	6398	46
15	.50377	.49623	1.9850	.58318	1.7147	1.1576	.13616	.86383	45
16 17	. 0402	. 9597 . 9572	.9840	. 8357 . 8396	.7136 .7124	.1578 ·.1580	. 3631	. 6369 . 6354	44
18	0453	9547	.9820	8435	.7113	.1582	. 3660	6339	42
19	. 0478	9522	.9811	. 8474	.7101	.1584	. 3675	6325	41
20	.50503	.49497	1.9801	.58513	1.7090	1.1586	.13690	.86310	40
21 22	. 0528	. 9472	.9791	. 8552	.7079	.1588	. 3704	. 6295	39
22	. 0553	9447	9781	8591	.7067	.1590	. 3719	. 6281	38
23 24	. 0578	9422	.9771 .9761	. 8630 . 8670	.7056	.1592 .1594	. 3734	. 6266 . 6251	37 36
25	.50628	49371	1.9752	.58709	.7044 1.7033	1.1596	.13763	.86237	35
26	. 0653	9346	.9742	. 8748	.7022	.1598	3778	6222	34
26 27	. 0679	9321	.9732	. 8787	.7010	.1600	. 3793	6207	33
28 29	. 0704	. 9296	.9722	. 8826	.6999	.1602	. 3807	. 6192	32
29	. 0729	9271	.9713	. 8865	.6988	.1604	. 3822	. 6178	31
30 81	.50754	. 49246	1.9703 .9693	.58904 . 8944	1.6977 .6965	1.1606 .1608	.13837	.86163 . 6148	30 29
82	. 0779	9196	.9683	. 8983	.6954	.1610	3867	6133	28
83	. 0829	9171	.9674	9022	.6943	.1612	3881	6118	27
84	0854	. 9146	.9664	. 9061	.6931	.1614	. 3896	. 6104	26
35	.50879	.49121	1.9654	.59100	1.6920	1.1616	.13911	.86089	25
36	. 0904	9096	.9645	. 9140	.6909	.1618	. 3926	. 6074	24 23
87 88	. 0929	9071 9046	.9635 .9625	. 9179 . 9218	.6898 .6887	.1620 .1622	. 3941	. 6059 . 6044	23
39	. 0979	9021	.9616	9258	.6875	.1624	3970	6030	22 21
40	.51004	48096	1.9606	.59297	1.6864	1.1626	.13985	.86015	20
41	1029	8971	.9596	. 9336	.6853	.1628	. 4000	. 6000	19
42	. 1054	. 8946	.9587	. 9376	.6842	.1630	. 4015	. 5985	18
43	. 1079	8921	.9577	. 9415 . 9454	.6831	.1632	. 4030	. 5970 . 5955	17 16
44 45	. 1104 .51129	. 8896 .48871	.9568 1.9558	.59494	.6820 1.6808	.1634 1.1636	.14059	.85941	15
46	. 1154	8846	.9549	. 9533	.6797	.1638	4074	5926	14
47	1179	8821	.9539	. 9572	.6786	.1640	4089	. 5911	13
48	. 1204	. 8796	.9530	. 9612	.3775	.1642	. 4104	. 5896	12
49	. 1229	. 8771	.9520	. 9651	.6764	.1644	. 4119	. 5881	11
50	.51254	.48746	1.9510	.59691	1.6753	1.1646	.14134	.85866 . 5851	10
51 52	. 1279	8721 8696	.9501 .9491	. 9730 . 9770	.6742 .6731	.1648 .1650	4164	5836	1 8
53	. 1329	8671	.9482	9809	.6720	.1652	4178	5821	8 7
54	. 1354	8646	.9473	. 9849	.6709	.1654	4193	5806	6 5
55	.51379	.48621	1.9463	.59888	1.6698	1.1656	.14208	.85791	5
56	. 1404	8596	.9454	. 9928	.6687	.1658	. 4223	5777	4
57	. 1429	8571	.9444	9967	.6676	.1660	. 4238	5762	8
58 59	. 1454 . 1479	. 8546 . 8521	.9435	.60007	.6665 .6654	.1662 .1664	4268	. 5747 . 5732	2
60	. 1504	8496	.9416	. 0086	.6643	.1666	4283	5717	Ô
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

120° 59°

310	1	Na	tural Tr	igonom	etrical	Punction	ns.	14	180
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.51504	.48496	1.9416	.60086	1.6643	1.1666	.14283	.85717	60
1	. 1529	. 8471	.9407	. 0126	.6632	.1668	. 4298	. 5702	59
2	. 1554	. 8446	.9397	. 0165	.6621	.1670	. 4313	. 5687	58 57
3 4	. 1578 . 1603	8421	.9388 .9378	. 0205	.6610 .6599	.1672	. 4328	. 5672 . 5657	57
5	.51628	.48371	1.9369	.60284	1.6588	1.1676	.14358	.85642	56 55
5 6 7 8 9	. 1653	. 8347	.9360	. 0324	-6577	1.1676 .1678	. 4373	. 5627	54
7	. 1678	. 8322	.9350	. 0363	.6566 .6555	.1681	. 4388	. 5612	54 53
8	. 1703	8297	.9341	. 0403	.6555	.1683	. 4403	. 5597	52 51
10	. 1728 .51753	. 8272 .48247	.9332 1.9322	. 0443 .60483	.6544 1.6534	.1685 1.1687	. 4418 .14433	. 5582 .85566	51 50
ii	. 1778	8222	.9313	. 0522	.6523	.1689	. 4448	. 5551	49
12	. 1803	8197	.9304	. 0562	.6512	.1691	4463	. 5536	48
13	. 1827	. 8172	.9295	. 0602	.6501	.1693	. 4479	. 5521	47
14 15	1852	. 8147	.9285	. 0642	.6490	.1695	. 4494	. 5506	46
15	.51877 . 1902	. 8098	1.9276 .9267	.60681 . 0721	1.6479	1.1697	.14509	.85491	45
16 17	1902	. 8073	.9258	. 0721	.6469 .6458	.1699 .1701	. 4524 . 4539	. 5476 . 5461	44 43
18	. 1952	. 8048	9248	. 0801	.6447	.1703	4554	. 5446	42
18 19	. 1977	8023	9239	. 0841	.6436	.1705 1.1707	. 4569	. 5431	41
20	.52002	.47998	1.9230	.60881	1.6425	1.1707	.14584	.85416	40
20 21 22 23	. 2026	. 7973	.9221	. 0920	.6415	.1709	. 4599	5400	39
22	. 2051 . 2076	. 7949	.9212	. 0960	.6393	.1712 .1714	. 4615 . 4630	. 5385	38 37
24	2101	7899	.9193	. 1040	.6383	.1716	. 4645	. 5355	136
25	.52126	.47874	1.9184	.61080	1.6372	1.1718	.14660	.85340	35
26	. 2151	. 7849	.9175	. 1120	.6361	.1720	. 4675	. 5325	34
24 25 26 27 28	. 2175	. 7824	.9166	. 1160	.6350	.1722	. 4690	. 5309	36 35 34 33 32 31
28	. 2200 . 2225	. 7800 . 7775	.9157 .9148	. 1200 . 1240	.6340 .6329	.1724 .1726	. 4706 . 4721	. 5294	32
29 30 31	.52250	.47750	1.9139	.61280	1.6318	1.1728	.14736	.85264	37
31	. 2275	. 7725	.9130	. 1320	.6308	.1730	. 4751	. 5249	30 29 28 27
32	. 2299	. 7700	.9121	. 1360	.6297	.1732	. 4766	. 5234	28
32 33 34	. 2324	. 7676 . 7651	.9112	. 1400	.6286	.1734	. 4782	. 5218	27
35	. 2349	.47626	.9102 1.9093	. 1440 .61480	.6276	.1737 1.1739	. 4797	. 5203	26 25
36	. 2398	. 7601	.9084	. 1520	1.6265 .6255	.1741	. 4827	. 5173	24
36 37	. 2423	. 7577	1.9075	. 1560	.6244	.1743	. 4842	. 5157	23 22
38 39	. 2448	. 7552	.9066	. 1601	.6233	.1745	. 4858	. 5142	22
3 9	. 2473 .52498	. 7527	.9057	. 1641	.6223	.1747	4873	. 5127	21
41	. 2522	. 7477	1.9048 .9039	.61681 . 1721	1.6212 .6202	1.1749 .1751	.14888	.85112	20 19
42	. 2547	7453	.9030	. 1761	.6191	.1753	4919	5081	18
43	. 2572	. 7428	.9021	. 1801	.6181	.1756	. 4934	. 5066	17
44	. 2597	. 7403	.9013	. 1842	.6170	.1758	. 4949	. 5050	16
45	.52621	.47379	1.9004	.61882	1.6160	1.1760	.14965	.85035	15
46 47	. 2646 . 2671	. 7354 . 7329	.8995 .8986	. 1922 . 1962	.6149 .6139	.1762 .1764	. 4980	. 5020 . 5004	14 13
48	. 2695	7304	.8977	2004	.6128	.1766	5011	4989	12
49	. 2720	. 7280	.8968	2043	.6118	.1768	5026	. 4974	11
50	.52745	.47255	1.8959	.62083	1.6107	1.1770	.15041	.84959	10
51 52	. 2770 . 2794	. 7230 . 7205	.8950	. 2123	.6097	.1772	. 5057	. 4943	9
53	. 2819	7203	.8941 .8932	. 2164	.6086 .6076	.1775 .1777	. 5072	. 4928 . 4912	1 2
54	. 2844	7156	.8924	. 2244	.6066	.1779	5103	4897	8 7 6 5 4 3 2
55	.52868	.47131	1.8915	.62285	1.6055	1.1781	.15118	.84882	5
56 57	. 2893	. 7107	.8906	. 2325	.6045	.1783	. 5133	. 4866	4
57	. 2918	. 7082	.8897	. 2366	.6034	.1785	. 5149	. 4851	3
58 59	. 2942	. 7057	.8888 .8879	. 2406 . 2446	.6024 .6014	.1787 .1790	. 5164	. 4836 . 4820	2
60	. 2992	7008	.8871	. 2487	.6003	.1792	5195	. 4820	0
M.		Vrs. sin.				Cosec'nt			M.
D1.	COSIDE.	vrs. sin.	Secant.	Cotang.	Tang.	(Cosec nt	I V FS. COS.	Sine.	INI.

121° 58°

3 2 °	Natural Trigonometrical Punctions. 147								47°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.52992	.47008	1.8871	.62487	1.6003	1.1792	.15195	.84805	60
1	. 3016	. 6983	.8862	. 2527	.5993	.1794	. 5211	. 4789	59
2	. 3041	. 6959	.8853	. 2568	.5983	.1796	. 5226	. 4774	58
3	. 3066	. 6934	.8844	. 2608	.5972	.1798	. 5241	. 4758	57
4 5	. 3090	. 6909 .46885	.8836 1.8327	. 2649	.5962 1.5952	.1800 1.1802	. 5257	. 4743	56
6	. 3140	. 6860	.8318	. 2730	.5941	.1805	. 5288	.84728 . 4712	55 54
7	. 3164	6835	.8809	2770	.5931	.1807	. 5303	4697	58
8	. 3189	. 6811	.8801	. 2811	.5921	.1809	. 5319	. 4681	53 52
9	. 3214	6786	.8792	. 2851	.5910	.1811	. 5334	. 4666	51
10	.53238	.46762	1.8783	.62892	1.5900	1.1813	.15350	.84650	50
11	. 3263	6737	.8775	. 2933	.5890	.1815	. 5365	. 4635	49
12	. 3288	6712	.8766	. 2973	.5880	.1818	. 5381	. 4619	48
13 14	. 3312	. 6688	.8757 .8749	. 3014	.5869 .5859	.1820 .1822	. 5396	. 4604 . 4588	47
15	.53361	.46638	1.8740	.63095	1.5849	1.1824	.15427	.84573	46 45
16	. 3386	. 6614	.8731	. 3136	.5839	.1826	. 5443	. 4557	44
17	. 3411	6589	.8723	. 3177	.5829	.1828	. 5458	. 4542	43
18	. 3435	6565	.8714	. 3217	.5818	.1831	. 5474	. 4526	42
19	. 3460	. 6540	.8706	. 3258	.5808	.1833	. 5489	. 4511	41
20 21	.53484	.46516	1.8697	.63299	1.5798	1.1835	.15505	.84495	40
21	. 3509	6491	.8688	. 3339	.5788	.1837	. 5520	. 4479	39
22 23	. 3533	. 6466	.8680	. 3380	.5778	.1839	. 5536	. 4464	38 37
23	. 3558	. 6442	.8671	. 3421	.5768	.1841	. 5552	. 4448	37
24	. 3583	6417	.8663	. 3462	.5757	.1844	. 5567	. 4433	36 35 34 33 32 31
25 26 27 28	.53607	. 6368	1.8654 .8646	.63503	1.5747 .5737	1.1846 .1848	.15583	.84417 . 4402	35
20	. 3656	6344	.8637	3584	.5727	.1850	. 5614	. 4386	00
21	. 3681	6319	.8629	. 3625	.5717	.1852	. 5630	. 4370	99
29	. 3705	6294	.8620	. 3666	.5707	.1855	. 5645	. 4355	31
30	.53730	.46270	1.8611	.63707	1.5697	1.1857	.15661	.84339	30
31	. 3754	. 6245	.8603	. 3748	.5687	.1859	. 5676	. 4323	30 29 28 27
32	. 3779	. 6221	.8595	. 3789	.5677	.1861	. 5692	. 4308	28
83	. 3803	6196	.8586	. 3830	.5667	.1863	. 5708	. 4292	27
34	. 3828	. 6172	.8578	. 3871	.5657	.1866	. 5723	. 4276	26
35	.53852	.46147	1.8569	.63912	1.5646	1.1868	.15739	.84261	26 25 24 23 22
36 37	. 3877	. 6123	.8561 .8552	. 3953	.5636 .5626	.1870 .1872	. 5755	. 4245 . 4229	24
38	. 3926	6074	.8544	4035	.5616	.1874	5786	. 4214	133
39	. 3950	6049	.8535	4076	.5606	.1877	5802	4198	21
40	.53975	.46025	1.8527	.64117	1.5596	1.1879	.15817	.84182	20
41	. 3999	. 6000	.8519	. 4158	.5586	.1881	. 5833	. 4167	19
42	. 4024	. 5976	.8510	. 4199	.5577	.1883	. 5849	. 4151	18
43	. 4048	. 5951	.8502	. 4240	.5567	.1886	. 5865	. 4135	17
44	. 4073	5927	.8493	. 4281	.5557	.1888	. 5880	. 4120	16
45	.54097	.45902	1.8485	.64322	1.5547	1.1890	.15896	.84104	15
46	. 4122	. 5878	.8477	. 4363	.5537	.1892	. 5912	4088	14
47 48	. 4146 . 4171	. 5854 . 5829	.8468 .8460	. 4404	.5527 .5517	.1894 .1897	. 5927	. 4072 . 4057	13 12
48	. 4171	. 5805	.8452	. 4487	.5507	.1899	. 5959	. 4041	11
50	.54220	.45780	1.8443	.64528	1.5497	1.1901	.15975	.84025	10
51	. 4244	. 5756	.8435	. 4569	.5487	.1903	. 5991	4009	2
52	. 4268	. 5731	.8427	. 4610	.5477	.1906	. 6006	3993	8 7
53	. 4293	. 5707	.8418	. 4652	.5467	.1908	. 6022	. 3978	
54	. 4317	. 5682	.8410	. 4693	.5458	.1910	. 6038	. 3962	6
55	.54342	.45658	1.8402	.64734	1.5448	1.1912	.16054	.83946	5
56	. 4366	. 5634	.8394	4775	.5438	.1915	. 6070	. 3930	4
57	4391	. 5609	.8385	. 4817	.5428	.1917	6085	. 3914	3
58 59	. 4415	. 5585 . 5560	.8377	. 4858	.5418	.1919	6101	. 3899	1
60	. 4464	. 5536	.8361	. 4941	.5399	.1922	. 6133	. 3867	ō
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

22° 57°

330	•	Na	tural Tr	igonom	etrical l	ıs.	146°		
M.	Sine.	Vrs. cos.	'Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.54464	.45536	1.8361	.64941	1.5399	1.1924	.16133	.83867	60
1	. 4488	. 5512	.8352	. 4982	.5389	.1926	. 6149	. 3851	59
2	. 4513	. 5487	.8344	. 5023	.5379	.1928	. 6165	. 3835	58 57
3	. 4537	. 5463	.8336	. 5065	.5369	.1930	. 6180	. 3819	57
4	. 4561 .54586	. 5438	.8328	5106	.5359	.1933	. 6196	. 3804	56 55 54
5 6	. 4610	.45414 .5390	1.8320 .8311	.65148 . 5189	1.5350 .5340	1.1935 .1937	. 6228	.83788 . 3772	54
7	. 4634	5365	.8303	5231	.5330	.1939	6244	3756	53
8	. 4659	5341	.8295	5272	.5320	.1942	6260	3740	53 52 51
ğ	. 4683	. 5317	.8287	5314	.5311	1944	6276	8724	51
10	.54708	.45292	1.8279	.65355	1.5301	1.1946	.16292	.83708	50
11	. 4732	. 5268	.8271	. 5397	.5291	.1948	. 6308	3692	49
12	. 4756	. 5244	.8263	. 5438	.5282	.1951	. 6323	. 3676	48
13	. 4781	. 5219	.8255	. 5480	.5272	.1953	. 6339	. 3660	47
14	. 4805 .54829	. 5195	.8246	. 5521	.5262	1955	. 6355	3644	46
15 16	. 4854	.45171 . 5146	1.8238 .8230	.65563 .5604	1.5252 .5243	1.1958 .1960	.16371	.83629 . 3613	45 44
17	. 4878	5122	.8222	. 5646	.5233	.1962	6403	3597	43
18	4902	. 5098	.8214	. 5688	.5223	.1964	6419	3581	42
19	4926	. 5073	.8206	5729	.5214	.1967	6435	3565	41
20	.54951	.45049	1.8198	.65771	1.5204	1.1969	.16451	.83549	40
21	. 4975	. 5025	.8190	. 5813	.5195	.1971	. 6467	3533	39 38 37
22	. 4999	. 5000	.8182	. 5854	.5185	.1974	. 6483	. 3517	38
23	. 5024	. 4976	.8174	. 5896	.5175	.1976	. 6499	. 3501	37
24	. 5048	. 4952	.8166	. 5938	.5166	.1978	6515	. 3485	36
25 26	.55072	. 4928	1.8158	.65980	1.5156	1.1980	.16531	.83469	36 35 34 33 32
27	. 5121	. 4879	.8150 .8142	6063	.5147 .5137	.1983 .1985	. 6547	3453	39
28	. 5145	4855	.8134	6105	.5127	.1987	. 6579	3421	39
29	. 5169	4830	.8126	6147	.5118	.1990	6595	3405	31
30	.55194	.44806	1.8118	.66188	1.5108	1.1992	.16611	.83388	30
81	. 5218	. 4782	.8110	6230	.5099	.1994	. 6627	. 3372	30 29 28
32	. 5242	. 4758	.8102	. 6272	.5089	.1997	. 6643	. 3356	28
33	. 5266	. 4733	.8094	. 6314	.5080	.1999	. 6660	. 3340	1 27
84	5291	. 4709	.8086	. 6356	.5070	.2001	. 6676	. 3324	26 25 24
35 36	.55315	.44685	1.8078	.66398	1.5061	1.2004	.16692	.83308	25
37	. 5339	. 4661	.8070 .8062	. 6440 . 6482	.5051	.2006	6708	3292	24
38	. 5388	4612	.8054	6524	.5032	.2010	6740	3260	23 22
89	. 5412	4588	.8047	6566	.5023	.2013	6756	3244	21
40	.55436	.44564	1.8039	.66608	1.5013	1.2015	.16772	.83228	20
41	. 5460	. 4540	.8031	. 6650	.5004	.2017	. 6788	. 3211	19
42	. 5484	. 4515	.8023	. 6692	.4994	.2020	. 6804	. 3195	18
43	. 5509	. 4491	.8015	. 6734	.4985	.2022	. 6821	. 3179	17
44	. 5533	. 4467	.8007	6776	.4975	.2024	. 6837	. 3163	16
45 46	.55557	.44443	1.7999 .7992	. 66818 . 6860	1.4966	1.2027	.16853	.83147	15 14
47	. 5605	4395	.7984	. 6902	.4957 .4947	.2029 .2031	. 6885	. 3131	13
48	. 5629	4370	.7976	6944	.4938	.2034	6901	3098	12
49	. 5654	. 4346	7968	6986	.4928	2036	6918	3082	lii
50	.55678	.44322	1.7960	.67028	1.4919	1.2039	.16934	.83066	10
51	. 5702	. 4298	.7953	. 7071	.4910	.2041	. 6950	. 3050	9
52	. 5726	. 4274	.7945	. 7113	.4900	.2043	6966	. 3034	8
53	. 5750	. 4250	.7937	. 7155	.4891	.2046	. 6982	. 3017	17
54	. 5774	4225	.7929	7197	.4881	.2048	. 6999	. 3001	6
55 50	.55799	.44201	1.7921	.67239	1.4872	1.2050	.17015	.82985	5
56 57	. 5823	. 4177 . 4153	.7914	. 7282 . 7324	.4863	.2053	. 7031	. 2969	3
58	. 5871	4129	.7906 .7898	7366	.4853	.2055 .2057	. 7047 . 7064	. 2952	2
59	. 5895	4105	.7891	. 7408	.4835	.2060	7080	2920	ĺi
60	. 5919	. 4081	.7883	. 7451	.4826	.2062	7096	2904	ō
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

