THE CARPENTERS' STEEL SQUARE, AND ITS USES.

BEING A DESCRIPTION OF THE SQUARE, AND ITS USES IN OBTAINING THE LENGTHS AND BEVELS OF ALL KINDS OF RAFTERS, HIPS, GROINS, BRACES, BRACKETS, PUR-LINS, COLLAR-BEAMS, AND JACK-RAFTERS;

ALSO, ITS APPLICATION IN OBTAINING THE BEVELS AND CUTS FOR HOPPERS, SPRING MOULDINGS, OCTAGONS, STAIRS, DIMINISHED STILES, ETC., ETC., ETC.

ILLUSTRATED BY OVER SEVENTY WOOD-CUTS.

BY

FRED. T. HODGSON,

Editor of the "Builder and Woodworker."


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PREFACE TO SECOND EDITION.

The rapid disposal of the first edition of the "Steel Square and Its Uses," has rendered it incumbent for the publisher to issue a second and larger edition; and recognizing this condition, in connection with the fact that the work has met with more than a passing favor from those who make daily use of the Steel Square, it has been deemed necessary to make the present edition more useful by adding a number of solutions of mechanical problems by aid of the instrument, and other matters that will render the work more valuable to the operative mechanic.

The Author has reason to, and does, feel pleased at the appreciation the working mechanics of this country have evinced for this work; and is assured, by the numerous letters, and other indications of good feeling he has received on all hands, that the present enlargement of the work has not been made unnecessarily or too soon.

Feeling confident that the additions to the present edition will commend themselves to the toiling thousands who have daily use for the "Steel Square," the publishers send the enlarged work out to the public with a knowledge that it will be welcomed by those who are most interested in the subject of which it treats.

New York, Jan. 1, 1883.
PREFACE.

Some time ago, the author of this little work contributed a series of papers on the Steel Square and Its Uses, to the American Builder, and since their appearance, he has received hundreds of letters from as many persons residing in various parts of the United States, Canada, Australia and New Zealand, in which the writers requested him to publish the papers in book form. Partly in compliance with these requests, and partly at the solicitation of personal friends, together with a knowledge that a cheap but thorough work of the kind, would be of service to all persons who have occasion to use a steel square, he has consented, with the aid of the present enterprising publishers, to issue the work as now offered.

It is only of late years that American workmen have begun fully to understand the capabilities of the steel square; and even now, only a few of the best workmen have any idea of what can be accomplished with it when in skilful hands.

It is not claimed that the rules and methods shown in this little work are either new or original; they have been known to advanced workmen for many years past; but it is claimed that they have never before been brought together and put in so handy a shape as
PREFACE.

in the present book; and it is further claimed that many of the
rules herein illustrated and explained, have never appeared in
print previous to the publication of the papers on the subject in the
magazine referred to above.

Should this little volume prove of service to the man who toils
with axe, saw and plane, for his daily bread, and profitable to the
publishers who risk their money on its publication, it will have
fulfilled its mission, as designed by

THE AUTHOR.

New York, 1886.

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THE CARPENTERS' STEEL SQUARE,
AND ITS USES.

PART I.

Preliminary.—There is nothing of more importance to a young man who is learning the business of house-joinery and carpentry, than that he should make himself thoroughly conversant with the capabilities of the tools he employs. It may be that, in some of the rules shown in this work, the result could be attained much readier with other aids than the square; but the progressive mechanic will not rest satisfied with one method of performing operations when others are within his reach.

In the hand of the intelligent mechanic the square becomes a simple calculating machine of the most wonderful capacity, and by it he solves problems of the kinds continually arising in mechanical work, which by the ordinary methods are more difficult to perform.

The great improvement which the arts and manufactures have attained within the last fifty years, renders it essential that every person engaged therein should use his utmost exertions to obtain a perfect knowledge of the trade he
professes to follow. It is not enough, nowadays, for a person to have attained the character of a good workman; that phrase implies that quantum of excellence, which consists in working correctly and neatly, under the directions of others. The workman of to-day, to excel, must understand the principles of his trade, and be able to apply them correctly in practice. Such an one has a decided advantage over his fellow-workman; and if to his superior knowledge he possesses a steady manner, and industrious habits, his efforts cannot fail of being rewarded.

It is no sin not to know much, though it is a great one not to know all we can, and put it all to good use. Yet, how few mechanics there are who will know all they can? Men apply for employment daily who claim to be finished mechanics, and profess to be conversant with all the ins and outs of their craft, and who are nowadays backward in demanding the highest wages going, who, when tested, are found wanting in knowledge of the simplest formulas of their trade. They may, perhaps, be able to perform a good job of work after it is laid out for them by a more competent hand; they may have a partial knowledge of the uses and application of their tools; but, generally, their knowledge ends here. Yet some of these men have worked at this trade or that for a third of a century, and are to all appearances, satisfied with the little they learned when they were apprentices. True, mechanical knowledge was not always so easily obtained as at present, for nearly all works on the constructive arts were written by professional architects, engineers, and designers, and however unexceptionable in other respects, they were generally couched in such language, technical and mathematical, as to be perfectly unintelligible to the majority of workmen; and instead of acting as aids to the ordinary inquirer, they enveloped in mystery the simplest solutions of every-day problems, discouraging nine-tenths of workmen on the very threshold of inquiry, and causing them to abandon further efforts to master the intricacies of their respective trades.

Of late years, a number of books have been published, in which the authors and compilers have made commendable efforts to simplify matters pertaining to the arts of carpentry and joinery, and the mechanic of to-day has not the difficulties of his predecessors to contend with. The workman of old could excuse his ignorance of the higher branches of his trade, by saying that he had no means of acquiring a knowledge of them. Books were beyond his reach, and trade secrets were guarded so jealously, that only a limited few were allowed to know them, and unless he was made of better stuff than the most of his fellow-workmen, he was forced to plod on in the same groove all his days.

Not so with the mechanic of to-day; if he is not well up in all the minutae of his trade, he has but himself to blame, for although there is no royal road to knowledge, there are hundreds of open ways to obtain it; and the young mechanic who does not avail himself of one or other of these ways to enrich his mind, must lack energy, or be altogether indifferent about his trade, and may be put down as one who will never make a workman.

I have thought that it would not be out of place to preface this work on the "Steel Square," with the foregoing remarks, in the hope that they may stimulate the young mechanic, and urge him forward to conquer what at best are only imaginary difficulties. A willing heart and a
clear head will most assuredly win honorable distinction in any trade, if they are only properly used. Indeed, during an experience of many years in the employment and superintendence of mechanics of every grade, from the green "wood-hagler" to the finished and accomplished workman, I have invariably discovered that the finished workman was the result of persistent study and application, and not, as is popularly supposed, a natural or spontaneous production. It is true that some men possess greater natural mechanical abilities than others, and consequently a greater aptitude in grasping the principles that underlie the constructive arts; but, as a rule, such men are not reliable; they may be expert, equal to any mechanical emergency, and quick at mastering details, but they are seldom thorough, and never reliable where long sustained efforts are required.

The mechanic who reaches a fair degree of perfection by experience, study and application, is the man who rises to the surface, and whose steadiness and trustworthiness force themselves on the notice of employers and superintendents. I have said this in order to give encouragement to those young mechanics who find it up-hill work to master the intricacies of the various arts they are engaged in, for they may rest assured that in the end work and application will be sure to win; and I am certain that a thorough study of the steel square and its capabilities will do more than anything else to aid the young workman in mastering many of the mechanical difficulties that will confront him from time to time in his daily occupation.

It must not be supposed that the work here presented exhausts the subject. The enterprising mechanic will find opportunity for using the square in the solution of many problems that will crop up during his daily work, and the principles herein laid down will aid very much towards correct solutions. In framing roofs, bridges, trestle-work, and constructions of timber, the Steel Square is a necessity to the American carpenter; but only a few of the more intelligent workmen ever use it for other purposes than to make measurements, lay off the mortices and tenons, and square over the various joints. Now, in framing bevel work of any description, the square may be used with great advantage and profit. Posts, girts, braces, and struts of every imaginable kind may be laid out by this wonderful instrument, if the operator will only study the plans with a view of making use of his square for obtaining the various bevels, lengths and cuts required to complete the work in hand. Tapering structures—the most difficult the framer meets with—do not contain a single bevel or length that can not be found by the square when properly applied, and it is this fact I wish to impress on my readers, for it would be impossible, in this work, to give every possible application of the square to work of this kind. I have, therefore, only given such examples as will enable any one to apply some one of them to any work in hand.

The Square—Historical and Descriptive.—Doubtless, in the early ages of mankind, when solid structures became a necessity, the want of an instrument similar to the square must have been felt at every "turn and corner," and there can be no question about one having been used—rude and imperfect perhaps—in erecting the first square or rectangular building that was ever built on this earth.
The Greeks, who were an inventive people, and who were apt to ascribe to themselves more credit than was really their due, in the way of inventions and discoveries, lay claim to be the inventors of the instrument. Pliny says that Theodorus, a Greek of Samos, invented the square and level. Theodorus was an artist of some note, but it is evident that the square and level, in some form or other, were used long before his time, even in his own country, for some of the finest temples in Athens and other Grecian cities, had been built long before his time; and the Pyramids of Egypt were hoary with age when he was in swaddling cloths. Indeed, the “square,” as a constructive tool, must of necessity have found a place in the “kit” of the earliest builders. Evidences of its presence have been found in the ruins of pre-historic nations, and are abundant in the remains of ancient Petra, Nineveh, Babylon, Etruria, and India. South American ruins of great antiquity in Brazil, Peru, and other places, show that the unknown races that once inhabited the South American Continent, were familiar with many of the uses of the square. Egypt, however, that cradle of all the arts, furnishes us with the most numerous, and, perhaps, the most ancient evidences of the use of the square; paintings and inscriptions on the rock-cut tombs, the temples, and other works, showing its use and application, are plentiful. In one instance, a whole “kit” of tools was found in a tomb at Thebes, which consisted of mallets, hammers, bronze nails, small tools, drills, hatchets, adzes, squares, chisels, etc.; one bronze saw and one adze have the name of Thothmes III., of the 18th dynasty, stamped on their blades, showing that they were made nearly 3,500 years ago. The constructive and decorative arts at that time were in their zenith in Egypt, and must have taken at least 1,000 years to reach that stage. Consequently, the square must have been used by workmen of that country, at least, four thousand years ago.

The British Museum contains many tools of pre-historic origin, and the square is not the least of them. Herculaneum and Pompeii contribute evidences of the importance of this useful tool. On some of the paintings recently discovered in those cities, the different artisans can be seen at home in their own workshops, with their work-benches, saw-horses, tools, and surroundings, much about the same as we would find a small carpenter shop of to-day, where all the work is done by hand; the only difference being a change in the form of some of the tools, which, in some instances, had been better left as these old workmen devised them.

It can make no difference, however, to the modern workman, as to when or where the square was first used; suffice to know, that, at present, we have squares immensely superior to anything known to the ancients, and it may be added, that so perfect has the machinery for the manufacture of steel squares become, that a defective tool is now the exception. Of course this relates to the products of manufacturers of repute, and not to the cheap squares, or to those said to be “first-class,” that were made ten or fifteen years ago. The tool we recommend elsewhere is the best made, both as to quality of material, accuracy of workmanship, and amount of useful matter on its faces.
Description of the Square.—In the foregoing sketch I have given a few hints as to the kind of square to purchase when it is necessary to buy; in many cases, however, this book will find its way into the hands of mechanics and others, who will have old and favorite squares in their chests or works, and who will not care to dispose of a "well-tried friend" for the purpose of filling its place with another, simply because I have recommended it. To these workmen I would say that I do not advise a change, provided the old square is true, and the inches and subdivisions are properly and accurately defined. I wish it distinctly understood that old squares, if true, and marked with inches and sub-divisions of inches, will perform nearly every solution presented in this book.

The lines and figures formed on the squares of different make, sometimes vary, both as to their position on the square, and their mode of application, but a thorough understanding of the application of the scales and lines shown on any first-class tool, will enable the student to comprehend the use of the lines and figures exhibited on other first-class squares.

To insure good results, it is necessary to be careful in the selection of the tool. The blade of the square should be 24 inches long, and two inches wide, and the tongue from 14 to 18 inches long and 1½ inches wide. The tongue should be exactly at right angles with the blade, or in other words the "square" should be perfectly square.

To test this question, get a board, about 12 or 14 inches wide, and four feet long, dress it on one side, and true up one edge as near straight as it is possible to make it. Lay the board on the bench, with the dressed side up, and the trued edge towards you, then apply the square, with the blade to the left, and mark across the prepared board with a penknife blade, pressing close against the edge of the tongue; this process done to your satisfaction, reverse the square, and move it until the tongue is close up to the knife mark; if you find that the edge of the tongue and mark coincide, it is proof that the tool is correct enough for your purposes.

This, of course, relates to the inside edge of the blade, and the outside edge of the tongue. If these edges should not be straight, or should not prove perfectly true, they should be filed or ground until they are straight and true. The outside edge of the blade should also be "trued" up and made exactly parallel with the inside edge, if such is required. The same process should be gone through on the tongue. As a rule, squares made by firms of repute are perfect, and require no adjusting; nevertheless, it is well to make a critical examination before purchasing.

The next thing to be considered is the use of the figures, lines, and scales, as exhibited on the square. It is supposed that the ordinary divisions and sub-divisions of the inch, into halves, quarters, eighths, and sixteenths are understood by the student; and that he also understands how to use that part of the square that is sub-divided into twelfths of an inch. This being conceded, we now proceed to describe the various rules as shown on all good squares; but before proceeding further, it may not be out of place to state, that on the tool recommended in this book, one edge is subdivided into thirty-seconds of an inch.

This fine sub-division will be found very useful, particularly so when used as a scale to measure drawings made in
half, quarter, one-eighth, or one-sixteenth of an inch to the foot.

I now refer the reader to the square shown in the Frontispiece. It is the one recommended in the foregoing pages, and is the most complete square in the market, and manufactured, I believe, by one firm. It is known to the trade as No. 100, and this number will be found stamped always on the face side of the square at the junction of the tongue and blade. The following instructions refer to the Frontispiece and accompanying cuts.

The diagonal scale is on the tongue at the junction with blade, Fig. 1, and is for taking off hundredths of an inch. The lengths of the lines between the diagonal and the perpendicular are marked on the latter. Primary divisions are tenths, and the junction of the diagonal lines with the longitudinal parallel lines enables the operator to obtain divisions of one hundredth part of an inch; as, for example, if we wish to obtain twenty-four hundredths of an inch, we place the compasses on the "dots" on the fourth parallel line, which covers two primary divisions, and a fraction, or four-tenths, of the third primary division, which added together makes twenty-four hundredths of an inch. Again, if we wish to obtain five tenths and seven hundredths, we operate on the seventh line, taking five primaries and the fraction of the sixth where the diagonal intersects the parallel line, as shown by the "dots," on the compasses, and this gives us the distance required.

The use of this scale is obvious, and needs no further explanation.

Fig. 2 a shows the position of the "dots" or "points" referred to in the foregoing example of the use of the diagonal scale.

**Board, Plank and Scahtung Measure.**—Perhaps, with the single exception of the common inch divisions on the square, no set of figures on the instrument will be found more useful to the active workman than that known as the board rule. A thorough knowledge of its use may be obtained by ten minutes' study, and, when once obtained, is always at hand and ready for use.

The following explanations are deemed sufficiently clear to give the reader a full knowledge of the workings of the rule. If we examine Fig. 2, in the Frontispiece, we will find under the figure 12, on the outer edge of the blade, where the length of the boards, plank, or scantling to be measured, is given, and the answer in feet and inches is found under the inches in width that the board, etc., measures. For example, take a board nine feet long and five inches wide; then under the figure 12, on the second line will be found the figure 9, which is the length of the board; then run along this line to the figure.
directly under the five inches (the width of the board), and we find three feet nine inches, which is the correct answer in "board measure." If the stuff is two inches thick, the sum is doubled; if three inches thick, it is trebled, etc., etc. If the stuff is longer than any figures shown on the square, it can be measured by dividing and doubling the result. This rule is calculated, as its name indicates, for board measure, or for surfaces 1 inch in thickness. It may be advantageously used, however, upon timber by multiplying the result of the face measure of one side of a piece by its depth in inches. To illustrate, suppose it be required to measure a piece of timber 25 feet long, 10 x 14 inches in size. For the length we will take 12 and 13 feet. For the width we will take 10 inches, and multiply the result by 14. By the rule a board 12 feet long and 10 inches wide contains 10 feet, and one 13 feet long and 10 inches wide, 10 feet 10 inches. Therefore, a board 25 feet long and 10 inches wide must contain 20 feet and 10 inches. In the timber above described, however, we have what is equivalent to 14 such boards, and therefore we multiply this result by 14, which gives 291 feet and 8 inches, the board measure.

The "board measure," as shown on the portion of the

square, Fig. 3, gives the feet contained in each board according to its length and width. This style of figuring squares, for board measure, is going out of date, as it gives the answer only in feet.

Fig. 3 a. shows the method now in use for board measure. This shows the correct contents in feet and inches. It is a portion of the blade of the square, as shown at Fig. 2, on the Frontispiece.

**Brace Rule.**—The "brace rule" is always placed on the tongue of the square, as shown in the central space at x, Fig. 1.

This rule is easily understood; the figures on the left of the line represent the "run" or the length of two sides of a right angle, while the figures on the right represent the exact length of the third side of a right-angled triangle, in inches, tenths, and hundredths. Or, to explain it in another way, the equal numbers placed one above the other, may be considered as representing the sides of a square, and
the third number to the right the length of the diagonal of that square. Thus the exact length of a brace from point to point having a run of 33 inches on a post, and a run of the same on a girt, is 46.67 inches. The brace rule varies somewhat in the matter of the runs expressed in different squares. Some squares give a few brace lengths of which the runs upon the post and beam are unequal.

Octagonal Scale.—The "octagonal scale," as shown on the central division of the upper portion of blade, is on the opposite side of the square to the "brace rule," and runs along the centre of the tongue as at s s. Its use is as follows: Suppose a stick of timber ten inches square. Make a centre line, which will be five inches from each edge; set a pair of compasses, putting one leg on any of the main divisions shown on the square in this scale, and the other leg on the tenth subdivision. This division, pricked off from the centre line on the timber on each side, will give the points for the gauge-lines. Gauge from the corners both ways, and the lines for making the timber octagonal in its section are obtained. Always take the same number of spaces on your compasses as the timber is inches square from the centre line. Thus, if a stick is twelve inches square, take twelve spaces on the compasses; if only six inches square, take six spaces on the compasses, etc., etc. The rule always to be observed is as follows: Set off from each side of the centre line upon each face as many spaces by the octagon scale as the timber is inches square. For timbers larger in size than the number of divisions in the scale, the measurements by it may be doubled or trebled, as the case may be.

The diagram, Fig. 4 a, shows the application of the rule applied to the end of a stick of timber or on a plane surface. Let B C D E, be the square equal to six inches on a side. Draw the centre lines, B C and D E, then with the
divers take from the scale six parts, and lay off this distance from the centre of each; as B 1, B 2, E 3 and E 4, C 5 and C 6, D 7 and D 8. Draw lines from 1 to 8, 2 to 3, 4 to 5, 6 to 7, and the octagon figure is complete.

A rule for laying off octagons is figured on nearly all carpenters' two-foot rules, marked off from the inner edges of the rule; one set of figures is denoted by the letter r, another set is denoted by the letter m. That set marked r measures the distance from the edge of the square to the points indicated in the diagram, by the figures 1, 2, 3, 4, etc. The set marked m is used for finding the points 1, 2, 3, 4, etc., by measuring from the middle or centre lines, B, E, C, D.

I have now fully described all the lines, figures, and scales that are usually found on the better class of squares now in use; but I may as well here remark that there are squares in use of an inferior grade, that are somewhat dif-
Fence.—A necessary appendage to the steel square in solving mechanical problems, is, what I call, for the want of a better name, an adjustable fence. This is made out of a piece of black walnut or cherry 2 inches wide, and 2 feet 10 inches long (being cut so that it will pack in a tool chest), and \( 1\frac{3}{8} \) inches thick; run a gauge line down the centre of both edges; this done, run a saw kerf cutting down these gauge lines at least one foot from each end, leaving about ten inches of solid wood in the centre of fence. We now take our square and insert the blade in the saw kerf at one end of the fence, and the tongue in the kerf, at the other, the fence forming the third side of a right-angle triangle, the blade and the tongue of the square forming the other two sides. A fence may be made to do pretty fair service, if the saw kerf is all cut from one end as shown at Fig. 4. The one first described, however, will be found the most serviceable. The next step will be to make some provision for holding the fence tight on the square; this is best done by putting a No. 10 \( 1\frac{3}{8} \) inch screw in each end of the fence, close up to the blade and tongue; having done this, we are ready to proceed to business.

**Application.**—The fence being made as desired, in either of the methods mentioned, and adjusted to the square, work can be commenced forthwith.

The first attempt will be to make a pattern for a brace, for a four-foot “run.” Take a piece of stuff already prepared, six feet long, four inches wide and half-inch thick, gauge it three-eighths from jointed edge.