123° 56°

349)	Na	tural Tr	igonom	etrical l	Function	15.	14	45°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.55919	.44081	1.7883	.67451	1.4826	2.2062	.17096	.82904	60
1	. 5943	. 4057	.7875 .7867	. 7493	.4816	.2064	. 7112	2887	59
3	. 5967 . 5992	. 4032	.7867	. 7535 . 7578	.4807 .4798	.2067 .2069	. 7129 . 7145	. 2871 . 2855	58 57
4	6016	3984	.7852	7620	.4788	.2072	7161	. 2839	56
5	.56040	.43960	1.7844	.67663	1.4779	1.2074	.17178	.82822	55
6	. 6064	. 3936	.7837	. 7705	.4770	.2076	. 7194	. 2806	54
7	6088	3912	.7829	. 7747	.4761	.2079	. 7210	. 2790	58
8	. 6112 . 6136	. 3888 . 3864	.7821 .7814	. 7790 . 7832	.4751 .4742	.2081	. 7227 . 7243	. 2773 . 2757	52 51
10	.56160	.43840	1.7806	.67875	1.4733	1.2086	.17259	.82741	50
11	. 6184	3816	.7798	. 7917	.4724	.2088	. 7276	. 2724	49
12	. 6208	. 3792	.7791	. 7960	.4714	.2091	. 7292	. 2708	48
13	. 6232	. 3768	.7783	8002	.4705	.2093	. 7308	. 2692	47
14 15	. 6256 .56280	. 3743 .43719	.7776 1.7768	. 8045 .68087	.4696 1.4687	1.2095 1.2098	. 7325	. 2675 .82659	46 45
16	. 6304	3695	.7760	. 8130	.4678	.2100	7357	. 2643	44
17	6328	3671	.7753	. 8173	.4669	.2103	7374	2626	43
18	. 6353	. 3647	.7745	. 8215	.4659	.2105	. 7390	. 2610	42
19	. 6377	. 3623	.7738	8258	.4650	.2107	. 7406	. 2593	41
20	.56401	.43599	1.7730	.68301	1.4641	1.2110	.17423	.82577	40
21 22	. 6425 . 6449	. 3575 . 3551	.7723 .7715	. 8343 . 8386	.4632 .4623	.2112 .2115	. 7439 . 7456	. 2561 . 2544	39 38
23	6473	3527	7708	8429	.4614	.2117	7472	2528	37
24	6497	3503	7700	. 8471	.4605	2119	7489	2511	36
25	.56521	.43479	1.7693	.68514	1.4595	1.2122	.17505	.82495	35
26	. 6545	. 3455	.7685	. 8557	.4586	.2124	. 7521	. 2478	34
27	. 6569	. 3431	.7678	. 8600	.4577	.2127	. 7538	. 2462	33 32
28 29	. 6593 . 6617	. 3407 . 3383	.7670 .7663	. 8642 . 8685	.4568 4550	.2129 .2132	. 7554	. 2445	32 31
30	.56641	.43359	1.7655	.68728	.4559 1.4550	1.2134	.17587	.82413	37
31	. 6664	. 3335	.7648	8771	.4541	.2136	. 7604	2396	30 29
32	. 6688	. 3311	.7640	. 8814	.4532	.2139	. 7620	. 2380	28
83	. 6712	. 3287	.7633	. 8857	.4523	.2141	. 7637	. 2363	27
34	6736	. 3263	.7625	. 8899	.4514	.2144	. 7653	. 2347	26
35 36	.56760 . 6784	.43239 . 3216	1.7618 .7610	.68942 . 8985	1.4505 .4496	1.2146 .2149	.17670 . 7686	.82330 . 2314	25 24
37	6808	3192	.7603	9028	.4487	.2151	7703	2297	23
38	6832	3168	.7596	. 9071	.4478	.2153	. 7719	2280	23 22
39	. 6856	. 3144	.7588	. 9114	.4469	.2156	. 7736	. 2264	21
40	.56880	.43120	1.7581	.69157	1.4460	1.2158	.17752	.82247	20
41 42	. 6904 . 6928	. 3096 . 3072	.7573 .7566	. 9200 . 9243	.4451	.2161 .2163	. 7769 . 7786	. 2231 . 2214	19 18
43	. 6952	3048	.7559	9286	.4433	.2166	7802	2198	17
44	6976	3024	.7551	9329	4424	2168	7819	2181	16
45	.57000	.43000	1.7544	.69372	1.4415	1.2171	.17835	.82165	15
46	. 7023	. 2976	.7537	. 9415	.4406	.2173	. 7852	. 2148	14
47	. 7047	. 2952	.7529	. 9459	.4397	.2175	. 7868	. 2131	13 12
48 49	. 7071 . 7095	. 2929 . 2905	.7522 .7514	. 9502 . 9545	.4388	.2178	. 7885 . 7902	. 2115	11
50	.57119	.42881	1.7507	69588	1.4370	1.2183	.17918	.82082	10
51	. 7143	2857	.7500	9631	.4361	.2185	. 7935	. 2065	9
52	. 7167	. 2833	.7493	. 9674	.4352	.2188	. 7951	. 2048	8 7
53	. 7191	. 2809	.7485	. 9718	.4343	.2190	. 7968	. 2032	7
54	. 7214	2785	.7478	. 9761	.4335	.2193	. 7985	2015	é
55 56	.57238 . 7262	. 42761	1.7471 .7463	.69804 . 9847	1.4326 .4317	1.2195 .2198	.18001	.81998 . 1982	5 4
57	. 7286	2714	.7456	9891	.4308	.2200	. 8035	. 1965	3
58	7310	2690	.7449	9934	.4299	2203	. 8051	1948	3 2 1
59	. 7334	. 2666	.7442	. 9977	.4290	.2205	. 8068	. 1932	
60	. 7358	. 2642	.7434	.70021	.4281	.2208	. 8085	. 1915	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

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35	•	Na	tural Tı	igonom	metrical Functions. 14				
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.57358	.42642	1.7434	.70021	1.4281	1.2208	.18085	.81915	60
1	. 7381	. 2618	.7427	. 0064	.4273	.2210	. 8101	. 1898	59
2	. 7405	. 2595	.7420	. 0107	.4264	.2213	. 8118	. 1882	58 57
3	. 7429	. 2571	.7413	. 0151	.4255	.2215	. 8135	. 1865	56
4 5	. 7453 .57477	. 2547 .42523	.7405 1.7398	. 0194 .70238	.4246 1.4237	.2218 1.2220	. 8151 .18168	. 1848 .81832	55
6	7500	2499	.7391	. 0281	.4228	.2223	. 8185	. 1815	54
7	7524	2476	.7384	. 0325	.4220	.2225	8202	. 1798	53
8	. 7548	. 2452	.7377	. 0368	.4211	.2228	. 8218	. 1781	52
9	. 7572	2428	.7369	. 0412	.4202	.2230	. 8235	. 1765	51
10	.57596	.42404	1.7362	.70455	1.4193	1.2233	.18252	.81748	50
11 12	. 7619 . 7643	2380 2357	.7355 .7348	. 0499	.4185 .4176	.2235	. 8269 . 8285	. 1731 . 1714	49 48
13	7667	2333	.7341	. 0586	.4167	.2240	. 8302	1698	47
14	7691	2309	.7334	. 0629	.4158	.2243	. 8319	1681	46
15	.57714	.42285	1.7327	.70673	1.4150	1.2245	.18336	.81664	45
16	. 7738	2262	.7319	. 0717	.4141	.2248	. 8353	. 1647	44
17	. 7762	2238	.7312	. 0760	.4132	.2250	. 8369	. 1630	43
18	. 7786 . 7809	2214 2190	.7305	. 0804	.4123	.2253	. 8386	. 1614	42
19 20	.57833	42167	.7298 1.7291	. 0848 .70891	.4115 1.4106	.2255 1.2258	. 8403	. 1597 .81580	41
21	7857	2143	.7284	. 0935	.4097	.2260	. 8437	. 1563	39
21 22 23	7881	2119	7277	. 0979	.4089	.2263	8453	. 1546	38
23	. 7904	2096	.7270	. 1022	.4080	.2265	. 8470	. 1530	37
24	7928	2072	.7263	. 1066	.4071	.2268	. 8487	. 1513	36
25	.57952	.42048	1.7256	.71110	1.4063	1.2270	.18504	.81496	35
26	. 7975 . 7999	. 2024 . 2001	.7249 .7242	. 1154	.4054	.2273	. 8521 . 8538	. 1479	34 33
27 28	8023	1977	.7234	1241	.4045 .4037	.2278	. 8555	. 1445	32
29	8047	1953	7227	1285	4028	.2281	. 8571	1428	31
30	.58070	.41930	1.7220	.71329	1.4019	1.2283	.18588	.81411	30
81	. 8094	. 1906	.7213	. 1373	.4011	.2286	8605	. 1395	29
32	. 8118	1882	.7206	. 1417	.4002	.2288	. 8622	. 1378	28
33	. 8141 . 8165	. 1859 . 1835	.7199 .7192	. 1461 . 1505	.3994 .3985	.2291 .2293	. 8639 . 8656	. 1361 . 1344	27 26
34 35	.58189	41811	1.7185	.71549	1.3976	1.2296	.18673	.81327	25
36	8212	1788	.7178	. 1593	.3968	.2298	. 8690	. 1310	24
37	8236	. 1764	.7171	. 1637	.3959	.2301	. 8707	. 1293	23
38	. 8259	. 1740	.7164	. 1681	.3951	.2304	. 8724	. 1276	22
89	8283	1717	.7157	. 1725	.3942	.2306	. 8741	. 1259	21
40	.58307	.41693	1.7151	.71769	1.3933	1.2309	.18758	.81242 . 1225	20 19
41 42	8330 8354	. 1669 . 1646	.7144 .7137	. 1813 . 1857	.3925 .3916	.2311 .2314	. 8775 . 8792	. 1223	18
43	8378	1622	.7130	1901	.3908	.2316	. 8809	. 1191	17
44	. 8401	1599	.7123	1945	.3899	.2319	. 8826	. 1174	16
45	.58425	.41575	1.7116	.71990	1.3891	1.2322	.18843	.81157	15
46	8148	. 1551	.7109	. 2034	.3882	.2324	. 8860	. 1140	14
47	8472	. 1528	.7102	. 2078	.3874	.2327	. 8877 . 8894	. 1123	13 12
48 49	. 8496 . 8519	. 1504	.7095 .7088	. 2166	.3865 .3857	.2329	. 8911	. 1089	ii
50	.58543	.41457	1.7081	.72211	1.3848	1.2335	.18928	.81072	10
51	8566	. 1433	.7075	2255	.3840	.2337	. 8945	. 1055	9
52	8590	. 1410	.7068	. 2299	.3831	.2340	. 8962	. 1038	8 7
53	. 8614	. 1386	.7061	. 2344	.3823	.2342	. 8979	. 1021	7
54	8637	. 1363	.7054	. 2388	.3814	.2345	. 8996	. 1004	6
55 56	.58661 .8684	.41339 .1316	1.7047	.72432 . 2477	1.3806 .3797	1.2348 .2350	.19013	.80987 . 0970	5
56 57	8708	1292	.7040	2521	.3789	.2353	. 9047	. 0953	3
58	8731	1268	.7027	2565	.3781	.2355	9064	. 0936	l ž
59	8755	. 1245	.7020	. 2610	.3772	.2358	. 9081	. 0919	1
60	. 8778	. 1221	.7013	. 2654	.3764	.2361	. 9098	. 0902	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

36°	•	Na	tural Tr	igonom	etrical l	Punction	15.	14	43°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.58778	.41221	1.7013	.72654	1.3764	1.2361	.19098	.80902	60
1	. 8802	. 1198	.7006	. 2699	.3755	.2363	. 9115	. 0885	59
2	. 8825	. 1174	.6999	. 2743	.3747	.2366	. 9132	. 0867	58 57
3	. 8849	. 1151	.6993	. 2788	.3738	.2368	. 9150	. 0850	57
5	. 8873 .58896	. 1127 .41104	.6986 1.6979	. 2832 .72877	.3730 1.3722	.2371 1.2374	. 9167 .19184	. 0833 .80816	56 55
8	. 8920	1080	.6972	. 2921	.3713	.2376	9201	. 0799	54
6	8943	1057	.6965	2966	3705	2379	9218	0782	53
8	. 8967	1033	.6959	. 3010	.3697	.2382	. 9235	. 0765	52
9	. 8990	. 1010	.6952	. 3055	.3688	.2384	. 9252	. 0747	51
10	.59014	.40986	1.6945	.73100	1.3680	1.2387	.19270	.80730	50
11	9037	. 0963	.6938	. 3144	.3672	.2389	. 9287	. 0713	49
12 13	. 9060 . 9084	. 0939	.6932 .6925	. 3189 . 3234	.3663 .3655	.2392	. 9304 . 9321	. 0696	48 47
14	9107	0892	.6918	3278	.3647	.2397	9338	. 0662	46
15	.59131	.40869	1.6912	.73323	1.3638	1.2400	19355	.80644	45
15 16	. 9154	. 0845	.6905	. 3368	.3630	.2403	9373	0627	44
17	. 9178	. 0822	.6898	. 3412	.3622	.2405	. 9390	. 0610	43
18	. 9201	. 0799	.6891	. 3457	.3613	.2408	9407	. 0593	42
19	9225	. 0775	.6885	3502	.3605	.2411	9424	. 0576	41
20 21 22	.59248 . 9272	. 0728	1.6878 .6871	.73547 . 3592	1.3597 .3588	1.2413 .2416	.19442 . 9459	.80558 . 0541	40 39
21	9295	0705	.6865	3637	.3580	.2419	9476	. 0524	38
23 I	9318	0681	.6858	3681	3572	2421	9493	0507	38 37
24	. 9342	. 0658	.6851	. 3726	.3564	.2424	. 9511	. 0489	36
25	.59365	.40635	1.6845	.73771	1.3555	1.2427	.19528	.80472	35
25 26 27	. 9389	. 0611	.6838	. 3816	.3547	.2429	. 9545	. 0455	34
27	. 9412	0588	.6831	. 3861	.3539	.2432	. 9562	. 0437	33
28 29	. 9435 . 9459	. 0564	.6825 .6818	. 3906 . 3951	.3531 .3522	.2435 .2437	. 9580 . 9597	. 0403	32 31
30	.59482	.40518	1.6812	.73996	1.3514	1.2440	.19614	.80386	30
81	9506	. 0494	.6805	. 4041	.3506	.2443	. 9632	. 0368	29
32	9529	. 0471	.6798	. 4086	.3498	.2445	. 9649	. 0351	128
33	9552	. 0447	.6792	. 4131	.3489	.2448	. 9666	. 0334	27
34	. 9576	. 0424	6785	. 4176	.3481	.2451	. 9683	. 0316	26
35	.59599	.40401	1.6779	.74221	1.3473	1.2453	.19701	.80299	25
36 37	. 9622	. 0377	.6772 .6766	. 4266 . 4312	.3465 .3457	.2456 .2459	. 9718 . 9736	. 0282	24 23
38	9646	0331	.6759	4357	.3449	.2461	9753	. 0247	22
39	9692	0307	.6752	. 4402	.3440	.2464	9770	. 0230	21
40	.59716	.40284	1.6746	.74447	1.3432	1.2467	.19788	.80212	20
41	. 9739	. 0261	.6739	. 4492	.3424	.2470	. 9805	. 0195	19
42	. 9762	. 0237	.6733	4538	.3416	.2472	. 9822	. 0177	18
43	9786	. 0214	.6726	4583	.3408	.2475	. 9840	. 0160	17
44 45	. 9809 .59832	. 0191 .40167	.6720 1.6713	. 4628 .74673	.3400 1.3392	.2478 1.2480	. 9857	. 0143 .80125	16 15
46	. 9856	. 0144	.6707	4719	.3383	.2483	. 9892	. 0108	14
47	9879	0121	.6700	4764	.3375	.2486	9909	. 0090	13
48	. 9902	. 0098	.6694	4809	.3367	.2488	. 9927	. 0073	12
49	. 9926	. 0074	.6687	. 4855	.3359	.2491	. 9944	. 0056	11
50	.59949	.40051	1.6681	.74900	1.3351	1.2494	.19962	.80038	10
51	. 9972	. 0028	.6674	. 4946	.3343	.2497	. 9979	. 0021	9
52 53	. 9995	. 0004	.6668 .6661	. 4991	.3335	.2499 .2502	.9997	. 0003	8 7
54	. 0042	. 9958	.6655	5082	.3319	.2505	. 0031	9968	ءُ ا
55	.60065	.39935	1.6648	.75128	1.3311	1.2508	.20049	.79951	6 5
56	. 0088	. 9911	.6642	. 5173	.3303	.2510	. 0066	. 9933	4
57	. 0112	9888	.6636	. 5219	.3294	.2513	. 0084	. 9916	8
58	. 0135	. 9865	.6629	. 5264	.3286	.2516	. 0101	. 9898	8 2 1
59	. 0158	. 9842	.6623	. 5310	.3278	.2519	. 0119	9881	
60	. 0181	. 9818	.6616	. 5355	.3270	.2521	. 0136	. 9863	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