Take the square as arranged at Fig. 5, and place it on the prepared stuff as shown at Fig. 6. Adjust the square so that the twelve-inch lines coincide exactly with the gauge line \( o, o, o, o \). Hold the square firmly in the position now obtained, and slide the fence up the tongue and blade until it fits snugly against the jointed edge of the prepared stuff, screw the fence tight on the square, and be sure that the 12 inch marks on both the blade and the tongue are in exact position over the gauge-line.

I repeat this caution, because the successful completion of the work depends on exactness at this stage.

We are now ready to lay out the pattern. Slide the square to the extreme left, as shown on the dotted lines at \( x \), mark with a knife on the outside edges of the square, cutting the gauge-line. Slide the square to the right until the 12 inch mark on the tongue stands over the knife mark on the gauge-line; mark the right-hand side of the square cutting the gauge-line as before, repeat the process four times, marking the extreme ends to cut off, and we have the length of the brace and the bevels.

Square over, with a try square, at each end from the gauge-line, and we have the toe of the brace. The lines, \( s, s \), shown at the ends of the pattern, represent the tenons that are to be left on the braces. This pattern is now com-
plete; to make it handy for use, however, nail a strip 2 inches wide on its edge, to answer for a fence as shown at k, and the pattern can then be used either side up.

The cut at Fig. 7, shows the brace in position, on a reduced scale. The principle on which the square works in the formation of a brace can easily be understood from this cut, as the dotted lines show the position the square was in when the pattern was laid out.

It may be necessary to state that the "square," as now arranged, will lay out a brace pattern for any length, if the angle is right, and the run equal. Should the brace be of great length, however, additional care must be taken in the adjustment of the square, for should there be any departure from truth, that departure will be repeated every time the square is moved, and where it would not affect a short run, it might seriously affect a long one.

To lay out a pattern for a brace where the run on the beam is three feet, and the run down the post four, proceed as follows:

Prepare a piece of stuff, same as the one operated on for four feet run; joint and gauge it. Lay the square on the left-hand side, keep the 12 inch mark on the tongue, over the gauge-line, place the 9 inch mark on the blade, on the gauge-line, so that the gauge-line forms the third side of a right-angle triangle, the other sides of which are nine and twelve inches respectively.

Now proceed as on the former occasion, and as shown at Fig. 8, taking care to mark the bevels at the extreme ends. The dotted lines show the positions of the square, as the pattern is being laid out.

Fig. 9 shows the brace in position, the dotted lines show
where the square was placed on the pattern. It is well to thoroughly understand the method of obtaining the lengths and bevels of irregular braces. A little study, will soon enable any person to make all kinds of braces.

If we want a brace with a two feet run, and a four feet run, it must be evident that, as two is the half of four, so on the square take 12 inches on the tongue, and 6 inches on the blade, apply four times, and we have the length, and the bevels of a brace for this run.

For a three by four feet run, take 12 inches on the tongue, and 9 inches on the blade, and apply four times, because, as 3 feet is \(\frac{3}{4}\) of four feet, so 9 inches is \(\frac{3}{4}\) of 12 inches.

**Rafters.**—Fig. 10 shows a plan of a roof, having twenty-six feet of a span.

The span of a roof is the distance over the wall plates measuring from A to A, as shown in Fig. 10. It is also the extent of an arch between its abutments.

There are two rafters shown in position on Fig. 10. The one on the left is at an inclination of quarter pitch, and marked B, and the one on the right, marked C, has an inclination of one-third pitch. These angles, or inclinations rather, are called quarter and third pitch, respectively, because the height from level of wall plates to ridge of roof is one-quarter or one-third the width of building, as the case may be.

At Fig. 11, the rafter B is shown drawn to a larger scale; you will notice that this rafter is for quarter pitch, and for convenience, it is supposed to consist of a piece of stuff 2 inches by 6 inches by 17 feet. That portion of the rafter that projects over the wall of the building, and forms the eve, is three or more inches in width, just as we please. The length of the projecting piece in this case is one foot—it may be more or less to suit the eve, but the line must continue from end to end of the rafter, as shown on the plan, and we will call this line our working line.

We are now ready to lay out this rafter, and will proceed as follows: We adjust the fence on the square the same as for braces, press the fence firmly against the top edge of rafter, and place the figure 12 inches on the left-hand side, and the figure 6 in on the right-hand side, directly over the working line, as shown on the plan. Be very exact about getting the figures on the line, for the quality of the
work depends much on this; when you are satisfied that you are right, screw your fence tight to the square. Commence at No. 1 on the left, and mark off on the working line; then slide your square to No. 2, repeat the marking and continue the process until you have measured off thirteen spaces, the same as shown by the dotted lines in the drawing. The last line on the right-hand side will be the plumb cut of the rafter, and the exact length required. It will be noticed that the square has been applied to the timber thirteen times.

The reason for this is, that the building is twenty-six feet wide, the half of which is thirteen feet, the distance that one rafter is expected to reach, so, if the building was thirty feet wide, we should be obliged to apply the square fifteen times instead of thirteen. We may take it for granted, then, that in all cases where this method is employed to obtain the lengths and bevels, or cuts of rafters, we must apply the square half as many times as there are feet in the width of the building being covered. If the roof to be covered is one-third pitch, all to be done is to take 12 inches on one side of the square and 8 inches on the other, and operate as for quarter pitch.

We shall frequently meet with roofs much more acute than the ones shown, but it will be easy to see how they can be managed. For instance, where the rafters are at right-angles to each other, apply the square the same as for braces of equal run, that is to say, keep the 12 mark on the blade, and the 12 mark on the tongue, on the working line. When a roof is more acute, or "steeper" than a right-angle, take a greater figure than twelve on one side of the square, and twelve on the other.

Whenever a drawing of a roof is to be followed, we can soon find out how to employ the square, by laying it on the drawing, as shown in Fig. 12. Of course, something depends on the scale to which the drawing is made. If any of the ordinary fractions of an inch are used, the intelligent workman will have no difficulty in discovering what figures to make use of to get the "cuts" and length desired.

Sometimes there may be a fraction of a foot in this division; when such is the case, it can be dealt with as follows: suppose there is a fraction of a foot, say 8 inches, the half of which would be 4 inches, or 1/8 of a foot; then, if the roof is quarter pitch, all to be done is to place the square, with the 4 inch mark on the blade, and the 2 inch mark on the tongue, on the centre line of the rafter, and the distance between these points is the extra length required, and the line down the tongue is the bevel at the point of the rafter. On Fig. 13, is shown an application of this method. All other pitches and fractions can be treated in this manner without overtaxing the ingenuity of the workman.
Sufficient has been shown to enable the student, if he has mastered it, to find the lengths and bevels of any common rafter; therefore, for the present, we will leave saddle roofs, and try what can be done with the square in determining the lengths and bevels of "hips," valleys, and cripples.

Fig. 14 shows how to get bevels on the top end of vertical boarding, at the gable ends, suitable for the quarter pitch at Fig. 10.

At Fig. 15, is shown a method for finding the bevel for horizontal boarding, collar ties, etc.

**Hip Rafters.**—Fig. 16, is supposed to be the pitch of a roof furnished by an architect, with the square applied to the pitch. The end of the long blade must only just enter
the fence, as shown in the drawing, and the short end must be adjusted to the pitch of the roof, whatever it may be. Fig. 17 shows the square set to the pitch of the hip rafter. The squares as set give the plumb and level cuts. Fig. 18 is the rafter plan of a house 18 by 24 feet; the rafters are laid off on the level, and measure nine feet from centre of ridge to outside of wall; there should be a rafter pattern with a plumb cut at one end, and the foot cut at the other, got out as previously shown. (Figs. 16, 17, 18, P.) When the rafter foot is marked, place the end of the long blade of the square to the wall line, as in drawing, and mark across the rafter at the outside of the short blade, and these marks on the rafter pitch will correspond with two feet on the level plan; slide the square up the rafter and place the end of the long blade to the mark last made, and mark outside the short blade as before, repeat the application until nine feet are measured off, and then the length of the rafter is correct; remember to mark off one-half the thickness of ridge-piece.

The rafters are laid off on part of plan to show the appearance of the rafters in a roof of this kind, but for working purposes the rafters 1, 2, 3, 4, 5, and 6, with one hip rafter, is all that is required.

**Hip-roof Framing.**—We first lay off common rafter, which has been previously explained; but deeming it necessary to give a formula in figures to avoid making a plan, we take \(\frac{3}{2}\) pitch. This pitch is \(\frac{3}{2}\) the width of building, to point of rafter from wall plate or base. For an example, always use 8, which is \(\frac{3}{2}\) of 24, on tongues for altitude; 12, \(\frac{3}{2}\) the width of 24, on blade for base. This cuts common rafter. Next is the hip-rafter. It must be understood that
the diagonal of $12$ and $12$ is $17$ in framing, and the hip is
the diagonal of a square added to the rise of roof; therefore we take $8$ on tongue and $17$ on blade; run the same
number of times as common rafter (rule to find distance
of hip diagonal $a^2 + a^2 + b^2 = y^2$). To cut jack rafters, divide
the numbers of openings for common rafter. Suppose we
have $5$ jacks, with six openings, our common rafter $12$ feet
long, each jack would be $2$ feet shorter. First $10$ feet,
second $8$ feet, third $6$ feet, and so on. The top down cut
the same as cut of common rafter; foot also the same.
To cut mitre to fit hip. Take half the width of building
on tongue and length of common rafter on blade; blade
gives cut. Now find the diagonal of $8$ and $12$, which
is $14''$, call it $14$ $7-16$, take $12$ on tongue, $14$ $7-16$ on
blade; blade gives cut. The hip-rafter must be beveled to
suit jacks; height of hip on tongue, length of hip on blade;
tongue gives bevel. Then we take $8$ on tongue $183/4$ on
blade; tongue gives the bevel. Those figures will span all
cuts in putting on cornice and sheathing. To cut bed
moulds for gable to fit under cornice, take half width of
building on tongue length of common rafter on blade;
blade gives cut; machine mouldings will not member, but
this gives a solid joint; and to member properly it is neces-
sary to make moulding by hand, the diagonal plumb cut
differences. I find a great many mechanics puzzled to
makes the cuts for a valley. To cut planceer, to run up
valley, take heighth of rafter on tongue, length of rafter on
blade; tongue gives cut. The plumb cut takes the height
of hip-rafter on tongue, length of hip-rafter on blade;
tongue gives cut. These figures give the cuts for $3/2$ pitch
only, regardless of width of building.

For a hopper the mitre is cut on the same principle.
To make a butt joint, take the width of side on blade, and
half the flare on tongue; the latter gives the cut. You
will observe that a hip-roof is the same as a hopper in-
vverted. The cuts for the edges of the pieces of a hexagonal
hopper are found this way: Subtract the width of one
piece at the bottom from the width of same at top, take
remainder on tongue, depth of side on blade; tongue gives
the cut. The cut on the face of sides: Take $7-12$ of the
rise on tongues and the depth of side on blade; tongue
gives cut. The bevel of top and bottom: Take rise on
blade, run on tongue; tongue gives cut.

Fig. 19 exhibits two methods of finding the "backing"
of the angle on hip-rafter. The methods are as simple as
any known. Take the length of the rafter on the blade,
and the rise on the short blade or tongue, place the
square on the line D E, the plan of the hip, the angle is
given to bevel the hip-rafter, as shown at F. This method
gives the angle, only for a right-angled plan, where the
pitches are the same, and no other.

The other method applies to right, obtuse, and acute
angles, where the pitches are the same. At the angle D
will be seen the line from the points $K$ & $L$, at the intersec-
tion of the sides of the angle rafter with the sides of the
plan.

With one point of the compass at D, describe the curve
from the line as shown. Tangential to the curve draw
the dotted line, cutting A, then draw a line parallel to A B,
the pitch of the hip. The pitch or bevel, will be found
at C, which is a section of the hip-rafter.

This problem is taken from "Gould's Carpenters'
Guide,” but has been in practice among workmen for many years.

Fig. 20 exhibits a method of finding the cuts in a mitre box, by placing the square on the line AB at equal distances from the heel of the square, say ten inches. The bevel is shown to prove the truth of the lines by applying it to opposite sides of the square.

Stairs.—In laying out stairs with the square, it is necessary to first determine the height from the top of the floor on which the stairs start from, to the floor on which they are to land; also the “run” or the distance of their horizontal stretch. These lengths being obtained, the rest is easy.

Fig. 21 shows a part of a stair string, with the “square” laid on, showing its application in cutting out a pitch-board. As the square is placed it shows 10 inches for the tread and 7 inches for the rise.

To cut a pitch-board, after the tread and rise have been
determined, proceed as follows: Take a piece of thin, clear stuff, and lay the square on the face edge, as shown in the figure, and mark out the pitch-board with a sharp knife; then cut out with a fine saw and dress to knife marks, nail a piece on the longest edge of the pitch-board for a fence, and it is ready for use.

Fig. 22 is a rod, with the number and heighth of steps for a rough flight of stairs to lead down into a cellar or elsewhere.

Fig. 23 is a step-ladder, sufficiently inclined to permit a person to pass up and down on it with convenience. To lay off the treads, level across the pitch of the ladder, set the short side of the square on the floor, at the foot of the string, after the string is cut, to fit the floor and trimmer joists. Fasten the fence on the square, as shown at Fig. 5. The height of the steps in this case is nine inches, so it will be seen that it is an easy matter to lay off the string, as the
long side of the square hangs plumb, and nine inches up its length will be the distance from one step to the next one.

Fig. 24 shows the square and fence in position on the string.

The opening in the floor at the top of the string shows the ends of trimming joists, five feet apart.

Fig. 25 shows how to divide a board into an even number of parts, each part being equal, when the same is an uneven number of inches, or parts of an inch in width. Lay the square as shown, with the ends of the square on the edges of the board, then the points of division will be found at 6, 12, and 18, for dividing the board in four equal parts; or at 4, 8, 12, 16, and 20 if it is desired to divide the board into six equal parts. Of course, the common two-foot rule will answer this purpose as well as the square, but it is not always convenient.

Fig. 26 shows how a circle can be described by means of a "steel square" without having recourse to its centre.

At the extremities of the diameter, A, O, fix two pins, as shown; then by sliding the sides of the square in contact with the pins, and holding a pencil at the point X, a semi-circle will be struck. Reverse the square, repeat the process, and the circle is complete.

Miscellaneous Rules — The following rules have been tested over and over again by the writer, and found reliable in every instance. They have been known to advanced workmen for many years, but were never published, so far as the writer knows, until they appeared in the Builder and Wood-Worker, some years ago:

Measurement.—Let us suppose that we have a pile of lumber to measure, the boards being of different widths, and say 16 feet long. We take our square and a bevel with a long blade and proceed as follows: First we set the bevel at 12 inches on the tongue of the square, because we want to find the contents of the board in feet, 12 inches being one foot; now we set the other end of the bevel blade on the 16 inch mark on the blade of the square, because the boards are 16 feet long. Now, it must be quite evident to any one who would think for a moment, that a board 12 inches, or one foot wide, and 16 feet long, must contain 16 feet of lumber. Very well, then we have 16, the length, on the blade. Now, we have a board 11 inches wide, we just move our bevel from the 12 inch mark to the 11 inch mark, and look on the blade of the square for the true answer; and so on with any width, so long as the stuff is 16 feet long. If the stuff is 2 inches thick, double the answer, if 3 inches thick, treble the answer, etc.

Now, if we have stuff 14 feet long, we simply change the bevel blade from 16 inches on the square blade, to 14 inches, keeping the other end of the bevel on the 12 inch mark, 12 inches being the constant figure on that side of the square, and it will easily be seen that any length of stuff within the range of the square can be measured accurately by this method.

If we want to find out how many yards of plastering or painting there are in a wall, it can be done by this method quite easily. Let us suppose a wall to be 12 feet high and 18 feet long, and we want to find out how many yards of plastering or painting there are in it, we set the bevel on the 9 inch mark on the tongue (we take 9 inches because 9
square feet make one square yard,) we take 18 inches, one of the dimensions of the wall, on the blade of the square; then after screwing the bevel tight, we slide it from 9 inches to 12 inches, the latter number being the other dimension, and the answer will be found on the blade of the square. It must be understood that 9 inches must be a constant figure when you want the answer to be in yards, and in measuring for plastering it is as well to set the other end of the bevel on the figure that corresponds with the height of the ceiling, and then there will require no movement of the bevel further than to place it on the third dimension. This last rule is a very simple and very useful one; of course “openings” will have to be allowed for, as this rule gives the whole measurement.

If the diagonal of any parallelogram within the range of the square is required, it can be obtained as follows: Set the blade of the bevel on 8 3/4 in. on the tongue of the square, and at 12 3/8 in. on the blade; securely fasten the bevel at this angle. Now, suppose the parallelogram or square to be 11 inches on the side, then move the bevel to the 11 inch mark on the tongue of the square, and the answer, 15 9-16, will be found on the blade. All problems of this nature can be solved with the square and bevel as the latter is now set. There is no particular reason for using 8 3/4 and 12 3/8, only that they are in exact proportion to 70 and 99. 43 3/8 and 6 3-16 would do just as well, but would not admit as ready an adjustment of the bevel.

To find the circumference of a circle with the square and bevel proceed as follows: Set the bevel to 7 on the tongue and 22 on the blade; move the bevel to the given diameter on the tongue of the square, and the approximate answer will be found on the blade. When the circumference is wanted the operation is simply reversed, that is, we put the bevel on the blade and look on the tongue of the square for the answer.

If we want to find the side of the greatest square that can be inscribed in a given circle, when the diameter is given, we set the bevel to 8 3/8 on the tongue and 12 on the blade. Then set the bevel of the diameter, on the blade, and the answer will be found on the tongue.

The circumference of an ellipse or oval is found by setting 5 3/8 inches on the tongue and 8 3/4 inches on the blade; then set the bevel to the sum of the longest and shortest diameters on the tongue, and the blade gives the answer.

To find a square of equal area to a given circle, we set the bevel to 9 3/4 inches on the tongue, and 17 1/2 inches on the blade; then move the bevel to the diameter of the circle on the blade, and the answer will be found on the tongue. If the circumference of the circle is given, and we want to find a square containing the same area, we set the bevel to 5 1/4 inches on the tongue and 19 1/4 inches on the blade.

On Fig. 27 is shown a method to determine the proportions of any circular presses or other cylindrical bodies, by the use of the square. Suppose the small circle, N, to be five inches in diameter and the circle R is ten inches in diameter, and it is required to make another circle, Z, to contain the same area as the two circles N and R. Measure line a, on the square D, from five on the tongue to 10 on the blade, and the length of this line A from the two points named will be the diameter of the larger circle Z. And again, if you want to run these circles into a fourth one, set the diameter of the third on the tongue of the square,
and the diameter of $z$ on the blade, and the diagonal will give the diameter of the fourth or largest circle, and the same rule may be carried out to infinite extent. The rule is reversed by taking the diameter of the greater circle and laying diagonally on the square, and letting the ends touch whatever points on the outside edge of the square. These points will give the diameter of two circles, which combined, will contain the same area as the larger circle. The same rule can also be applied to squares, cubes, triangles, rectangles, and all other regular figures, by taking similar dimensions only; that is, if the largest side of one triangle is taken, the largest side of the other must also be taken, and the result will be the largest side of the required triangle, and so with the shortest side.

In Fig. 28 we show how the centre of a circle may be determined without the use of compasses; this is based on the principle that a circle can be drawn through any three points that are not actually in a straight line. Suppose we take $A B C D$ for four given points, then draw a line from $A$ to $D$, and from $B$ to $C$; get the centre of these lines, and square from these centres as shown, and when the square crosses, the line, or where the lines intersect, as at $X$, there will be the centre of the circle. This is a very useful rule, and by keeping it in mind the mechanic may very frequently save himself much trouble, as it often happens that it is necessary to find the centre of the circle, when the compasses are not at hand.

In Fig. 29 we show how the square can be used, in lieu of the trammel, for the production of ellipses. Here the square, $E D F$, is used to form the elliptical quadrant, $A B$, instead of the cross of the trammel; $h \ell k$ may be simply pins, which can be pressed against the sides of the square while the tracer is moved. In this case the adjustment is obtained by making the distance, $h \ell$, equal to the semi-axis minor, and the distance $\ell k$, equal to the semi-axis major.
Fig. 30 shows a method of describing a parabola by means of a straight rule and a square, its double ordinate and abscissa being given. Let AC be the double ordinate, and DB the abscissa. Bisect DC in F; join BF, and draw FE perpendicular to BF, cutting the axis BD produced in F. From B set off BG equal to DE, and G will be the focus of the parabola. Make BL equal to BG, and lay the rule on straight-edge HK on L, and parallel to AC. Take a string, MG, equal in length to LE; attach one of its ends to a pin, or other fastening, at G, and its other end to the end M of the square MNOD. If now the square be slid along the straight-edge, and the string be pressed against its edge MN, a pencil placed in the bight at F will describe the curve.

The two arms of a horizontal lever are respectively 9 inches and 13 inches in length from the suspending point; a weight of 10 lbs. is suspended from the shorter arm, and it is required to know what weight will be required to suspend on the long arm to make it balance. Set a bevel on the blade of square at 13 inches and the other end of the bevel on the 9 inch mark on tongue of square, then slide the bevel from 13 inches to 10 on the blade of square, and the answer will be found on the tongue of the square. It is easy to see how this rule can be reversed so that a weight required for the shorter arm can be found.