37°	Natural Trigonometric					Punctio	ions. 142		
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.60181	.39818	1.6616	.75355	1.3270	1.2521	.20136	.79863	60
123456789	. 0205	. 9795 . 9772	.6610	. 5401	.3262	.25?4	. 0154	. 9846	59
2	. 0228	9772	.6603	. 5447	.3254	.2527	. 0171	. 9828	58
3	. 0251 . 0274	. 9749	.6597 .6591	. 5492 . 5538	.3246	.2530 .2532	. 0189	. 9811	57
5	.60298	. 9726 .39702	1.6584	.75584	1 3230	1.2535	.20224	.79776	56 55 54 53 52
6	. 0320	. 9679	.6578	5629	1.3230 .3222	.2538	. 0242	. 9758	54
7	0344	9656	.6572	. 5675	.3214	.2541	. 0259	. 9741	53
8	0367	. 9633	.6565	. 5721	.3206	.2543	. 0277	. 9723	52
9	. 0390	9610	.6559	5767	.3198	.2546	. 0294	9706	51
10 11 12	.60413	.39586	1.6552	.75812	1.3190	1.2549	.20312	.79688	50
41	. 0437 . 0460	. 9563 . 9540	.6546 .6540	. 5858 . 5904	.3182 .3174	.2552 .2554	. 0329	. 9670 . 9653	49 48
13	. 0483	9517	.6533	. 5950	.3166	.2557	. 0365	9635	47
14	. 0506	9494	.6527	5996	.3159	.2560	0382	9618	46
15	.60529	.39471	1.6521	.76042	1.3151	1.2563	.20400	.79600	45
16	. 0552	. 9447	.6514	. 6088	.3143	.2565	. 0417	. 9582	44
17	. 0576	. 9424	.6508	. 6134	.3135	.2568	. 0435	9565	43
18	. 0599	. 9401	.6502	6179	.3127	.2571	. 0453	9547	42
19	. 0622	9378	.6496	. 6225 .76271	.3119	.2574 1.2577	. 0470	. 9530 .79512	41
20 21	.60645 . 0668	.39355 . 9332	1.6489 .6483	6317	1.3111 .3103	.2579	. 0505	9494	40
22	. 0691	9309	.6477	6364	.3095	.2582	. 0523	9477	38
23	. 0714	9285	.6470	6410	.3087	.2585	. 0541	9459	39 38 37 36 35 34 33 32
24	. 0737	. 9262	.6464	. 6456	.3079	.2588	. 0558	. 9441	36
25 26 27 28	.60761	.39239	1.6458	.76502	1.3071	1.2591	.20576	.79424	35
26	. 0784	. 9216	.6452	. 6548	.3064	.2593	. 0594	. 9406	34
27	. 0807	. 9193	.6445	6594	.3056	.2596 .2599	. 0611	9388	33
29	. 0830	. 9170 . 9147	.6439 .6433	. 6640	.3048	.2602	. 0629	9371	31
80	60876	39124	1.6427	76733	1.3032	1.2605	.20665	79335	30
81	. 0899	. 9101	.6420	. 6779	.3024	.2607	. 0682	. 9318	31 30 29 28 27
82	. 0922	. 9078	.6414	6825	.3016	.2610	. 0700	9300	28
83	. 0945	9055	.6408	. 6871	.3009	.2613	. 0718	. 9282	27
84	. 0963	. 9031	.6402	. 6918	.3001	.2616	. 0735	. 9264	26 25 24 23 22
35 36 37	.60991	.39008	1.6396	.76964 . 7010	1.2993	1.2619 .2622	.20753	.79247 . 9229	23
97	. 1014 . 1037	. 8985 . 8962	.6389 .6383	7057	.2985 .2977	.2624	0789	9211	23
38	. 1061	8939	.6377	7103	.2970	.2627	. 0806	9193	22
39	. 1084	. 8916	.6371	7149	.2962	.2630	. 0824	. 9176	21
40	.61107	.38893	1.6365	.77196	1.2954	1.2633	.20842	.79158	l 20
41	. 1130	. 8870	.6359	. 7242	.2946	.2636	. 0860	. 9140	19
42	. 1153	8847	.6352	. 7289	.2938	.2639	. 0878	. 9122	18
43	. 1176	. 8824 . 8801	.6346 .6340	. 7335 . 7382	.293 1 .2923	.2641 .2644	. 0895	9104	17 16
45	. 1199 .61222	38778	1.6334	77428	1.2915	1.2647	.20931	79069	15
46	. 1245	. 8755	.6328	7475	.2907	.2650	. 0949	9051	14
47	. 1268	8732	.6322	. 7521	.2900	.2653	. 0967	9033	13
48	. 1290	. 8709	.6316	. 7568	.2892	.2656	. 0984	. 9015	12
49	. 1314	. 8686	.6309	. 7614	.2884	.2659	. 1002	. 8998	11
50	.61337	.38663	1.6303	.77661	1.2876	1.2661 .2664	.21020	.78980 . 8962	10
51	. 1360	. 8640	.6297	. 7708 . 7754	.2869 .2861	.2667	. 1038 . 1056	8944	1 8
52 53	. 1383 . 1405	. 8617 . 8594	.6291 .6285	7801	.2853	.2670	. 1074	8926	9 8 7 6 5
54	. 1428	. 8571	.6279	7848	.2845	2673	1091	8908	6
54 55	.61451	.38548	1.6273	.77895	1.2838	1.2676	.21109	.78890	5
56 57	. 1474	. 8525	.6267	. 7941	.2830	.2679	. 1127	. 8873	3
57	. 1497	. 8503	.6261	. 7988	.2822	.2681	. 1145	. 8855	3
58 59	. 1520	8480	.6255	. 8035	.2815	.2684	. 1163	. 8837	2 1
60	. 1543 . 1566	. 8457 . 8434	.6249 .6243	. 8082 . 8128	.2807 .2799	.2687 .2690	. 1181	. 8819 . 8801	6
OU.	. 1500	. 0101	.0213	. 0120	.2109	.2050	. 1100	. 6001	<u>_</u>
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.
400									200

£27° 52°

380	•	Na	tural Tr	igonom	etrical Functions.			14	110
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.61566	.38434	1.6243	.78128	1.2799	1.2690	.21199	.78801	60
1	. 1589	. 8411	.6237	. 8175	.2792	.2693	. 1217	8783	59
2	. 1612	8388	.6231	. 8222	.2784	.2696	. 1235	. 8765	58
3	. 1635	8365	.6224	8269	.2776	.2699	. 1253	. 8747 . 8729	57
4 5	. 1658 .61681	. 8342 .38319	.6218 1.6212	. 8316 .78363	.2769 1.2761	.2702 1.2705	. 1271	.78711	56
6	. 1703	. 8296	.6206	. 8410	.2753	.2707	. 1306	. 8693	55 54
7	1726	8273	.6200	8457	.2746	.2710	1324	. 8675	53
8	1749	8251	.6194	8504	.2738	.2713	. 1342	. 8657	52
9	. 1772	8228	.6188	8551	.2730	.2716	. 1360	. 8640	51
10	.61795	.38205	1.6182	78598	1.2723	1.2719	.21378	.78622	50
11	. 1818	8182	.6176	. 8645	.2715	.2722	. 1396	8604	49
12	. 1841	8159	.6170	. 8692	.2708	.2725	. 1414	. 8586	48
13 14	. 1864 . 1886	. 8136 . 8113	.6164 .6159	. 8739 . 8786	.2700 .2692	.2728 .2731	. 1432	. 8568 . 8550	47 46
15	.61909	.38091	1.6153	.78834	1.2685	1.2734	.21468	.78532	45
16	. 1932	8068	.6147	. 8881	.2677	.2737	. 1486	. 8514	44
17	1955	8045	.6141	8928	.2670	2739	1504	8496	43
18	. 1978	8022	.6135	8975	.2662	.2742	1522	. 8478	42
19	2001	. 7999	.6129	. 9022	.2655	.2745	. 1540	. 846 0	41
20	.62023	.37976	1.6123	.79070	1.2647	1.2748	.21558	.78441	40
21 22 23 24	. 2046	. 7954	.6117	9117	.2639	.2751	. 1576	. 8423	39
22	. 2069	. 7931	.6111	9164	.2632	.2754	. 1594	. 8405	38 37 36
23	2092	. 7908	.6105	. 9212	.2624	.2757	. 1612	. 8387	37
24	. 2115 .62137	. 7885 .37862	.6099 1.6093	. 9259 .79306	.2617 1.2609	.2760 1.2763	. 1631	. 8369 .78351	36
25 26	. 2160	. 7840	6087	9354	.2602	.2766	.21649	. 8333	35 34
27	2183	7817	.6081	9401	.2594	2769	1685	. 8315	23
28	2206	7794	.6077	9449	2587	2772	1703	8297	33 32 31
29	2229	7771	.6070	9496	.2579	.2775	1721	8279	31
27 28 29 30	.62251	.37748	1.6064	.79543	1.2572	1.2778	.21739	.78261	30
31	. 2274	. 7726	.6058	. 9591	.2564	.2781	. 1757	. 8243	30 29 28 27 26 25 24
32	. 2297	. 7703	.6052	. 9639	.2557	.2784	. 1775	8224	28
33	. 2320	. 7680	.6046	. 9686	.2549	.2787	. 1793	. 8206	27
34	. 2342	. 7657	.6040	. 9734	.2542	.2790	. 1812	. 8188	26
35	.62365 . 2388	.37635	1.6034	.79781 . 9829	1.2534 .2527	1.2793 .2795	.21830	.78170	122
36 37	. 2411	. 7612 . 7589	.6029	9876	.2519	2798	. 1848 . 1866	. 8152 . 8134	24
38	2433	7566	.6017	9924	2512	2801	1884	8116	23 22
39	2456	7544	.6011	9972	.2504	.2804	1902	. 8097	21
40	.62479	.37521	1.6005	.80020	1.2497	1.2807	.21921	.78079	20
41	. 2501	. 7498	.6000	. 0067	.2489	.2810	. 1939	. 8061	19
42	. 2524	7476	.5994	. 0115	.2482	.2813	. 1957	. 8043	18
43	. 2547	. 7453	.5988	. 0163	.2475	.2816	. 1975	8025	17
44	2570	. 7430	.5982	. 0211	.2467	.2819	. 1993	. 8007	16
45	.62592	.37408	1.5976 .5971	.80258 . 0306	1.2460 .2452	1.2822 .2825	.22011	.77988 . 7970	15
46 47	. 2615 . 2638	. 7385 . 7362	.5965	. 0354	.2452	.2828	2030	. 7952	14 13
48	2660	7340	.5959	. 0402	.2437	.2831	2066	7934	12
49	2683	7317	.5953	. 0450	.2430	2834	2084	7915	iĩ
50	.62706	37294	1.5947	.80498	1.2423	1.2837	22103	.77897	îō
51	2728	. 7272	.5942	. 0546	.2415	.2840	. 2121	. 7879	9
52	. 2751	7249	. 593 6	. 0594	.2408	.2843	. 2139	. 7861	8 7
53	. 2774	7226	.5930	. 0642	.2400	.2846	. 2157	. 7842	7
54	2796	. 7204	.5924	. 0690	.2393	.2849	. 2176	. 7824	6 5 4
55	.62819	.37181	1.5919	.80738	1.2386	1.2852	.22194	.77806	5
56 57	. 2841	7158 7136	.5913	. 0786	.2378 .2371	.2855 .2858	. 2212	7788	4
58	2864 2887	71136	.5907 .5901	. 0882	.2364	.2861	. 2230	. 7769 . 7751	1 3
59	2909	7090	.5896	. 0930	.2356	.2864	2267	7733	3 2 1
60	2932	7068	.5890	. 0978	.2349	2867	2285	7715	Ô
	Cosine	Vrs. sin	Secant.	Cotang	Tang.	Cosec'nt	Vrs. cos	Sine.	M.
					,	, , , , , , , , , , , , , , , , , , ,	1		

399	•	Na	tural Ti	rigonom	etrical	Punction	ns.	1	40°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.62932	.37068	1.5890	.80978	1.2349	1.2867	.22285	.77715	60
1	. 2955	. 7045	.5884	. 1026	.2342	.2871	. 2304	. 7696	59
2	. 2977	. 7023	.5879	. 1075	.2334	.2874	. 2322	. 7678	58
3 4	. 3000	. 7000	.5873	. 1123	.2327	.2877	. 2340	. 7660 . 7641	57
4	. 3022 .63045	. 6977 .36955	.5867 1.5862	. 1171 .81219	1.2312	1.2883	.22377	77623	56 55
5 6	3067	. 6932	.5856	. 1268	2305	.2886	2395	7605	54
7	. 3090	6910	.5850	. 1316	.2297	.2889	. 2414	7586	53
8	. 3113	. 6887	.5845	. 1364	.2290	.2892	. 2432	7568	53 52
9	. 3135	. 6865	.5839	. 1413	.2283	.2895	. 2450	. 7549	51
10	.63158	.36842	1.5833	.81461	1.2276	1.2898	.22469	.77531	50
11 12	. 3180	6820	.5828	. 1509	.2268	.2901 .2904	. 2487 . 2505	. 7513 . 7494	49
13	. 3203 . 3225	6797	.5822 .5816	. 1558 . 1606	2254	2907	2524	7476	47
14	. 3248	6752	.5811	1655	.2247	.2910	2542	7458	46
15	.63270	36729	1.5805	.81703	1.2239	1.2913	.22561	.77439	45
16	. 3293	. 6707	.5799	. 1752	.2232	.2916	. 2579	. 7421	44
17	. 3315	. 6684	.5794	. 1800	.2225	.2919	2597	7402	43
18	. 3338	. 6662	.5788	. 1849	.2218	.2922	2616	. 7384	42
19	. 3360	. 6639	.5783	. 1898	.2210	.2926	2634	. 7365	41
20	.63383	.36617	1.5777	.81946	1.2203 .2196	1.2929 .2932	.22653	.77347	40
21 22	. 3405 . 3428	6594	.5771 .5766	. 1995 . 2043	.2196	.2932	. 2671 . 2690	. 7329 . 7310	39 38
23	. 3450	6549	.5760	2092	.2181	2938	2708	7292	37
24	. 3473	6527	.5755	2141	.2174	.2941	2727	7273	36
25	.63495	.36504	1.5749	.82190	1,2167	1.2944	.22745	.77255	35 34
26	. 3518	. 6482	.5743	. 2238	.2160	.2947	. 2763	. 7236	34
27	. 3540	. 6459	.5738	. 2287	.2152	.2950	2782	. 7218	33 32
28	. 3563	6437	.5732	. 2336	.2145	.2953	. 2800	. 7199	32
29	. 3585	6415	.5727	. 2385	.2138 1.2131	.2956 1.2960	. 2819 .22837	. 7181	31
30 31	.63608 . 3630	.36392	1.5721 .5716	.82434 . 2482	.2124	.2963	2856	.77162 - 7144	30 29 28 27
32	. 3653	6347	.5710	2531	.2117	.2966	2874	7125	28
33	. 3675	6325	.5705	2580	.2109	2969	2893	7107	27
34	. 3697	. 6302	.5699	. 2629	.2102	.2972	. 2912	7088	26
35	.63720	.36280	1.5694	.82678	1.2095	1.2975	.22930	.77070	25
36	. 3742	. 6258	.5688	. 2727	.2088	.2978	. 2949	. 7051	24
37	. 3765	. 6235	.5683	. 2776	.2081	.2981	2967	. 7033	23
38 39	. 3787 . 3810	6213	.5677	. 2825 . 2874	.2074	.2985 .2988	. 2986 . 3004	. 7014	22 21
40	.63832	. 6190 .36168	.5672 1.5666	.82923	1.2059	1.2991	23023	.76977	20
41	. 3854	. 6146	.5661	. 2972	2052	2994	3041	. 6958	19
42	. 3877	6123	.5655	3022	2045	2997	3060	. 6940	18
43	3899	. 6101	.5650	. 3071	.2038	.3000	. 3079	6921	17
44	. 3921	. 6078	.5644	. 3120	.2031	.3003	. 3097	. 6903	16
45	.63944	.36056	1.5639	.83169	1.2024	1.3006	.23116	.76884	15
46	. 3966	. 6034	.5633	. 3218	.2016	.3010	3134	. 6865	14
47 48	. 3989 . 4011	. 6011	.5628 .5622	. 3267 . 3317	.2009 .2002	.3013 .3016	. 3153 . 3172	. 6847 . 6828	13 12
49	. 4033	. 5967	.5617	. 3366	.1995	.3019	3190	6810	iĩ
50	.64056	35944	1.5611	.83415	1.1988	1.3022	23209	.76791	10
51	. 4078	. 5922	.5606	. 3465	.1981	.3025	. 3227	. 6772	9
52	. 4100	. 5900	.5600	. 3514	.1974	.3029	. 3246	. 6754	8
53	. 4123	. 5877	.5595	. 3563	.1967	.3032	. 3265	. 6735	7
54	. 4145	. 5855	.5590	. 3613	.1960	.3035	. 3283	. 6716	6
55	.64167	.35833	1.5584	.83662	1.1953	1.3038	.23302	.76698 . 6679	5 4
56 57	. 4189 . 4212	. 5810	.5579	. 3712 . 3761	.1946 .1939	.3041 .3044	3339	. 6660	9
58	. 4212	. 5788 . 5766	.5573 .5568	3811	.1939	.3044	. 3358	. 6642	2
59	. 4256	5743	.5563	3860	1924	.3051	3377	6623	3 2 1
60	4279	5721	.5557	3910	.1917	.3054	. 3395	6604	ō
M.		Vrs. sin.	l	Cotang.	Tang.	Cosec'nt	Vra con	Sine.	М.
D1.	совине.	1 4 19. 0111.	Decant.	Octours.	Tang.	LOOPER HE	1 10. 006.	Dillo.	- AL.

129° 50°

40°	,	Na	tural Ti	igonom	etrical	Punction	ns.	1.	39°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.64279	.35721	1.5557	.83910	1.1917	1.3054	.23395	.76604	60
1	. 4301	. 5699	.5552	. 3959	.1910	.3057	. 341/2	. 6586	59
2 3	. 4323	. 5677	.5546	. 4009	.1903	.3060	. 3433	. 6567	58
4	. 4345 . 4368	. 5654 . 5632	.5541	. 4059 . 4108	.1896 .1889	.3064 .3067	3452	. 6548	57 56
5	.64390	.35610	.5536 1.5530	.84158	1.1882	1.3070	.23489	.76511	55
. 6	. 4412	. 5588	.5525	. 4208	.1875	.3073	. 3508	. 6492	54
7	. 4435	. 5565	.5520	. 4257	.1868	.3076	. 3527	. 6473	53
8	. 4457	. 5543	.5514	. 4307	.1861	.3080	. 3545	. 6455	52
9	. 4479	. 5521	.5509	. 4357	.1854	.3083	. 3564	. 6436	51
10	.64501	.35499	1.5503	.84407	1.1847	1.3086	.23583	.76417	50
11	. 4523	. 5476	.5498	. 4457	.1840	.3089	. 3602	. 6398	49
12 13	. 4546 . 4568	. 5454 . 5432	.5493 .5487	. 4506 . 4556	.1833	.3092 .3096	. 3620	. 6380	48 47
14	4590	5410	.5482	. 4606	.1819	.3099	3658	6342	46
15	.64612	.35388	1.5477	.84656	1.1812	1.3102	.23677	.76323	45
16	. 4635	. 5365	.5471	. 4706	.1805	.3105	. 3695	6304	44
17	4657	. 5343	.5466	. 4756	.1798	.3109	. 3714	. 6286	43
18 19	. 4679	. 5321	.5461	. 4806	.1791	.3112	. 3733	. 6267	42
19	. 4701	. 5299	.5456	. 4856	.1785	.3115	. 3752	. 6248	41
20	.64723	.35277	1.5450	.84906	1.1778	1.3118	.23771	.76229	40
21 22	. 4745	. 5254 . 5232	.5445	. 4956	.1771	.3121	3790	. 6210 . 6191	39
23	. 4768 . 4790	5232	.5440 .5434	. 5006	.1764 .1757	.3125 .3128	3827	. 6173	38 37
20	. 4812	5188	.5429	. 5107	.1750	.3131	. 3846	6154	36
24 25 26	.64834	.35166	1.5424	.85157	1.1743	1.3134	.23865	.76135	35
26	. 4856	. 5144	.5419	. 5207	1736ء اا	.3138	. 3884	. 6116	34
27	. 4878	. 5121	.5413	. 5257	.1729	.3141	. 3903	. 6097	33
28	. 4900	. 5099	.5408	. 5307	.1722	.3144	. 3922	. 6078	32
29 80	. 4923	. 5077	.5403	. 5358	.1715	.3148	. 3940	. 6059	31
80	.64945	.35055	1.5398	.85408	1.1708	1.3151	.23959	.76041	30 29 28 27
31 32	. 4967 . 4989	5033	.5392 .5387	. 5458 . 5509	.1702 .1695	.3154 .3157	3978	6022	29
33	. 5011	4989	.5382	. 5559	.1688	.3161	. 4016	. 5984	27
34	. 5033	4967	.5377	. 5609	.1681	.3164	4035	. 5965	26
35	.65055	.34945	1.5371	.85660	1.1674	1.3167	.24054	.75946	25
3 6	. 5077	. 4922	.5366	. 5710	.1667	.3170	. 4073	. 5927	24
37	. 5099	. 4900	.5361	. 5761	.1660	.3174	. 4092	. 5908	23 22
38	. 5121	4878	.5356	. 5811	.1653	.3177	. 4111	. 5889	22
39	. 5144	. 4856	.5351	. 5862	.1647	.3180	4130	. 5870	21 20
40 41	.65166 . 5188	.34834 .4812	1.5345 .5340	.85912 . 5963	1.1640 .1633	1.3184 .3187	. 24149	.75851	19
42	. 5210	4790	.5335	. 6013	.1626	.3190	4186	5813	18
43	5232	4768	.5330	6064	1619	.3193	4205	. 5794	17
44	. 5254	. 4746	.5325	. 6115	.1612	.3197	. 4224	. 5775	16
45	.65276	.34724	1.5319	.86165	1.1605	1.3200	.24243	.75756	15
46	. 5298	4702	.5314	. 6216	.1599	.3203	. 4262	. 5737	14
47	. 5320	4680	.5309	. 6267	.1592	.3207	. 4281	. 5718	13
48	. 5342 . 5364	. 4658 . 4636	.5304	. 6318 . 6368	.1585 .1578	.3210 .3213	. 4300	. 5699 . 5680	12
49 50	.65386	.34614	1.5294	.86419	1.1571	1.3217	,24338	.75661	10
51	. 5408	. 4592	.5289	. 6470	.1565	3220	. 4357	5642	1 9
52	. 5430	4570	.5283	6521	.1558	.3223	. 4376	5623	8
53	. 5452	. 4548	.5278	6572	.1551	.3227	4396	. 5604	8 7
54	5474	. 4526	.5273	. 6623	.1544	.3230	. 4415	. 5585	6
55	.65496	.34504	1.5268	.86674	1.1537	1.3233	.24434	.75566	5
56	. 5518	. 4482	.5263	. 6725	.1531	.3237	. 4453	. 5547	4
57	. 5540	. 4460	.5258	. 6775	.1524	.3240	. 4472	. 5528	3
58 59	. 5562	. 4438	.5253	. 6826	.1517	3243	. 4491	. 5509 . 5490	3 2 1
60	. 5584 . 5606	. 4394	.5248 .5242	. 6878 . 6929	.1510 .1504	.3247 .3250	4510	5471	ō
-	. 5550	. 1001	.0212	. 0020	.1001	.0200	. 1025	. 01.1	<u> </u>
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