Fig. 31 shows how to get the flare for a hopper 4 feet across the top and 16 inches perpendicular depth. Add to the depth one-third of the required size of the discharge.
hole (the draft represents a 6-inch hole), which makes 18 inches, which is represented on the tongue of the square. (The figures on the draft are 9 and 12, which produce the same bevel.) Then take one-half, 24 inches of the width across the top of the hopper, which is represented on the blade of the square. Than scribe along the blade as represented by the dotted lines, which gives the required flare. (The one-third added to the depth is near enough for all practical purpose for the discharge.)

Fig. 32 shows how to apply the square to the edge of a board in order to obtain the bevel to form the joint. Using the same figures as in Fig. 31, scribe across the edge of the board by the side of the tongue, as shown by dotted lines. The long point being the outside.

On Fig. 33 we show a quick method of finding the centre of a circle: Let N N, the corner of the square, touch the circumference, and where the blade and tongue cross it will be divided equally; then move the square to any other place and mark in the same way and straight edge across, and where the line crosses A, B, as at O, there will be the centre of the circle.
1 and 2, Fig. 34, are taken from Gould's Wood-Working Guide.

The portion marked A, exhibits a method of finding the lines for eight-squaring a piece of timber with the square, by placing the block on the piece, and making the points seven inches from the ends of the square, from which to draw the lines for the sides of the octagonal piece required.

At the heel of the square is shown a method of cutting a board to fit any angle with the square and compass, by placing the square in the angle, and taking the distance from the heel of the square to the angle A, in the compass; then lay the square on the piece to be fitted, with the distance taken, and from the point A, draw the line A B, which will give the angle to cut the piece required.

At 2 is shown a method of constructing a polygonal figure of eight sides; by placing the square on the line A B, with equal distances on the blade and tongue, as shown; the curve lines show the method of transferring the distances; the diagonal gives the intersection at the angles.

There are at least a dozen different ways of forming octagonal figures by the square; some of them are tedious and difficult, while others cannot be applied under all circumstances. The method shown at Fig. 35 is handy and easily understood.

An equilateral triangle can be formed by taking half of one side on the tongue of the square, as shown at Fig. 36. The line along the edge of the tongue forms the mitre for the triangle, and the line along the edge of the blade forms the mitre cut for the joints of a hexagon, and as six equi-
lateral triangles form a hexagon when one point of each is placed at a central point, it follows that a hexagon may be constructed by the square above.

The following is a good method for obtaining the cuts for a horizontal and raking cornice; it is correct and simple; the gutter to be always cut a square mitre.

The seat or run of the rafter on the blade, Fig. 37, the rise of the roof on the tongue, A C, mark against the tongue, gives the cut for the side of the box, A C. The diagonal A, B, which is the length of the rafter on the blade A, D, the seat of the rafter on the tongue D, s, mark against the blade gives the cut across the box, A D. D A C is the mitre cut to fit the gutter; then if we square across the box from A, it gives B, A, C the cut for the gable peak.

At Fig. 38 is shown a method for obtaining either the butt or mitre cuts, for "Hopper" work.

The line, s s, in the cut represents the edge of a board; the line, A B, the flare of hopper. Lay the square on the face of the board so that the blade will coincide with flare of hopper, A B, then mark by the tongue the line B C, then square from edge of board, s s, cutting the angle B.

Now we have a figure that will, when used on the steel square, give the cuts for a hopper of any flare, either with butt or mitre joints.

To find bevel to cut across face of board:
Take A B on blade and A D on tongue, bevel of tongue is the bevel required.

To find the bevel for butt-joint: Take B C on blade and A D on tongue; bevel of tongue is the bevel required.

To find the bevel for mitre joint: Take B C on blade and D C on tongue; bevel of tongue is the bevel required.

It will be seen that this is a very simple method of solving what is usually considered a very difficult problem.
PART II.

The following useful applications of the square were kindly furnished for this work, by Mr. Croker; several of them are new and original:

Consider the blade of the square as representing the span of a building, but without any reference to actual or scale measurement. Next, some particular portion of the blade is to be taken as the rise of the supposed building; if a third, fourth, or half pitch is required, then a third, fourth, or a half of the blade is conceived as the rise which with half the blade solves the pitch. From this it will be seen that half the blade is always taken as the base of the theoretical common rafter. Where we have to deal with irregular pitches—by which is meant those pitches which are not a quarter, sixth, third, half, etc., of the building—then the square is to be applied to the irregular pitch with the blade lying in the direction of the pitch and the centre of the blade at the intersection of pitch and base line of the common rafter, and the resulting distance on the tongue, where it intersects the base line, is the distance to be taken as the rise of the theoretical rafter.

Let us now take a hip-roof over a square plan (for all the rules apply only to square planned building), and the practical problems supposed to need solution are: Length of common rafters, the plumb and level cuts; length of hip-rafter, its plumb and level cuts; bevel of jacks and sheeting boards against the hips; “backing” of the hip-rafter, top and down bevel of a purlin mitering against the hip with its surface in line with the plane of the roof. If the student can readily and intelligently solve these problems, he will be in a position to make extensions in the principles involved. Let the width of building under consideration be 24 feet wide, and of one third pitch.

Fig. 36.

Let 1, 12, Fig. 36, be the base of the theoretical common rafter, eight inches rise, equal to one third of the blade, because it is a third pitch; mark along the blade and extend the heel, making it and 12 equal to half the width of the actual building to a scale of 1 1/2 inch to a foot; this is a much better scale to work by than an inch one, being larger and more legible, eighthths being inches, sixteenths, 1/2 inches, etc., thus enabling very accurate measurements to be taken. By the way, it is a good plan to have the square stamped off on the eighthths side at every 1 1/2 inches for feet, for more readily counting the scale; then mark along the tongue at 1, which gives 1 12 the length of common rafter; level cut on blade and plumb cut on tongue. Next take the rise of the theoretical common rafter on the tongue, and 17 inches
on the blade, as the theoretical base of the hip-rafter; place the square as shown at Fig. 37; then multiply the actual base of common rafter 12, (Fig. 36.) by \(1\frac{14}{16} = 16\frac{9}{16}\) feet, or 17 feet, practically, which set off on blade at A 17; mark on tongue at B, then B 17 is the length of hip-rafter. For the bevels of jacks and sheeting-boards against hips take the diagonal B 12—theoretical rafter—Fig. 36, on the blade with half the blade—the theoretical base—and place the square as shown at Fig. 38, then mark along the blade for bevel of jacks, and along tongue for bevel of sheeting-boards.

For the "backing" of hip, take the diagonal of the theoretical hip-rafter, 8, 17 (Fig. 37), on the blade, and its rise—8 inches—on the tongue, and place square as shown at Fig. 39; mark by the tongue which gives the bevel required. To get the upper bevel of a purlin lying in the plane of the roof, take the bevel at tongue (Fig. 38), for the down bevel take the blade distance 147—16 (Fig. 38) on the blade with the theoretical rise—8; place the square as shown at Fig. 40; mark by the tongue which gives the bevel required.

Fig. 41 shows how any length or breadth within the extent of the blade of the square can be instantly divided into any equal parts. Let A and B represent the edges of a board, say 8\(\frac{3}{4}\) inches, wide, to be divided into 5 equal parts; take any
convenient 5 parts, say 15 inches, because $5 \times 3 = 15$, placing heel of square fair to edge B, and 15 to edge A; mark off at every 3 inches on blade, as shown, and draw lines through these points, which will divide the board as required. We will here show how the square can be used to solve problems in proportion; for instance, if 1500 feet of boards cost $10.75, what will 600 feet cost? Take 15 on the blade

![Fig. 41](image1)

and 10.75 on the tongue, and place the square as shown at Fig. 41, then count from 15 towards B, and from this point draw parallel to tongue; 6 A, this is the answer required.

![Fig. 42](image2)

Figs. 42 and 43 show quite a novel and useful way of bisecting any angle. Let A 12, A B be the given sides of an acute angle to be bisected. At any convenient point as C square C D from C 12. Now take C D on the tongue, and the sum of A D and A C on the blade of the square, place as shown in the Figure, then mark by the blade, which is the bisection required. If the angle is obtuse, as A B, A F, (Fig. 42), produce a convenient distance, as A C, square over C D, take C D on the tongue, and the sum of A D, A C, on the blade, place square as shown, and mark by the tongue for the required bisection.

![Fig. 44](image3)

Fig. 44 shows a handy way of finding the bevel of rails to diminish door stiles. Place the square fair with the known joint A B, mark by the tongue, then the resulting bevel at A is the same as that at B.
PART III.

The following rules have been gathered from various sources, chiefly, however, from papers recently published in the Scientific American Supplement, by John O. Connell, of St. Louis, and from papers contributed to the Builder and Wood-Worker, by Wm. E. Hill, of Terre Haute, Ind.

*Fig. 45 shows how an octagon can be produced by the aid of a steel square. Prick off the distance A O equal to half the distance of the square; mark this distance on the blade of the square from B to O, place the square on the diagonal, as shown, and square over each way. Do the same at every angle, and the octagon is complete.

To obtain the same figure with the compasses, proceed as follows: Take half the diagonal on the compasses, make a little over a quarter sweep from C, and at the intersection at D and C, then D and C form one side of an octagonal figure.

Again: take a piece of timber twelve inches square, as at Fig. 46; take twelve inches on the blade and tongue from A to B, and A to C, mark at the point A, operate similarly on the opposite edge, and the marked points will be guides for guage-lines for the angles forming an octagon. The remaining three sides of the timber can be treated in the same manner.

These points can be found with a carpenter's rule as follows: Lay the
rule on the timber, partly opened, as shown, in the cut, "prick off" at the figures 7 and 17 as at A and B, and these points will be the guides for the gauge-lines. The same points can be found by laying the square diagonally across the timber and "pricking" off 7 and 17.

To make a moulder's flask octagonal proceed as follows: The flask to be four feet across. Multiply $4 \times 5$ (as an octagon is always as 5 to 12 nearly), which gives 20; divide by 12, which gives $1\frac{3}{5}$ feet, cut mitre to suit this measurement, nail into corners of square box, and you have an octagon flask at once.

Another method of constructing an octagon is shown at Fig. 47. Take the side as a b for a radius, describe an arc cutting the diagonal at d; square over from d to e, and the point e will then be the gauge-guide for all the sides.

Another method (Fig. 48) is to draw a straight line, c b, any length; then let a b and a c be corresponding figures on the blade and tongue of the square, mark along either and measure the distance of required octagon; move

![Diagram](image_url)

Fig. 48.

the square and mark also. Now use the square the same as before, and the marks c b and b d are the points required.

Fig. 49 shows the application of a long bevel to a square, by which some calculations can be made with greater ease and quickness than by the usual arithmetical process. The largest size of carpenter's bevel placed under the framing square will answer in nearly every case. One edge of each blade should be perfectly straight and the edge of I should be cut out in several places to see the blade h, when placed under the square. The two blades should be fastened together by a thumb-screw. There
should be three holes in L, one near each end and one in
the middle, and a notch filed by each hole, so that the
blade E, may be shifted when necessary.

![Diagram](image)

*To Find the Diagonal of a Square* by this instrument, set
the blade E to 8\(\frac{3}{4}\) inches on the tongue and 12\(\frac{3}{8}\) inches
on the blade. Then screw the bevel fast; and supposing
the side of the square in question is 11 inches, move blade
E to the 11 inch mark on the tongue, keeping blade L
against the square, when blade E will touch 15 9-16 inches
on the blade, which is the required diagonal. There is no
special reason for using 8\(\frac{3}{4}\) and 12\(\frac{3}{8}\); other numbers may
be employed provided the proportion of 70 to 99 exists
between them. In the problem just solved as in all that
follow, the bevel being once set to solve a particular ques-

*J. O. Connell.

**Polygons Inscribed in Circles.** — In the following table, set
the bevel to the pair of numbers under the polygon to be
inscribed.

<table>
<thead>
<tr>
<th>No. of sides</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
<th>11</th>
<th>12</th>
</tr>
</thead>
<tbody>
<tr>
<td>Radius</td>
<td>56</td>
<td>70</td>
<td>74</td>
<td>Side</td>
<td>60</td>
<td>98</td>
<td>92</td>
<td>89</td>
<td>89</td>
<td>85</td>
</tr>
<tr>
<td>Side</td>
<td>97</td>
<td>99</td>
<td>87</td>
<td>equal to radius</td>
<td>52</td>
<td>75</td>
<td>15</td>
<td>55</td>
<td>45</td>
<td>44</td>
</tr>
</tbody>
</table>

If we require the radius of a circle which will circum-
scribe an octagon 8 inches on a side, we refer to column 8,
take 98 parts on the blade and 75 on tongue, and
tighten the bevel. As the side of a hexagon equals the
radius of its circle, the side of an octagon must be less than
the radius; hence we shift to 8 inches, that end of the bevel
blade which gives the lesser number, in this case, on the
tongue of the square, as the 75 parts to which the bevel
was set are less than the 98. The required radius is then
indicated on the blade.

We will now explain the figures used in stepping round
a circle forming inscribed polygons from three to twelve
sides: Set bevel or fence to 12 on blade, and the number
opposite each polygon on tongue; move to diameter of
circle; answer of the side of polygon on tongue.

<table>
<thead>
<tr>
<th>Name</th>
<th>No. of Sides</th>
<th>Gauge Points</th>
</tr>
</thead>
<tbody>
<tr>
<td>Triangle</td>
<td>3</td>
<td>10 40</td>
</tr>
<tr>
<td>Square</td>
<td>4</td>
<td>8 40</td>
</tr>
<tr>
<td>Pentagon</td>
<td>5</td>
<td>7 05</td>
</tr>
<tr>
<td>Hexagon</td>
<td>6</td>
<td>5 00</td>
</tr>
<tr>
<td>Heptagon</td>
<td>7</td>
<td>5 21</td>
</tr>
<tr>
<td>Octagon</td>
<td>8</td>
<td>4 50</td>
</tr>
<tr>
<td>Enneagon</td>
<td>9</td>
<td>4 41</td>
</tr>
<tr>
<td>Decagon</td>
<td>10</td>
<td>3 71</td>
</tr>
<tr>
<td>Undecagon</td>
<td>11</td>
<td>3 39</td>
</tr>
<tr>
<td>Dodecagon</td>
<td>12</td>
<td>3 11</td>
</tr>
</tbody>
</table>
To divide a circle into a given number of parts, multiply the corresponding number in column one and the product is the chord to lay off on circumference. The side of a polygon is known, to find the radius of a circle that will circumscribe: Multiply the given side by the corresponding number opposite of polygon in column two.

<table>
<thead>
<tr>
<th>No. of Sides</th>
<th>Name of Polygon</th>
<th>Angle of Polygon</th>
<th>Column 1</th>
<th>Column 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>Triangle</td>
<td>60</td>
<td>1710</td>
<td>5712</td>
</tr>
<tr>
<td>4</td>
<td>Square</td>
<td>90</td>
<td>1441</td>
<td>7051</td>
</tr>
<tr>
<td>5</td>
<td>Pentagon</td>
<td>108</td>
<td>1773</td>
<td>8510</td>
</tr>
<tr>
<td>6</td>
<td>Hexagon</td>
<td>120</td>
<td>Radius</td>
<td>Side</td>
</tr>
<tr>
<td>7</td>
<td>Heptagon</td>
<td>51 3:7</td>
<td>128 4:7</td>
<td>8077</td>
</tr>
<tr>
<td>8</td>
<td>Octagon</td>
<td>45</td>
<td>135</td>
<td>7053</td>
</tr>
<tr>
<td>9</td>
<td>Nonagon</td>
<td>45</td>
<td>140</td>
<td>6840</td>
</tr>
<tr>
<td>10</td>
<td>Decagon</td>
<td>36</td>
<td>144</td>
<td>6180</td>
</tr>
<tr>
<td>11</td>
<td>Undecagon</td>
<td>32 8:11</td>
<td>147 3:11</td>
<td>5634</td>
</tr>
<tr>
<td>12</td>
<td>Dodecagon</td>
<td>30</td>
<td>159</td>
<td>5176</td>
</tr>
</tbody>
</table>

The side of a polygon is known, to find the length of perpendicular: Set bevel or fence to the tabulated numbers below. Example: The side of an octagon is 12, set bevel to 23 on tongue, 27 11-16 on blade. Blade gives the answer.

<table>
<thead>
<tr>
<th>No. of Sides</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
<th>11</th>
<th>12</th>
</tr>
</thead>
<tbody>
<tr>
<td>Perpendicular</td>
<td>9</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>5</td>
<td>6</td>
<td>7</td>
<td>10</td>
<td>11</td>
</tr>
<tr>
<td>Side of Polygon</td>
<td>31 175</td>
<td>23 144</td>
<td>15 26</td>
<td>23 7</td>
<td>27 10</td>
<td>30 3</td>
<td>20 2</td>
<td>23 4</td>
<td>26</td>
<td></td>
</tr>
</tbody>
</table>

To Inscribe three Equal Circles in a circle of given diameter. Set to 61 2 on tongue and 14 on blade. Move the bevel to the given diameter on the blade and the required diameter appears on the tongue.

Four equal circles require a bevel of 2’91 and 14.
The following also, is another use for the square and bevel combined.

If a person is drawing a machine on a scale of 1 1/4 inch to the foot, he may simply lay a common rule under the square, touching the 12 inch mark on the blade, and the 1 1/4 inch mark on the tongue; he then possesses a contrivance by which he may easily reduce from one scale to the other. For instance, if a piece of stick 23 4 inches square is to go into the construction, the draughtsman finds the 9 2 4 inch mark on the blade, that is 23 4 inches back from the 12 inch mark, and measures square out to the rule. This distance is the reduced section of the stick.

A straight mark, drawn on a table or a drawing board, serves as well as a rule.

Conveyors’ shaft 5 inches in diameter, 12 feet long, pitch of flights 9 inches; make a postboard template; multiplying the diameter by 3 141 6 gives the base, and the 9 is the altitude. The paper would be 9 inches altitude, 15 71-100 base; draw a line along shaft, place altitude or 9 inches along this line, scribe along the hypothenuse; this gives the spiral course of flight. This principle also teaches how to cut round sticks of straight timber by marking along base of template. Take square on each end the same as taking a stick out of wind, before striking lines.

The cuts for the edges of the pieces of a hexagonal hopper are found by subtracting the width of one piece at the bottom, viz., the width of same at top, and taking the remainder on the tongue, and depth of side on blade. The tongue gives the cut. For the cut on the face of the sides, take 7 12 of the rise on the tongue, and the depth of side on the blade. The tongue gives the cut. The bevel for the top and bottom edges is found by taking the rise on the blade, and the run on the tongue; the latter gives the cut.

To find the cut of an octagonal hopper for the face of
the board and also the edge, subtract the rise from the width of side; take the remainder on the tongue and width of side on blade; the tongue gives the cut. The edge of the stuff is to be square when applying the bevel. The bevel for the top and bottom edges of the sides is found by taking the rise on the blade, and run on the tongue, the latter gives the cut. This makes the edges horizontal. The edges are not to be beveled till the four sides are cut.

To Lay off Angles of 60° and 30°.—Mark any number of inches, say 14, on an indefinite line. Place the blade against one extremity of this distance, and the 7 inch mark of the tongue at the other. The tongue then forms an angle of 60° with the indefinite line, and the blade an angle of 30°.

To Find the Bevels and Width of Sides and Ends of a Square Hopper.—Fig. 50. The large square represents the upper edges of the hopper and the small one the lower edges, or base. The width of the sides and ends is found in this way: Take the run \( a b \) on the tongue, and the perpendicular height \( a d \) on the blade. It is thus found in the same manner as the length of a brace. To find the cut for a butt joint, take width of side on blade and half the length of the base on tongue; the latter gives the cut. For a mitre joint take width of side on the blade and perpendicular height on tongue; the latter gives the cut.

For the cut across the sides of the boards, take the run \( a b \) on the tongue, and the width of side on blade; the tongue gives the cut. The inside corners of the sides and ends are longer than the outside, so if a hopper is to be of a certain size, the lengths of ends and sides are to be measured on the inside edge of each piece, and the bevels struck across the edges to these marks. This is only in case of butt joints. Of course if the hopper is to be square, the thickness of the sides must be taken from the ends.

If the top and bottom edges are to be horizontal, the bevel is thus found: Take the perpendicular height of hopper on the blade and the run on the tongue, the latter gives both cuts. A hopper can be made by the above method by getting the outside dimensions at top and bottom, and the perpendicular height.

In large hoppers pieces are put down along the corners.
to strengthen them. The length, and the bevel to fit the corner are thus found: Suppose the top of hopper is 8 feet, and the bottom 18 inches square. Find the diagonals of each, subtract the one from the other, and half the remainder is the run for the corner piece. From the length of this run, \( l \), and the rise, \( a \), we find the length of the corner piece. To find the bevel or backing, take on the blade the length of the corner piece and on the tongue the rise; the latter gives the bevel. Another method is to draw the line, \( l \), to represent the seat of the corner piece, set off square with this the line \( m \), of the same length as the run, \( a \). Then draw \( n \), which is the length of the corner piece. To find the backing, draw a line, \( p \), anywhere across \( l \), at right angles therewith, and at its intersection with line, \( l \), strike a circle tangent to \( n \). From the point of intersection of the circle with \( l \), draw lines to the extremities of \( p \). The angle made by these lines is the bevel or backing.