130° 49°

41°	•	Na	tural Tr	igonom	etrical	Function	15.	1.	38°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.65606	.34394	1.5242	.86929	1.1504	1.3250	.24529	.75471	60
1	. 5628	. 4372	.5237	. 6980	.1497	.3253	. 4548	. 5452	59
2 3	. 5650	. 4350	.5232	. 7031	.1490	.3257	. 4567	. 5433 . 5414	58 57
4	. 5672 . 5694	. 4328 . 4306	.5227 .5222	. 7082 . 7133	.1483 .1477	.3260 .3263	. 4586 . 4605	. 5394	56
5	.65716	.34284	1.5217	.87184	1.1470	1.3267	.24624	75375	55
6	. 5737	4262	.5212	. 7235	.1463	.3270	. 4644	. 5356	54
7	. 5759	. 4240	.5207	. 7287	.1456	.3274	. 4663	. 5337	53
8	. 5781	. 4219	.5202	. 7338	.1450	.3277	. 4682	. 5318	52
9	. 5803	4197	.5197	. 7389	.1443	.3280	. 4701	. 5299	51
10	.65825	.34175	1.5192	.87441	1.1436 .1430	1.3284 .3287	.24720 . 4739	.75280 . 5261	50 49
11 12	. 5847 . 5869	. 4153 . 4131	.5187 .5182	. 7492 . 7543	.1423	.3290	4758	5241	48
13	. 5891	4109	.5177	7595	.1416	.3294	4778	5222	47
14	5913	4087	.5171	. 7646	.1409	.3297	4797	5203	46
15	.65934	.34065	1.5166	.87698	1.1403	1.3301	.24816	.75184	45
16	. 5956	. 4043	.5161	. 7749	.1396	.3304	. 4835	. 5165	44
17	. 5978	. 4022	.5156	. 7801	.1389	.3307	. 4854	. 5146	43
18	. 6000	. 4000	.5151	. 7852	.1383	.3311	. 4873	. 5126	42
19	. 6022	3978	.5146	. 7904	.1376	.3314	. 4893	. 5107	41
20	.66044	.33956	1.5141	.87955	1.1369 .1363	1.3318 .3321	.24912	.75088	40 39
20 21 22	. 6066 . 6087	. 3934	.5136 .5131	. 8007 . 8058	.1356	.3324	. 4931 . 4950	. 5049	38
23	6109	3891	.5126	. 8110	.1349	3328	4970	5030	37
24	6131	. 3869	5121	. 8162	.1343	.3331	4989	5011	36
25	.66153	.33847	1.5116	.88213	1.1336	1.3335	.25008	.74992	35
26	. 6175	. 3825	.5111	8265	.1329	.3338	. 5027	. 4973	34
27 28	. 6197	. 3803	.5106	. 8317	.1323	.3342	. 5047	. 4953	33
28 7	. 6218	3781	.5101	. 8369	.1316	.3345	. 5066	. 4934	32
29	. 6240	3760	.5096	. 8421	.1309	.3348	. 5085	. 4915	31
80	.66262	.33738 .3716	1.5092 .5087	.88472 . 8524	1.1303 .1296	1.3352 .3355	. 5124	.74895 . 4876	30
31 32	6305	3694	.5082	8576	.1290	.3359	. 5143	4857	29 28
33	6327	3673	.5077	8628	.1283	.3362	. 5162	4838	27
34	. 6349	. 3651	.5072	. 8680	.1276	.3366	. 5181	. 4818	26
35	.66371	.33629	1.5067	.88732	1.1270	1.3369	.25201	.74799	25
36	. 6393	. 3607	.5062	. 8784	.1263	.3372	. 5220	. 4780	24
37	. 6414	. 3586	.5057	. 8836	.1257 .1250	.3376	. 5239	4760	23 22
38 39	. 6436 . 6458	. 3564	.5052	. 8888 . 8940	.1250	.3379	. 5259	4741	21
40	.66479	.33520	1.5042	.88992	1.1237	1.3386	. 5278	.74702	20
41	6501	3499	.5037	. 9044	.1230	.3390	. 5317	4683	19
42	6523	3477	.5032	. 9097	.1224	.3393	. 5336	4664	18
43	6545	. 3455	.5027	. 9149	.1217	.3397	. 5355	. 4644	17
44	. 6566	. 3433	.5022	. 9201	.1211	.3400	. 5375	. 4625	16
45	.66588	.33412	1.5018	.89253	1.1204	1.3404	.25394	.74606	15
46	. 6610	. 3390	.5013	. 9306	.1197	.3407	. 5414	. 4586	14
47 48	. 6631 . 6653	. 3368	.5008	. 9358	.1191	.3411	. 5433	. 4567 . 4548	13 12
49	. 6675	. 3325	.4998	. 9463	.1178	.3418	. 5472	4528	lii
50	.66697	.33303	1.4993	.89515	1.1171	1.3421	.25491	.74509	10
51	. 6718	. 3282	.4988	. 9567	.1165	.3425	. 5510	. 4489	9
52	. 6740	. 3260	.4983	. 9620	.1158	.3428	. 5530	. 4470	8 7
53	. 6762	. 3238	.4979	. 9672	.1152	.3432	. 5549	. 4450	7
54	. 6783	. 3217	.4974	. 9725	.1145	.3435	. 5569	. 4431	6
55	.66805	.33195	1.4969	.89777	1.1139	1.3439	.25588	.74412	5 4
56 57	. 6826 . 6848	3173	.4964	. 9830	.1132	.3442	. 5608	4392	4
58	. 6870	. 3152 . 3130	.4959	. 9882 . 9935	.1126 .1119	.3446	. 5627	• 4373 • 4353	3 2
59	6891	3108	.4949	9988	.1113	.3453	. 5666	. 4334	Ιí
60	. 6913	3087	.4945	.90040	.1106	.3456	. 5685	4314	ō
									_
M.	Corina	Vrs. sin.	Secant	Cotang.	Tang.	Cosec'nt	Vrs cos	Sine.	M.

42°	Netucal	Trigonometrical	Empetions
74	Marmiar	i i igonometi icai	I WHICHIOMS.

42	,	Na	tural li	rigonom	etrical	Function	ns.	1	37 ^u
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.66913	.33087	1.4945	.90040	1.1106	1.3456	.25685	.74314	60
0 1 2 3 4 5 6 7	. 6935	3065	.4940	. 0093	.1100	.3460	. 5705	. 4295	59
2	. 6956	3044	.4935	. 0146	.1093	.3463	. 5724	4275	58
3	. 6978 . 6999	. 3022	.4930 .4925	. 0198	.1086 .1080	.3467 .3470	. 5744 . 5763	. 4256 . 4236	57 56
5	.67021	32979	1.4921	.90304	1.1074	1.3474	.25783	.74217	55
6	. 7043	. 2957	.4916	. 0357	.1067	.3477	. 5802	4197	54
7	. 7064	. 2936	.4911	. 0410	.1061	.3481	. 5822	. 4178	53
8	. 7086	. 2914	.4906	. 0463	.1054	.3485	. 5841	. 4158	52
9 10	. 7107 .67129	. 2893 .32871	.4901 1.4897	. 0515	.1048 1.1041	.3488 1.3492	. 5861 .25880	. 4139 .74119	51 50
ii	7150	2849	.4892	. 0621	.1035	.3495	. 5900	. 4100	49
12	. 7150 . 7172 . 7194	2828	.4887	. 0674	.1028 .1022	.3499	. 5919	. 4080	48
13	. 7194	. 2806	.4882	. 0727	.1022	.3502	. 5939	. 4061	47
14	. 7215	2785	.4877	. 0780	.1015	.3506	. 5959	. 4041	46
15 16	.67237 . 7258	.32763 . 2742	1.4873 .4868	.90834 . 0887	1.1009 .1003	1.3509 .3513	.25978 .5998	.74022	45
17	7280	2720	.4863	. 0940	.0996	.3517	6017	3983	43
iš	. 7301	2699	.4858	. 0993	.0990	.3520	. 6037	3963	42
19	. 7323	. 2677	.4854	. 1046	.0983	.3524	. 6056	. 3943	41
20	.67344	.32656	1.4849	.91099	1.0977	1.3527	.26076	.73924	40
21 22	. 7366 . 7387	. 2634 . 2613	.4844	. 1153 . 1206	.0971	.3531 .3534	. 6096 . 6115	. 3904 . 3885	39 38
23	7409	2591	.4835	1259	.0958	.3538	6135	. 3865	37
24	. 7430	2570	.4830	. 1312	.0951	.3542	. 6154	3845	36
25	.67452	.32548	1.4825	.91366	1.0945	1.3545	.26174	.73826	35
26	. 7473	. 2527	.4821	. 1419	.0939	.3549	. 6194	. 3806	34
27	. 7495 . 7516	. 2505 . 2484	.4816 .4811	. 1473 . 1526	.0932	.3552 .3556	. 6213 . 6233	. 3787 . 3767	33 32
27 28 29	. 7537	2462	.4806	1580	.0920	.3560	6253	. 3747	31
30	.67559	.32441	1.4802	.91633	1.0913	1.3563	.26272	.73728	30
31	. 7580	. 2419	.4797	. 1687	.0907	.3567	. 6292	. 3708	29
32	. 7602	2398	.4792	. 1740	.0900	.3571	. 6311	. 3688	28
33 34	. 7623 . 7645	2377 2355	.4788 .4783	. 1794 . 1847	.0894	.3574	. 6331 . 6351	. 3669 . 3649	27 26
35	.67666	32334	1.4778	.91901	1.0881	1.3581	.26371	.73629	25
36	7688	2312	.4774	. 1955	.0875	.3585	. 6390	. 3610	24
37	. 7709	. 2291	.4769	. 2008	.0868	.3589	. 6410	. 3590	23 22
38	. 7730	2269	.4764	. 2062	.0862	.3592	. 6430	3570	22
39 40	. 7752 .67773	. 2248 .32227	.4760 1.4755	. 2116 .92170	.0856 1.0849	.3596 1.3600	. 6449	. 3551 .73531	21 20
41	. 7794	2205	.4750	. 2223	.0843	.3603	. 6489	. 3511	19
12	7816	2184	.4746	2277	.0837	.3607	. 6508	. 3491	18
43	. 7837	. 2163	.4741	. 2331	.0830	.3611	. 6528	. 3472	17
44	. 7859	. 2141	.4736	2385	.0824	.3614	. 6548	. 3452	16
45 46	.67880 .7901	.32120 . 2098	1.4732 .4727	.92439	1.0818	1.3618 .3622	. 6587	.73432 . 3412	15 14
47	7923	2077	.4723	. 2493 . 2547	.0805	.3625	6607	. 3393	13
48	7944	2056	.4718	. 2601	.0799	.3629	. 6627	. 3373	12
49	. 7965	. 2034	.4713	. 2655	.0793	.3633	. 6647	. 3353	11
50	.67987	.32013	1.4709	.92709	1.0786	1.3636	.26666	.73333	10
51 52	8008 8029	. 1992 . 1970	.4704	2763 2817	.0780	.3640 .3644	. 6686 . 6706	3314	8
53	8051	1949	.4699 .4695	2871	.0767	.3647	6726	3274	1 %
54	8072	1928	.4690	2926	.0761	.3651	. 6746	. 3254	6
55	.68093	.31907	1.4686	.92980	1.0755	1.3655	.26765	.73234	7 6 5 4
56	. 8115	. 1885	.4681	. 3034	.0749	.3658	. 6785	. 3215	4
57	. 8136 . 8157	. 1864	.4676	3088	.0742	.3662	6805	. 3195	3 2
58 59	. 8178	. 1843 . 1821	.4672 .4667	. 3143 3197	.0736 .0730	.3666 .3669	. 6825 . 6845	. 3175 . 3155	ī
60	. 8200	. 1800	.4663	. 3251	.0724	.3673	. 6865	3135	Ô
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.
132	20								470

439	•	Na	tural T	rigonom	etrical	Punctio	ns.	1.	36°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.68200	.31800	1.4663	.93251	1.0724	1.3673	.26865	.73135	60
1	. 8221	. 1779	.4658	. 3306	.0717	.3677	. 6884	. 3115	59
2	. 8242	1758	.4654	. 3360	.0711	.3681	. 6904	. 3096	58
3	. 8264	1736	.4649	. 8415	.0705	.3684	6924	. 3076	57
4 · 5	. 8285 .68306	. 1715 .31694	.4644 1.4640	. 3469 .93524	.0699 1.0692	.3688 1.3692	. 6944	. 3056 .73036	56
6	. 8327	1673	.4635	3578	.0686	.3695	. 6984	3016	55 54 53 52
7	8349	1651	.4631	3633	.0680	.3699	7004	2996	53
8	8370	. 1630	.4626	. 3687	.0674	.3703	7023	. 2976	52
9	. 8391	. 1609	.4622	. 3742	.0667	.3707	. 7043	. 2956	51
10	.68412	.31588	1.4617	.93797	1.0661	1.3710	.27063	,72937	50 49
11	. 8433	1566	.4613	. 3851	.0655	.3714	. 7083	. 2917	49
12 13	. 8455 . 8476	. 1545 . 1524	.4608 .4604	. 3906 . 3961	.0649	.3718 .3722	. 7103 . 7123	. 2897 . 2877	48 47
14	. 8497	1503	4599	4016	.0636	.3725	7143	2857	46
15	.68518	31482	1.4595	.94071	1.0630	1.3729	.27163	.72837	45
16	8539	. 1460	.4590	4125	.0624	.3733	. 7183	2817	44
17	. 8561	. 1439	.4586	. 4180	.0618	.3737	. 7203	. 2797	43
18	. 8582	. 1418	.4581	. 4235	.0612	.3740	. 7223	. 2777	42
19	. 8603	. 1397	.4577	. 4290	.0605	.3744	. 7243	2757	41
20 21 22 23	.68624	.31376	1.4572	.94345	1.0599	1.3748	.27263	.72737	40
21	. 8645 . 8666	. 1355 . 1333	.4568 .4563	. 4400 . 4455	.0593 .0587	.3752	7283	. 2717 . 2697	39 38
93	8688	1312	.4559	4510	.0581	.3756 .3759	7322	2677	37
24	8709	1291	4554	4565	.0575	.3763	7342	2657	36
24 25	.68730	.31270	1.4550	94620	1.0568	1.3767	.27362	.72637	35
26	. 8751	. 1249	.4545	. 4675	.0562	.3771	. 7382	. 2617	34
26 27 28 29	. 8772	. 1228	.4541	. 4731	.0556	.3774	. 7402	. 2597	37 36 35 34 33 32
28	. 8793	. 1207	.4536	. 4786	.0550	.3778	. 7422	. 2577	32
30	. 8814	. 1186	.4532 1.4527	. 4841 .94896	.0544	.3782	. 7442	. 2557	31
81	.68835 .8856	.31164 . 1143	.4523	. 4952	1.0538 .0532	1.3786 .3790	.27462 . 7482	. 2517	30 29 28 27 26 25 24 23 22 21 20 19 18
32	8878	1122	.4518	5007	.0525	.3794	7503	2497	28
33	. 8899	1101	.4514	5062	.0519	.3797	7523	2477	27
34	. 8920	. 1080	.4510	. 5118	.0513	.3801	. 7543	. 2457	26
85	.68941	.31059	1.4505	.95173	1.0507	1.3805	.27563	.72437	25
86	. 8962	1038	.4501	. 5229	.0501	.3809	. 7583	. 2417	24
37 88	. 8983 . 9004	. 1017	.4496 .4492	. 5284 . 5340	.0495	.3813	. 7603 . 7623	2397	23
39	9025	. 0975	.4487	. 5395	.0483	.3816 .3820	7(43	2357	21
40	.69046	.30954	1.4483	.95451	1.0476	1.3824	27663	.72337	20
11	. 9067	. 0933	.4479	. 5506	.0470	.3828	. 7683	. 2317	19
42	. 9088	. 0912	.4474	. 5562	.0464	.3832	. 7703	. 2297	18
43	. 9109	. 0891	.4470	. 5618	.0458	.3836	7723	. 2277	17
44	. 9130	. 0870	.4465	. 5673	.0452	.3839	. 7743	. 2256	16
45 46	.69151 . 9172	.30849	1.4461 .4457	.95729 . 5785	1.0446 .0440	1.3843 .3847	.27764	.72236	15 14
47	9193	. 0807	.4452	. 5841	.0434	.3851	7804	2196	13
48	9214	. 0786	.4448	. 5896	.0428	.3855	7824	. 2176	12
49	9235	. 0765	.4443	. 5952	.0422	.3859	. 7844	. 2156	11
50	.69256	.30744	1.4439	.96008	1.0416	1.3863	.27864	.72136	10
51	. 9277	. 0723	.4435	. 6064	.0410	.3867	. 7884	. 2115	9
52	. 9298	. 0702	.4430	. 6120	.0404	.3870	. 7904	. 2095	8 7
53 54	. 9319	. 0681	.4426 .4422	. 6176 . 6232	.0397 .0391	.3874 .3878	. 7925 . 7945	. 2075 . 2055	1 6
55	.69361	.30639	1.4417	.96288	1.0385	1.3882	27965	.72035	6 5
56	. 9382	. 0618	.4413	. 6344	.0379	.3886	7985	2015	4
56 57	. 9403	. 0597	.4408	. 6400	.0373	.3890	. 8005	. 1994	3
58	. 9424	. 0576	.4404	. 6456	.0367	.3894	. 8026	. 1974	3 2 1
59	. 9445	. 0555	.4400	. 6513	.0361	.3898	. 8046	. 1954	
60	. 9466	. 0534	.4395	. 6569	.0355	.3902	. 8066	. 1934	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

449	•	Na	tural T	igonom	etrical l	135°			
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.69466	.30534	1.4395	.96569	1.0355	1.3902	.28066	.71934	60
1	. 9487	. 0513	.4391	. 6625	.0349	.3905	. 8086	. 1914	59
2	. 9508	0492	.4387	. 6681	.0343	.3909	8106	. 1893	58
3	. 9528 . 9549	. 0471	.4382 .4378	. 6738 . 6794	.0337	,3913 .3917	. 8127 . 8147	. 1873 . 1853	57 56
4 5 6 7	.69570	.30430	1.4374	.96850	1.0325	1.3921	.28167	.71833	55
6	. 9591	. 0409	.4370	. 6907	.0319	.3925	. 8187	. 1813	54
7	. 9612	. 0388	.4365	. 6963	.0313	.3929	. 8208	, 1792	53
8	. 9633	. 0367	.4361	. 7020	.0307	.3933 .3937	. 8228 . 8248	. 1772	52
9 10	. 9654 .69675	.30325	.4357 1.4352	. 7076 .97133	.0301 1.0295	1.3941	.28268	. 1752 .71732	51 50
ii	9696	0304	.4348	7189	.0289	.3945	8289	. 1711	49
12	9716	0283	.4344	. 7246	.0283	.3949	. 8309	. 1691	48
13	. 9737	0263	.4339	. 7302	.0277	.3953	. 8329	. 1671	47
14	. 9758	. 0242	.4335	. 7359	.0271	.3957	. 8349 .28370	. 1650 .71630	46
15	.69779 . 9800	.30221	1.4331 .4327	.97416 . 7472	1.0265 .0259	1.3960 .3964	. 8390	. 1610	45 14
16 17	. 9821	0179	.4322	7529	.0253	3968	. 8410	1589	43
18	9841	0158	4318	. 7586	.0247	3972	. 8431	. 1569	42
19	9862	0138	.4314	. 7643	.0241	.3976	. 8451	. 1549	41
20	.69883	.30117	1.4310	.97699	1.0235	1.3980	.28471	.71529	40
21 22	. 9904	. 0096	4305	. 7756	.0229	.3984	. 8492	1508	39
23	9925 9945	. 0075	.4301 .4297	. 7813 . 7870	.0223	.3988 .3992	. 8512 . 8532	. 1488 . 1468	38 37
24	9966	0034	4292	7927	.0212	3996	. 8553	1447	36
25	.69987	30013	1.4288	97984	1.0206	1.4000	.28573	.71427	35
	.70008	.29992	.4284	. 8041	.0200	.4004	. 8593	. 1406	34
26 27 28 29	. 0029	. 9971	.4280	. 8098	.0194	.4008	. 8614	. 1386	33
28	. 0049	9950	.4276	. 8155 . 8212	.0188	.4012 .4016	. 8634 . 8654	. 1366 . 1345	32 31
30	. 0070	. 9930	.4271 1.4267	.98270	.0182 1.0176	1.4020	.28675	71325	30
31	. 0112	9888	.4263	8327	.0170	.4024	. 8695	. 1305	29
32	. 0132	. 9867	.4259	8384	.0164	.4028	. 8716	. 1284	28
33	. 0153	. 9847	.4254	. 8441	.0158	.4032	. 8736	. 1264	27
34	. 0174	9826	.4250	. 8499	.0152	.4036	. 8756	. 1243	26 25
35 36	.70194 . 0215	. 9785	1.4246 .4242	.98556 . 8613	1.0146 .0141	1.4040 .4044	. 28777	. 1203	24
37	. 0236	9764	.4238	8671	.0135	.4048	. 8818	1182	23
38	0257	9743	.4233	8728	.0129	.4052	. 8838	. 1162	22
89	. 0277	. 9722	.4229	8786	.0123	.4056	. 8859	. 1141	21
40	.70298	.29702	1.4225	.98843	1.0117	1.4060	.28879	.71121	20
41	. 0319	. 9681	.4221	. 8901 . 8958	.0111 .0105	.4065	. 8899 . 8920	. 1100	19 18
4 2 4 3	. 0339	. 9660	.4217 .4212	. 9016	.0099	.4073	. 8940	1059	17
44	. 0381	. 9619	.4208	. 9073	.0093	.4077	8961	1039	16
45	.70401	.29598	1.4204	.99131	1.0088	1.4081	.28981	.71018	15
46	. 0422	. 9578	.4200	. 9189	.0082	.4085	. 9002	. 0998	14
47	. 0443	9557	.4196	9246	.0076	.4089	. 9022	. 0977	13 12
48 49	0463 . 0484	. 9536 . 9516	.4192	. 9304 . 9362	.0070	.4093	. 9063	. 0936	ii
50	.70505	.29495	1.4183	.99420	1.0058	1.4101	.29084	.70916	10
51	. 0525	. 9475	.4179	. 9478	.0052	.4105	. 9104	. 0895	9
52	. 0546	. 9454	.4175	9536	.0047	.4109	. 9125	. 0875	8 7
53	. 0566	. 9433	.4171	. 9593	.0041	.4113	. 9145	. 0854	6
54 55	. 0587 .70608	. 9413	.4167 1.4163	9651	1.0035	.4117 1.4122	. 9166	.70813	5
55 56	. 0628	. 9372	.4159	. 9767	.0023	.4126	9207	. 0793	4
57	. 0649	9351	.4154	. 9826	.0017	.4130	. 9228	. 0772	3
58	. 0669	. 9330	.4150	. 9884	.0012	.4134	. 9248	. 0752	3 2 1
59	. 0690	. 9310	.4146	. 9942	.0006	.4138	. 9269	0731	
60	. 0711	. 9289	.4142	1.0000	.0000	.4142	. 9289	. 0711	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

Squares, Cubes, Square Roots, Cube Roots, Circumferences and Circular Areas of Nos. from 1 to 520

						
No.	Square	Cube	Sq. Root	Cube Root		CLE
			- Dq. Root		Circum.	Area
1	ı	ı	1.0000	1.0000	3.142	0.7854
2	4	1 8	1.4142	1.2599	6.283	
		1				3.1416
3	9 16	27	1.7321	1.4422	9.425	7.0686
4		64	2.0000	1.5874	12.566	12.5664
5	25	125	2.2361	1.7100	15.708	19.6350
6	36	216	2.4495	1.8171	18.850	28.2743
7 8	49	343	2.6458	1.9129	21.991	38.4845
8	64	512	2.8284	2.0000	25.133	50.2655
9	81	729	3.0000	2.0801	28.274	63.6173
10	100	1000	3.1623	2.1544	31.416	78.5398
11	121	1331	3.3166	2.2240	34.558	95.033
12	144	1728	3.4641	2.2894	37.699	113.007
13	169	2197	3.6056	2.3513	40.841	132.732
14	196	2744	3.7417	2.4101	43.982	153.938
15	225	3375	3.8730	2.4662	47.124	176.715
16	256	4096	4.0000	2.5198	50.265	201.062
17	280	4913	4.1231	2.5713	53.407	226.980
18	324	5832	4.2426	2.6207	56.549	254.469
19	361	6859	4.3589	2.6684	59.690	283.529
20	400	8000	4.4721	2.7144	62.832	314.159
21	441	9261	4.5826	2.7589	65.973	346.361
22	484	10648	4.6904	2.8020	69.115	380.133
	529	12167	4.7958	2.8439	72.257	415.476
23	576	13824	4.8990	2.8845		452.389
24		15625	5.0000		75.398	490.874
25	625	15025	3.0000	2.9240	78.540	490.074
26	676	17576	5.0990	2.9625	81.681	530.929
27 28	729	19683	5.1962	3.0000	84.823	572.555
28	784	21952	5.2915	3.0366	87.965	615.752
29	841	24389	5.3852	3.0723	91.106	660.520
30	900	27000	5.4772	3.1072	94.248	706.858
31	961	29791	5.5678	3.1414	90.389	754.768
32	1024	32768	5.6569	3.1748	100.531	804.248
33	1080	35937	5.7446	3.2075	103.673	855.299
34	1156	39304	5.8310	3.2396	106.814	907.920
35	1225	42875	5.9161	3.2711	109.956	962.113
36	1206	46656	6.0000	3.3019	113.007	1017.88
37	1369	50653	6.0828	3.3322	116.239	1075.21
37 38	1444	54872	6.1644	3.3620	119.381	1134.11
-	1521	• •	6.2450	3.3012	122.522	1194.59
39 40	1600	59319	6,3246	3.4200	125.660	1256.64
40	1,000	1 54000	0.3240	3.42.00	123.000	1230.04

SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

		1			Cm	CLE
No.	Square	Cube	Sq. Root	Cube Root	Circum.	Area
				-	Circuii.	
41	1681	68921	6.4031	3.4482	128.81	1320.25
42	1764	74088	6.4807	3.4760	131.95	1385.44
4.3	1840	79507	6.5574	3.5034	135.00	1452.20
44	1936	85184	6.6332	3.5303	138.23	1520.53
45	2025	91125	6.7082	3.5569	141.37	1590.43
_						
46	2116	97336	6.7823	3.5830	144.51	1661.90
47	2209	103823	6.8557	3.6088	147.65	1734-94
48	2304	110592	6.9282	3.6342	150.80	1809.56
49	2401	117649	7.0000	3.6593	153.94	1885.74
50	2500	125000	7.0711	3.6840	157.08	1963.50
51	2601	132651	7.1414	3.7084	160.22	2042.82
52	2704	140608	7.2111	3.7325	163.36	2123.72
53	2809	148877	7.2801	3.7563	166.50	2206.18
54	2916	157464	7.3485	3.7798	169.65	2290.22
55	3025	166375	7.4162	3.8030	172.79	2375.83
56	3136	175616	7.4833	3.8259	175.93	2463.01
57	3249	185193	7.5498	3.8485	179.07	2551.76
58	3364	195112	7.6158	3.8709	182.21	2642.08
59 6 0	3481	205379	7.6811	3.8930	185.35	2733.97
60	3600	216000	7.7460	3.9149	188.50	2827.43
61	3721	226981	7.8102	3.9365	191.64	2922.47
62	3844	238328	7.8740	3.9579	194.78	3019.07
63	3969	250047	7.9373	3.9791	197.92	3117.25
64	4096	262144	8.0000	4.0000	201.06	3216.99
65	4225	274625	8.0623	4.0207	204.20	3318.31
66	4356	287496	8.1240	4.0412	207.35	3421.19
67	4489	300763	8.1854	4.0615	210.49	3525.65
68	4624	314432	8.2462	4.0817	213.63	3631.68
6 9	4761	328509	8.3066	4.1016	216.77	3739.28
70	4900	343000	8.3666	4.1213	219.91	3848.45
71	5041	357911	8.4261	4.1408	223.05	3959.19
72	5184	373248	8.4853	4.1602	226.19	4071.50
73	5329	389017	8.5440	4.1793	229.34	4185.39
74	5476	405224	8.6023	4.1983	232.48	4300.84
7 5	5625	421875	8.6603	4.2172	235.62	4417.86
76	5776	438976	8.7178	4.2358	238.76	4536.46
77	5929	456533	8.7750	4.2543	241.90	4656.63
78	6084	474552	8.8318	4.2727	245.04	4778.36
79 80	6241	493039	8.8882	4.2908	248.19	4901.67
80	6400	512000	8.9443	4.3089	251.33	5026.55
		1	<u> </u>	1	!	

SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

	AND C	IRCULAR F	TREAS OF A	105. FRO	4 1 10 52	
No.	Square	Cube	Sq. Root	Cube Root		CLE
110.	Square	Cube	Sq. Root	Cube Root	Circum.	Area
8τ	6561	531441	9.0000	4.3267	254.47	5153.00
82	6724	551368	9.0554	4-3445	257.61	5281.02
83	6889	571787	9.1104	4.3621	260.75	5410.61
84	7056	592704	9.1652	4.3795	263.89	5541.77
85	7225	614125	9.2195	4.3968	267.04	5674.50
					0	-0-00
86	7396	636056	9.2736	4.4140	270.18	5808.80
87	7569	658503	9.3274	4.4310	273.32	5944.68
88	7744	681472	9.3808	4.4480	276.46	6082.12
89	7921	704969	9.4340	4.4647	279.60	6221.14
90	8100	729000	9.4868	4.4814	282.74	6361.73
91	8281	753571	9.5394	4.4979	285.88	6503.88
92	8464	778688	9.5917	4.5144	289.03	6647.61
93	8649	804357	9.6437	4.5307	292.17	6792.91
93 94	8836	830584	9.6954	4.5468	295.31	6939.78
9 4 95	9025	857375	9.7468	4.5629	298.45	7088.22
93	9023	05/3/3	' ' '	4.3029	290.45	7000.22
96	9216	884736	9.7980	4.5789	301.59	7238.23
97	9409	912673	9.8489	4.5947	304.73	7389.81
98	9604	941192	9.8995	4.6104	307.88	7542.96
99	9801	970299	9.9499	4.6261	311.02	7697.69
100	10000	1000000	10.0000	4.6416	314.16	7853.98
101	10201	1030301	10.0499	4.6570	317.30	8011.85
102	10404	1061208	10.0995	4.6723	320.44	8171.28
103	10600	1001200	10.1489	4.6875	323.58	8332.20
104	10816	1124864	10.1489	4.7027	326.73	8494.87
	1	1157625		1	320.73	8659.01
105	11025	1157025	10.2470	4.7177	329.07	1
106	11236	1191016	10.2956	4.7326	333.01	8824.73
107	11449	1225043	10.3441	4.7475	336.15	8992.02
108	11664	1259712	10.3923	4.7622	339.29	9160.88
100	11881	1295029	10.4403	4.7769	342.43	9331.32
110	12100	1331000	10.4881	4.7914	345.58	9503.32
111	12321	1367631	10.5357	4.8059	348.72	9676.89
111	12321	1404928	10.5830	4.8203	351.86	9852.03
		1404928	10.5330	4.8346		10028.7
113	12769			4.8488	355.00	
114	12996	1481544	10.6771	4.8629	358.14	10207.0
115	13225	1520875	10.7238	4.0029	361.28	10386.9
116	13456	1560896	10.7703	4.8770	364.42	10568.3
117	13689	1601613	10.8167	4.8910	367.57	10751.3
118	13924	1643032	10.8628	4.9049	370.71	10935.9
119	14161	1685159	10.9087	4.9187	373.85	11122.0
120	14400	1728000	10.9545	4.9324	376.99	11309.7
			1			

SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

No. Company Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color Color						
No.	Square	Cube	Sq. Root	Cube Root	Circum.	Area
					Circuit.	Aica
121	14641	1771561	11.0000	4.9461	380.13	11499.0
122	14884	1815848	11.0454	4-9597	383.27	11689.9
123	15129	1860867	11.0905	4.9732	386.42	11882.3
124	15376	1906624	11.1355	4.9866	389.56	12076.3
125	15625	1953125	11.1803	5.0000	392.70	12271.8
3		-9333		January		
126	15876	2000376	11.2250	5.0133	395.84	12469.0
127	16129	2048383	11.2694	5.0265	398.98	12667.7
128	16384	2097152	11.3137	5.0397	402.12	12868.0
129	16641	2146689	11.3578	5.0528	405.27	13069.8
130	16900	2197000	11.4018	5.0658	408.41	13273.2
131	.17161	2248091	11.4455	5.0788	411.55	13478.2
132	17424	2299968	11.4891	5.0016	414.60	13684.8
133	17689	2352637	11.5326	5.1045	417.83	13892.9
134	17956	2406104	11.5758	5.1172	420.07	14102.6
135	18225	2460375	11.6190	5.1299	424.12	14313.9
	1	-400373	,	3.2-99	4-4	-43-3-9
136	18496	2515456	11.6619	5.1426	427.26	14526.7
137	18769	2571353	11.7047	5.1551	430.40	14741.1
138	19044	2628072	11.7473	5.1676	433-54	14957.1
139	19321	2685619	11.7898	5.1801	436.68	15174.7
140	19600	2744900	11.8322	5.1925	439.82	15393.8
141	19881	2803221	11.8743	5.2048	442.96	15614.5
142	20164	2863288	11.9164	5.2171	446.11	15836.8
143	20449	2924207	11.9583	5.2293	449.25	16060.6
144	20736	2985984	12.0000	5.2415	452.39	16286.0
145	21025	3048625	12.0416	5.2536	455.53	16513.0
146	21316	3112136	12.0830	5.2656	458.67	16741.5
147	21609	3176523	12.1244	5.2776	461.81	16971.7
148	21904	3241792	12.1655	5.2896	464.96	17203.4
149	22201	3307949	12.2066	5.3015	468.10	17436.6
150	22500	3375000	12.2474	5.3133	471.24	17671.5
151	22801	3442951	12.2882	5.3251	474.38	17907.9
152	23104	3511808	12.3288	5.3368	477.52	18145.8
153	23409	3581577	12.3693	5.3485	480.66	18385.4
154	23716	3652264	12.4097	5.3601	483.81	18626.5
155	24025	3723875	12.4499	5.3717	486.95	18869.2
156	24336	3796416	12.4900	5.3832	490.09	19113-4
157	24649	3869893	12.5300	5.3947	493.23	19359.3
158	24964	3944312	12.5698	5.4061	496.37	19606.7
159	25281	4019679	12.6005	5.4175	499.51	19855.7
160	25600	4096000	12.6491	5.4288	502.65	20106.2
	-3550	1		3.4200	,,,,,,	-5155.2

Squares, Cubes, Square Roots, Cube Roots, Circumferences and Circular Areas of Nos. from 1 to 520

	CIRCLE					
No.	Square	Cube	Sq. Root	Cube Root		
					Circum.	Area
161	05007	4772087	12.6886	F 4407	505.80	20258
162	2592I 26244	4173281	12.7279	5.4401	508.94	20358.3
163	26569			5.4514	512.08	20867.2
		4330747	12.7671	5.4626		
164 165	26896	4410944	12.8452	5-4737 5-4848	515.22 518.36	21124.1
105	27225	4492125	12.0452	5.4040	510.30	21382.5
166	27556	4574296	12.8841	5-4959	521.50	21642.4
167	27889	4657463	12.9228	5.5069	524.65	21904.0
168	23224	4741632	12.9615	5.5178	527.79	22167.1
160	28561	4826800	13.0000	5.5288	530.93	22431.8
170	28900	4913000	13.0384	5.5397	534.07	22698.0
-,-		49-3000	-31-3-4	3.3391	3347	-209010
171	29241	5000211	13.0767	5.5505	537.21	22965.8
172	29584	5088448	13.1149	5.5613	540.35	23235.2
173	29929	5177717	13.1529	5.5721	543.50	23506.2
174	30276	5268024	13.1909	5.5828	546.64	23778.7
175	30625	5359375	13.2288	5.5934	549.78	24052.8
176	30976	5451776	13.2665	5.6041	552.92	24328.5
177	31329	5545233	13.3041	5.6147	556.06	24605.7
178	31684	5639752	13.3417	5.6252	559.20	24884.6
179	32041	5735339	13.3791	5.6357	562.35	25164.9
180	32400	5832000	13.4164	5.6462	565.49	25446.9
181	6-		6		-60 6-	
182	32761	5929741	13.4536	5.6567	568.63	25730.4
183	33124	6028568	13.4907	5.6671	571.77	26015.5
	33489	6128487	13.5277	5.6774	574.91	26302.2
184	33856	6229504	13.5647	5.6877	578.05	26590.4
185	34225	6331625	13.6015	5.6980	581.19	26880.3
186	34596	6434856	13.6382	5.7083	584.34	27171.6
187	34969	6539203	13.6748	5.7185	587.48	27464.6
188	35344	6644672	13.7113	5.7287	590.62	27759.1
180	35721	6751269	13.7477	5.7388	593.76	28055.2
190	36100	6859000	15.7840	5.7489	596.90	28352.9
-90	30100	0039000	23.7040	3.7409	390.90	2033219
191	36481	6967871	13.8203	5.7590	600.04	28652.1
192	36864	7077888	13.8564	5.7690	603.19	28952.9
193	37249	7189057	13.8924	5.7790	606.33	29255.3
194	37636	7301384	13.9284	5.7890	609.47	29559.2
195	38025	7414875	13.9642	5.7989	612.61	29864.8
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196	38416	7529536	14.0000	5.8088	615.75	30171.9
197	38809	7645373	14.0357	5.8186	618.89	30480.5
198	39204	7762392	14.0712	5.8285	622.04	30790.7
199	39601	7880599	14.1067	5.8383	625.18	31102.6
200	40000	8000000	14.1421	5.8480	628.32	31415.9
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Squares, Cubes, Square Roots, Cube Roots, Circumferences and Circular Areas of Nos. from 1 to 520