Another method generally employed for finding the bevels of hoppers is to bevel the top and bottom edges of the sides and ends to the angle they are to stand at, then to lay a bevel set to a mitre, or angle of 45°, on the beveled edge, and that will lay off a mitre joint, while a try-square will lay off a butt joint. An angle of 45° will mitre only those boxes with sides which are vertical and square with each other.

When the sides and ends of a rectangular box or hopper are of the same width, that is, when sides and ends slope at equal angles, the bevels, either butt or mitre, are found as for square hoppers.

When a hopper has the sides and ends of different widths, that is, when sides and ends stand at different angles,
should be measured along the middle, as the dotted lines show. This is the full length; half the thickness of the ridge-pole is to be taken off, measured square back from the bevel.

The bevel of the upper end of a hip-rafter is called the down bevel. It is always square with the lower end bevel, hence these bevels are found by the parts taken on the square to find the lengths of the hip-rafters. Another method is to take 17 inches on the blade and the number of inches of rise to the foot, that is, the rise in inches divided by half the width of roof in feet—on the tongue. The tongue gives the down bevel, the blade the lower end bevel. The reason for the foregoing is that when the hip-rafters are square with each other, the seat of the hip is the diagonal of a square whose side is half the width of building. The diagonal of a square with a 12 inch side is 17 inches nearly. So if the rise of roof in 1 foot is 6 inches, the rise of hip-rafter will be that only in 17 inches. The directions here given assume that the hip-rafter abuts the ridge-pole at right angles, but as the ground plan of the roof shows that they meet at an acute angle, another bevel must be considered, called the side bevel of the hip-rafters. Were there no slope to the roof, the bevel where they meet the ridge pole would be an angle of 45°, as the hips would be square with each other. When a pitch or slope is given, the hips depart from the right angle, and therefore the side bevels are always less than 45°. Take the length of hip on the blade, and its run on the tongue; the blade gives the cut.

Backing of the hip-rafters. The backs of the hip-rafters must be beveled to lie even with the planes of the roof. This bevel must slope from the middle toward either side.

It is found by taking the length of hip on blade, and the rise of the roof on tongue. The latter gives the bevel.

To find the lengths of the jack-rafters: Suppose there are to be four between the corner and the first common rafter; then there are five spaces, which, by dividing 7 foot 6 inches by 5, are 1 foot 2 inches from centre to centre of jacks. The rise of roof, also divided by 5, gives 1 foot rise for the shortest rafter. The run is 1 foot 6 inches; as both rise and run are given, the length down and lower bevels are found therefrom. The next jack has double the rise, run and length of the first; the following one three times, and the fourth four times. All the measurements are to proceed on or from the middle lines of the jacks.

The side bevel of all the jack-rafters is obtained by taking the length of a common rafter on the blade and its run on the tongue; the bevel on the blade gives the result.

Let us now consider the end of the building out of square. Fig. 52 illustrates the method of laying down the seats of the hips. To find the lengths of these hips, the lengths of the seats must be got by taking half the width of building on blade, and the distance from the end of the dotted line crossing the roof, to the corner on the tongue. The length
of the seat so obtained taken on the square, with the rise of
the roof, gives the length of the respective hip-rafter.

The down and lower end bevels are found as in the pre-
vious hip-rafters. To obtain each side bevel, add the dis-
tance from the dotted line to the corner and the gain of
the hip-rafter; take the sum on the blade, and half the width
of building on the tongue; the latter gives the cut.

The lengths, etc., of the jack-rafters on the side, are de-
termined as at the square end of the roof; the side bevel
being found by taking the length of a common rafter on
the blade, and the distance from the dotted line to corner
on the tongue. The latter showing the bevel.

The lengths of jack-rafters on the end. Assuming there
are to be four jacks between the corner and the centre in-
cluded, half the length of the end of the roof must be di-
vided by 5. One side of the roof being 3 feet longer than
the other, we place 3 feet, on tongue, and 15 feet, the width
of building, on the blade, and thus obtain the distance from
corner to corner on the end of the roof. Half this divided
by 5 gives the distance of the jacks apart. The distance
from where the middle lines of the hips meet to the middle
point of the end of the roof is also to be divided by 5, the
quotient giving the run of the shortest rafter. The rise is
the same as for the jacks on the square end.

These rules give the full length of rafter, so that when
hips come against a ridge-pole or jacks against a hip, half
the thickness of pole or hip, squared back from their down
bevels, must be taken off.

Side bevels of these jacks are obtained by adding the
distance from the dotted line to the corner to the gain of
a common rafter in running that distance; take this on the

blade, and half the width of building on the tongue. The
blade gives the bevel.

Trusses.—Fig. 53. A is the straining beam, B the brace,
T the tie beam. Generally the brace has about one-third
the length of tie beam for a run. From the rise and run
find the length and lower end bevel of the brace. After
marking the lower end bevel on the stick, add to it just
what is cut out of the tie beam. The bevel of the upper
end of the brace where it butts against the straining beam
is found in the following manner. Take the length of the

brace, or a proportional part, and mark it on the edge of a
board; take half the rise of the brace on the tongue, lay it
to one of these marks on the board, and move the blade
till it touches the other mark on board. A line drawn
along the tongue gives the bevel for both brace and stra-
ing beam. The angle made between brace and straining
beam is thus bisected. Lay off the measurements from
the outside of the timbers. Put a bolt where shown, with
a washer under the, head to fit the angle of straining
beam and brace.
There are quite a number of methods of obtaining approximate proportions of the diameter of circles to their circumferences. The true proportion, or, as it is sometimes expressed, “the squaring of the circle,” is one of those feats, like the discovery of “perpetual motion,” and is as far from being accomplished now as ever. At any rate, it makes but little difference at this time, to the operative mechanic, whether the circle can be squared or not, so long as he can get near enough to the truth to satisfy the requirements at hand satisfactorily; and to aid him in this, the following method is shown of obtaining the circumferences of circles when the diameter is given, by use of the square. Of course, as shown in the cut, the rule will apply to circles of any reasonable dimensions.

Let $A B$, Fig. 54, be a straight line, or the straight edge of a board; then apply the square as shown, placing the 16-inch mark on the blade at $C$, and the 5-inch mark on the tongue at $D$. See that the junctions of the blade and tongue of the square with the line $A B$, are accurately placed, for on this depends the truth of the results. Now, suppose we wish to ascertain the circumference of a circle whose diameter is 8 inches; commencing at the point, $C$, we space off the diameter, 8 inches, three times, on the line $C O$, as shown at 8", 8", 8"; then square down the line 8", $F$, then $C F$ will be the circumference of a circle whose diameter is 8. It will be seen, by dotted lines in the cut, that the circumference equals the diagonal of a rectangle whose sides are respectively 24 and 7 1/2 inches; so that by adopting these figures (24 and 7 1/2) it enables the operative to use the full length and capacity of the square. The better way, however, is to work from a basis of 16 and 5, and draw the lines, $C O$ and $A B$, to considerable length, so that they may be made available for dimensions beyond the range of the square. Now, let us suppose an instance where the circumference of a circle is wanted, whose diameter is 10; we simply space off three tens, or thirty inches, on the line $C O$, which, in this case, is at $K$. Square down from $K$ to $R$, and $C R$ is the length sought.

Now, to prove this, let us proceed as follows: Diam. = $10 \times 3.1416 = 31.4160$, or nearly thirty-one inches and fifteen thirty-seconds of an inch. Now, if we measure $C R$, we will find that the distance is exactly 31.4160 inches, and is, therefore, the answer sought. It will be seen by these examples that the circumferences of circles may be easily obtained when the diameters are known. So, also, may the diameters be found when the circumferences are known, for by laying off the circumference on the line $A B$, as $C D$ in Fig. 54, for instance, and then applying the square as there exhibited, and dividing the distance from the heel of the square to the point $C$ into three equal parts. One of these parts is the diameter of the circle whose circumference equals the distance from $C$ to $D$. 
In my experience, I have frequently been asked how a mitre, or equal joint, could be laid off by using the square.

The matter is so simple, that it was thought unnecessary to insert it in the first edition, but the many inquiries on the subject that have been received since the work was published, induces me to give a few examples of the manner in which advanced workmen generally accomplish this end. Let Fig. 55 represent an oblique angle formed by two parallel boards. To obtain the joint, A, space off equal distances from the point 1 to 3, 3, then square over from the lines, R, R, keeping the heel of the square at the points, 3, 3. At the junction of the lines formed by the tongue of the square at 0 will be one point, and 1 will be the other by which the joint line, A, is defined.

To find the line of juncture for an acute angle, we proceed as follows: Fig. 56 represents two parallel boards: 1 the extreme angle, 3, 3 equal distances from the angle and are the points where the heel of the square must rest to form the lines o, 3; o shows the junction of the lines formed by the blade of the square. Draw a line from 0 to 1, and the line, A, formed, is the bevel required.

It will be seen, by these two examples, that the bevel of a junction at any angle may be obtained by this method. Sometimes, when estimating on work, it becomes necessary to get the length of braces and other timbers, that would require considerable figuring to obtain if the usual method of finding the length of the third side of a right-angled triangle was adopted. The square, at this juncture, may be made use of with advantage, where the length of the lines wanted is within the range of the instrument, and almost any dimensions may be manipulated, by making the subdivisions of the inch represent inches, feet, or yards. Suppose we want to get the length of a brace with unequal run of 7 and 12 feet respectively. Lay the two-foot rule...
across the square, putting the end on 7 on the tongue, and cutting the 12-inch line on the blade; then, as shown in Fig. 57, we will have on the side of the rule A B, 13 feet 11 inches, or say 14 feet, which is near enough for the estimator's purpose, and if required for working purposes, the exact length and bevels may be obtained by careful measurement.

Conclusion.—The ingenious and intelligent workman, after thoroughly mastering the foregoing applications of the "Steel Square," will awaken to the fact that the tool may be used for the solution of a thousand and one little matters that will crop up in his every-day calling, and by a combination or adaptation of the rules presented, he will be able to overcome all ordinary difficulties in obtaining cuts, bevels, and lines for roofs, hoppers, mouldings, etc.

PART IV.

Miscellaneous Rules and Memoranda.—The practical carpenter and joiner will frequently want to use the more elaborate methods of obtaining solutions where the problems are complicated and various; and the following rules are inserted in this work with a view of reaching some of the problems that appear to be beyond the range of the Steel Square without making such intricate combinations as would be sure to lead to confusion in ordinary hands.