Crp					CLE	
No.	Square	Cube	Sq. Root	Cube Root	Circum.	Area
		 		l	Circuii.	~
201	40401	8120601	14.1774	5.8578	631.46	31730.9
202	40804			5.8675	634.60	32047.4
203	41200	8365427	14.2127	5.8771	637.74	32365.5
203	41616	8489664	14.2829	5.8868	640.89	32685.1
-	42025	8615125	14.3178	5.8964	644.03	33006.4
205	42025	0015125	14.3170	3.0904	044.03	33000.4
206	42436	8741816	14.3527	5.9059	647.17	33329.2
207	42849	8869743	14.3875	5.9155	650.31	33653.5
208	43264	8998912	14.4222	5.9250	653.45	33979.5
200	43681	9129329	14.4568	5.9345	656.59	34307.0
210	44100	9261000	14.4914	5-9439	659.73	34636.1
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211	44521	9393931	14.5258	5-9533	662.88	34966.7
212	44944	9528128	14.5602	5.9627	666.02	35298.9
213	45369	9663597	14.5945	5.9721	669.16	35632.7
214	45796	9800344	14.6287	5.9814	672.30	35968.1
215	46225	9938375	14.6629	5.9907	675-44	36305.0
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216	46656	10077696	14.6969	6.0000	678.58	36643.5
217	47089	10218313	14.7300	6.0092	681.73	36983.6
218	47524	10360232	14.7648	6.0185	684.87	37325.3
219	47961	10503459	14.7986	6.0277	688.01	37668.5
220	48400	10648000	14.8324	6.0368	691.15	38013.3
221	48841	10793861	14.8661	6.0459	694.29	38359.6
221	49284	10941048	14.8997	6.0550	697.43	38707.6
	49729	11089567	14.0332	6.0641	700.58	39057.1
223 224	50176	11239424	14.9552	6.0732	703.72	39408.1
	50625	11390625	15.0000	6.0822	706.86	39760.8
225	30025	11390023	13.000	0.0022	700.00	39700.0
226	51076	11543176	15.0333	6.0912	710.00	40115.0
227	51529	11697083	15.0665	6.1002	713.14	40470.8
228	51984	11852352	15.0997	6.1001	716.28	40828.1
229	52441	12008989	15.1327	6.1180	719.42	41187.1
230	52000	12167000	15.1658	6.1260	722.57	41547.6
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231	53361	12326391	15.1987	6.1358	725.71	41909.6
232	53824	12487168	15.2315	6.1446	728.85	42273.3
233	54289	12649337	15.2643	6.1534	731.99	42638.5
234	54756	12812904	15.2971	6.1622	735-13	43005.3
235	55225	12977875	15.3297	6.1710	738.27	43373.6
236	55696	13144256	15.3623	6.1797	741.42	43743.5
237	56169	13312053	15.3948	6.1885	744.56	44115.0
238	56644	13481272	15.4272	6.1972	747.70	44488.1
239	57121	13651919	15.4596	6.2058	750.84	44862.7
240	57600	13824000	15.4919	6.2145	753.98	45238.9
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SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

	AND C	IRCULAR A	REAS OF	NOS. FRO	M 1 TO 52	<u> </u>
No.	l c	Cube	Sq. Root	Cube Root	Crr	CLE
140.	Square	Cube	Sq. Root	Cube Root	Circum.	Area
241	58081	13997521	15.5242	6.2231	757.12	45616.7
242	58564	14172488	15.5563	6.2317	760.27	45996.1
243	59049	14348907	15.5885	6.2403	763.41	46377.0
244	59536	14526784	15.6205	6.2488	766.55	46759.5
245	60025	14706125	15.6525	6.2573	769.69	47143.5
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246	60516	14886936	15.6844	6.2658	772.83	47529.2
247	61009	15069223	15.7162	6.2743	775-97	47916.4
248	61504	15252992	15.7480	6.2828	779.12	48305.1
249	62001	15438249	15.7797	6.2912	782.26	48695.5
250	62500	15625000	15,8114	6.2996	785.40	49087.4
057	63001	15813251	15.8430	6.3080	788.54	49480.9
251 252	63504	16003008	15.8745	6.3164	791.68	49875.9
252 253	64009	16194277	15.0745	6.3247	794.82	50272.6
	64516	16387064	15.9374	6.3330	797.96	50670.7
254	65025	16581375	15.9374	6.3413	801.11	51070.5
255	05025	10301373	15.9007	0.3413	001.11	310/0.5
256	65536	16777216	16.0000	6.3496	804.25	51471.9
257	66049	16974593	16.0312	6.3579	807.39	51874.8
258	66564	17173512	16.0624	6.3661	810.53	52279.2
259	67081	17373979	16.0935	6.3743	813.67	52685.3
26o	67600	17576000	16.1245	6.3825	81ŏ.8i	53092.9
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261	68121	17779581	16.1555	6.3907	819.96	53502.1
262	68644	17984728	16.1864	6.3988	823.10	53912.9
263	69169	18191447	16.2173	6.4070	826.24	54325.2
264	6 9696	18399744	16.2481	6.4151	829.38	54739.1
265	70225	18609625	16.2788	6.4232	832.52	55154.6
266	6	-006	-6	6	904 66	55571.6
267	70756	18821096	16.3095	6.4312	835.66 838.81	
267 268	71289 71824	19034163	16.3401	6.4393	841.95	55990.3
		19248832	16.3707	6.4473		56410.4
269	72361	19465109	16.4012	6.4553	845.09 848.23	57255·5
270	72900	19083000	16.4317	6.4633	040.23	3/233.3
271	73441	19902511	16.4621	6.4713	851.37	57680.4
272	73984	20123648	16.4924	6.4792	854.51	58106.9
273	74529	20346417	16.5227	6.4872	857.66	58534.9
274	75076	20570824	16.5529	6.4951	860.80	58964.6
275	75625	20796875	16.5831	6.5030	863.94	59395.7
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276	76176	21024576	16.6132	6.5108	867.08	59828.5
277	76729	21253933	16.6433	6.5187	870.22	60262.8
278	77284	21484952	16.6733	6.5265	873.36	60698.7
279	77841	21717639	16.7033	6.5343	876.50	61136.2
280	78400	21952000	16.7332	6.5421	879.65	61575.2
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SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

				Ī	CIR	CLE
No.	Square	Cube	Sq. Root	Cube Root	Circum.	Area
281	78961	22188041	16.7631	6.5499	882.79	62015.8
282	79524	22425768	16.7929	6.5577	885.93	62458.0
283	80089	22665187	16.8226	6.5654	889.07	62901.8
284	80656	22906304	16.8523	6.5731	892.21	63347.1
285	81225	23149125	16.8819	6.5808	895.35	63794.0
286	81796	23393656	16.9115	6.5885	898.50	64242.4
287	82369	23639903	16.9411	6.5962	901.64	64692.5
288	82944	23887872	16.9706	6.6039	904.78	65144.1
289	83521	24137569	17.0000	6.6115	907.92	65597.2
290	84100	24389000	17.0294	6.6191	911.06	66052.0
291	84681	24642171	17.0587	6.6267	914.20	66508.3
292	85264	24897088	17.0880	6.6343	917.35	66966.2
293	85849	25153757	17.1172	6.6419	920.49	67425.6
294	86436	25412184	17.1464	6.6494	923.63	67886.7
295	87025	25672375	17.1756	6.6569	926.77	68349.3
296	87616	25934336	17.2047	6.6644	929.91	68813.5
297	88209	26198073	17.2337	6.6719	933.05	69279.2
298	88804	26463592	17.2627	6.6794	936.19	69746.5
299	89401	26730899	17.2916	6.6860	939.34	70215-4
300	90000	27000000	17.3205	6.6943	942-48	70685.8
301	90601	27270901	17.3494	6.7018	945.62	71157.9
302	91204	27543608	17.3781	6.7092	948.76	71631.5
303	91809	27818127	17.4069	6.7166	951.90	72106.6
304	92416	28094464	17.4356	6.7240	955.04	72583-4
305	93025	28372625	17.4642	6.7313	958.19	73061.7
306	93636	28652616	17.4929	6.7387	961.33	73541.5
307	94249	28934443	17.5214	6.7460	964.47	74023.0
308	94864	29218112	17.5499	6.7533	967.61	74506.0
309	95481	29503629	17.5784	6.7606	970.75	74990.6
310	96100	29791000	17.6068	6.7679	973.89	75476.8
311	96721	30080231	17.6352	6.7752	977.04	75964.5
312	97344	30371328	17.6635	6.7824	980.18	76453.8
313	97969	30664297	17.6918	6.7897	983.32	76944.7
314	98596	30959144	17.7200	6.7969	986.46	77437.1
315	99225	31255875	17.7482	6.8041	989 .60	77931.1
316	99856	31554496	17.7764	6.8113	992.74	78426.7
317	100489	31855013	17.8045	6.8185	995.88	78923.9
318	101124	32157432	17.8326	6.8256	999.03	79422.6
319	101761	32461759	17.8606	6.8328	1002.20	79922.9
320	102400	32768000	17.8885	6.8399	1005.30	80424.8
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SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

		T T		T	Cri	CLE
No.	Square	Cube	Sq. Root	Cube Root	Circum.	Area
321	103041	33076161	17.9165	6.8470	1008.5	80928.2
322	103684	33386248	17.9444	6.8541	6.1101	81433.2
323	104329	33698267	17.9722	6.8612	1014.7	81939.8
324	104976	34012224	18.0000	6.8683	1017.9	82448.0
325	. 105625	34328125	18.0278	6.8753	1021.0	82957.7
326	106276	34645976	18.0555	6.8824	1024.2	83469.0
327	106929	34965783	18.0831	6.8894	1027.3	83981.8
328	107584	35287552	18.1108	6.8964	1030.4	84496.3
329	108241	35611289	18.1384	6.9034	1033.6	85012.3
330	108900	35937000	18.1659	6.9104	1036.7	85529.9
331	109561	36264691	18.1934	6.9174	1039.9	86049.0
332	110224	36594368	18.2200	6.9244	1043.0	86569.7
333	110889	36926037	18.2483	6.9313	1046.2	87092.0
334	111556	37259704	18.2757	6.9382	1049.3	87615.9
3 35	112225	37595375	18.3030	6.9451	1052.4	88141.3
336	112896	37933056	18.3303	6.9521	1055.6	88668.3
337	113569	38272753	18.3576	6.9589	1058.7	89196.9
338	114244	38614472	18.3848	6.9658	1061.9	89727.0
339	114921	38958219	18.4120	6.9727	1065.0	90258.7
340	115600	39304000	18.4391	6.9795	1068.1	90792.0
341	116281	39651821	18.4662	6.9864	1071.3	91326.9
342	116964	40001688	18.4932	6.9932	1074-4	91323.3
343	117649	40353607	18.5203	7.0000	1077.6	92401.3
344	118336	40707584	18.5472	7.0068	1080.7	92940.9
345	119025	41063625	18.5742	7.0136	1083.8	93482.0
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346	119716	41421736	18.6011	7.0203	1087.0	94024.7
347	120409	41781923	18.6279	7.0271	1090.1	94569.0
348	121104	42144192	18.6548	7.0338	1093.3	95114.9
349	121801	42508549	18.6815	7.0406	1096.4	95662.3
350	122500	42875000	18.7083	7.0473	1099.6	96211.3
351	123201	43243551	18.7350	7.0540	1102.7	96761.8
352	123904	43614208	18.7617	7.0607	1105.8	97314.0
353	124609	43986977	18.7883	7.0674	1109.0	97867.7
354	125316	44361864	18.8149	7.0740	1112.1	98423.0
355	126025	44738875	18.8414	7.0807	1115.3	98979.8
356	126736	45118016	18.8680	7.0873	1118.4	99538.2
357	127449	45499293	18.8944	7.0940	1121.5	100098
358	128164	45882712	18.9209	7.1006	1124.7	100660
359	128881	46268279	18.9473	7.1072	1127.8	101223
360	129600	46656000	18.9737	7.1138	1131.0	101788
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Squares, Cubes, Square Roots, Cube Roots, Circumferences and Circular Areas of Nos. from 1 to 520

AND CIRCULAR AREAS OF NOS. FROM 1 10 320						
No.	Square	Cube	Sq. Root	Cube Root		
					Circum.	Area
361	120201	47045881	70.0000	7.1204	TT24 T	700254
301	130321		19.0000	7.1269	1134.1	102354
362	131044	47437928	19.0263		1137.3	102922
363	131769	47832147	19.0526	7.1335	1140.4	103491
364	132496	48228544	19.0788	7.1400	1143.5	104062
365	133225	48627125	19.1050	7.1466	1146.7	104635
366	133956	49027896	19.1311	7.1531	1149.8	105209
367	134689	49430863	19.1572	7.1596	1153.0	105785
368	135424	49836032	19.1833	7.1661	1156.1	106362
369	136161	50243409	19.2094	7.1726	1159.2	106941
370	136900	50653000	19.2354	7.1791	1162.4	107521
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371	137641	51064811	19.2614	7.1855	1165.5	108103
372	138384	51478848	19.2873	7.1920	1168.7	108687
373	139129	51895117	19.3132	7.1984	1171.8	109272
374	139876	52313624	19.3391	7.2048	1175.0	109858
375	140625	52734375	19.3649	7.2112	1178.1	110447
376	141376	53157376	19.3907	7.2177	1181.2	111036
377	142129	53582633	19.4165	7.2240	1184.4	111628
378	142884	54010152	19.4422	7.2304	1187.5	112221
379	143641	54439939	19.4679	7.2368	1190.7	112815
379 380	144400	54872000	19.4936	7.2432	1193.8	113411
•	144400	348/2000	19.4930	7.2432	1193.0	113411
381	145161	55306341	19.5192	7.2495	1196.9	114009
382	145924	55742968	19.5448	7.2558	1200.1	114608
383	146689	56181887	19.5704	7.2622	1203.2	115209
384	147456	56623104	19.5959	7.2685	1206.4	115812
385	148225	57066625	19.6214	7.2748	1209.5	116416
386	148996	57512456	19.6469	7.2811	1212.7	117021
3 ⁸ 7	149769	57960603	19.6723	7.2874	1215.8	117628
388 388			19.6977			11/028
300	150544	58411072		7.2936	1218.9	118237
389	151321	58863869	19.7231	7.2999	1222.1	
390	152100	59319000	19.7484	7.3061	1225.2	119459
391	152881	59776471	19.7737	7.3124	1228.4	120072
392	153664	60236288	19.7990	7.3186	1231.5	120687
393	154449	60698457	19.8242	7.3248	1234.6	121304
394	155236	61162984	19.8494	7.3310	1237.8	121922
395	156025	61629875	19.8746	7.3372	1240.9	122542
396	156816	62000126	19.8997	7 ,,,,	T244 F	123163
	157609	62099136		7.3434	1244.1	123103
397			19.9249	7.3496	1247.2	
398	158404	63044792	19.9499	7.3558	1250.4	124410
399	159201	63521199	19.9750	7.3619	1253.5	125036
400	160000	64000000	20.0000	7.3684	1256.6	125664
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SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES, AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

		1				
No.	Square	Cube	Sq. Root	Cube Root		CLE
	l			-	Circum.	Area
401	160801	64481201	20.0250	7.3742	1250.8	126203
402	161604	64964808	20.0499	7.3803	1262.0	126923
403	162400	65450827	20.0749	7.3864	1266.1	
404	163216	65939264	20.0998	7.3925	1269.2	127556
405	164025	66430125	20.1246	7.3925	-	128190
405	104025	00430125	20.1240	7.3900	1272.3	128825
406	164836	66923416	20.1494	7.4047	1275.5	129462
407	165649	67419143	20.1742	7-4108	1278.6	130100
· 408	166464	67917312	20.1990	7-4169	1281.8	130741
409	167281	68417929	20.2237	7.4229	1284.9	131382
410	168100	68921000	20.2485	7.4290	1288.1	132025
411	168921	69426531	00 0707			
412	169744		20.2731	7-4350	1291.2	132670
	170569	69934528	20.2978	7.4410	1294.3	133317
413		70444997	20.3224	7.4470	1297.5	133965
414	171396	70957944	20.3470	7.4530	1300.6	134614
415	172225	71473375	20.3715	7-4590	1303.8	135265
416	173056	71991296	20.3961	7.4650	1306.9	135918
417	173889	72511713	20.4206	7.4710	1310.0	136572
418	174724	73034632	20.4450	7-4770	1313.2	137228
419	175561	73560059	20.4695	7.4829	1316.3	137885
420	176400	74088000	20.4939	7.4889	1319.5	138544
421	177241	74618461	20.5183	7.4948	1322.6	139205
422	178084	75151448	20.5426	7.5007	1325.8	139867
423	178929	75686967	20.5670	7.5067	1328.9	140531
424	179776	76225024	20.5913	7.5126	1332.0	141196
425	180625	76765625	20.6155	7.5185	1335.2	1411963
_		1		1.5105	1333.4	141003
426	181476	77308776	20.6398	7.5244	1338 .3	142531
427	182329	77854483	20.6640	7.5302	1341.5	143201
428	183184	78402752	20.6882	7.5361	1344.6	143872
429	184041	78953589	20.7123	7.5420	1347 .7	144545
430	184900	79507000	20.7364	7.5478	1350.9	145220
431	185761	80062991	20.7605	7.5537	1354.0	145896
432	186624	80621568	20.7846	7.5595	1357.2	146574
433	187489	81182737	20.8087	7.5654	1360.3	147254
434	188356	81746504	20.8327	7.5712	1363.5	147934
435	189225	82312875	20.8567	7.5770	1366.6	148617
		" ."		1	•	
436	190096	82881856	20.8806	7.5828	1369.7	149301
437	190969	83453453	20.9045	7.5886	1372.9	149987
438	191844	84027672	20.9284	7.5944	1376.0	150674
439	192721	84604519	20.9523	7.6001	1379.2	151363
440	193600	85184000	20.9762	7.6059	1382.3	152053
	<u> </u>	·		<u>' </u>		

SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

No. Square Cube Sq. Root Cube Root Circum. Area		1 .	1		T	Сп	CLE
441 194481 85766121 21.0000 7.6117 1385.4 152745 442 195364 86350888 21.0238 7.6174 1388.6 153439 443 196249 86938307 21.0476 7.6232 1391.7 154134 444 197136 87528384 21.0713 7.6289 1394.9 154830 445 198016 88716536 21.1187 7.6040 1398.0 155528 446 198016 89716536 21.1187 7.6460 1404.3 156030 447 199800 89314623 21.11896 7.6574 1410.6 158337 450 202500 91125000 21.2132 7.6631 1413.7 157633 451 203401 91733851 21.2368 7.6688 1416.9 159751 452 204304 92345408 21.2637 7.6744 1420.0 160460 453 205161 93576664 21.3073 7.6857 1425.1 16183 <th>No.</th> <th>Square</th> <th>Cube</th> <th>Sq. Root</th> <th>Cube Root</th> <th></th> <th></th>	No.	Square	Cube	Sq. Root	Cube Root		
442 195364 86350888 21.0238 7.6174 1388.6 153439 443 196249 86938307 21.0476 7.6232 1391-7 154134 444 197136 87528384 21.0705 7.6289 1398.0 155228 446 198916 88716536 21.1187 7.6403 1401.2 156228 447 199809 89314623 21.1186 7.6517 1407-4 157633 448 200704 89915302 21.1860 7.6517 1407-4 157633 450 202500 91125000 21.2132 7.6631 1413.7 159033 451 203401 91733851 21.2368 7.6688 1416.9 159751 452 204304 92345408 21.2368 7.6681 1420.0 160460 453 205200 92959677 21.2838 7.6801 1423.1 161171 452 204304 92345408 21.3567 7.6914 1420.0 160460 <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>							
443	441				7.6117		152745
444 197136 87528384 21.0713 7.6289 1394.9 154830 445 198025 88121125 21.0950 7.6346 1398.0 155528 446 198016 88716536 21.1187 7.6403 1401.2 156228 447 199809 80314623 21.1187 7.6400 1404.3 156930 448 200704 89915302 21.1600 7.6574 1410.6 157633 450 202500 90518849 21.1896 7.6674 1410.6 159751 451 203401 91733851 21.2368 7.6688 1416.9 159751 452 204304 92345408 21.2603 7.6744 1420.0 160460 453 205209 92959677 21.2838 7.6857 1426.3 162597 455 207936 94818816 21.3574 7.6970 1432.6 163313 457 208849 95443993 21.3542 7.6970 1435.7 164030 <td></td> <td></td> <td></td> <td>21.0238</td> <td></td> <td>1388.6</td> <td>153439</td>				21.0238		1388.6	153439
445 198025 88121125 21.0950 7.6346 1398.0 155528 446 198916 88716536 21.1187 7.6403 1401.2 156228 447 199809 89314623 21.1187 7.6400 1401.2 156228 447 199809 89314623 21.11860 7.6571 1407.4 157633 448 200704 89915392 21.1860 7.6571 1407.4 157633 450 202500 9112500 21.1896 7.6571 1410.7 159043 451 203401 91733851 21.2368 7.6688 1416.9 159751 452 204304 92345408 21.2363 7.6681 1413.7 159043 451 204304 92345408 21.2368 7.6688 1416.9 150751 452 204304 92345408 21.2363 7.6857 1426.3 16183 453 20793 94818816 21.3542 7.6970 1432.6 163313	443			21.0476	7.6232	1391.7	154134
446 198916 88716536 21.1187 7.6403 1401.2 156228 447 199809 89314623 21.1424 7.6460 1404.3 156930 448 200704 89915392 21.1660 7.6517 1407.4 157633 450 202500 91125000 21.2132 7.6631 1413.7 159043 451 203401 91733851 21.2368 7.6688 1416.9 159751 452 204304 92345408 21.2603 7.6744 1420.0 160460 453 205209 92959677 21.2838 7.6801 1423.1 161171 454 206116 93576664 21.3073 7.6954 1420.0 160460 455 207025 94196375 21.3307 7.6914 1429.4 162597 456 207036 94818816 21.3542 7.6070 1432.6 163313 457 208849 95443993 21.3776 7.7026 1435.7 164030 458 209764 96071912 21.4009 7.7082 1438.9 164748 459 210681 907336000 21.4476 7.7194 1445.1 166190 97336000 21.4476 7.7194 1445.1 166190 460 21500 97336000 21.4476 7.7194 1445.1 166914 462 213444 98611128 21.4942 7.7306 1451.4 167639 465 216225 100544625 21.5639 7.7473 1460.8 169823 466 219021 10054065 21.5870 7.7529 1464.0 170554 467 218089 101847563 21.6102 7.7584 1467.1 171287 470 220900 103823000 21.600 7.7850 1470.3 172021 470 220900 103823000 21.6564 7.7695 1473.4 172277 470 220900 103823000 21.6564 7.7695 1473.4 172277 470 220900 103823000 21.6564 7.7695 1473.4 172277 470 220900 103823000 21.6564 7.7695 1473.4 172277 470 220900 103823000 21.6564 7.7695 1473.4 172277 470 220900 103823000 21.6564 7.7695 1473.4 172277 470 220900 103823000 21.6564 7.7695 1473.4 172277 470 220900 103823000 21.6564 7.7695 1473.4 172277 470 220900 103823000 21.6564 7.7695 1473.4 172277 470 220900 103823000 21.6564 7.7695 1470.3 172021 474 222784 105154048 21.7256 7.7860 1482.8 174074 472 222784 105154048 21.7256 7.7860 1482.8 174074 472 222784 105154048 21.7256 7.7860 1482.8 174074 473 222784 105154048 21.7256 7.7860 1482.8 174074 473 222784 105154048 21.7256 7.7860 1482.8 174074 17052 27750 106496424 21.7715 7.7900 1489.1 176460 175716 476 226576 107850176 21.8174 7.8079 1495.4 179052 179052 1790523 21.8662 7.8188 1501.7 179451 479 229441 109902239 21.8861 7.8243 1504.8 180203				21.0713	7.6289	1394.9	154830
447 199809 89314623 21.1424 7.6460 1404.3 156930 448 200704 89915392 21.1660 7.6517 1407.4 157633 7.5509 202500 91125000 21.2132 7.6631 1413.7 159043 451 203401 91733851 21.2368 7.6688 1416.9 159043 452 204304 92345408 21.2603 7.6744 1420.0 160460 453 205209 92959677 21.2838 7.6861 1423.1 161171 454 206116 93576664 21.3073 7.6857 1426.3 161883 455 207025 94196375 21.3307 7.6914 1429.4 162597 456 207036 94818816 21.3542 7.6970 1432.6 163313 457 208849 95443993 21.3776 7.7026 1435.7 164030 458 209764 96071912 21.4009 7.7082 1438.9 164748 459 210681 96702579 21.4243 7.7138 1442.0 165468 460 211600 97336000 21.4476 7.7194 1445.1 166190 461 212521 97072181 21.4709 7.7250 1448.3 166914 462 213444 98611128 21.4902 7.7362 1454.6 168365 166225 100544625 21.5639 7.7473 1460.8 169823 466 217156 101194696 21.5870 7.7418 1457.7 169093 465 216225 100544625 21.5639 7.7750 1448.3 169823 460 219961 103161709 21.6564 7.7695 1473.4 172287 470 220900 103823000 21.6795 7.7750 1470.3 172021 172021 172021 103823000 21.6795 7.7750 1470.3 172021 172021 172021 172022 103823000 21.6795 7.7750 1470.5 173494 471 221841 104487111 21.7025 7.7805 1479.7 174234 172757 17362 1436.0 175766 173494 172 222784 105154048 21.7256 7.7805 1479.7 174234 172757 173494 172257 17364 1740.3 172051 173494 172 222784 105154048 21.7256 7.7805 1479.7 174234 172757 173494 1742 222784 105154048 21.7256 7.7805 1479.7 174234 172757 173494 172757 173494 172757 173494 1742275 105851333 21.8403 7.8134 1498.5 174974 172752 108531333 21.8403 7.8134 1498.5 177052 17706 1479 229441 109902239 21.8861 7.8243 1504.8 150203	445	198025	88121125	21.0950	7.6346	1398.0	155528
448 200704 89915392 21.1660 7.6517 1407.4 157633 449 201601 90518849 21.1896 7.6574 1410.6 158337 450 202500 91125000 21.2132 7.6631 1413.7 159043 451 203401 91733851 21.2368 7.6688 1416.9 159751 452 204304 92345408 21.2603 7.6744 1420.0 160460 453 205209 92959677 21.2838 7.6857 1426.3 161171 454 206116 93576664 21.3073 7.6857 1426.3 161883 455 207036 94818816 21.3377 7.6914 1429.4 162597 456 207036 94818816 21.3542 7.6970 1432.6 163313 457 208849 95443993 21.3776 7.7026 1435.7 164030 450 216081 96702579 21.4243 7.7138 1442.0 165468 <td>446</td> <td></td> <td>88716536</td> <td>21.1187</td> <td>7.6403</td> <td>1401.2</td> <td>156228</td>	4 46		88716536	21.1187	7.6403	1401.2	156228
448 200704 89915392 21.1660 7.6517 1407.4 157633 449 201601 90518849 21.1896 7.6574 1410.6 158337 450 202500 91125000 21.2132 7.6631 1413.7 159043 451 203401 91733851 21.2368 7.6688 1416.9 150751 452 204304 92345408 21.203 7.6744 1420.0 160460 453 205209 92959677 21.2838 7.6857 1426.3 161171 454 206116 93576664 21.3073 7.6857 1426.3 161883 455 207936 94818816 21.3776 7.6970 1432.6 163313 457 208849 95443993 21.3776 7.7026 1435.7 164030 458 209764 96702579 21.4243 7.7138 1442.0 165468 450 210681 96702579 21.4243 7.7194 1445.1 166190 <td></td> <td>199809</td> <td>89314623</td> <td>21.1424</td> <td>7.6460</td> <td>1404.3</td> <td>156930</td>		199809	89314623	21.1424	7.6460	1404.3	156930
449 201601 90518849 21.1896 7.6574 1410.6 158337 450 202500 91125000 21.2132 7.6631 1413.7 159043 451 203401 91733851 21.2368 7.6688 1416.9 159751 452 204304 92345408 21.2603 7.6744 1420.0 160460 453 205209 92959677 21.2838 7.6861 1423.1 161171 454 206116 93576664 21.3073 7.6857 1426.3 161883 455 207025 94196375 21.3307 7.6914 1429.4 162597 456 207936 94818816 21.3542 7.6970 1432.6 163313 457 208849 95443993 21.3776 7.7026 1435.7 164030 459 210681 96702579 21.4243 7.7138 1442.0 165468 450 211600 97336000 21.4476 7.7194 1445.1 166190 <td>448</td> <td>200704</td> <td>89915392</td> <td>21.1660</td> <td>7.6517</td> <td>1407.4</td> <td></td>	448	200704	89915392	21.1660	7.6517	1407.4	
450 202500 91125000 21.2132 7.6631 1413.7 159043 451 203401 91733851 21.2368 7.6688 1416.9 159751 452 204304 92345408 21.2603 7.6744 1420.0 160460 453 205209 92959677 21.2838 7.6861 1423.1 161171 454 206116 93576664 21.3073 7.6857 1426.3 161883 455 207025 94196375 21.3307 7.6914 1429.4 162597 456 207936 94818816 21.3542 7.6970 1432.6 163313 457 208849 95443993 21.3776 7.7026 1435.7 164330 458 209764 96071912 21.4009 7.7082 1438.9 165468 450 216081 96702579 21.4243 7.7138 1442.0 165468 460 213444 98611128 21.4709 7.7250 1448.3 166019 <td>449</td> <td>201601</td> <td>90518849</td> <td>21.1896</td> <td>7.6574</td> <td>1410.6</td> <td></td>	449	201601	90518849	21.1896	7.6574	1410.6	
452 204304 92345408 21.2603 7.6744 1420.0 160460 453 205209 92959677 21.2838 7.6801 1423.1 161171 454 206116 93576664 21.3073 7.6857 1426.3 161883 455 207025 94196375 21.3307 7.6914 1429.4 162597 456 207936 94818816 21.3542 7.6970 1432.6 163313 457 208849 95443993 21.3776 7.7026 1435.7 164030 458 209764 96071912 21.4009 7.7082 1438.9 164748 459 210681 96702579 21.4243 7.7138 1442.0 165468 460 211600 97336000 21.4476 7.7194 1445.1 166190 461 212521 97972181 21.4709 7.7250 1448.3 166914 462 213444 98611128 21.4942 7.7306 1451.4 167639 463 214369 99252847 21.5174 7.7362 1454.6 168365 464 215296 99897344 21.5407 7.7418 1457.7 169093 465 216225 100544625 21.5639 7.7473 1460.8 169823 466 217156 101194696 21.5870 7.7529 1464.0 170554 467 218089 101847563 21.6102 7.7584 1467.1 171287 468 219024 102503232 21.6333 7.7639 1470.3 172021 469 219961 103161709 21.6564 7.7695 1473.4 172271 470 220900 103823000 21.6795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7860 1482.8 174974 472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 476 226576 107850176 21.8174 7.8079 1495.4 177052 476 226576 107850176 21.8174 7.8079 1495.4 177052 477 227529 108531333 21.8403 7.8134 1498.5 178701 478 228484 109215352 21.8861 7.8243 1504.8 180203	450	202500	91125000	21.2132		1413.7	
452 204304 92345408 21.2603 7.6744 1420.0 160460 453 205209 92059677 21.2838 7.6801 1423.1 161181 454 206116 93576664 21.3073 7.6857 1426.3 161883 455 207025 94196375 21.3307 7.6914 1429.4 162597 456 207936 94818816 21.3542 7.6970 1432.6 163313 457 208849 95443993 21.3776 7.7026 1435.7 164030 458 209764 96071912 21.4009 7.7082 1438.9 164748 459 210681 96702579 21.4243 7.7138 1442.0 165468 460 211600 97336000 21.4476 7.7194 1445.1 166190 461 212521 97072181 21.4709 7.7250 1448.3 166914 462 213444 98611128 21.4709 7.7250 1448.3 166914 463 214369 99252847 21.5174 7.7362 1454.6 168365 464 215296 99897344 21.5407 7.7418 1457.7 169093 465 216225 100544625 21.5639 7.74473 1460.8 169823 466 217156 101194696 21.5870 7.7529 1464.0 170554 467 218089 101847563 21.6102 7.7584 1467.1 171287 468 219024 102503232 21.6333 7.7639 1470.3 172021 469 219961 103161709 21.6564 7.7695 1473.4 172287 470 220900 103823000 21.6795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7860 1482.8 174974 472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 476 226576 107850176 21.8174 7.8079 1495.4 177025 476 226576 107850176 21.8174 7.8079 1495.4 177025 476 226576 107850176 21.8174 7.8079 1495.4 177025 476 226576 107850176 21.8174 7.8079 1495.4 177025 477 227529 108531333 21.8403 7.8134 1498.5 178701 479 229441 109902239 21.8861 7.8243 1504.8 1500.3						1416.9	159751
453 205209 92959677 21.2838 7.6801 1423.1 161171 454 206116 93576664 21.3073 7.6857 1426.3 161883 455 207025 94196375 21.3307 7.6914 1429.4 162597 456 207936 94818816 21.3542 7.6970 1432.6 163313 457 208849 95443993 21.3776 7.7026 1435.7 104030 458 209764 96071912 21.4009 7.7082 1438.9 164748 459 210681 96702579 21.4243 7.7138 1442.0 165468 460 211600 97336000 21.4476 7.7194 1445.1 166190 461 212521 97972181 21.4709 7.7250 1448.3 166914 462 213444 98611128 21.4942 7.7306 1451.4 167639 463 214369 99252847 21.5174 7.7362 1454.6 168365 464 215296 99897344 21.5407 7.7418 1457.7 160903 465 216225 100544625 21.5639 7.7473 1460.8 169823 466 217156 101194696 21.5870 7.7529 1464.0 170554 467 218089 101847563 21.6102 7.7584 1467.1 171287 468 219024 102503232 21.6333 7.7639 1470.3 172021 470 220900 103823000 21.6564 7.7055 1473.4 172757 470 220900 103823000 21.6795 7.7850 1470.5 173494 471 221841 104487111 21.7025 7.7860 1482.8 174974 473 223729 105823817 21.7945 7.8025 1492.3 179504 477 2225525 107171875 21.7945 7.8025 1492.3 179050 476 226556 107850176 21.8174 7.8079 1495.4 179052 476 226576 107850176 21.8174 7.8079 1495.4 179052 17706 477 227529 108531333 21.8403 7.8134 1498.5 179016 479 229441 109902239 21.8861 7.8243 1504.8 150203	452	204304	92345408		7.6744	1420.0	
455 207025 94196375 21.3307 7.6914 1429.4 162597 456 207036 94818816 21.3542 7.6970 1432.6 163313 457 208849 95443993 21.3776 7.7026 1435.7 164030 458 209764 96071912 21.4009 7.7082 1438.9 164748 459 210681 96702579 21.4243 7.7138 1442.0 165468 460 211600 97336000 21.4476 7.7194 1445.1 166190 461 212521 97972181 21.4709 7.7250 1448.3 166914 462 213444 98611128 21.49042 7.7306 1451.4 167639 463 214369 99252847 21.5174 7.7362 1454.6 168365 464 215296 99897344 21.5407 7.7418 1457.7 160903 465 216225 100544625 21.5639 7.7473 1460.8 169823 466 217156 101194696 21.5870 7.7584 1467.1 171287 468 219024 102503232 21.6333 7.7639 1470.3 172021 469 219961 103161709 21.6564 7.7695 1473.4 172257 470 220900 103823000 21.0795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7805 1479.7 174234 472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 474 224676 106496424 21.7715 7.7970 1489.1 176460 475 225525 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177952 476 226576 107850176 21.8174 7.8079 1495.4 177952 477 227529 108531333 21.8403 7.8134 1498.5 178701 478 228484 109215352 21.8632 7.8188 1501.7 179451 479 229441 109902339 21.8861 7.8243 1504.8 180203				21.2838		1423.1	161171
455 207025 94196375 21.3307 7.6914 1429.4 162597 456 207936 94818816 21.3542 7.6970 1432.6 163313 457 208849 95443993 21.3776 7.7026 1435.7 164030 458 209764 96071912 21.4009 7.7082 1438.9 164748 459 210681 96702579 21.4243 7.7138 1442.0 165468 460 211600 97336000 21.4476 7.7194 1445.1 166190 461 212521 97972181 21.4709 7.7250 1448.3 166914 462 213444 98611128 21.4942 7.7306 1451.4 167639 463 214369 99252847 21.5174 7.7362 1454.6 168365 464 215296 99897344 21.5407 7.7418 1457.7 169093 465 216225 100544625 21.5639 7.7473 1460.8 169823 466 217156 101194696 21.5870 7.7529 1464.0 170554 467 218089 101847563 21.6102 7.7584 1467.1 171287 469 219961 103161709 21.6564 7.7695 1470.3 172021 470 220900 103823000 21.6795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7805 1479.7 174234 472 222784 105154048 21.7256 7.7805 1479.7 174234 472 222784 105154048 21.7256 7.7805 1479.7 174234 473 223729 105823817 21.7945 7.8025 1492.3 177052 1771875 21.7945 7.8025 1492.3 177052 17706 477 226576 107850176 21.8174 7.8079 1495.4 177052 177052 228484 109215352 21.8632 7.8188 1501.7 179451 479 229441 109902239 21.8861 7.8243 1504.8 150203				21.3073	7.6857	1426.3	161883
457 208849 95443993 21:3776 7.7026 1435.7 104030 458 209764 90071912 21:4009 7.7082 1438.9 164748 459 210681 90702579 21:4243 7.7138 1442.0 165468 460 211600 97336000 21:4476 7.7194 1445.1 166190 461 212521 97972181 21:4709 7.7250 1448.3 166914 462 213444 98611128 21:4942 7.7306 1451.4 167639 463 214369 99252847 21:5174 7.7362 1454.6 168365 404 215296 99897344 21:5407 7.7418 145.7 169093 465 216225 100544625 21:5639 7.7473 1460.8 169823 466 217156 101194696 21:5870 7.7529 1464.0 170554 467 218089 101847503 21:6102 7.7584 1467.1 171287 469 219961 103161709 21:6564 7.7695 1470-3 172021 470 220900 103823000 21:0795 7.7750 1470-3 172021 470 220900 103823000 21:0795 7.7750 1470-5 173494 471 221841 104487111 21:7025 7.7805 1470-7 174234 472 222784 105154048 21:7256 7.7805 1479.7 174234 473 223729 105823817 21:7486 7.7915 1486.0 175716 474 224676 106496424 21:7715 7.7970 1489.1 176460 475 225625 107850176 21:8174 7.8079 1495.4 177052 17807 478 228484 109215352 21:8632 7.8188 1501.7 179451 479 229441 109902239 21:8861 7.8243 1504.8 180203	455	207025	94196375	21.3307	7.6914	1429.4	162597
458 209764 96071912 21.4009 7.7082 1438.9 164748 459 210681 96702579 21.4243 7.7138 1442.0 165468 460 211600 97336000 21.4476 7.7194 1445.1 166190 461 212521 97972181 21.4709 7.7250 1448.3 166914 462 213444 98611128 21.4942 7.7306 1451.4 167639 463 214369 99252847 21.5174 7.7362 1454.6 168365 464 215296 99897344 21.5407 7.7418 1457.7 169093 465 216225 100544625 21.5639 7.7473 1460.8 169823 466 217156 101194696 21.5870 7.7529 1464.0 170554 467 218089 101847563 21.6102 7.7584 1467.1 171287 468 219024 102503232 21.6333 7.7639 1470.3 172021 469 219961 103161709 21.6564 7.7695 1473.4 172275 470 220900 103823000 21.6795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7805 1479.7 174234 472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 475 225625 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177055 476 226576 107850176 21.8174 7.8079 1495.4 177055 478 2228484 109215352 21.8632 7.8188 1501.7 170451 479 229441 109902239 21.8861 7.8243 1504.8 180203			94818816	21.3542	7.6970	1432.6	163313
459			95443993		7.7026	1435.7	
459 210681 96702579 21.4243 7.7138 1442.0 165468 460 211600 97336000 21.4476 7.7194 1445.1 160190 461 212521 97972181 21.4709 7.7250 1448.3 166914 462 213444 98611128 21.4942 7.7306 1451.4 167639 463 213590 99897344 21.5174 7.7362 1454.6 168365 465 216225 100544625 21.5639 7.7418 1457.7 169093 466 217156 101194696 21.5870 7.7529 1464.0 170554 467 218089 101847563 21.6102 7.7584 1467.1 171287 468 219024 102503232 21.6333 7.7639 1470.3 172201 470 220900 103823000 21.6564 7.7695 1473.4 172275 470 220900 103823000 21.6795 7.7860 1470.5 173	458			21.4009			
461 212521 97972181 21.4709 7.7250 1448.3 166914 462 213444 98611128 21.4942 7.7306 1451.4 167639 463 214369 99252847 21.5174 7.7362 1454.6 168365 464 215296 99897344 21.5407 7.7418 1457.7 169093 465 216225 100544625 21.5639 7.7473 1460.8 169823 466 217156 101194696 21.5870 7.7529 1464.0 170554 467 218089 101847563 21.6102 7.7584 1467.1 171287 468 219024 102503232 21.6333 7.7639 1470.3 172021 469 219961 103161709 21.6564 7.7695 1473.4 172257 470 220900 103823000 21.6795 7.7780 1476.5 173494 471 221841 104487111 21.7025 7.7805 1470.7 174234 472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 474 224676 106496424 21.7715 7.7970 1489.1 176460 475 225625 107850176 21.8174 7.8079 1495.4 177052 476 226576 107850176 21.8174 7.8079 1495.4 177052 476 226576 107850176 21.8174 7.8079 1495.4 177052 477 227529 108531333 21.8403 7.8134 1498.5 178701 479 229441 109902239 21.8861 7.8243 1504.8 180203					7.7138	1442.0	165468
462 213444 98611128 21.4942 7.7366 1451.4 167639 463 214369 99252847 21.5174 7.7362 1454.6 168365 464 215296 99897344 21.5407 7.7418 1457.7 169093 465 216225 100544625 21.5639 7.7473 1460.8 169823 466 217156 101194696 21.5870 7.7529 1464.0 170554 467 218089 101847563 21.6102 7.7584 1467.1 171287 468 219024 102503232 21.6333 7.7639 1470.3 172021 470 220900 103823000 21.6564 7.7605 1473.4 172757 470 220900 103823000 21.6564 7.7605 1473.4 172757 470 220900 103823000 21.6795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7805 1479.7 174234 472 222784 105154048 21.7256 7.7800 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 474 224676 106496424 21.7715 7.7970 1489.1 170460 475 225625 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177952 476 226576 107850176 21.8174 7.8079 1495.4 177952 477 227529 108531333 21.8632 7.8188 1501.7 170451 479 229441 109902239 21.8861 7.8243 1504.8 180203	460	211600	97336000	21.4476		1445.1	166190
463				21.4709	7.7250	1448.3	166914
464 215296 99897344 21.5407 7.7418 1457.7 169093 465 216225 100544625 21.5639 7.7473 1460.8 169823 466 217156 101194696 21.5870 7.7529 1464.0 170554 467 218089 101847563 21.6102 7.7584 1467.1 171287 468 219024 102503232 21.6333 7.7639 1470.3 172021 469 219961 103161709 21.6564 7.7695 1473.4 172757 470 220900 103823000 21.6795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7805 1479.7 174234 472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 474 224676 106496424 21.7715 7.7970 1489.1 176460 475 225025 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177952 477 227529 108531333 21.8403 7.8134 1498.5 178701 478 228484 109215352 21.8632 7.8188 1501.7 170451 170451 479 229441 109902239 21.8861 7.8243 1504.8 180203				21.4942	7.7306	1451.4	167639
465 216225 100544625 21.5639 7.7473 1460.8 169823 466 217156 101194696 21.5870 7.7529 1464.0 170554 467 218089 101847563 21.6102 7.7584 1467.1 171287 468 219024 102503232 21.6333 7.7639 1470.3 172021 469 219961 103161709 21.6564 7.7695 1473.4 172757 470 220900 103823000 21.6795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7805 1479.7 174234 472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 474 224676 10649624 21.7715 7.7970 1489.1 176460 475 225625 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177952 477 227529 108531333 21.8403 7.8134 1498.5 178701 478 228484 109215352 21.8632 7.8188 1501.7 170451 479 229441 109902239 21.8861 7.8243 1504.8 180203		214369		21.5174	7.7362	1454.6	168365
405 210225 100544625 21.5639 7.7473 1460.8 169823 466 217156 101194696 21.5870 7.7529 1464.0 170554 467 218089 101847563 21.6102 7.7584 1467.1 171287 468 219024 102503232 21.6333 7.7639 1470.3 172021 469 219961 103161709 21.6564 7.7605 1473.4 172757 470 220900 103823000 21.6795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7805 1479.7 174234 472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 474 224676 106496424 21.7715 7.7970 1489.1 176460 475 225525 107171875 21.8174 7.8079 1492.3 <t< td=""><td></td><td></td><td></td><td></td><td>7.7418</td><td>1457.7</td><td>169093</td></t<>					7.7418	1457.7	169093
467 218089 101847563 21.6102 7.7584 1467.1 171287 468 219024 102503232 21.6333 7.7639 1470.3 172021 469 219961 103161709 21.6564 7.7605 1473.4 172757 470 220900 103823000 21.6795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7805 1479.7 174234 472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 474 224676 106496424 21.7715 7.7970 1489.1 176460 475 225025 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177952 477 227529 108531333 21.8403 7.8134 1498.5 178701 478 228484 109215352 21.8632 7.8188 1501.7 170451 479 229441 109902239 21.8861 7.8243 1504.8 180203	465	216225	100544625	21.5639	7.7473	1460.8	169823
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		217156	101194696	21.5870	7.7529	1464.0	170554
408 219024 102503232 21.6333 7.7639 1470.3 172021 469 219961 103161709 21.6564 7.7605 1473.4 172757 470 220900 103823000 21.6795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7865 1479.7 174234 472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 474 224676 106496424 21.7715 7.7970 1489.1 176460 475 225525 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177952 477 227529 108531333 21.8403 7.8134 1498.5 178701 478 228484 109215352 21.8632 7.8188 1501.7 <t< td=""><td></td><td>218089</td><td>101847563</td><td>21.6102</td><td></td><td></td><td></td></t<>		218089	101847563	21.6102			
469 219961 103161709 21.6564 7.7695 1473.4 172757 470 220900 103823000 21.6795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7805 1479.7 174234 472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 474 224676 106496424 21.7715 7.7970 1489.1 176460 475 225025 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177952 477 227529 108531333 21.8403 7.8134 1498.5 178701 478 228484 109215352 21.88632 7.8188 1501.7 179451 479 229441 109902339 21.8861 7.8243 1504.8 <			102503232	21.6333	7.7639		
470 220900 103823000 21.6795 7.7750 1476.5 173494 471 221841 104487111 21.7025 7.7805 1479.7 174234 472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 474 224676 106496242 21.7715 7.7070 1489.1 176460 475 225625 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177952 477 227529 108531333 21.8403 7.8184 1501.7 179451 478 228484 109215352 21.8632 7.8188 1501.7 179451 479 229441 109902239 21.8861 7.8243 1504.8 180203		219961		21.6564	7.7695	1473.4	
472 222784 105154048 21.7256 7.7860 1482.8 174974 473 223729 105823817 21.7486 7.7915 1486.0 175716 474 224676 106496424 21.7715 7.7970 1489.1 176460 475 225625 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177952 477 227529 108531333 21.8403 7.8184 1501.7 179451 479 229441 109902239 21.8861 7.8243 1504.8 150203	470	220900	103823000	21.6795			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$						1479.7	174234
473 223729 105823817 21.7486 7.7915 1486.0 175716 474 224676 106496424 21.7715 7.7970 1489.1 176460 475 225625 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177952 477 227529 108531333 21.8403 7.8134 1498.5 178701 478 228484 109215352 21.8632 7.8188 1501.7 179451 479 229441 109902239 21.8861 7.8243 1504.8 180203				21.7256	7.7860	1482.8	
474 224676 106496424 21.7715 7.7970 1489.1 176460 475 225625 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177952 477 227529 108531333 21.8403 7.8134 1498.5 178701 478 228484 109215352 21.8632 7.8188 1501.7 179451 479 229441 109902239 21.8861 7.8243 1504.8 180203	473	223729		21.7486	7.7915	1486.0	
475 225625 107171875 21.7945 7.8025 1492.3 177205 476 226576 107850176 21.8174 7.8079 1495.4 177952 477 227529 108531333 21.8403 7.8134 1498.5 178701 478 228484 109215352 21.8632 7.8188 1501.7 179451 479 229441 109902239 21.8861 7.8243 1504.8 180203	474			21.7715	7.7970	1489.1	
477 227529 108531333 21.8403 7.8134 1498.5 178701 478 228484 109215352 21.8632 7.8188 1501.7 179451 479 229441 109902239 21.8861 7.8243 1504.8 180203	475	225625	107171875				
477 227529 108531333 21.8403 7.8134 1498.5 178701 478 228484 109215352 21.8632 7.8188 1501.7 179451 479 229441 109902239 21.8861 7.8243 1504.8 180203						1495.4	177952
478 228484 109215352 21.8632 7.8188 1501.7 179451 479 229441 109902239 21.8861 7.8243 1504.8 180203							
479 229441 109902239 21.8861 7.8243 1504.8 180203					7.8188		
		, , , ,					180203
	480	230400	110592000	21.9089	7.8297		