Hip-Roofs.—The principles to be determined in a hip-roof are seven; namely:
1st. The angle which a common rafter makes with the level of the top of the building; that is, the pitch of the roof. 2nd. The angle which the hip-rafter makes with the level of the building. 3rd. The angles which the hip-rafter makes with the adjoining sides of the roof. This is called the backing of the hip. 4th. The height of the roof, or the "risc," as it is called. 5th. The lengths of the common rafters. 6th. The lengths of the hip-rafters. 7th. The distance between the centre line of the hip-rafter and the centre line of the first entire common rafter. The first, fourth, fifth and seventh are generally given, and from these the others may be found, as will be shown by the following illustrations: Let A B C D Fig. 58, be
the plan of a roof. Draw GH parallel to the sides, A D, B C, and in the middle of the distance between them.
From the points A, B, C, D, with any radius, describe the curves a b, a b, cutting the sides of the plan at a, b. From these points, with any radius, bisect the four angles of the plan at r, r, r, r, and from A, B, C, D, through the points, r, r, r, r, draw the lines of the hip-rafters, A G, B G, C H, D H, cutting the ridge-line, G H, in G and H, and produce them indefinitely. The dotted lines, e e, d f, are the seats of the last entire common rafters. Through any point in the ridge-line, I, draw E I F at right angles to G H. Make I K equal to the height or rise of roof, and join E K, F K; then E K is the length of a common rafter. Make G o, H o, equal to I K, the rise of the roof, and join A o, B o, C o, D o, for the length of the hip-rafters. If the triangles, A o C, B o G, be turned round their seats, A G, B G, until their perpendiculars are perpendicular to the plane of the plan, the points, o o, and the lines, G o, G o, will coincide, and the rafters, A o, B o, be in their true positions.

Fig. 58.

If the roof is irregular, and it is required to keep the ridge level, we proceed as shown in Fig. 59.

Bisect the angles of two ends by the lines A b, B b, C g, D G, in the same manner as in Fig. 58; and through G draw the lines G E, G F, parallel to the sides, C B, D A, re-

Fig. 59.

spectively cutting A b, B b, in E and F; join E F; then the triangle, E G F, is a flat, and the remaining triangle and trapeziums are the inclined sides. Join G b, and draw H I perpendicular to it; at the points M and N, where H I cuts the lines G E, G F, draw M K, N L perpendicular to H I, and make them equal to the rise; then draw H K, I L for the lengths of the common rafters. At E, set up E M perpendicular to B E; make it equal to M K or N L, and join B M for the length of the hip-rafter, and proceed in the same manner to obtain A m, C m, D m.

To find the backing of a hip-rafter, when the plan is
right-angled, we proceed as shown in Fig. 60. Let $bb$, $bc$ be the common rafters, $ad$ the width of the roof, and $ab$ equal to one-half the width. Bisect $bc$ in $a$, and join $aa$, $dd$. From $a$ set off $ac$, $ad$ equal to the height of the roof $ab$, and join $aa$, $dc$; then $ad$, $dc$ are the hip-rafters. To find the backing: from any point $h$ in $aa$, draw the perpendicular $hg$, cutting $aa$ in $g$; and through $g$ draw perpendicular to $aa$ the line $ef$, cutting $ab$, $ad$ in $e$ and $f$. Make $gh$ equal to $hh$, and join $ke$, $kf$; the angle $ef$ is the angle of the backing of the hip-rafter $c$.

Fig. 61 shows the method of obtaining the backing of the hip where the plan is not right angled.

Bisect $ad$ in $a$, and from $a$ describe the semicircle $ab$; draw $ab$ parallel to the sides $ab$, $dc$, and join $a$, $b$, $d$, for the seat of the hip-rafters. From $b$ set off on $ba$, $bd$, the lengths $bd$, $be$, equal to the height of the roof $bc$, and join $ac$, $dc$, for the lengths of the hip-rafters. To find the backing of the rafter:—In $aa$, take any point $k$, and draw $kk$ perpendicular to $ac$. Through $k$ draw $fg$ perpendicular to $ac$, meeting $ab$, $ad$ in $f$ and $g$. Make $hl$ equal to $kk$, and join $fl$, $gl$; the $flg$ is the backing of the hip.

Fig. 62 shows how to find the shoulder of purlins:
First, where the purlin has one of its faces in the plane of the roof, as at $e$. From $c$ as a centre, with any radius, describe the arc $dg$; and from the opposite extremities of the diameter, draw $dh$, $gm$ perpendicular to $bc$. From $e$ and $f$, where the upper adjacent sides of the purlin produced cut the curve, draw $ei$, $fl$ parallel to $dh$, $gm$; also draw $ck$ parallel to $dh$. From $l$ and $i$ draw $lm$ and $ih$. 
parallel to BC, and join $kh$, $km$. Then $km$ is the down bevel of the purlin, and $kh$ is its side bevel.

When the purlin has two of its sides parallel to the horizon. This simple case is shown worked out at $r$. It requires no explanation.

When the sides of the purlin make various angles with the horizon. Fig. 63 shows the application of the method described in Fig. 62 to these cases.

It sometimes happens, particularly in railroad buildings, that the carpenter is called upon to pierce a circular or conical roof with a saddle roof, and to accomplish this economically is often the result of much labor and perplexity if a correct method is not at hand.

The following method, shown in Fig. 64, is an excellent
one, and will no doubt be found useful in cases such as mentioned.

Let \( D H, F H \) be the common rafters of the conical roof, and \( K L, I L \) the common rafters of the smaller roof, both of the same pitch. On \( G H \) set up \( G C \) equal to \( M L \) the height of the lesser roof, and draw \( C D \) parallel to \( D F \), and from \( D \) draw \( C D \) perpendicular to \( D F \). The triangle \( D D C \), will then by construction be equal to the triangle \( K L M \), and will give the seat and the length and pitch of the common rafter of the smaller roof \( B \). Divide the lines of the seats in both figures, \( D C, K M \), into the same number of equal parts; and through the points of division in \( E \), from \( G \) as a centre, describe the curves \( C A, 2 G, 1 f \), and through those in \( D \), draw the lines \( 3 f, 4 G, M a \), parallel to the sides of the roof, and intersecting the curves in \( f g a \). Through these points trace the curves \( C f g a, A f g a \), which give the lines of intersection of the two roofs. Then to find the valley rafters, join \( C A, A a \); and on \( a \) erect the lines \( a b, a b \) perpendicular to \( C a \) and \( A a \), and make them respectively equal to \( M L \); then \( C b, A b \) is the length of the valley rafter, very nearly.

Fig. 65 shows how a curved hip-rafter may be obtained. The rafter shown in this instance is ogee in shape, but it makes no difference what shape the common rafter may be, the proper shape and length of hip may be obtained by this method. It will be noticed that one side of the example shown is wider than the other; this is to show that the rule will work correctly where the sides are unequal in width, as well as where they are equal. Let \( A B C, F E C \) represent the plan of the roof. \( F C G \) the profile of the wide side of the rafter. First, divide this rafter \( G C \) into any number of parts—in this case six. Transfer these points to the mitre line \( E B \), or, what is the same, the line in the plan representing the hip rafter. From the points thus established in \( E B \), erect perpendiculars indefinitely. With the dividers take the distance from the points in the line \( F C \), measuring to the points in the profile \( G C \), and set the same off on corresponding lines, measuring from \( E B \), thus establishing the points 1, 2, 3, etc.; then a line traced through these points will be the required hip rafter.

For the common rafter on the narrow side, continue the lines from \( E B \) parallel with the lines of the plan \( D E \) and \( A B \). Draw \( A D \) at right angles to these lines. With the dividers as before, measuring from \( F C \) to the points in \( G C \), set off corresponding distances from \( A D \), thus estab-
lishing the points shown between \( a \) and \( h \). A line traced through the points thus obtained will be the line of the rafter on the narrow side. This is supposed to be the return roof of a veranda, but is only shown as an example, for it is not customary to build verandas nowadays with an ogee roof, but with a rafter having a depression or cove in it. For accuracy it would be as well to make nearly - vice

the number of divisions shown from 1 to 6, as are there represented.

It has been shown, in the forepart of this work, how the bevels and lines for hoppers may be obtained by the aid of the square, and it is now proposed to show how the same results may be obtained by a system of lines. This method, in many shapes and forms, has been used from time immemorial by workmen, more particularly by carriage makers to obtain the bevels of splayed seats; the present way of expressing it, however, is comparatively recent.

If we make \( a 1 \), Fig. 66, represent the elevation of our hopper, and \( b 1 \) a portion of the plan, we proceed as follows: Lay off \( n s \), which is the bevel of one side, and \( n s p o \) the section of one end.

Place one foot of the dividers at \( n \), and with \( n s \) as radius describe the arc \( s u \), intersecting the right line \( n u \) in the point \( u \). At \( s \) erect the perpendicular \( st \), and draw the line \( u t \) at right angles to \( n u \). Connect \( n \) and \( t \); then the triangle \( mnt \) is the end bevel required. The line \( n t \) is the hypothenuse of a right-angled triangle, of which \( n u \) may be taken for the perpendicular and \( u t \) for the base. To find the mitre of which \( d e \) is the plan, project \( s \) and \( p \), as indicated in the plan by the full lines. With \( s p \) as radius and \( s \) as centre, describe the arc \( p r \). In the plan draw \( d g \), on which lay off the distance \( s r \), measuring from \( f \), as shown by \( f g \). Then \( d f \) is the mitre sought.

Fig. 67 shows the rule for finding the bevels for the sides of the hopper. From \( m \), the point at which \( b m \) intersects \( b c \), or the inner face of the hopper, erect the perpendicular \( m l \), intersecting \( r f \), or the upper edge of the hopper, in the point \( l \). Then \( l c \) shows how much longer the inside edge is required to be than the outside. In the plan draw \( tv \) parallel to \( sx \), making the distance between

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the two lines equal to $CF$ of the elevation, or, equal to the thickness of one side. From the point $L$ in the elevation

![Diagram]

Fig. 67.

drop the line $LW$, producing it until it cuts the mitre line $NO$, as shown at $W$. From $W$, at right angles to $LW$, erect the perpendicular $WV$, meeting the line $TV$ in the point $V$. Connect $V$ and $U$; then $TVU$ will be the angle sought. This bevel may be found at once by laying off the thickness of the side from the line $EM$, as shown by $NP$ in the elevation, and applying the bevel as shown. This course does away with the plan entirely, provided both sides have the same inclination.

There are several other ways by which the same results may be obtained; some of these will no doubt occur to the reader when laying out the lines as shown here.

Fig. 68 exhibits a method of obtaining the correct shape of a veneer for covering the splayed head of a gothic jamb.

![Diagram]

Fig. 68.

$E$ shows the horizontal sill, $EF$ the splay, $FA$ the line of the inside of jamb, $\delta$ the difference between front and back edges of jamb, $BA$ the line of splay. At the point of junction of the lines $BA, FA$, set one point of the compasses, and with the radius $AB$ draw the outside curve of $n$; then with the radius $AS$ draw the inside curve, and $n$ will be the veneer required. This will give the required shape for either side of the head.