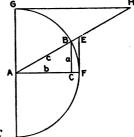
SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

	AND	IRCULAR A	READ OF	TOS. FROM		
No.	Square	Cube	Sq. Root	Cube Root		CLE
					Circum.	Area
.0-						
481	231361	111284641	21.9317	7.8352	1511.1	181711
482	232324	111980168	21.9545	7.8406	1514.3	182467
483	233289	112678587	21.9773	7.8460	1517-4	183225
484	234256	113379904	22.0000	7.8514	1520.5	183984
485	235225	114084125	22.0227 -	7.8568	1523.7	184745
486	236196	114791256	22.0454	7.8622	1526.8	185508
487	237169	115501303	22.0681	7.8676	1530.0	186272
488	238144	116214272	22.0907	7.8730	1533.1	187038
489	239121	116930169		7.8784	1536.2	187805
490	240100	117649000		7.8837	1539.4	188574
-		1	0,77	1		
491	241081	118370771	22.1585	7.8891	1542.5	189345
492	242064	119095488	22.1811	7.8944	1545.7	190117
493	243049	119823157	22.2036	7.8998	1548.8	190890
494	244036	120553784	22.2261	7.9051	1551.9	191665
495	245025	121287375	22.2486	7.9105	1555.1	192442
496	246016	122023936	22.2711	7.9158	1558.2	193221
497	247009	122763473	22.2935	7.9211	1561.4	194000
498	248004	123505992	22.3159	7.9264	1564.5	194782
499	249001	124251499	22.3383	7.9317	1567.7	195565
500	250000	125000000	22.3607	7.9370	1570.8	196350
501	251001	125751501	22.3830	7.9423	1573.9	197136
502	252004	1 26506008	22.4054	7.9476	1577.1	197923
503	253000	127263527	22.4277	7.9528	1580.2	198713
504	254016	128024064	22.4499	7.9581	1583.4	199504
505	255025	128787625	22.4722	7.9634	1586.5	200296
		120,0,023	22.4/22	' ' '	1300.3	200290
506	256036	129554216		7.9686	1589.7	201090
507	257049	130323843	22.5167	7.9739	1592.8	201886
508	258064	131096512	22.5389	7.9791	1595.9	202683
509	259081	131872229	22.5610	7.9843	1599.1	203482
510	260100	132651000	22.5832	7.9896	1602.2	204282
511	261121	133432831	22.6053	7.9948	1605.4	205084
512	262144	134217728		8.0000	1608.5	205887
513	263169	135005697	22.6495	8.0052	1611.Ğ	206692
514	264196	135796744	22.6716	8.0104	1614.8	207499
515	265225	136590875	22.6936	8.0156	1617.9	208307
516	266256	137388096	22.7156	8.0208	1621.1	200117
	267289	137388090		8.0260		209117
517 518	268324		22.7376		1624.2	209928
		138991832	22.7596	8.0311	1627.3	210741
519	269361	139798359	22.7816	8.0363	1630.5	211556
520	270400	140608000	22.8035	8.0415	1 6 33.6	212372
						·

Table 5. Trigonometric Functions and the Solution of Triangles

In the accompanying figure the trigonometric functions of the angle Abetween the lines B A and A C are as follows;

$$sin A = B C
cos A = A C
tan A = E F
cot A = G H
sec A = A E
cosec A = A H
ex-sec A = B E$$



In the right-angled triangle A B C let a equal the side B C opposite the angle A; let b equal the side A C opposite the angle B; let c equal A B, the side opposite the angle C.

Let $C = 90^{\circ}$ The following formulæ apply to right-angled triangles:

Angles.
$$A + B + C = 180^{\circ}$$
 Sides. $a = c \sin A = b \tan A$

$$A + B = 90^{\circ}$$

$$A = 90^{\circ} - B$$

$$B = 90^{\circ} - A$$

$$cos A = \frac{a}{c}$$

$$tan A = \frac{a}{b}$$

$$Area$$

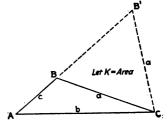
$$area = \frac{ab}{2}$$

$$area = \frac{ab}{2}$$

$$c = \sqrt{a^2 + b^2}$$

Oblique Triangles.

Note. Where an angle is more than 90° its sine, cosine, and tangent are equal to that of the angle (180° — the angle in question); that is, if the sine of 120° is desired take the sine of (180° — 120°) = 60°.



Given	Desired	Formulæ
A, B, a	C, b	$C = 180 - (A + B); b = \frac{a}{\sin A} \sin B$
	c, K	$c = \frac{a}{\sin A} \sin (A + B); K = \frac{a^2 \sin B \sin C}{2 \sin A}$
· A, a, b	В, С	$\sin B = \frac{\sin A}{a} b; C = 180^{\circ} - (A + B)$
	с	$c = \frac{a}{\sin A} \sin C$
	. ,	Two solutions are possible with B' as an acute angle and B as an obtuse angle
C, a, b	$\frac{1}{2}(A+B)$	$\frac{1}{3}(A+B) = 90^{\circ} - \frac{1}{3}C$
	$\frac{1}{2} (A - B)$	$\tan \frac{1}{2}(A-B) = \frac{a-b}{a+b} \tan \frac{1}{2}(A+B)$
	A B	$A = \frac{1}{2}(A + B) + \frac{1}{2}(A - B)$ $B = \frac{1}{2}(A + B) - \frac{1}{2}(A - B)$
	с	$c = (a - b) \frac{\sin \frac{1}{2} (A + B)}{\sin \frac{1}{2} (A - B)}$
	K	$K = \frac{1}{2} ab \sin C$
a, b, c	В	In the following formula $s = \frac{1}{2} (a + b + c)$
		$\sin \frac{1}{2} B = \sqrt{\frac{(s-a)(s-c)}{ac}}$
		$\sin B = \frac{2\sqrt{s(s-a)(s-b)(s-c)}}{ac}$
	K	$K = \sqrt{s(s-a)(s-b)(s-c)}$

EXPLANATION OF TABLES.

TABLE I. LOGARITHMS OF NUMBERS.—The logarithm of any number to any base is the index of the power to which the base must be raised to equal the number. The logarithms given in Table I are Briggs or Common Logarithms in which the base is 10. Then $100 = 10^2$, and the logarithm of 100 = 2. Also $200 = 10^{2.30103}$, and the logarithm of 200 = 2.30103. The integer of a logarithm is called the *characteristic*, and is one less than the number of integers in the number. The decimal part of the logarithm is called the *mantissa* and is given in Table I.

The mantissae of the logarithms in Table I are given to five places; while the numbers are given to four significant figures. Where there are more than four significant figures in the number, the table of proportional parts may be used. The star opposite certain logarithms shows that the two figures at the left are to be taken from the line below.

The logarithm of 1 is 0, and the logarithm of any number less than unity will be negative. It is much more convenient to use positive mantissae, and logarithms of numbers less than unity are written as cologarithms or modified logarithms in which the negative logarithm is subtracted from a positive integer as 10, 20, etc., 100, 200, etc.; and the cologarithm or modified logarithm is written as a positive logarithm with the integer shown as subtracted from the logarithm. For example the logarithm of 0.2 =logarithm of $\frac{1}{16} = \log$, $1 - \log$, 5 = 0.00000 - 0.69893 =The cologarithm or modified logarithm will be equal to the logarithm subtracted from 10 and is written 9.30103 - 10. The logarithm of $.00625 = \log_{10}.5 = \log_{10}.5$ $-\log$. 800 = 0.69897 - 2.90309 = -2.20412, or as a cologarithm or modified logarithm = 7.79588 - 10. The mantissae of the cologarithms of numbers less than unity are given in Table I.

The following rules should be kept in mind in using the table of logarithms.

- 1. The logarithm of a product is the sum of the logarithms of the factors.
- 2. The logarithm of a quotient is the difference of the logarithms of the dividend and divisor.
- 3. The logarithm of a power of a number is equal to the logarithm of the number multiplied by the index of the power.
- 4. The logarithm of a root of a number is equal to the logarithm of the number divided by the index of the root.
- 5. The logarithm of a fraction is equal to the logarithm of the numerator minus the logarithm of the denominator.
- 6. In dividing modified logarithms add a number to the positive and negative characteristics so that the resulting logarithm will have —10 following the logarithm. For example if 8.36748 —10 is to be divided by 3, the logarithm should be written 28.36748 —30; and dividing by 3 we have 9.45583 10.

Reverse the operation when multiplying modified logarithms.

- 7. The characteristic of the logarithm of an integer is always one less than the number of digits in the integral part of the number.
- 8. The characteristic of the cologarithm of a number less than unity (a decimal) is equal to 10 minus the number of the place to the right of the decimal point occupied by the first significant figure.

TABLE II. LOGARITHMIC FUNCTIONS OF ANGLES.

—To avoid the use of negative characteristics the logarithms of the functions of angles are written as cologarithms, 10 being added to the characteristic of each logarithm. In adding the logarithms of the functions of angles the correct number of tens should be subtracted from the result.

For angles from 0° to 45° and from 135° to 180° the headings at the tops of the columns are to be used; while from 45° to 90° and from 90° to 135° the headings at the bottoms of the columns are to be used; the minutes being read from the top down on the left of the page, and from the bottom up on the right of the page.

In using the logarithmic functions of angles in connection with logarithms of numbers it should be remembered that the logarithmic functions of angles are cologarithms and that 10 should be subtracted from each logarithmic function.

TABLE III. NATURAL FUNCTIONS OF ANGLES.—
For angles from 0° to 45° and from 135° to 180° the headings at the tops of the columns are to be used; while from 45° to 90° and from 90° to 135° the headings at the bottoms of the columns are to be used; the minutes being read from the top down on the left of the page and from the bottom up on the right of the page.

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